CS 315 Intermediate Algorithms Winter 2023

Assignment 2

Due 11:59 PM, Sunday, January 29, 2023

1 Description

For this assignment, you are to write a program which will take the description of a weighted directed acyclic graph from standard input and write to standard output two numbers measuring the graph. The program will need to compute (i) the length of the longest path from Node 1 to Node N, and (ii) the number of distinct paths from Node 1 to Node N that have the longest length found in part (i).

You may write your program in either Java, Python, C, or C++. Other languages need to be approved by the instructor. You may store the graph with either an adjacency list or an adjacency matrix. Your program should implement a linear time (i.e., O(n+m) if using an adjacency list and $O(n^2)$ if using an adjacency matrix) algorithm and will be tested on very large graphs, so you cannot possibly list them all.

2 Sample I/0

The first line of the input is a line containing two integers, N and M. N is the number of nodes—the nodes are $1, 2, 3, \ldots, N$ —and M is the number of edges. There follow M lines describing each edge. An edge description is a line containing three integers I J W, where $I \leq J$ (i.e., the edge from I to J) and W > 0. In your outputs, please output the texts of "longest path:" and "number of longest paths:" before the values you compute, respectively. See below.

input file inSample1.txt

5 7

1 2 7

1 3 10

2 4 8

2 5 3

3 4 5

3 5 10

4 5 5

Expected output:

```
longest path: 20
number of longest paths: 3
input file inSample2.txt
10 12
1 2 1
1 3 1
2 4 1
3 4 1
4 5 1
4 6 1
5 7 1
6 7 1
7 8 1
7 9 1
8 10 1
9 10 1
Expected output:
longest path: 6
```

3 Testing Protocol

number of longest paths: 8

We will test your program the same way "Assignment 0" was tested. Please check "Assignment 0". We will test your program by running your program at the command line. You will need to use **standard input**. Do not pass in the name of the file as an argument - do not encode the name of your input file in your program. We will run your program on several different test files, some of which may be generated by other programs and piped into yours.

We will not attempt to cause overflow on the number of paths - that number should fit into an int. If your program seems slow, which is often caused by trying to list all possible paths individually (exponential time!), be aware that we will test it on a graph with many paths.

You may want to consider the case where the graph is not connected or where there is no path from node 1 to node N. However, we will not test your program on any tricky inputs: there will be a path from node 1 to all other nodes, and from all nodes to node N.

4 Submission

Submit only a single source file. Please compress your single file into a ".zip" file and then submit it on Canvas. Feel free to let the instructor know if you have any questions regarding the submission.