Introduction to Artificial Intelligence CS 471/571(Fall 2023):

Lecture 14: Reinforcement Learning (Part 3)

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Source: http://ai.berkeley.edu/home.html

Reminder

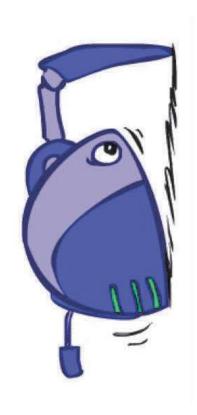
 Written assignment 3: MDPs and Reinforcement Learning
- Deadline: Nov 08th, 2023

Reinforcement Learning

- We still assume an MDP:
- \blacksquare A set of states $s \in S$
- A set of actions (per state) A
- A model T(s,a,s')
- A reward function R(s,a,s')
- Still looking for a policy $\pi(s)$



■ Big idea: Compute all averages over T using sample outcomes

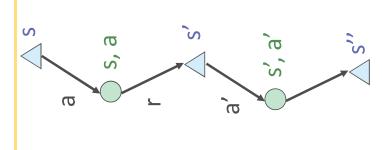


Model-Free Learning

- Model-free (temporal difference) learning
- Experience world through episodes

$$(s, a, r, s', a', r', s'', a'', r'', s'''' \dots)$$

- Update estimates each transition (s, a, r, s')
- Over time, updates will mimic Bellman updates



Q-Learning

- We'd like to do Q-value updates to each Q-state:

$$Q_{k+1}(s,a) \leftarrow \sum_{j} T(s,a,s') \left[R(s,a,s') + \gamma \max_{a'} Q_k(s',a') \right]$$

- But can't compute this update without knowing T, R

Instead, compute average as we go

Receive a sample transition (s,a,r,s')

This sample suggests

$$Q(s,a) \approx r + \gamma \max_{s'} Q(s',a')$$

■ But we want to average over results from (s,a) (Why?)

So keep a running average

$$Q(s,a) \leftarrow (1-\alpha)Q(s,a) + (\alpha) \left[r + \gamma \max_{a'} Q(s',a')\right]$$

Example

	\mathfrak{P}
•	A,
-	states:
E	OM.T.

4

2

Down

M

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Down

• Discount factor:
$$\gamma = 0.5$$

Learning rate:
$$\alpha = 0.5$$

$$Q(A, Down) = ?$$

$$Q(B, Up) = ?$$

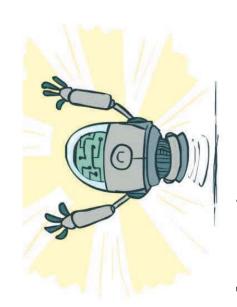
$$Q(s,a) \leftarrow (1-\alpha)Q(s,a) + (\alpha)\left[r + \gamma \max_{a'} Q(s',a')\right]$$

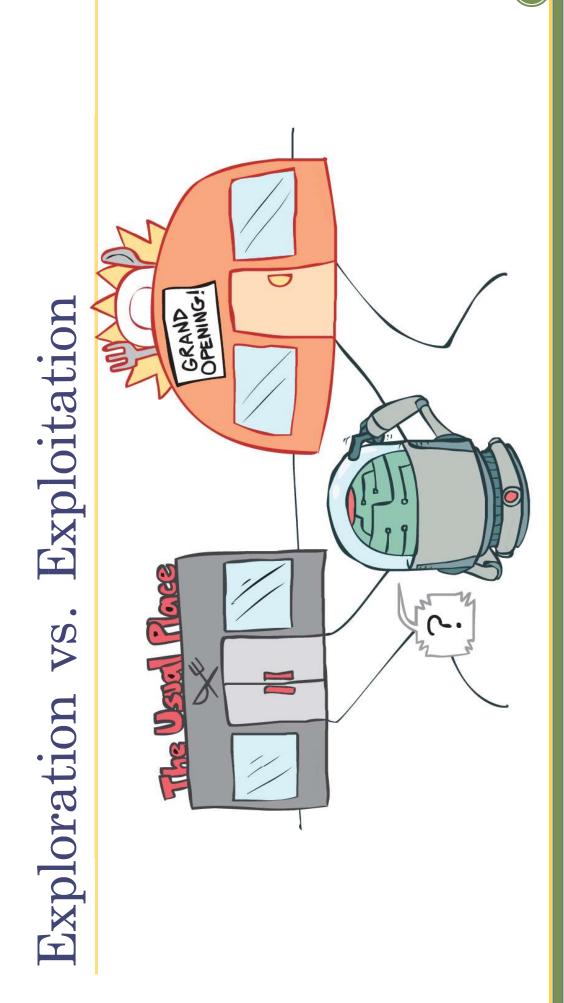
Q-Learning Properties

- Amazing result: Q-learning converges to optimal policy -- even if you're acting suboptimally!



- You have to explore enough
- You have to eventually make the learning rate small enough
- ... but not decrease it too quickly
- Basically, in the limit, it doesn't matter how you select actions





How to Explore?

- Several schemes for forcing exploration
- Simplest: random actions (e-greedy)
- Every time step, flip a coin
- With (small) probability e, act randomly
- With (large) probability 1-ɛ, act on current policy
- Problems with random actions?
- You do eventually explore the space, but keep thrashing around once learning is done
- One solution: lower ε over time
- Another solution: exploration functions



Exploration Functions

- When to explore?
- Random actions: explore a fixed amount
- Better idea: explore areas whose badness is not (yet) established, eventually stop exploring



 Takes a value estimate u and a visit count n, and returns an optimistic utility, e.g.

$$f(u,n) = u + k/n$$

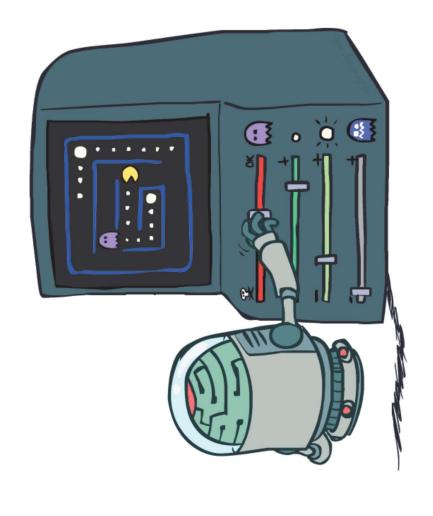
Regular Q-Update: $Q(s,a) \leftarrow_{\alpha} R(s,a,s') + \gamma \max_{a'} Q(s',a')$

Modified Q-Update:
$$Q(s, a) \leftarrow_{\alpha} R(s, a, s') + \gamma \max_{a'} f(Q(s', a'), N(s', a'))$$

• Note: this propagates the "bonus" back to states that lead to unknown states as well!

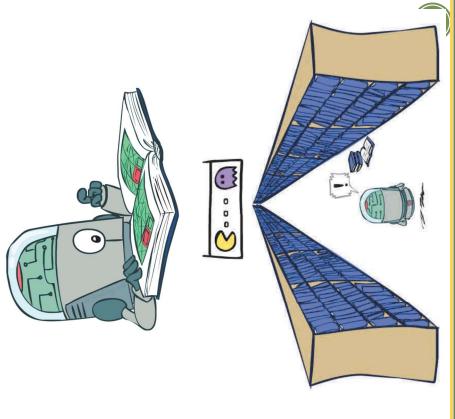


Approximate Q-Learning



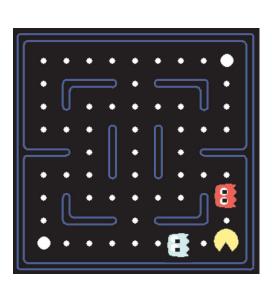
Generalizing Across States

- Basic Q-Learning keeps a table of all q-values
- In realistic situations, we cannot possibly learn about every single state!
- Too many states to visit them all in training
- Too many states to hold the q-tables in memory
- Instead, we want to generalize:
- Learn about some small number of training states from experience
- Generalize that experience to new, similar situations
- This is a fundamental idea in machine learning, and we'll see it over and over again

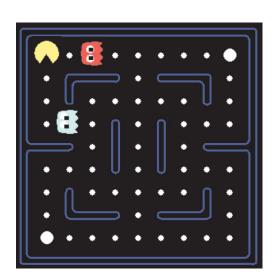


Example: Pacman

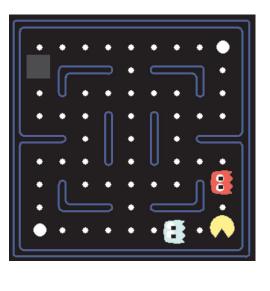
Let's say we discover through experience that this state is bad:



In naïve q-learning, we know nothing about this state:

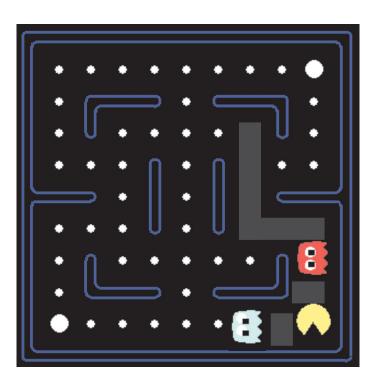


Or even this one!



Feature-Based Representations

- Solution: describe a state using a vector of features (properties)
- Features are functions from states to real numbers (often 0/1) that capture important properties of the
- Example features:
- Distance to closest ghost
- Distance to closest dot
- Number of ghosts
 - 1 / (dist to dot)²
- Is Pacman in a tunnel? (0/1)
- etc.
- Is it the exact state on this slide?
- Can also describe a q-state (s, a) with features (e.g. action moves closer to food)



Linear Value Functions

• Using a feature representation, we can write a q function (or value function) for any state using a few weights:

$$V(s) = w_1 f_1(s) + w_2 f_2(s) + \dots + w_n f_n(s)$$

$$Q(s,a) = w_1 f_1(s,a) + w_2 f_2(s,a) + \dots + w_n f_n(s,a)$$

- Advantage: our experience is summed up in a few powerful numbers
- Disadvantage: states may share features but actually be very different in

Approximate Q-Learning

$$Q(s,a) = w_1 f_1(s,a) + w_2 f_2(s,a) + \dots + w_n f_n(s,a)$$

Q-learning with linear Q-functions:

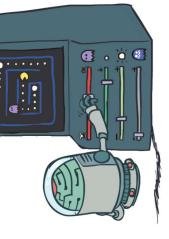
transition
$$=(s,a,r,s')$$

$$\operatorname{difference} = \left[r + \gamma \max_{a'} Q(s', a') \right] - Q(s, a)$$

$$Q(s,a) \leftarrow Q(s,a) + \alpha$$
 [difference]

$$w_i \leftarrow w_i + \alpha \left[\text{difference} \right] f_i(s, a)$$

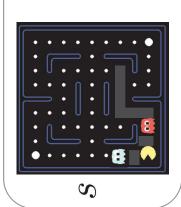




- Intuitive interpretation:
- Adjust weights of active features
- E.g., if something unexpectedly bad happens, blame the features that were on: disprefer all states with that state's features
- Formal justification: online least squares

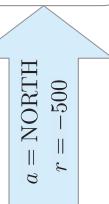
Example: Q-Pacman

$$Q(s, a) = 4.0 f_{DOT}(s, a) - 1.0 f_{GST}(s, a)$$



 $f_{DOT}(s, \text{NORTH}) = 0.5$

 $f_{GST}(s, \text{NORTH}) = 1.0$



 $Q(s',\cdot)=0$

$$Q(s, \text{NORTH}) = +1$$

$$r + \gamma \max_{a'} Q(s', a') = -500 + 0$$

difference = -501

 $w_{DOT} \leftarrow 4.0 + \alpha [-501] 0.5$ $w_{GST} \leftarrow -1.0 + \alpha [-501] 1.0$

 $Q(s,a) = 3.0 f_{DOT}(s,a) - 3.0 f_{GST}(s,a)$

Q-learning with Linear Approximation

Algorithm 4: Q-learning with linear approximation.

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Initialize q-value function Q with random weights w: Q(s, a; w) = \sum_{m} w_m f_m(s, a);
```

2 for episode = $1 \rightarrow M$ do

Get initial state s_0 ;

for $t=1 \rightarrow T$ do

With prob. ϵ , select a random action a_t ;

With prob. $1 - \epsilon$, select $a_t \in \operatorname{argmax}_a Q(s_t, a; w)$;

Execute selected action a_t and observe reward r_t and next state s_{t+1} ;

if episode terminates at step t+1otherwise $(r_t + \gamma \max_{a'} Q(s_{t+1}, a'; w))$ Set target $y_t = \begin{cases} r_t \\ r_t \end{cases}$

Perform a gradient descent step to update $w: w_m \leftarrow w_m + \alpha [y_t - Q(s_t, a_t; w)] f_m(s, a)$;