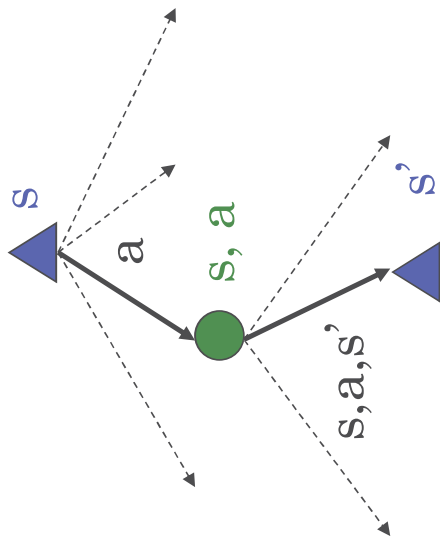


Recap: MDPs

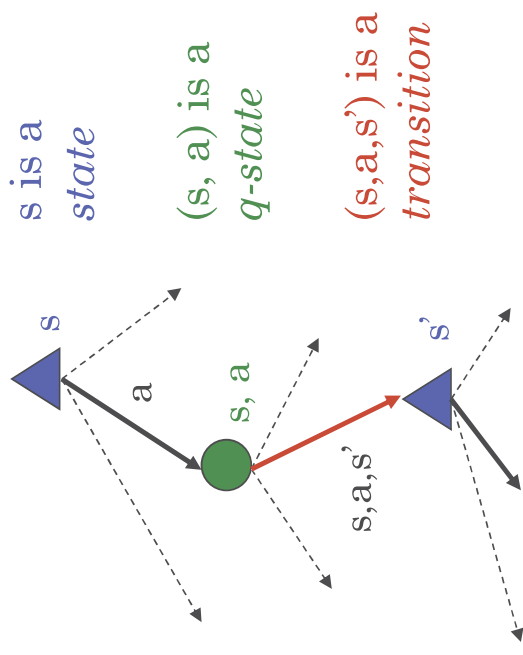
- Markov decision processes:
 - States S
 - Actions A
 - Transitions $P(s' | s, a)$ (or $T(s, a, s')$)
 - Rewards $R(s, a, s')$ (and discount γ)
 - Start state s_0

- Quantities:
 - Policy = map of states to actions
 - Utility = sum of discounted rewards
 - Values = expected future utility from a state (max node)
 - Q-Values = expected future utility from a q-state (chance node)



Optimal Quantities

- The value (utility) of a state s :
 $V^*(s)$ = expected utility starting in s and acting optimally
- The value (utility) of a q-state (s,a) :
 $Q^*(s,a)$ = expected utility starting out having taken action a from state s and (thereafter) acting optimally
- The optimal policy:
 $\pi^*(s)$ = optimal action from state s



Policy Iteration

- Alternative approach for optimal values:
 - **Step 1: Policy evaluation:** calculate utilities for some fixed policy (not optimal utilities!) until convergence
 - **Step 2: Policy improvement:** update policy using one-step look-ahead with resulting converged (but not optimal!) utilities as future values
 - Repeat steps until policy converges
- This is **policy iteration**
 - It's still optimal!
 - Can converge (much) faster under some conditions



Policy Iteration

- Evaluation: For fixed current policy π , find values with policy evaluation:
 - Iterate until values converge:

$$V_{k+1}^{\pi_i}(s) \leftarrow \sum_{s'} T(s, \pi_i(s), s') [R(s, \pi_i(s), s') + \gamma V_k^{\pi_i}(s')]$$

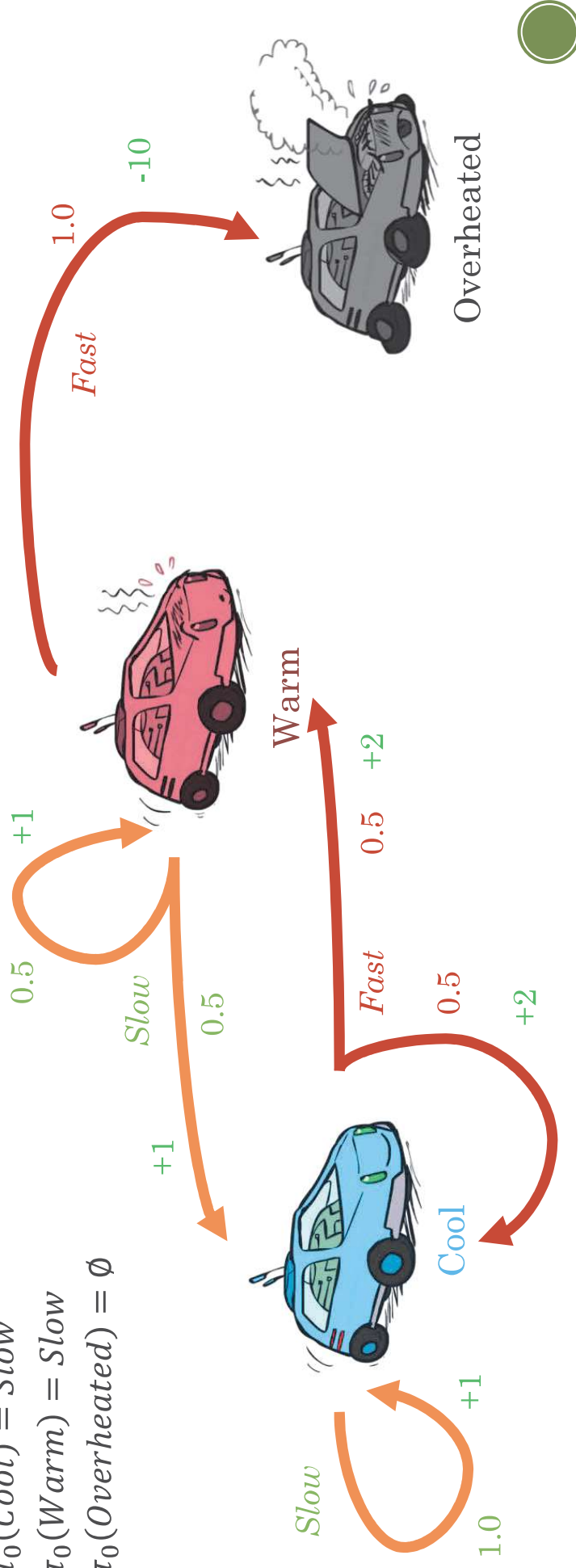
- Improvement: For fixed values, get a better policy using policy extraction
 - One-step look-ahead:

$$\pi_{i+1}(s) = \arg \max_a \sum_{s'} T(s, a, s') [R(s, a, s') + \gamma V^{\pi_i}(s')]$$

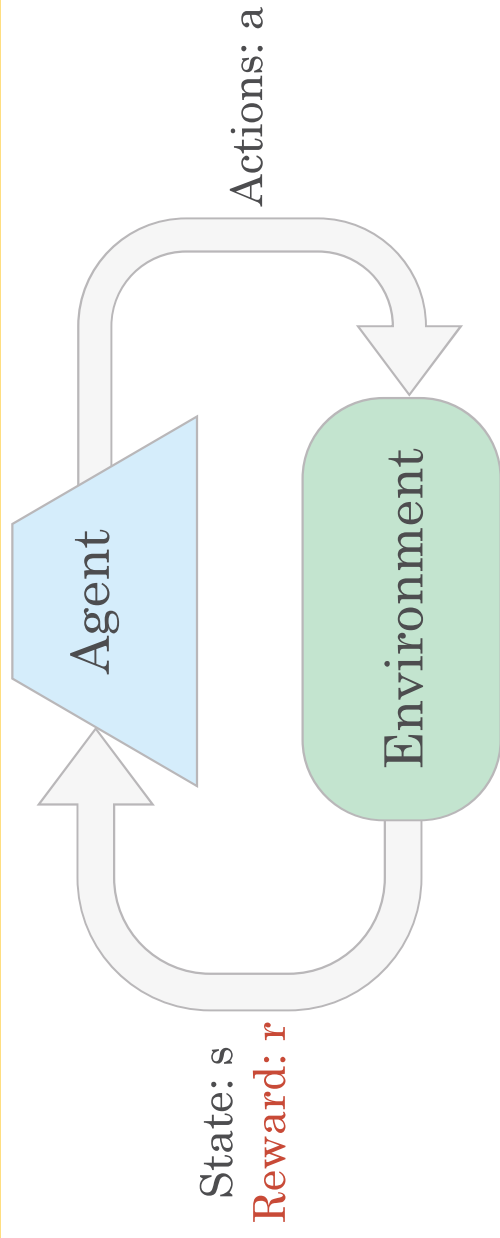


Example: Racing

- Discount: $\gamma = 0.1$
- Initial policy
 - $\pi_0(\text{Cool}) = \text{Slow}$
 - $\pi_0(\text{Warm}) = \text{Slow}$
 - $\pi_0(\text{Overheated}) = \emptyset$



Reinforcement Learning



- Basic idea:
 - Receive feedback in the form of **rewards**
 - Agent's utility is defined by the reward function
 - Must (learn to) act so as to **maximize expected rewards**
 - All learning is based on observed samples of outcomes!

