
CS 471/571 (Fall 2023): Introduction to Artificial Intelligence

Lecture 13: Reinforcement Learning (Part 2)

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Source: <http://ai.berkeley.edu/home.html>



Reminder and Announcement

- Project 2
 - Deadline: November 03, 2023

- Written assignment 3
 - Will be posted tomorrow
 - Deadline: November 08, 2023

Reinforcement Learning

- Still assume a Markov decision process (MDP):
 - A set of states $s \in S$
 - A set of actions (per state) A
 - A model $T(s,a,s')$
 - A reward function $R(s,a,s')$
- Still looking for a policy $\pi(s)$
- New twist: don't know T or R
 - I.e. we don't know which states are good or what the actions do
 - Must actually try out actions and states to learn



The Story So Far: MDPs and RL

Known MDP: Offline Solution

| Goal | Technique |
|---------------------------------|--------------------------|
| Compute V^* , Q^* , π^* | Value / policy iteration |
| Evaluate a fixed policy π | Policy evaluation |

Unknown MDP: Model-Based

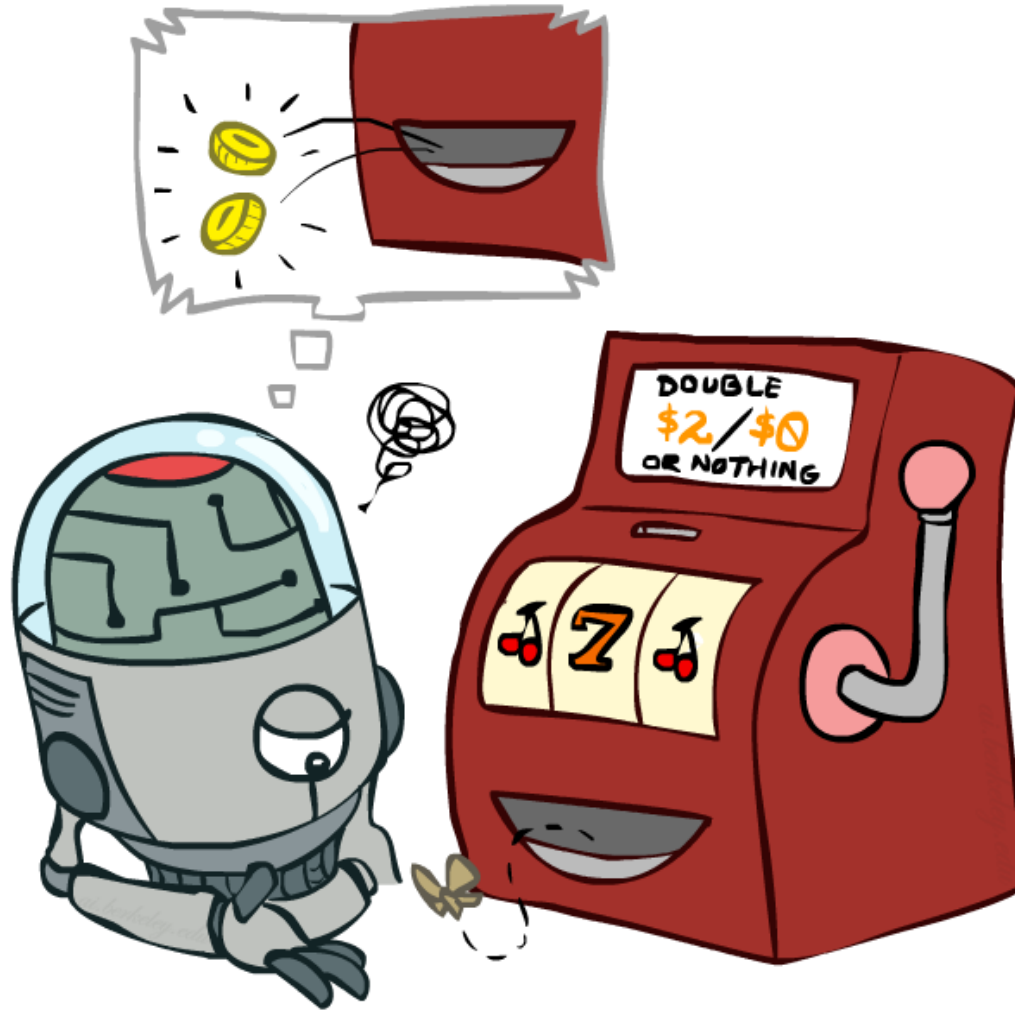
| Goal | Technique |
|---------------------------------|----------------------|
| Compute V^* , Q^* , π^* | VI/PI on approx. MDP |
| Evaluate a fixed policy π | PE on approx. MDP |

Unknown MDP: Model-Free

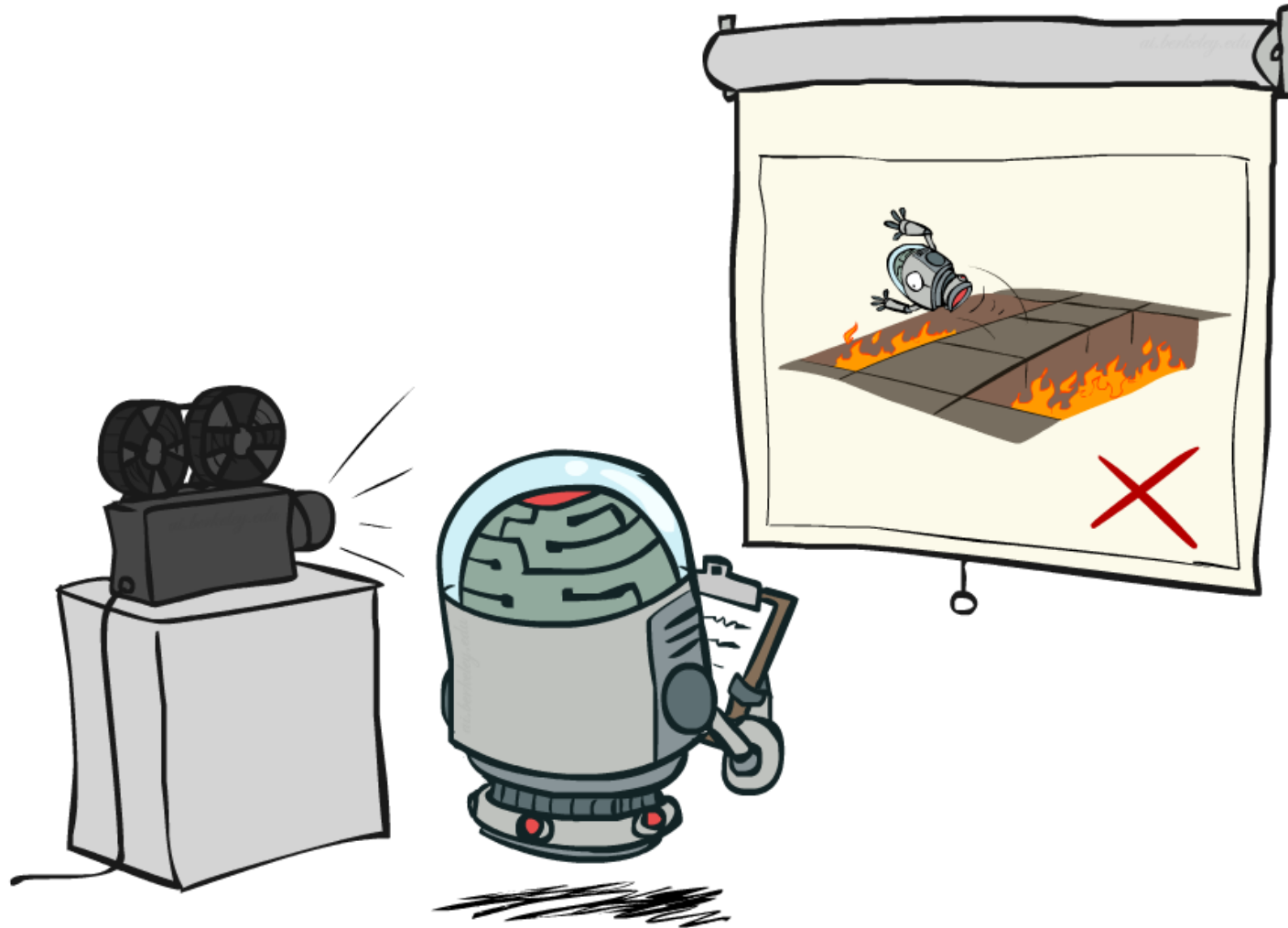
| Goal | Technique |
|---------------------------------|----------------|
| Compute V^* , Q^* , π^* | Q-learning |
| Evaluate a fixed policy π | Value Learning |



Model-Free Learning

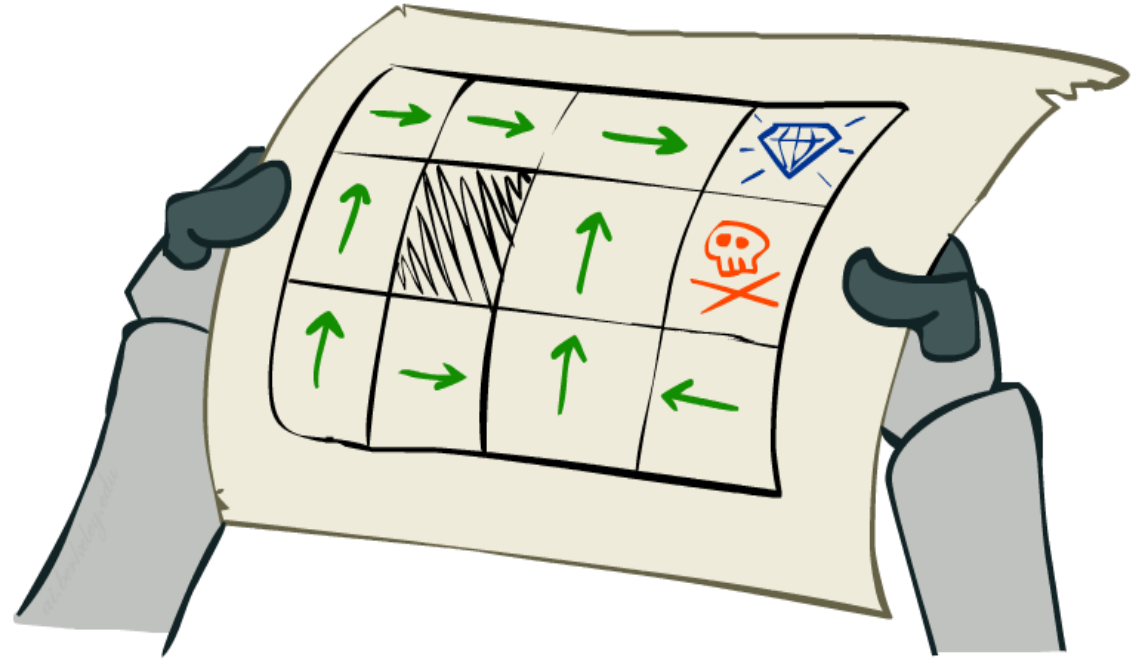


Passive Reinforcement Learning



Passive Reinforcement Learning

- Simplified task: policy evaluation
 - Input: a fixed policy $\pi(s)$
 - You don't know the transitions $T(s,a,s')$
 - You don't know the rewards $R(s,a,s')$
 - **Goal: learn the state values**
- In this case:
 - Learner is “along for the ride”
 - No choice about what actions to take
 - Just execute the policy and learn from experience
 - This is NOT offline planning! You actually take actions in the world.



Direct Evaluation

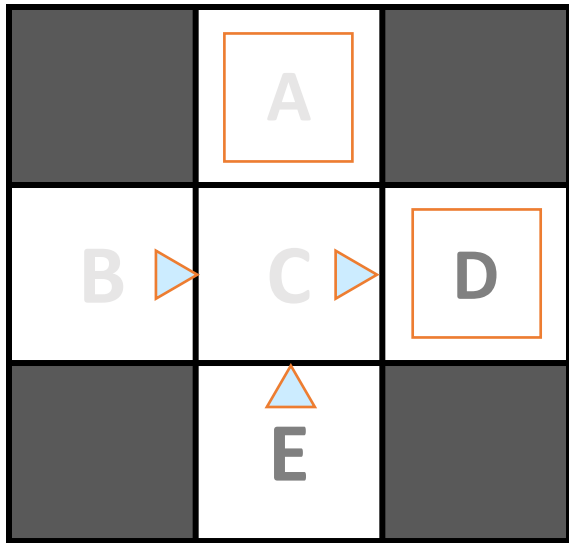
- Goal: Compute values for each state under π
- Idea: Average together observed sample values
 - Act according to π
 - Every time you visit a state, write down what the sum of discounted rewards turned out to be
 - Average those samples
- This is called direct evaluation



Example: Direct Evaluation

Input Policy

π



Assume: $\gamma = 1$

Observed Episodes
(Training)

Episode 1

B, east, C, -1
C, east, D, -1
D, exit, x, +10

Episode 2

B, east, C, -1
C, east, D, -1
D, exit, x, +10

Episode 3

E, north, C, -1
C, east, D, -1
D, exit, x, +10

Episode 4

E, north, C, -1
C, east, A, -1
A, exit, x, -10

Output Values

| | | |
|----|-----|-----|
| | -10 | |
| +8 | +4 | +10 |
| | -2 | |



Problems with Direct Evaluation

- What's good about direct evaluation?
 - It's easy to understand
 - It doesn't require any knowledge of T , R
 - It eventually computes the correct average values, using just sample transitions
- What bad about it?
 - It wastes information about state connections
 - Each state must be learned separately
 - So, it takes a long time to learn

Output Values

| | | |
|---------|----------|----------|
| | -10 A | |
| +8 B | +4 C | +10 D |
| | -2 E | |

If B and E both go to C under this policy, how can their values be different?

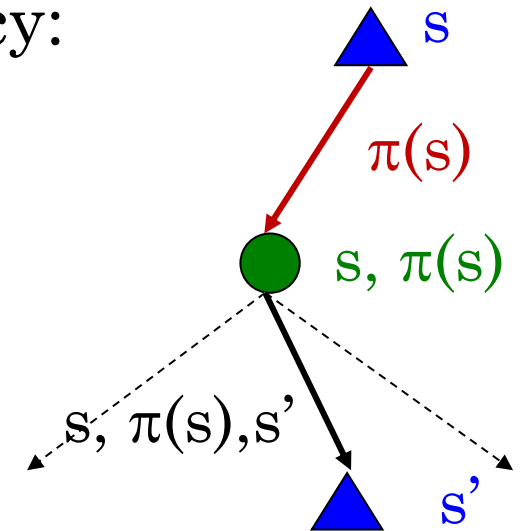


Why Not Use Policy Evaluation?

- Simplified Bellman updates calculate V for a fixed policy:
 - Each round, replace V with a one-step-look-ahead layer over V

$$V_0^\pi(s) = 0$$

$$V_{k+1}^\pi(s) \leftarrow \sum_{s'} T(s, \pi(s), s') [R(s, \pi(s), s') + \gamma V_k^\pi(s')]$$



- This approach fully exploited the connections between the states
- Unfortunately, we need T and R to do it!
- Key question: how can we do this update to V without knowing T and R ?
 - In other words, how to we take a weighted average without knowing the weights?



Sample-Based Policy Evaluation?

- We want to improve our estimate of V by computing these averages:

$$V_{k+1}^{\pi}(s) \leftarrow \sum_{s'} T(s, \pi(s), s') [R(s, \pi(s), s') + \gamma V_k^{\pi}(s')]$$

- Idea: Take samples of outcomes s' (by doing the action!) and average

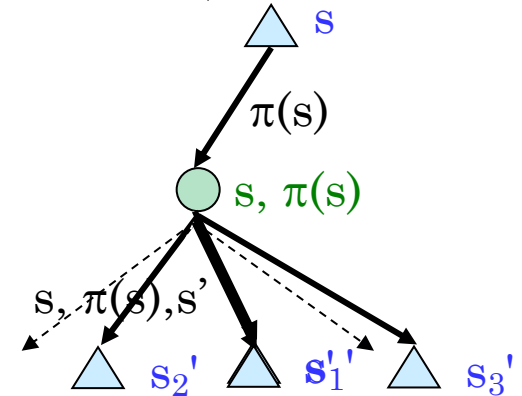
$$sample_1 = R(s, \pi(s), s'_1) + \gamma V_k^{\pi}(s'_1)$$

$$sample_2 = R(s, \pi(s), s'_2) + \gamma V_k^{\pi}(s'_2)$$

...

$$sample_n = R(s, \pi(s), s'_n) + \gamma V_k^{\pi}(s'_n)$$

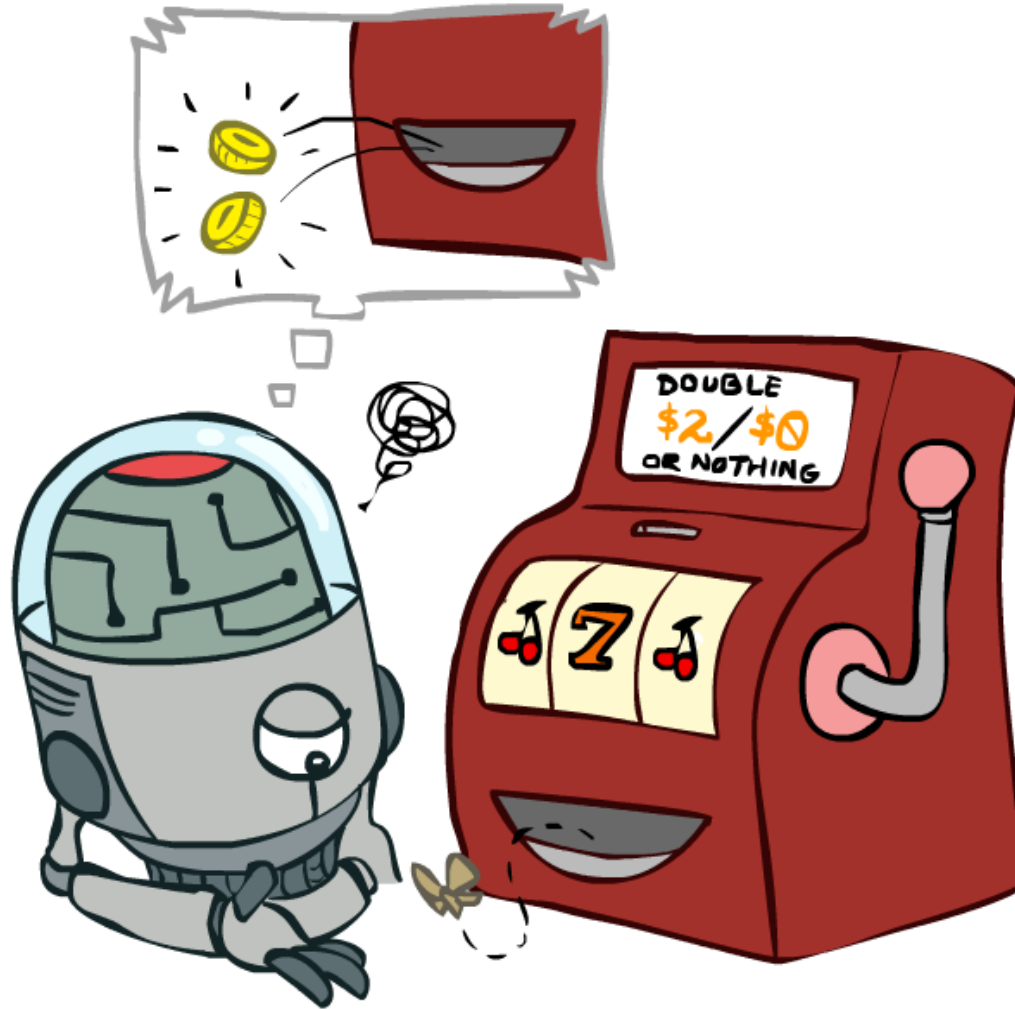
$$V_{k+1}^{\pi}(s) \leftarrow \frac{1}{n} \sum_i sample_i$$



*Almost! But we can't
rewind time to get
sample after sample
from state s .*

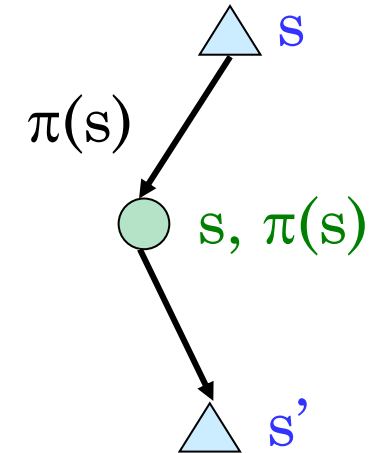


Temporal Difference Learning



Temporal Difference Learning

- Big idea: learn from every experience!
 - Update $V(s)$ each time we experience a transition (s, a, s', r)
 - Likely outcomes s' will contribute updates more often
- Temporal difference learning of values
 - Policy still fixed, still doing evaluation!
 - Move values toward value of whatever successor occurs: running average



Sample of $V(s)$: $sample = R(s, \pi(s), s') + \gamma V^\pi(s')$

Update to $V(s)$: $V^\pi(s) \leftarrow (1 - \alpha)V^\pi(s) + (\alpha)sample$

Same update: $V^\pi(s) \leftarrow V^\pi(s) + \alpha(sample - V^\pi(s))$



Exponential Moving Average

- Exponential moving average

- The running interpolation update: $\bar{x}_n = (1 - \alpha) \cdot \bar{x}_{n-1} + \alpha \cdot x_n$

- Makes recent samples more important:

$$\bar{x}_n = \frac{x_n + (1 - \alpha) \cdot x_{n-1} + (1 - \alpha)^2 \cdot x_{n-2} + \dots}{1 + (1 - \alpha) + (1 - \alpha)^2 + \dots}$$

- Forgets about the past (distant past values were wrong anyway)

- Decreasing learning rate (alpha) can give converging averages



Example: Temporal Difference Learning

States

| | | |
|---|---|---|
| | A | |
| B | C | D |
| | E | |

Assume: $\gamma = 1$, $\alpha = 1/2$

Observed Transitions

B, east, C, -2

| | | |
|---|---|---|
| | 0 | |
| 0 | 0 | 8 |
| | 0 | |

C, east, D, -2

| | | |
|----|---|---|
| | 0 | |
| -1 | 0 | 8 |
| | 0 | |

| | | |
|----|---|---|
| | 0 | |
| -1 | 3 | 8 |
| | 0 | |

$$V^\pi(s) \leftarrow (1 - \alpha)V^\pi(s) + \alpha [R(s, \pi(s), s') + \gamma V^\pi(s')]$$



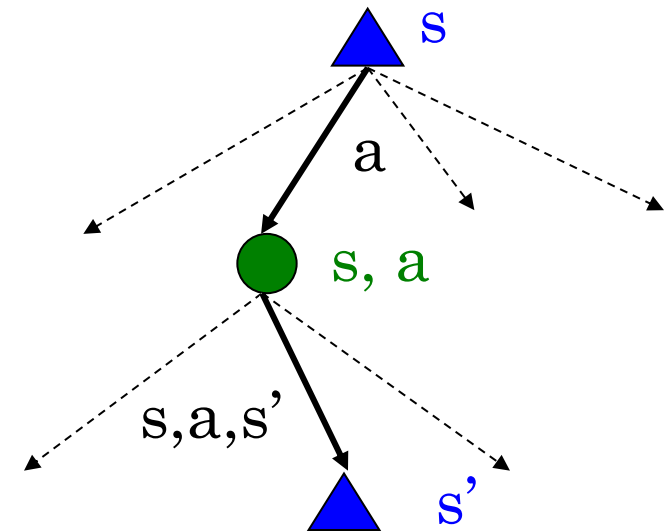
Problems with TD Value Learning

- TD value learning is a model-free way to do policy evaluation, mimicking Bellman updates with running sample averages
- However, if we want to turn values into a (new) policy, we're sunk:

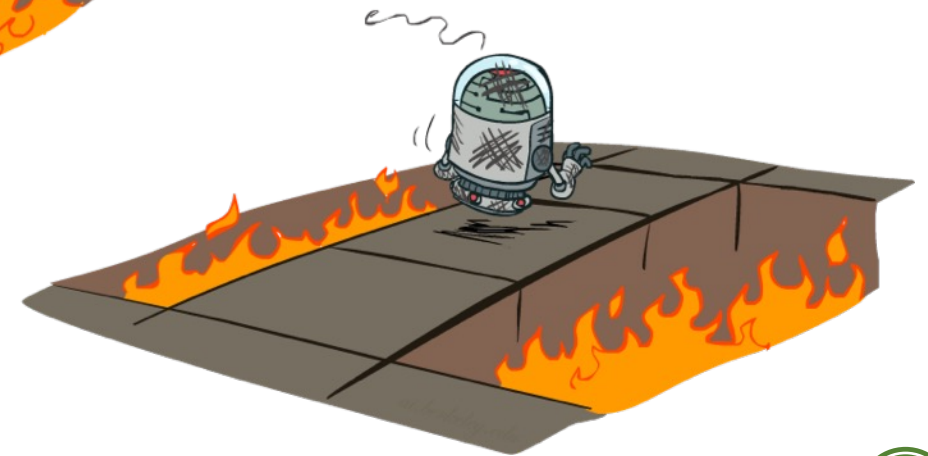
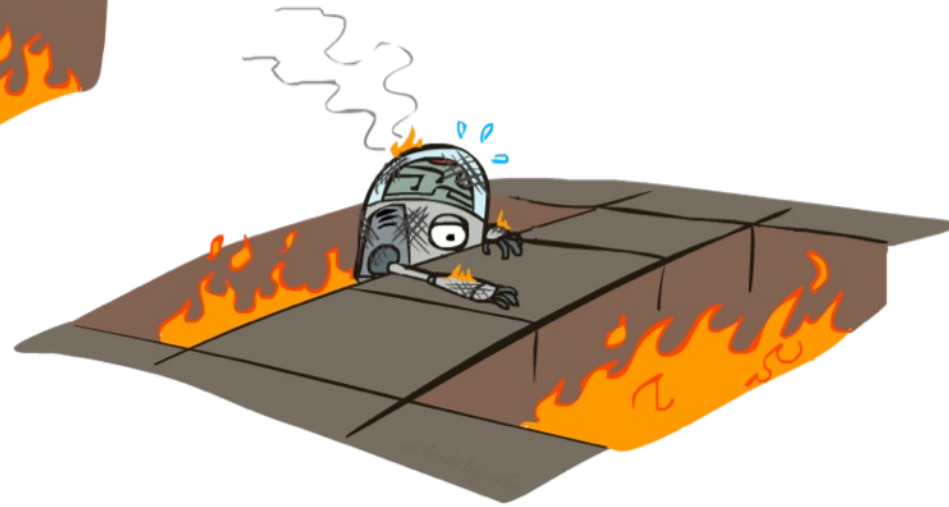
$$\pi(s) = \arg \max_a Q(s, a)$$

$$Q(s, a) = \sum_{s'} T(s, a, s') [R(s, a, s') + \gamma V(s')]$$

- Idea: learn Q-values, not values
- Makes action selection model-free too!

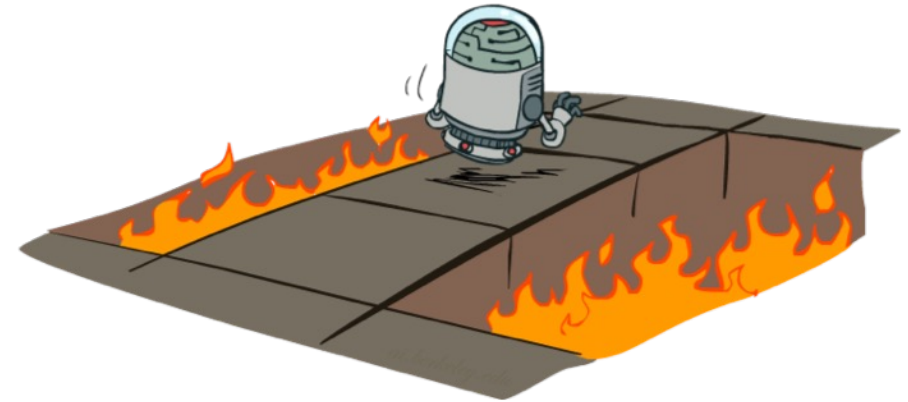


Active Reinforcement Learning



Active Reinforcement Learning

- Full reinforcement learning: optimal policies (like value iteration)
 - You don't know the transitions $T(s,a,s')$
 - You don't know the rewards $R(s,a,s')$
 - You choose the actions now
 - **Goal: learn the optimal policy / values**
- In this case:
 - Learner makes choices!
 - Fundamental tradeoff: exploration vs. exploitation
 - This is NOT offline planning! You actually take actions in the world and find out what happens...



Detour: Q-Value Iteration

- Value iteration: find successive (depth-limited) values
 - Start with $V_0(s) = 0$, which we know is right
 - Given V_k , calculate the depth $k+1$ values for all states:

$$V_{k+1}(s) \leftarrow \max_a \sum_{s'} T(s, a, s') [R(s, a, s') + \gamma V_k(s')]$$

- But Q-values are more useful, so compute them instead
 - Start with $Q_0(s,a) = 0$, which we know is right
 - Given Q_k , calculate the depth $k+1$ q-values for all q-states:

$$Q_{k+1}(s, a) \leftarrow \sum_{s'} T(s, a, s') [R(s, a, s') + \gamma \max_{a'} Q_k(s', a')]$$

