## Bayes Rule

Two ways to factor a joint distribution over two variables:

$$P(x,y) = P(x|y)P(y) = P(y|x)P(x)$$

That's my rule!

• Dividing, we get:

$$P(x|y) = \frac{P(y|x)}{P(y)}P(x)$$

- Why is this at all helpful?
- Lets us build one conditional from its reverse
- Often one conditional is tricky but the other one is simple

In the running for most important AI equation!





## •Given:

## P(D|W)

	Ь	8.0	0.2
P(W	R	sun	rain

Ь	0.1	0.0	0.7	0.3
W	sun	sun	rain	rain
D	wet	dry	wet	dry

What is P(W | dry)?

## Inference with Bayes' Rule

• Example: Diagnostic probability from causal probability:

$$P(\text{cause}|\text{effect}|) = \frac{P(\text{effect}|\text{cause})P(\text{cause})}{P(\text{effect})}$$

Example:

• M: meningitis, S: stiff neck

$$P(+m) = 0.0001$$
  
 $P(+s|+m) = 0.8$  Example  $P(+s|-m) = 0.01$ 

$$P(+m|+s) = \frac{P(+s|+m)P(+m)}{P(+s)} = \frac{P(+s|+m)P(+m)}{P(+s|+m)P(+m) + P(+s|-m)P(-m)} = \frac{0.8 \times 0.0001}{0.8 \times 0.0001 + 0.01 \times 0.999}$$

- Note: posterior probability of meningitis still very small
- Note: you should still get stiff necks checked out! Why?