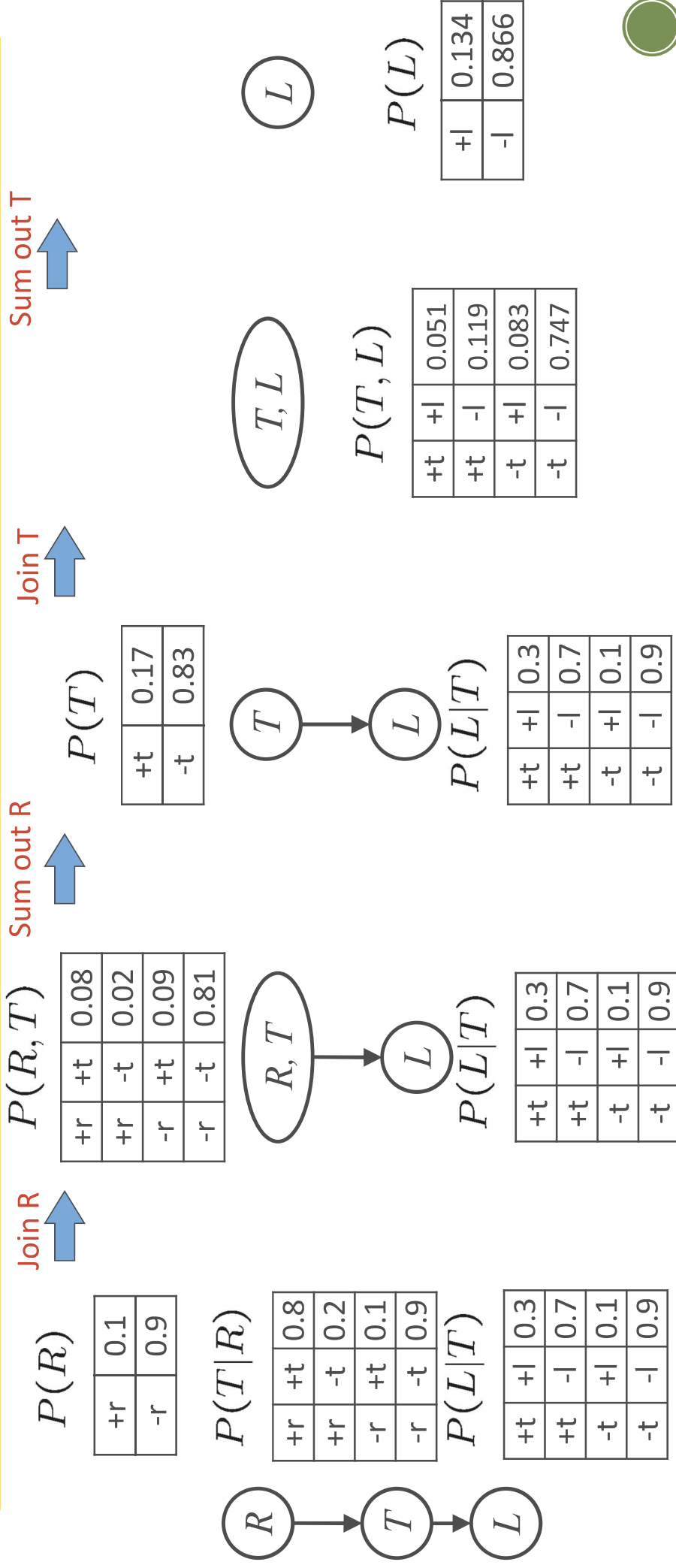


Marginalizing Early! (aka VE)



Evidence

- If evidence, start with factors that select that evidence
 - No evidence uses these initial factors:

$$P(R)$$

+r	0.1
-r	0.9

$$P(T|R)$$

+r	+t	0.8
+r	-t	0.2
-r	+t	0.1
-r	-t	0.9

$$P(L|T)$$

+t	+l	0.3
+t	-l	0.7
-t	+l	0.1
-t	-l	0.9

- Computing $P(L|+r)$ the initial factors become:

$$P(+r)$$

+r	0.1
----	-----

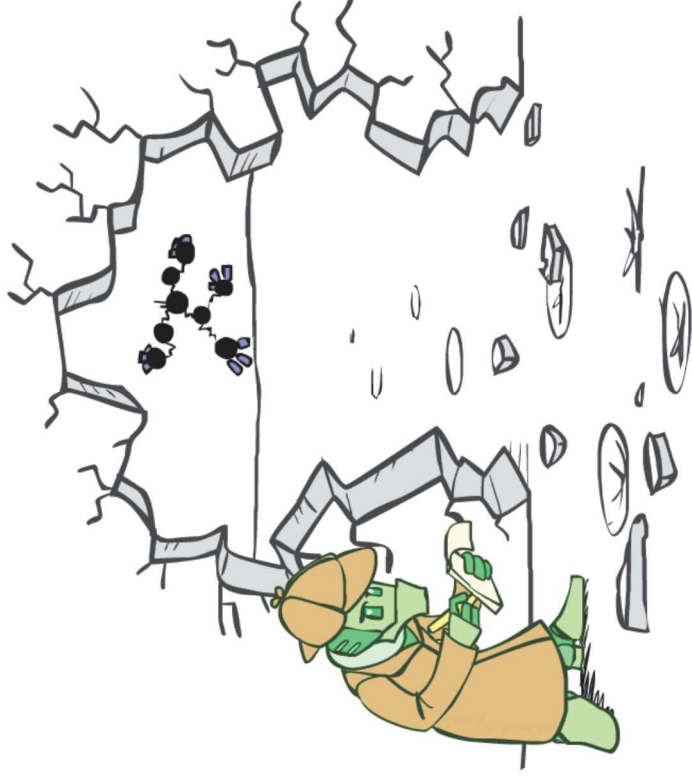
$$P(T|+r)$$

+r	+t	0.8
+r	-t	0.2

$$P(L|T)$$

+t	+l	0.3
+t	-l	0.7
-t	+l	0.1
-t	-l	0.9

- We eliminate all vars other than query + evidence



Evidence II

- Result will be a selected joint of query and evidence
 - E.g. for $P(L \mid +r)$, we would end up with:

$$P(+r, L)$$

+r	+l	0.026
+r	-l	0.074

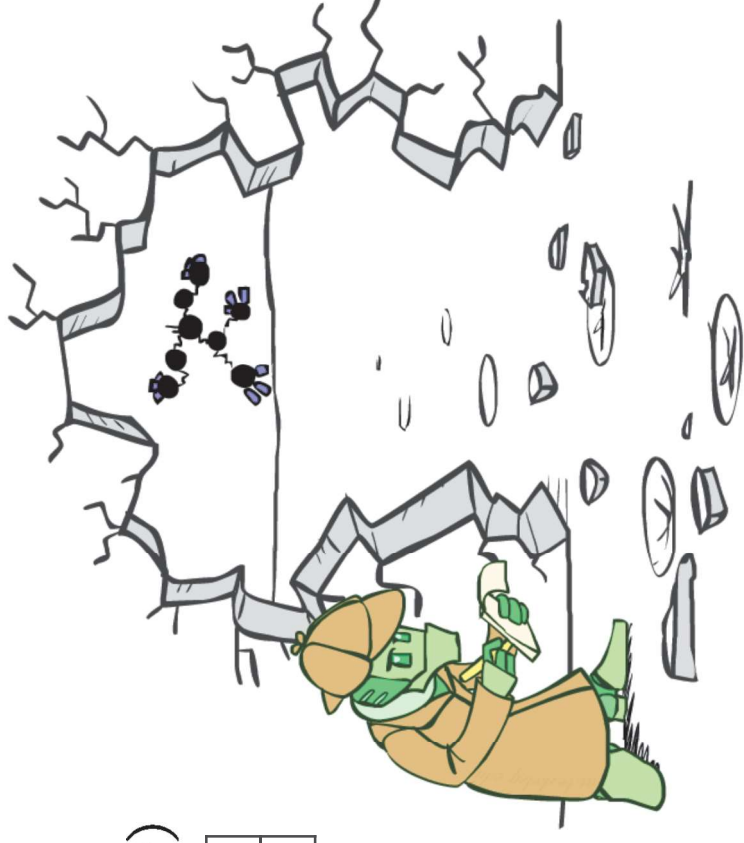
Normalize



$$P(L \mid +r)$$

+l	0.26
-l	0.74

- To get our answer, just normalize this!
- That's it!

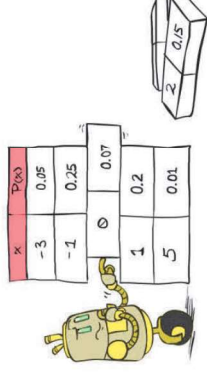


General Variable Elimination

- Query: $P(Q|E_1 = e_1, \dots, E_k = e_k)$

- Start with initial factors:

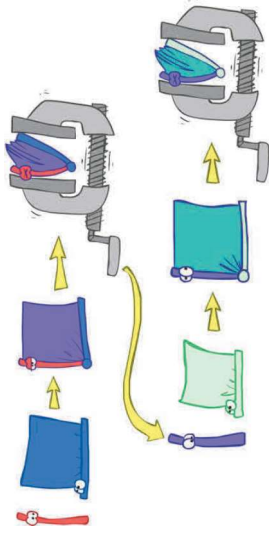
- Local CPTs (but instantiated by evidence)



x	P(x y)
-3	0.05
-1	0.25
0	0.07
1	0.2
5	0.01

- While there are still hidden variables (not Q or evidence):

- Pick a hidden variable H
 - Join all factors mentioning H
 - Eliminate (sum out) H



- Join all remaining factors and normalize

$$\left(\text{factors} \right) \times \frac{1}{Z}$$

