

Examining Treatment Strategies for Cholera Incorporating Spatial Dynamics

Group: Plague Doctors

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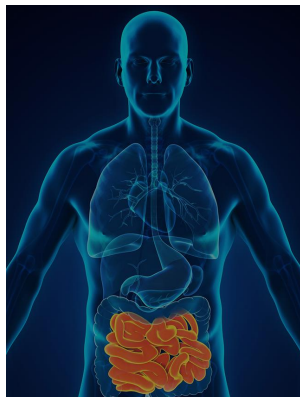
Instructor: Dr. David Earn

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- Treatments have not always gone as planned in history
- Cholera

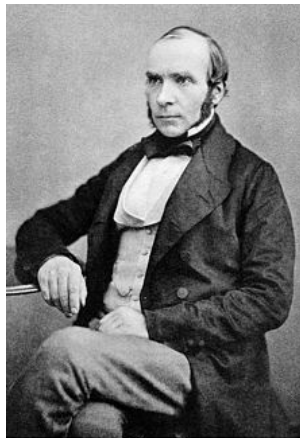
Some Biology on Cholera

- *Vibrio cholerae*
- Colonize small intestines
- 10
- Causes dehydration



Outbreaks in London (19th Century)

- 1832, 1849, 1854, 1866
- Miasma Theory
- John Snow



John Snow

Single-Patch Model

- Entire population (N) included
- 3 Compartments : S, I, R
- Compartment values are proportional
- Environment (Water)

SIRW Model Assumptions

- Birth Rate = Natural Death Rate and is constant
- Homogenous susceptibility to cholera across population
- No waning immunity
- No latency period
- Only infected individuals can infect the water sources
- Water source is still

SIRW Model



SIWR Model Phase Portrait

- Using the method of Next Generation Matrix (van den Driessche and Watmough, 2002)

$$F = \begin{pmatrix} \beta_i & \beta_w \\ 0 & 0 \end{pmatrix}$$
$$V = \begin{pmatrix} \frac{1}{\gamma + \mu + \alpha} & 0 \\ \frac{1}{\gamma + \mu + \alpha} & \frac{1}{\sigma} \end{pmatrix}$$

- R_0 is computed as the spectral radius of FV^{-1} :

$$\begin{aligned} \mathcal{R}_0 &= \rho(FV^{-1}) \\ &= \frac{\beta_i + \beta_w}{\gamma + \mu} \end{aligned}$$

- Two equilibria:

① DFE: $(S, I, R) = (1, 0, 0)$

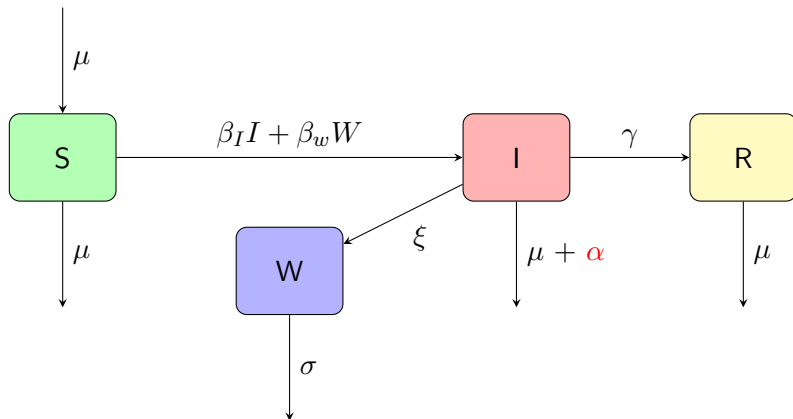
② EE: $(s^*, i^*, r^*) = (\frac{1}{R_0}, \frac{\mu}{\gamma + \mu}(1 - s^*), i^*)$

- The DFE is stable when $\mathcal{R}_0 < 1$
- The EE is stable when $\mathcal{R}_0 > 1$

Final Size

Effect of the 19th Century Treatments

- Added parameter death caused by cholera (α)



Effect of the 19th Century Treatments

Multi-Patch Model

Multi-Patch Model Assumptions

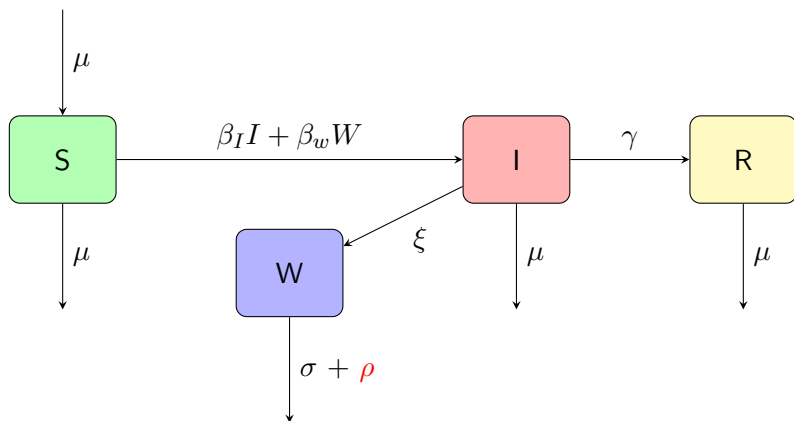
- No dispersal of individuals
- Infected individuals can infect the susceptible in neighboring patches
- All patches neighbouring i have the same transmission rate to patch i

Multi-Patch Model Simulation

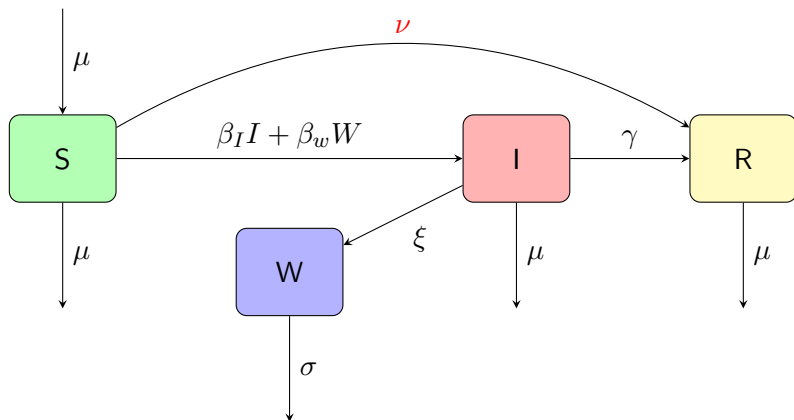
Treatment Strategies For Cholera

- 1 Sanitation of Water
- 2 Vaccinations
- 3 Antibiotics

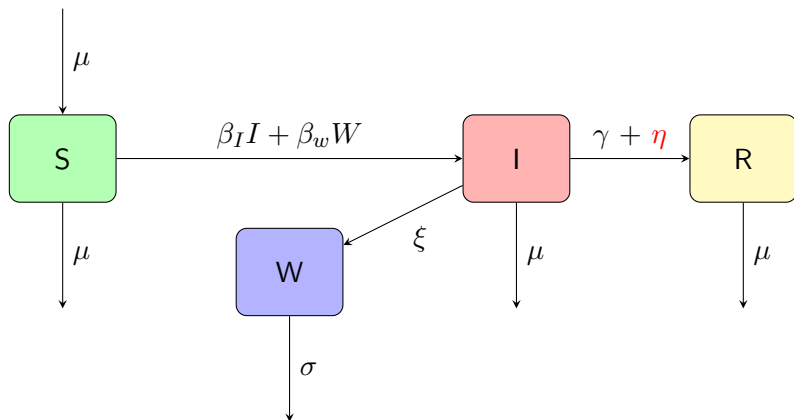
Sanitation of Water



Vaccinations



Antibiotics



Comparing the Treatment Strategies

Comparing the Treatment Strategies

Conclusions and Further Research

- 19th century outbreaks
- Significance of the using multi-patch model
- Our treatment simulations suggest. . .
- Further research on the spread of water borne diseases like cholera can be done in areas like. . .

Thank you!