

$$U_s = I_1 R = 100 \text{ V}$$

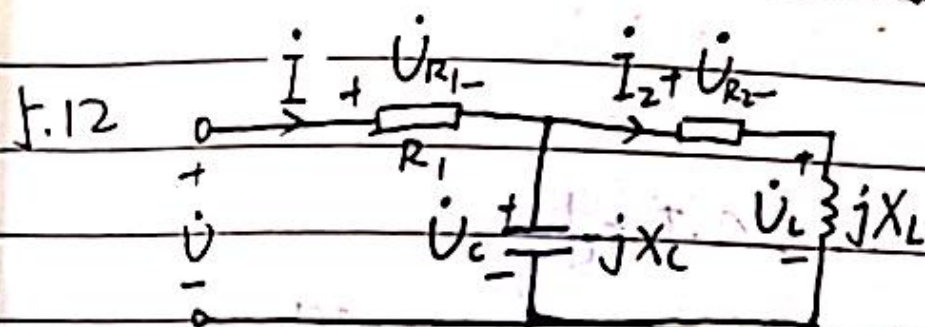
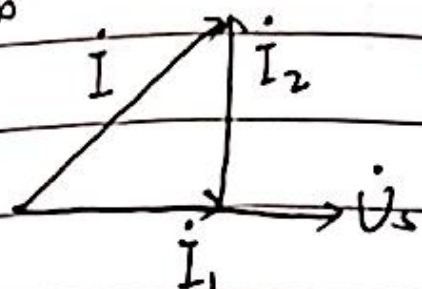
以 \dot{U}_s 为参考相量

\dot{I}_1 与 \dot{U}_s 同相

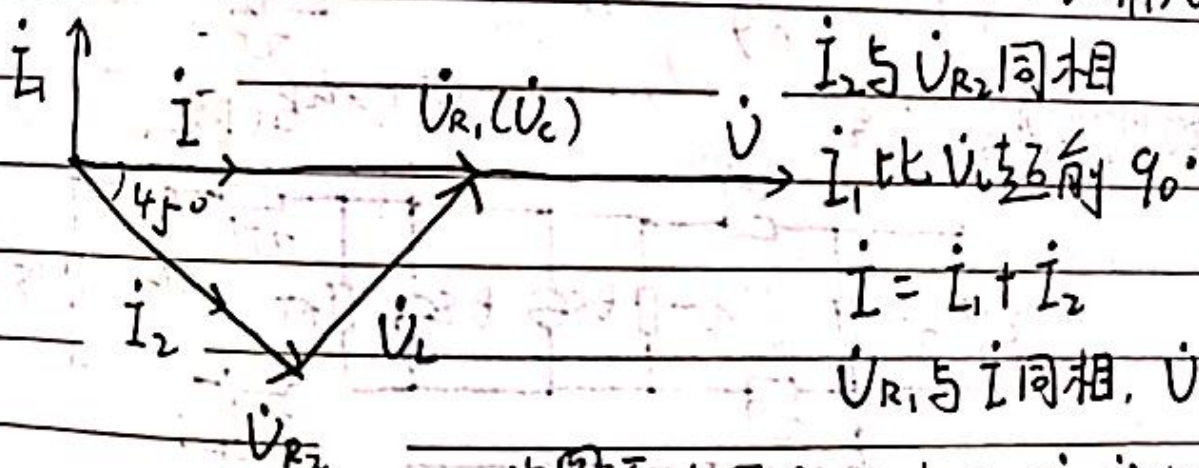
\dot{I}_2 比 \dot{U}_s 超前 90°

$$\dot{I} = \dot{I}_1 + \dot{I}_2$$

$$I = 10\sqrt{2} \text{ A}$$



\dot{U}_C 为参考相量: $\dot{U}_{R_2} + \dot{U}_L = \dot{U}_C$ 且 $U_{R_2} = U_L$, \dot{U}_C 比 \dot{U}_{R_2} 超前一个锐角, \dot{U}_{R_2} 与 \dot{U}_L 正交



\dot{I}_2 与 \dot{U}_{R_2} 同相

\dot{I}_1 比 \dot{U}_C 超前 90°

$$\dot{I} = \dot{I}_1 + \dot{I}_2$$

$$\dot{U}_{R_1} \text{ 与 } \dot{I} \text{ 同相, } \dot{U} = \dot{U}_{R_1} + \dot{U}_C$$

由图 $I_2 = 10\sqrt{2} \text{ A}$, $I_1 = 10 \text{ A}$, $\angle \dot{I}_1, \dot{I}_2 = 135^\circ$, 故 $I = 10 \text{ A}$

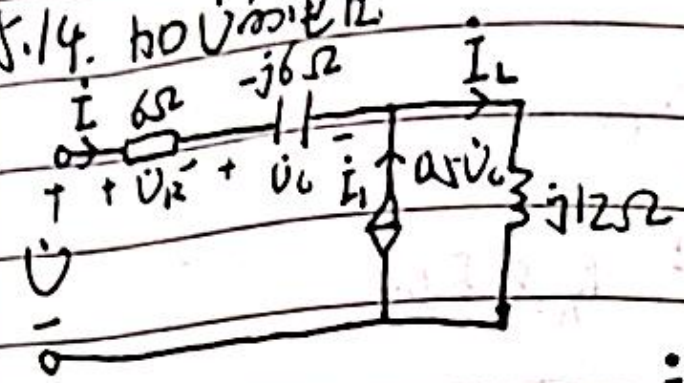
$$U_{R_1} = I R_1 = 100 \text{ V} \quad \angle \dot{U}, \dot{U}_{R_1} = 0^\circ \quad U_C = 100 \text{ V}$$

故: $\dot{U}_C = 100 \angle 0^\circ \text{ V}$ $\dot{U}_{R_1} = 100 \angle 0^\circ \text{ V}$ $\dot{U} = 200 \angle 0^\circ \text{ V}$

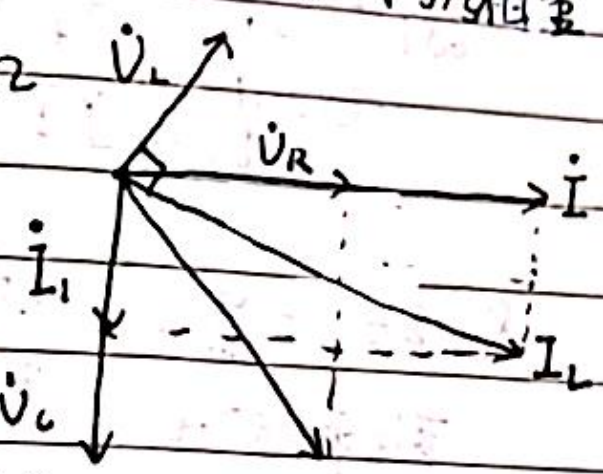
$$\dot{I} = 10 \angle 0^\circ \text{ A} \quad \dot{I}_1 = 10 \angle 90^\circ \text{ A} \quad \dot{I}_2 = 10\sqrt{2} \angle -45^\circ \text{ A}$$

$$\dot{U}_{R_2} = 50\sqrt{2} \angle -45^\circ \text{ V} \quad \dot{U}_L = 50\sqrt{2} \angle 45^\circ \text{ V}$$

5.14. 求 \dot{U} 的电压



以 $\dot{I} = I \angle 0^\circ$ 为参考相量



$$\dot{U}_R = 6\dot{I} = 6I \angle 0^\circ$$

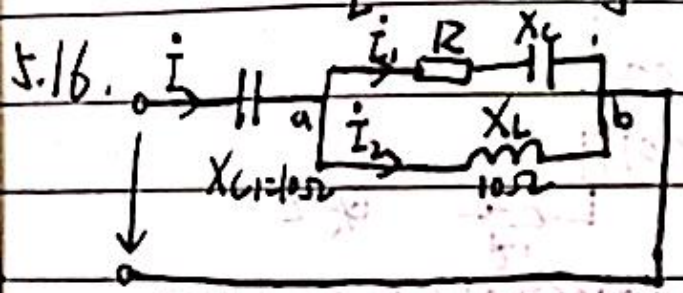
$$\dot{U}_C = -j6 \cdot \dot{I} = 6I \angle -90^\circ$$

$$\dot{I}_L = 0.5\dot{U}_C + \dot{I} = 3I \angle 90^\circ + I \angle 0^\circ = -3Ij + I$$

$$\dot{U}_L = \dot{I}_L \cdot 12j = 36I + 12Ij$$

$$\dot{U} = \dot{U}_R + \dot{U}_C + \dot{U}_L = 6I - 6Ij + 36I + 12Ij = 42I + 6Ij$$

$$Z = \frac{\dot{U}}{\dot{I}} = (42 + 6j) \Omega$$



$$\dot{I} = 5 \angle 45^\circ (A) \quad U = 50\sqrt{2} \angle 0^\circ (V)$$

$$U_C = \dot{I}(-10j) = (25\sqrt{2} - 25\sqrt{2}j) V$$

$$U_{ab} = U - U_C = (25\sqrt{2} + 25\sqrt{2}j) V$$

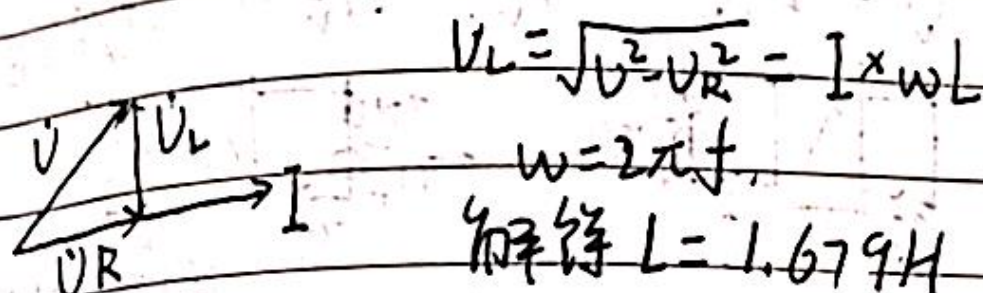
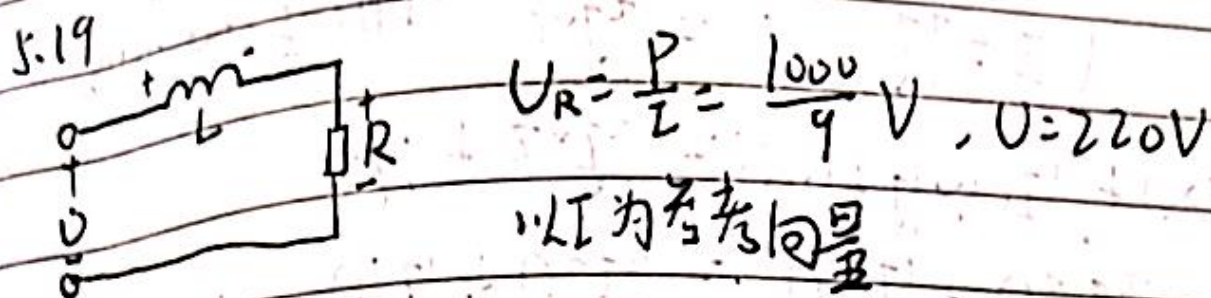
$$\dot{I}_2 = \frac{U_{ab}}{10j} = (\frac{5\sqrt{2}}{2} - \frac{5\sqrt{2}}{2}j) V$$

$$\dot{I}_1 = \dot{I} - \dot{I}_2 = 5\sqrt{2}j V$$

$$U_{ab} = \dot{I}_1 R + \dot{I}_1 (-X_C j) = 5\sqrt{2}Rj + 5\sqrt{2}X_C = 25\sqrt{2} + 25\sqrt{2}j$$

由实部相等, 虚部相等

$$R = 5\Omega \quad X_C = 5\Omega$$



5.18 复数功率 $\tilde{S} = \dot{U} \dot{I}^* = 30 \angle 45^\circ \times 10 \angle -15^\circ$

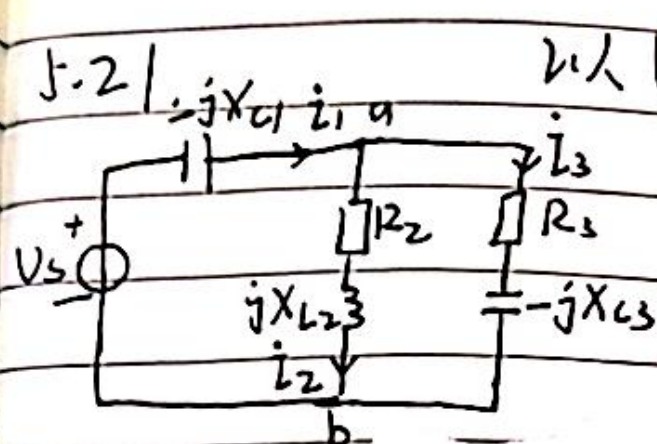
$= 300 \angle 30^\circ = 150j + 150\sqrt{3} \text{ VA}$

有功 $P = 150\sqrt{3} \text{ W}$

无功 $Q = 150 \text{ VAR}$

视在 $S = \sqrt{P^2 + Q^2} = 300 \text{ VA}$

5.2

以 \dot{U}_s 为参考相量 $\dot{U}_s = 20 \angle 0^\circ \text{ V}$

$$\dot{I}_1 = \frac{\dot{U}_s}{-jX_{L1} + (R_2 + jX_{L2}) / (R_3 - jX_{C3})}$$

$$= 3.0 + 1.98j$$

$$\tilde{S}_{L1} = \dot{I}_1 \cdot \bar{\dot{I}}_1 (-j) = -12.92j \text{ VA}$$

$$\dot{I}_2 = \dot{I}_1 \times \frac{R_2 - jX_{C3}}{R_2 + jX_{L2} + R_3 - jX_{C3}}$$

$$= 1.3 - 1.25j \text{ A}$$

$$\tilde{S}_{L2} = \dot{I}_2 \cdot \bar{\dot{I}}_2 (6 + 8j)$$

$$= 19.52 + 26.02j \text{ VA}$$

$$\tilde{S}_{L3} = 40.0 - 53.3j \text{ VA} \quad \dot{I}_3 = \dot{I}_1 - \dot{I}_2 = 1.7 + 3.23j \text{ A}$$

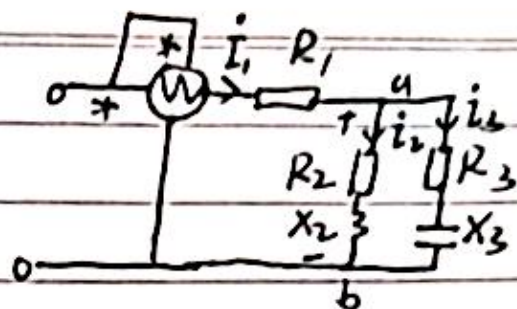
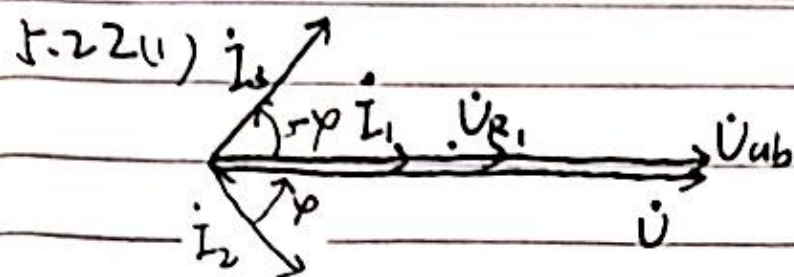
$$\tilde{S}_{L3} = \dot{I}_3 \cdot \bar{\dot{I}}_3 (3 - 4j)$$

$$= 40.0 - 53.3j \text{ VA}$$

电源

$$\tilde{S} = 60.0 - 39.6j \text{ VA}$$

$$\text{电源} \quad \tilde{S} = \dot{U}_s \bar{\dot{I}}_1 = 60.0 - 39.6j \text{ VA}$$



$$(2) P = UI_1 \cos 0^\circ \quad I_1 = 1A \quad I_1 = I_2 = I_3 = 1A$$

$$P = I_1^2 R_1 + I_2^2 R_2 + I_3^2 R_3$$

$$R_1 = R_2 = R_3 = 1\Omega \quad U_{ab} = U - I_1 R_1 = 2V$$

$$\text{由图} \quad X_3 = -\frac{U_{ab}}{I_3} \cos -60^\circ = \sqrt{3}\Omega$$

$$X_2 = \frac{U_{ab}}{I_2} \cos 60^\circ = \sqrt{3}\Omega$$

5.23. $\frac{1}{2} U_2$ 为参考同量 $I = \frac{P_2}{U_2 \cos \varphi_2} = 50.5A$

$$\dot{I} = 41.45 - j22.02A$$

$$\dot{U}_1 = Z_1 \dot{I} + \dot{U}_2$$

$$= 226.74 + j2.34j$$

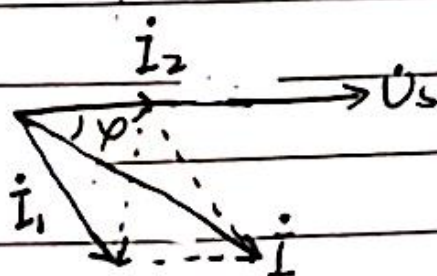
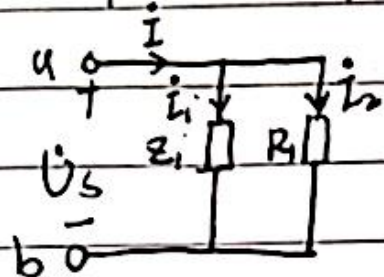
$$U_1 = 226.75V \quad \cos \alpha_1 = \frac{226.74}{226.75} \quad \sin \alpha_1 = \frac{2.34}{226.75}$$

$$\cos \alpha_1 = \cos (\alpha_1 + \varphi_2) = 0.895$$

$$P_1 = U_1 I \cos \alpha_1 \quad \eta = \frac{P_2}{P_1} = 0.976$$

$$\cos \alpha_1 = 0.895 \quad U_1 = 226.75V$$

5.24

以 U_S 为参考相量 $\dot{U}_S = 100 \angle 0^\circ \text{ V}$ 

$$\dot{i}_2 = \frac{\dot{U}_S}{R} = 5 \angle 0^\circ \text{ A} \quad \dot{i}_1 = 5 - 5\sqrt{3}j \text{ A}$$

$$\dot{i} = \dot{i}_1 + \dot{i}_2 = 10 - 5\sqrt{3}j \text{ A} \quad I = 0.5\sqrt{7} \text{ A} = 13.23 \text{ A}$$

$$\varphi = \varphi_u - \varphi_i = -\varphi_i$$

$$P = U_S I \cos \varphi = 1000 \text{ W} \quad \cos \varphi = \frac{10}{5\sqrt{7}} = 0.756$$

并联一个电容 $\dot{i}_C = I_C \angle 90^\circ$

$$\dot{i}' = \dot{i}_1 + \dot{i}_2 + \dot{i}_C = 10 + (-5\sqrt{3} + I_C)j$$

$$\sqrt{10^2 + (I_C - 5\sqrt{3})^2} = 11 \quad I_C = (\pm\sqrt{21} + 5\sqrt{3}) \text{ A}$$

$$I_C = \omega C \cdot U_S$$

由于 $5\sqrt{3} + \sqrt{21} > 5\sqrt{3} - \sqrt{21}$ 故选 $5\sqrt{3} - \sqrt{21}$ 电容最小。

$$\text{此时代入后 } C = \frac{I_C}{2\pi f \cdot U_S} = 129.8 \mu\text{F}$$

$$\cos \alpha' = \frac{10}{11} = 0.909$$