```
::= ALPHANUMERIC | *ALPHANUMERIC
                                                                                                                variables
                                                                                                          general labels
                                                                                                                    labels
    T
         ::= [t, \ldots]
                                                                                                                    stack
        ::= \langle \eta, \overset{\star}{\ell}, S \rangle
                                                                                                           stack\ frames
                                                                                                               programs
         ::= \ell : \hat{\ell} : d
                                                                                                                  clauses
         := x = e \mid \text{return } x \mid \text{goto } \ell \mid \text{goto } \ell \text{ if not } x
                                                                                                               directives
                 | raise x | catch x | pass
    B
         ::=
                \{x\mapsto m,\ldots\}
                                                                                                                bindings
   H
         ::= \{m \mapsto v, \ldots\}
                                                                                                                     heap
         ::= \mathbb{Z} \mid \mathbb{S} \mid [m,\ldots] \mid (m,\ldots) \mid B \mid F \mid M \mid *
                                                                                                                   values
         ::= \mathbb{Z} \mid \mathbb{S} \mid x \mid \det x(x,\ldots) = \{S\} \mid x(x,\ldots) \mid x.x \mid [x,\ldots] \mid (x,\ldots)
                                                                                                            expressions
    Y
         ::=
                 [y,\ldots]
                                                                                                       microcode\ stack
    Z
         ::= [z, \ldots]
                                                                                               microcode\ literal\ stack
                STORE | WRAP | BIND | LOOKUP | LIST n | TUPLE n
                                                                                               microcode\ instructions
        ::=
                 | Advance | Pop | Push S | Raise | Goto \ell | Gotoifn \ell
                  Call n | Convert n | Retrieve
                 ALLOCNAMEERROR ALLOCTYPEERROR ALLOCATTRERROR
        := x \mid m \mid v
    2.
                                                                                                     microcode\ literals
   \stackrel{\star}{m} ::= m \mid \eta \mid *
                                                                                           general memory locations
\eta, m
         ::= <address>
                                                                                                     memory locations
         ::= \langle \eta, \operatorname{def}(x, \ldots) \to S \rangle \mid \mathfrak{F} \mid \mathfrak{M}
    F
                                                                                                     general functions
   M
                \langle m, F \rangle
                                                                                                       general\ methods
\mathfrak{F},\mathfrak{M}
         ::= CallFunc | Type
                                                                                                       magic\ functions
    n
                                                                                                                 integers
```

Figure 1: Expression Grammar

Definition 0.1. *Initialization*

```
\begin{split} H_{\text{init}} &= \left\{ \eta_{\text{init}} \mapsto B_{\text{init}}, m_{\textit{None}} \mapsto \left\{ \; \right\}, m_{\textit{AttrError}} \mapsto \left\{ \; \right\}, m_{\textit{FunType}} \mapsto \left\{ \; \right\} \right\} \\ B_{\text{init}} &= \left\{ \star \textit{None} \mapsto m_{\textit{None}}, \text{AttributeError} \mapsto m_{\textit{AttrError}}, \text{FunctionType} \mapsto m_{\textit{FunType}} \right\} \\ t_{\text{init}} &= \left\langle \ell_{\text{init}}, S_{\text{init}} \right\rangle \\ T_{\text{init}} &= \left[ t_{\text{init}} \right] \\ \text{GetAttribute} &= \left\langle \eta, \; \textit{def} \left( o, a \right) \to \$1 = o.a; \right\rangle \\ \text{GetCall} &= \left\langle \eta, \; \textit{def} \left( f \right) \to \right\rangle \end{split}
```

("if \$1 == None then return getattribute(o._class_,a) else return \$1" - TC) (todo: add builtin mappings $m \mapsto F - TC$)

$$\begin{split} & m \notin H \qquad H' = H[m \mapsto v] \\ & Z \parallel [v, \operatorname{Store}] \parallel Y, T, H \longrightarrow^1 Z \parallel [m] \parallel Y, T, H' \end{split} \\ & W \cap H \qquad v = \operatorname{Getobj}(H, m) \\ & Z \parallel [m, \operatorname{Wrap}] \parallel Y, T, H \longrightarrow^1 Z \parallel [v] \parallel Y, T, H \end{split} \\ & \frac{B \cap H[\eta]}{Z \parallel [m, \operatorname{Wrap}]} \stackrel{B'}{\parallel} = B[x \mapsto m] \qquad H' = H[\eta \mapsto B'] \\ & \overline{Z \parallel [m, x, \operatorname{Bind}]} \parallel Y, T, H \longrightarrow^1 Z \parallel Y, T, H' \end{split} \\ & \frac{A \cap H[\eta]}{Z \parallel [m, x, \operatorname{Bind}]} \stackrel{A}{\parallel} = H[\eta] \stackrel{A}{\mapsto} H[\eta] \stackrel{A}$$

Figure 2: Microcommands

RAISE (NO EXCEPTION LABEL)
$$S(\ell) = \ell : * : d$$

$$\overline{Z \parallel [\text{Raise}] \parallel Y, [\langle \eta, \ell, S \rangle] \parallel T, H \longrightarrow^1 Z \parallel [\text{Pop, Raise}] \parallel Y, [\langle \eta, \ell, S \rangle] \parallel T, H}$$

$$\overline{Z \parallel [\text{Raise}] \parallel Y, [\langle \eta, \ell, S \rangle] \parallel T, H \longrightarrow^1 Z \parallel [\text{Pop, Raise}] \parallel Y, [\langle \eta, \ell, S \rangle] \parallel T, H}$$

$$S(\ell) = \ell : \ell_0 : d \qquad S(\ell_0) = \ell_0 : \ell_1 : \text{ catch } x \qquad Y' = [x, \text{Bind, Advance}]$$

$$Z \parallel [\text{Raise}] \parallel Y, [\langle \eta, \ell, S \rangle] \parallel T, H \longrightarrow^1 Z \parallel Y' \parallel Y, [\langle \eta, \ell_0, S \rangle] \parallel T, H$$

$$GOTO \ell$$

$$S(\ell) = \ell : \ell' : d$$

$$\overline{Z \parallel [\text{GOTO} \ell] \parallel Y, [\langle \eta, \ell', S \rangle] \parallel T, H \longrightarrow^1 Z \parallel Y, [\langle \eta, \ell, S \rangle] \parallel T, H}$$

$$GOTOIFN \ell (\text{SUCCESS})$$

$$\frac{H[m] = \text{False} \qquad S(\ell) = \ell : \ell' : d$$

$$\overline{Z \parallel [m, \text{GOTOIFN } \ell] \parallel Y, T, H \longrightarrow^1 Z \parallel [\text{GOTO } \ell] \parallel Y, T, H}$$

$$GOTOIFN \ell (\text{Fallure})$$

$$\frac{H[m] = \text{True}}{Z \parallel [m, \text{GOTOIFN } \ell] \parallel Y, T, H \longrightarrow^1 Z \parallel [\text{Advance}] \parallel Y, T, H}$$

$$Convert Function v$$

$$v = F$$

$$\overline{Z \parallel [v, m_1, \dots, m_n, \text{Convert } n] \parallel Y, T, H \longrightarrow^1 Z \parallel [v, m_1, \dots, m_n, \text{Call } n] \parallel Y, T, H}$$

$$Convert Method v$$

$$v = \langle m_0, F \rangle \qquad v' = F$$

$$\overline{Z \parallel [v, m_1, \dots, m_n, \text{Convert } n] \parallel Y, T, H \longrightarrow^1 Z \parallel [v', m_0, m_1, \dots, m_n, \text{Call } n+1] \parallel Y, T, H}$$

Figure 3: Microcommands (cont.)

$$CALL \ \text{FUNCTION} \ m \\ v = \langle \eta, \ \operatorname{def} \ (x_1, \dots, x_n) \to S \rangle \\ \underline{Y' = [\eta, \operatorname{PUSH} S, m_1, x_1, \operatorname{BIND}, \dots, m_n, x_n, \operatorname{BIND}]} \\ \overline{Z | | [v, m_1, \dots, m_n, \operatorname{Call} n] | | Y, T, H \longrightarrow^1 Z | | Y' | | Y, T, H} \\ CALL \ \text{FUNCTION} \ (\text{WRONG ARGS}) \\ v = \langle \eta, \ \operatorname{def} \ (x_1, \dots, x_q) \to S \rangle \qquad q \neq n \\ \overline{Z | | [v, m_1, \dots, m_n, \operatorname{Call} n] | | Y, T, H \longrightarrow^1 [\operatorname{AllocTypeError}, \operatorname{Raise}], T, H} \\ \frac{\operatorname{RETRIEVE} x}{Z | | [m, x, \operatorname{RETRIEVE}] | | Y, T, H \longrightarrow^1 Z | | [m'] | | Y, T, H} \\ \operatorname{RETRIEVE} x \ (\operatorname{ATTRIBUTEERROR}) \\ * = H[m][x] \\ \overline{Z | | [m, x, \operatorname{RETRIEVE}] | | Y, T, H \longrightarrow^1 [\operatorname{ALlocAttrError}, \operatorname{Raise}], T, H}$$

Figure 4: Microcommands (cont.)

Figure 5: Magic Functions

LITERAL ASSIGNMENT
$$S(\ell) = \ell : \ell' : x = e, e \text{ is of form } \mathbb{Z}, \mathbb{S}$$

$$\underline{v = e} \qquad Y = [v, \text{Store, Wrap, Store, } x, \text{Bind, Advance}]$$

$$[], [\langle \eta, \ell, S \rangle] || T, H \longrightarrow^1 Y, [\langle \eta, \ell, S \rangle] || T, H$$

$$(TODO: \textit{make literal category (ints, str, bool)} - TC)$$

$$Name \text{ Assignment}$$

$$\underline{S(\ell) = \ell : \ell' : x_1 = x_2} \qquad Y = [x_2, \text{Lookup, } x_1, \text{Bind, Advance}]$$

$$[], [\langle \eta, \ell, S \rangle] || T, H \longrightarrow^1 Y, [\langle \eta, \ell, S \rangle] || T, H$$

$$LIST \text{ Assignment}$$

$$S(\ell) = \ell : \ell' : x = [x_1, \dots, x_n]$$

$$Y = [(x_1, \text{Lookup}), \dots, (x_n, \text{Lookup}), \text{List } n, \text{Store, Wrap, Store, } x, \text{Bind, Advance}]$$

$$[], [\langle \eta, \ell, S \rangle] || T, H \longrightarrow^1 Y, [\langle \eta, \ell, S \rangle] || T, H$$

$$(Parentheses in Y group instructions together for convenience of reading. - TC)$$

$$Tuple \text{ Assignment}$$

$$S(\ell) = \ell : \ell' : x = [x_1, \dots, x_n]$$

$$Y = [(x_1, \text{Lookup}), \dots, (x_n, \text{Lookup}), \text{Tuple } n, \text{Store, Wrap, Store, } x, \text{Bind, Advance}]$$

$$[], [\langle \eta, \ell, S \rangle] || T, H \longrightarrow^1 Y, [\langle \eta, \ell, S \rangle] || T, H$$

$$FunctionDef \text{ Assignment}$$

$$S(\ell) = \ell : \ell' : x = \text{def } (x_1, \dots, x_n) = \{S'\} \qquad v = \langle \eta, \text{ def } (x_1, \dots, x_n) \to S' \rangle$$

$$Y = [v, \text{Store, Wrap, Store, } x, \text{Bind, Advance}]$$

$$[], [\langle \eta, \ell, S \rangle] || T, H \longrightarrow^1 Y, [\langle \eta, \ell, S \rangle] || T, H$$

$$Attribute \text{ Assignment}$$

$$S(\ell) = \ell : \ell' : x = x_1.x_2 \qquad Y = [x_1, \text{Lookup, } x_2, \text{ retrieve, } x, \text{ Bind, Advance}]$$

$$[], [\langle \eta, \ell, S \rangle] || T, H \longrightarrow^1 Y, [\langle \eta, \ell, S \rangle] || T, H$$

$$Call \text{ Assignment}$$

$$S(\ell) = \ell : \ell' : x = x_0.(x_1, \dots, x_n)$$

$$Y = [x_0, \text{Lookup, } \dots, x_n, \text{Lookup, Convert } n]$$

$$[], [\langle \eta, \ell, S \rangle] || T, H \longrightarrow^1 Y, [\langle \eta, \ell, S \rangle] || T, H$$

Figure 6: Operational Semantics: Assignment

$$S(\ell) = \ell : \stackrel{\star'}{\ell} : \mathbf{raise} \ x \qquad Y = [x, \mathsf{LookUP}, \mathsf{Raise}]$$

$$[], [\langle \eta, \ell, S \rangle] || T, H \longrightarrow^1 Y, [\langle \eta, \ell, S \rangle] || T, H$$

$$PASS$$

$$S(\ell) = \ell : \stackrel{\star'}{\ell} : \mathbf{pass} \qquad Y = [\mathsf{ADVANCE}]$$

$$[], [\langle \eta, \ell, S \rangle] || T, H \longrightarrow^1 Y, [\langle \eta, \ell, S \rangle] || T, H$$

$$RETURN$$

$$S(\ell) = \ell : \stackrel{\star'}{\ell} : \mathbf{return} \ x \qquad T = [\langle \eta', \ell'', S' \rangle] || T'$$

$$S(\ell'') = \ell'' : \stackrel{\star''}{\ell} : x' = e \qquad Y = [x, \mathsf{LookUP}, \mathsf{Pop}, x', \mathsf{Bind}, \mathsf{Advance}]$$

$$[], [\langle \eta, \ell, S \rangle] || T, H \longrightarrow^1 Y, [\langle \eta, \ell, S \rangle] || T, H$$

$$GOTO$$

$$S(\ell) = \ell : \stackrel{\star'}{\ell} : \mathsf{goto} \ \ell'' \qquad Y = [\mathsf{Goto} \ \ell'']$$

$$[], [\langle \eta, \ell, S \rangle] || T, H \longrightarrow^1 Y, [\langle \eta, \ell, S \rangle] || T, H$$

$$S(\ell) = \ell : \ell' : \mathsf{goto} \ \ell'' \quad \mathsf{if} \quad \mathsf{not} \ x \qquad Y = [x, \mathsf{LookuP}, \mathsf{GotoIfN} \ \ell'']$$

$$[], [\langle \eta, \ell, S \rangle] || T, H \longrightarrow^1 Y, [\langle \eta, \ell, S \rangle] || T, H$$

Raise

END OF FUNCTION

Figure 7: Operational Semantics: Flow

 $\frac{T = [\langle \eta, *, S \rangle]}{[\;], T, H \longrightarrow^{1} Y, T, H} Y = [PoP]$

 $\frac{t = \langle \eta', \ell, S' \rangle \qquad S(\ell) = \ell : \overset{\star'}{\ell} : x = e \qquad Y = [\text{Pop}, m_{\text{None}}, x, \text{Bind}, \text{Advance}]}{[\;], [\langle \eta, *, S \rangle, t] \, || \, T, H \longrightarrow^1 Y, [\langle \eta, *, S \rangle, t] \, || \, T, H}$

 $(m_{None} is a memory location reserved for None. - TC)$

End of Program

Definition 0.2.

LOOKUP
$$(H, \eta, x) = (todo - TC)$$

Definition 0.3.

$$H[m] = v, B_{obj} = \{ \star x_{value} \mapsto v, _getattribute_ \mapsto \mathfrak{Getattribute} \}$$

$$GetObj(H, m) = \begin{cases} B, & \text{if } v = B \\ B = B_{obj}[_class_ \mapsto \star_{\text{FUNTYPE}}], & \text{if } v = F \end{cases}$$

$$(1)$$

 $(getobj\ takes\ (H,m,memory\ location\ of\ getattribute)$ – TC)

Figure 8: Helper Functions