1 CoPylot

1.1 Grammar

The grammar of the language to be analyzed appears in Figure 2.

We assume throughout the rest of this document that a fixed program \hat{S} is under analysis. (TODO: describe here the idea of a bijection between labels and statements in this fixed program. – ZP)

1.2 Control Flow

The grammar of control flow graphs appears in Figure 3. (Discuss construction of initial graph. -ZP)

We write $\hat{o} \stackrel{?}{\blacktriangleleft} \hat{o}'$ to denote $(\hat{o} \blacktriangleleft \hat{o}' \in \hat{G} \text{ when } \hat{G} \text{ is understood from context.}$ Likewise, we write $\hat{o} \stackrel{?}{\ll} \hat{o}'$ to denote $(\hat{o} \ll \hat{o}' \in \hat{G} \text{ when } \hat{G} \text{ is understood from context.}$

We define a relation \longrightarrow 1 to perform control flow graph closure.

Definition 1.1. Let $\hat{G} \longrightarrow^1 \hat{G}'$ be the least relation satisfying the rules appearing in Figure 4. Throughout these rules, the predicates $\stackrel{?}{\ll}$ and $\stackrel{?}{\blacktriangleleft}$ refer to graph \hat{G} .

1.3 Value Lookup

The value lookup function uses the additional grammar in Figure 5.

Definition 1.2. Given a control-flow graph \hat{G} , let $\hat{G}(\hat{o}_0, \hat{K})$ be the function returning the least set \hat{V} which satisfies the following conditions:

1. Value Manipulation

(a) RESULT
If
$$\hat{K} = [\hat{v}]$$
, then $\hat{v} \in \hat{V}$.

2. Variable Lookup

(a) Value Discovery

If
$$\hat{o}_1 \overset{?}{\ll} \hat{o}_0$$
, $\hat{o}_1 = \hat{\ell}_1 : \hat{\ell}_2 : \hat{x} = \hat{v}$, and $\hat{K} = [\hat{x}] \mid\mid \hat{K}'$, then $\hat{G}(\hat{o}_1, [\hat{v}] \mid\mid \hat{K}') \subseteq \hat{V}$.

(b) VALUE SKIP

If
$$\hat{o}_1 \stackrel{?}{\ll} \hat{o}_0$$
, $\hat{o}_1 = \hat{\ell}_1 : \hat{\ell}_2 : \hat{x}' = \hat{v}$, $\hat{K} = [\hat{x}] || \hat{K}'$, and $\hat{x} \neq \hat{x}'$, then $\hat{G}(\hat{o}_1, \hat{K}) \subseteq \hat{V}$.

(c) Value Aliasing If
$$\hat{o}_1 \stackrel{?}{\ll} \hat{o}_0$$
, $\hat{o}_1 = \hat{\ell}_1 : \hat{\ell}_2 : \hat{x} = \hat{x}'$, and $\hat{K} = [\hat{x}] \mid\mid \hat{K}'$, then $\hat{G}(\hat{o}_1, [\hat{x}'] \mid\mid \hat{K}) \subseteq \hat{V}$

$$\begin{array}{c} \stackrel{*}{\ell} ::= \ell \mid \operatorname{End} \\ T ::= [\ell, \ldots] \\ t ::= [\ell \times S] \\ S ::= [s, \ldots] \\ d ::= x = \ell \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{return} x \\ d ::= x = \ell \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{return} x \\ d ::= x = \ell \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{return} x \\ d ::= x = \ell \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{return} x \\ d ::= x = \ell \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{return} x \\ d ::= x = \ell \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{return} x \\ d ::= x = \ell \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{return} x \\ d ::= \ell \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{return} x \\ d ::= \ell \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{return} x \\ d ::= \ell \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{return} x \\ d ::= \ell \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{return} x \\ d ::= \ell \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{return} x \\ d ::= \ell \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{return} x \\ d ::= \ell \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{return} x \\ d ::= \ell \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{return} x \\ d ::= \ell \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{return} x \\ d ::= \ell \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{return} x \\ d ::= \ell \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{return} x \\ d ::= \ell \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{return} x \\ d ::= \ell \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{return} x \\ d ::= \ell \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{return} x \\ d ::= \ell \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{def} x \mid \operatorname{def} x(x, \ldots) = \{S\} \mid \operatorname{def}$$

Figure 1: Operation Semantics

$$\begin{split} S(\ell) = \ell : \ell' : pass & \ell \overset{S}{\blacktriangleleft} \ell'' \\ \hline [\langle \ell, S \rangle] & || T, H, E, P, \eta \longrightarrow^1 [\langle \ell'', S \rangle] & || T, H, E, P, \eta \end{split}$$
 Return
$$\underbrace{S(\ell) = \ell : \ell' : return \qquad T = [t, \langle \ell'', S' \rangle] & || T' \qquad \eta' = P[\eta] \qquad \ell'' \overset{S'}{\blacktriangleleft} \ell'''}_{[t, \langle \ell'', S' \rangle] & || T, H, E, P, \eta \longrightarrow^1 [\langle \ell'', S' \rangle] & || T', H, E, P, \eta' \end{split}$$

$$S'(\ell'') = \ell'' : \ell''' : x_1 = x_2(x_3)$$
 $\eta' = P[\eta]$ $B = E(\eta')$ $B' = B[x_1 \mapsto m]$ $E' = E[\eta' \mapsto B']$

NAME STATEMENT

$$\frac{S(\ell) = \ell : \ell' : e \qquad \forall x \in e \exists B[x] \qquad \ell \overset{s'}{\blacktriangleleft} \ell''}{\left[\langle \ell, S \rangle \right] || T, H, E, P, \eta \longrightarrow^{1} \left[\langle \ell', S \rangle \right] || T, H, E, P, \eta}$$

END OF FUNCTION

$$\frac{T = \left[\left\langle \text{End}, S \right\rangle, \left\langle \ell, S' \right\rangle \right] || \ T' \qquad \eta' = P[\eta] \qquad \ell \overset{s'}{\blacktriangleleft} \ell'}{\left[\left\langle \text{End}, S \right\rangle, \left\langle \ell, S' \right\rangle \right] || \ T, H, E, P, \eta \longrightarrow^1 \left[\left\langle \ell', S' \right\rangle \right] || \ T', H, E, P, \eta'}$$

$$\begin{split} & \text{End of Program} \\ & T = [(\text{end}, t)] \\ & \overline{T, H, E, P, \eta \longrightarrow^1 [], H, E, P, \eta'} \end{split}$$

Figure 1: Operation Semantics (cont.)

Figure 2: Normalized Python Language Grammar

Figure 3: Control Flow Graph Grammar

Figure 4: Control Flow Graph Closure

$$\hat{K} ::= [\hat{k}, \ldots]$$
 lookup stacks $\hat{k} ::= \hat{x} \mid \hat{v} \mid \text{Capture}(\mathbb{N}) \mid \text{Jump}(\hat{o})$ lookup stack elements

Figure 5: Value Lookup Grammar