



Universidade Estadual de Londrina
Departamento de Computação
Programa de Mestrado em
Computação
Módulo 5 - processamento
morfológico de imagens

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Sumário

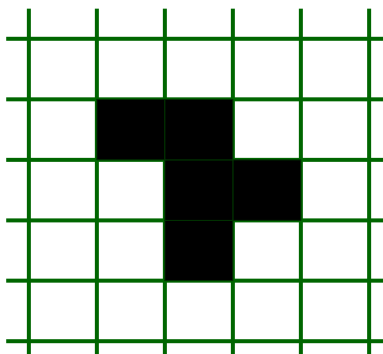
- Erosão e dilatação
- Operação de abertura e fechamento
- Detecção de borda, preenchimento de buracos
- Exercícios
- Referências Bibliográficas



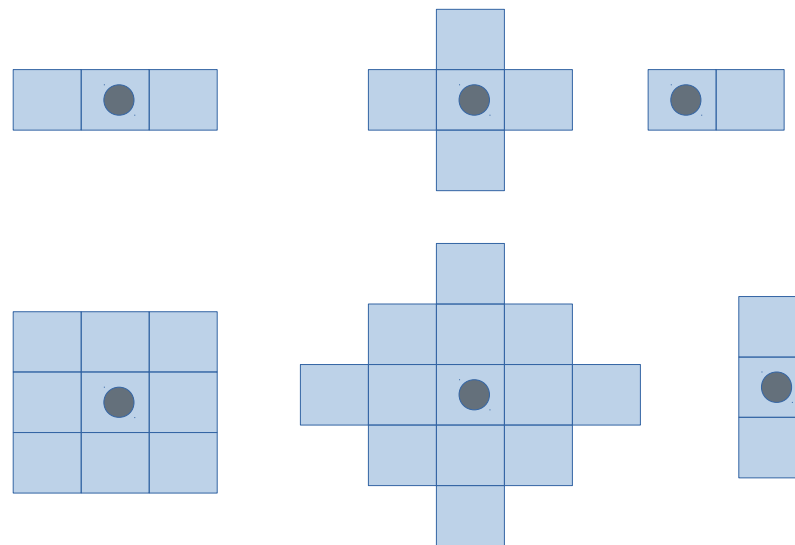
Morfologia Matemática

Morfologia- extrai informações relativas a geometria e a topologia de objetos contidos em uma imagem. Utiliza um elemento estruturante para extração das informações. Usa teoria de conjuntos como formalismo matemático.

Objeto de interesse



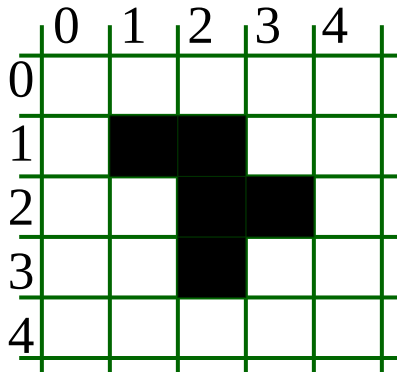
Elementos estruturantes



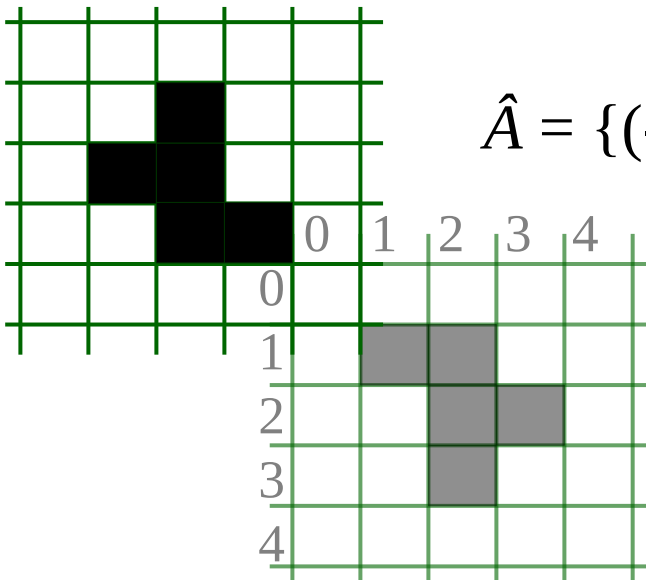


Reflexão

$$\hat{B} = \{w \mid w = -b, \text{ para } b \in B\}$$



$$A = \{(1,1), (1,2), (2,2), (3,2), (2,3)\}$$



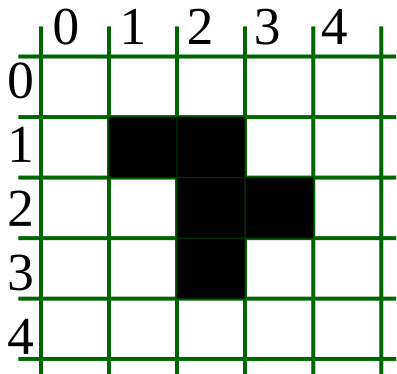
$$\hat{A} = \{(-1,-1), (-1,-2), (-2,-2), (-3,-2), (-2,-3)\}$$



Translação do conjunto B em relação a z

Dado $z = (z_1, z_2)$

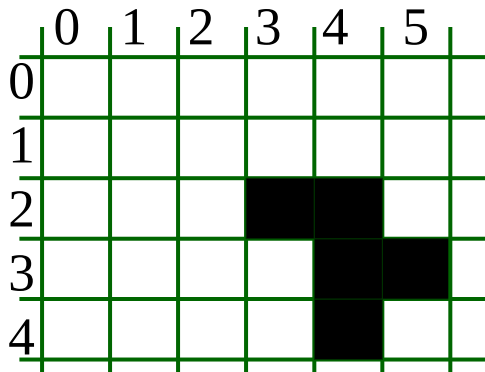
Ex:



$$(B)_z = \{c \mid c = b + z, \text{ para } b \in B\}$$

$$Z = (1, 2)$$

$$A = \{(1,1), (1,2), (2,2), (3,2), (2,3), \}$$

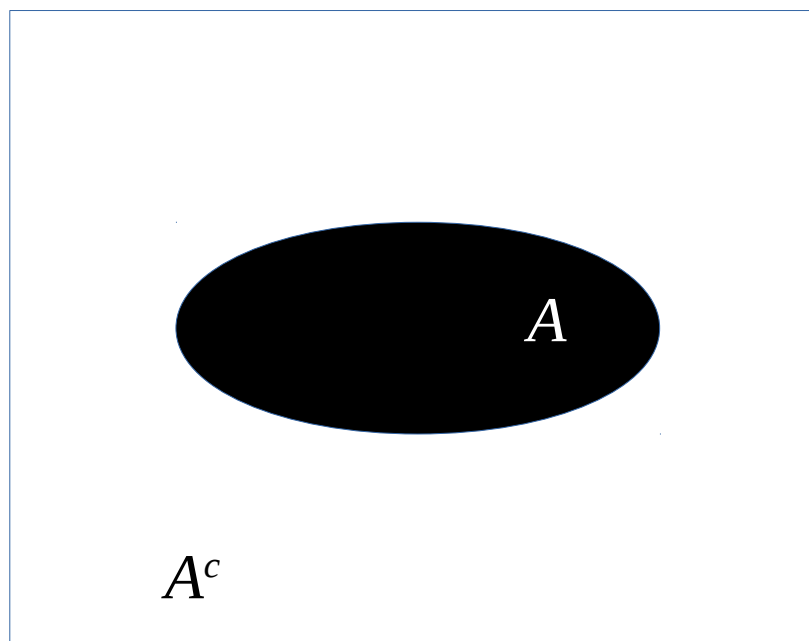


$$(A)_z = \{(2,3), (2,4), (3,4), (4,4), (3,5), \}$$



Complemento do Conjunto A

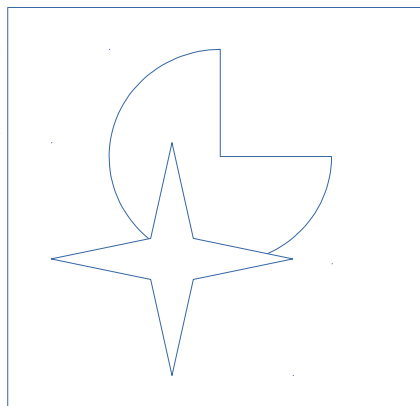
$$A^c = \{x \mid x \notin A\}$$



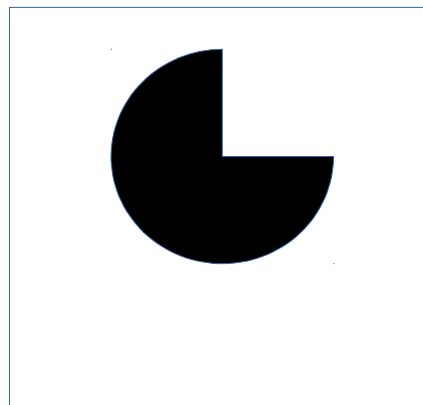


Diferença, entre A e B

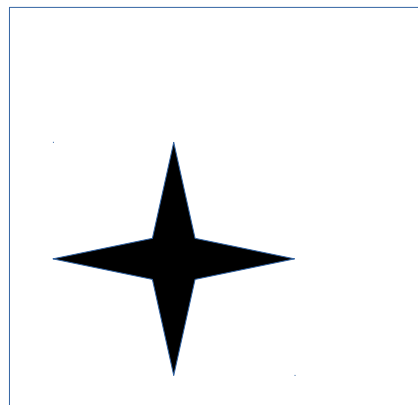
$$A - B = \{x \mid x \in A, x \notin B\} = A \cap B^c$$



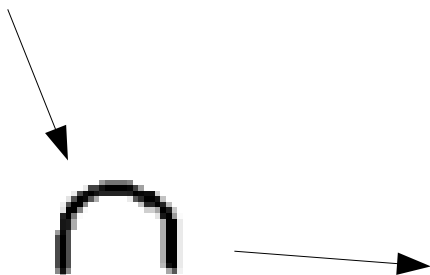
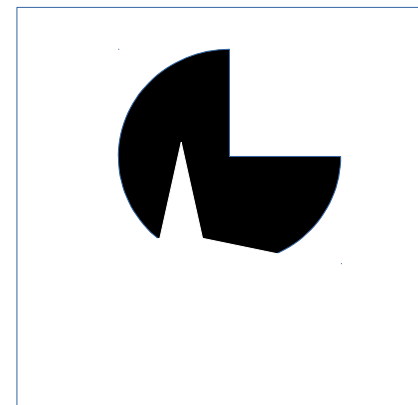
A



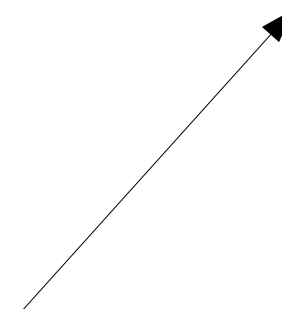
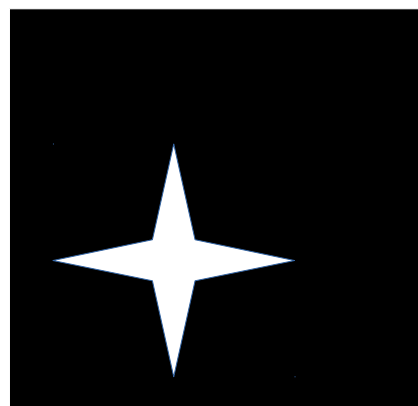
B



$A - B$



B^c

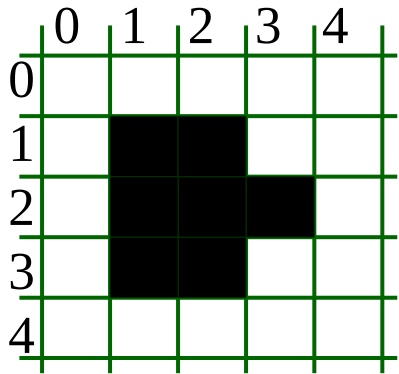




Erosão

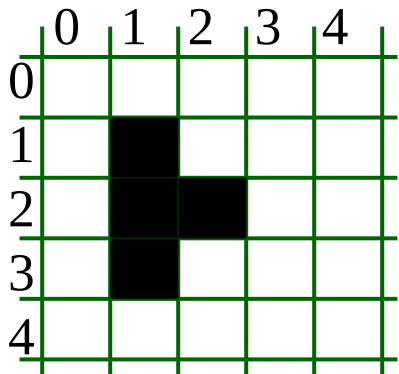
$$A \ominus B = \{z \mid (B)_z \subseteq A\}$$

B transladado por z está contido em a



$$A = \{(1,1), (1,2), (2,1), (2,2), (3,1), (3,2), (2,3)\}$$

$$B = \{(0,0), (0,1)\}$$

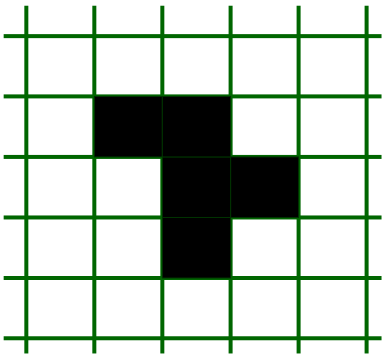


$$A \ominus B = ?$$

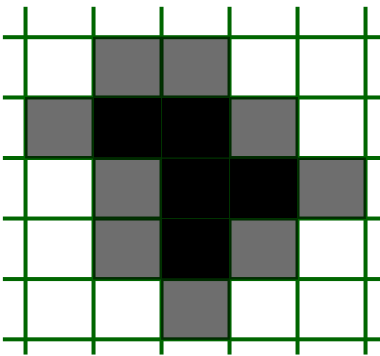
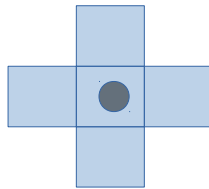


Dilatação

A



B



$$A \oplus B = \{z \mid (\hat{B})_z \cap A \neq \emptyset\}$$



Dualidade

$$(A \ominus B)^c = A^c \oplus \hat{B}$$

$$(A \oplus B)^c = A^c \ominus \hat{B}$$

Caso o elemento estruturante for simétrico então: $B = \hat{B}$

$$(A \ominus B)^c = A^c \oplus \hat{B}$$

Neste caso pode-se fazer a erosão pela dilatação do fundo da imagem utilizando o mesmo elemento estruturante.



Operação de Abertura

$$A \circ B = (A \ominus B) \oplus B$$

Duas operações:

Primeiro erosão depois dilatação com o mesmo elemento estruturante.

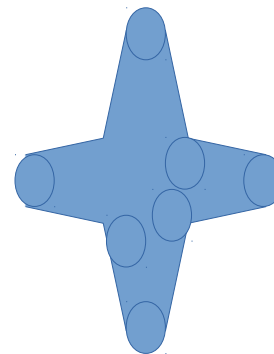
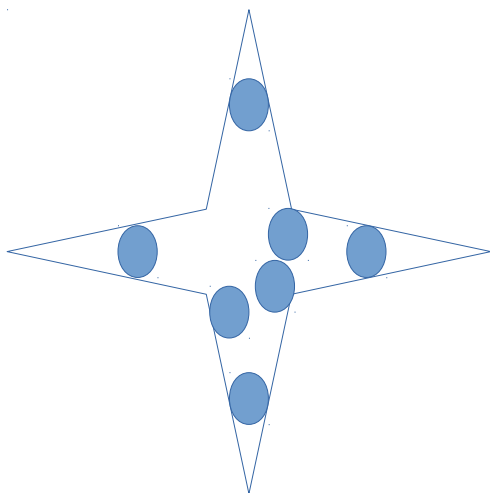
Elimina conjuntos de pixels menores que os Elementos estruturantes. Suaviza.

Elimina detalhes finos na imagem.



Interpretação Geométrica da operação de Abertura

$$A \circ B = \bigcup \{ (B)_x \mid (B)_x \subset A \}$$



Ajuste de B em A



Fechamento

$$A \bullet B = (A \oplus B) \ominus B$$

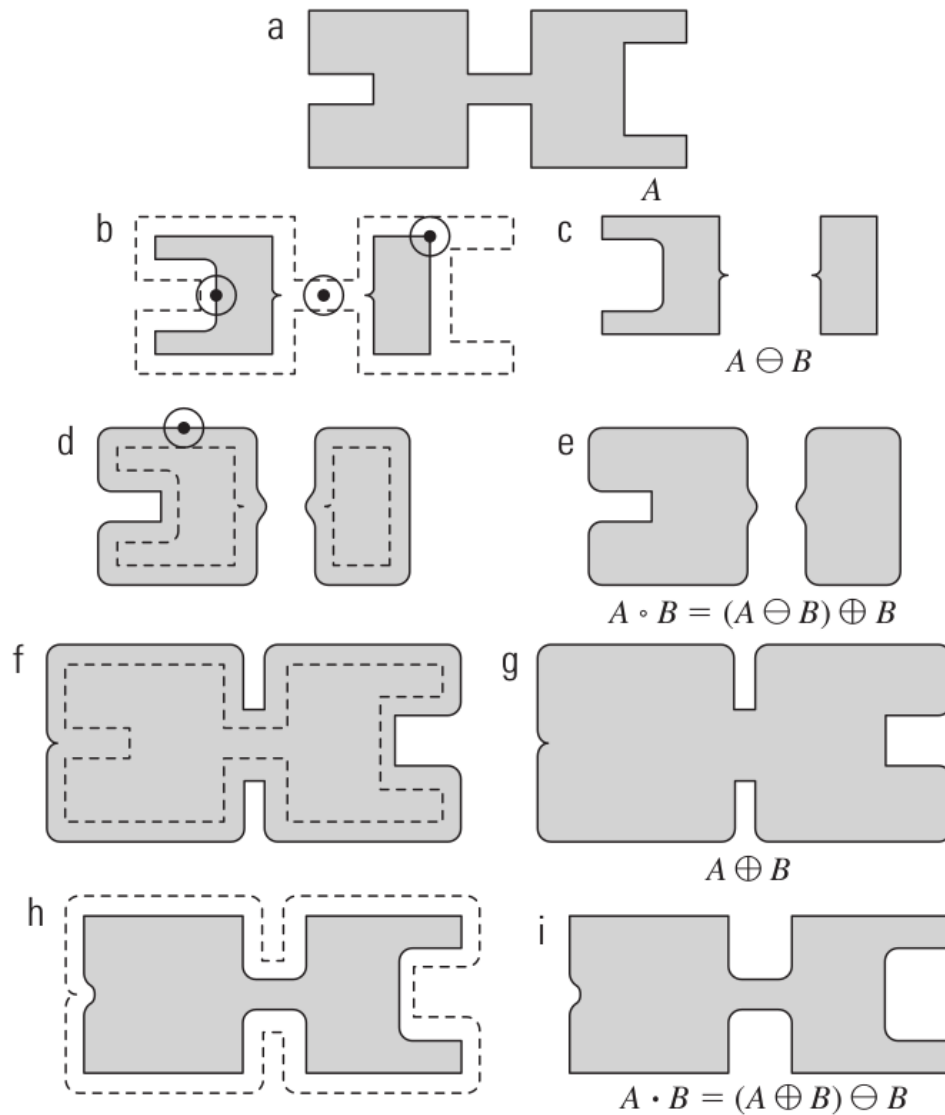
Duas operações:

Primeiro dilatação depois erosão com o mesmo elemento estruturante.

Elimina buracos e vazios menores que os Elementos estruturantes. Suaviza.



Resumo

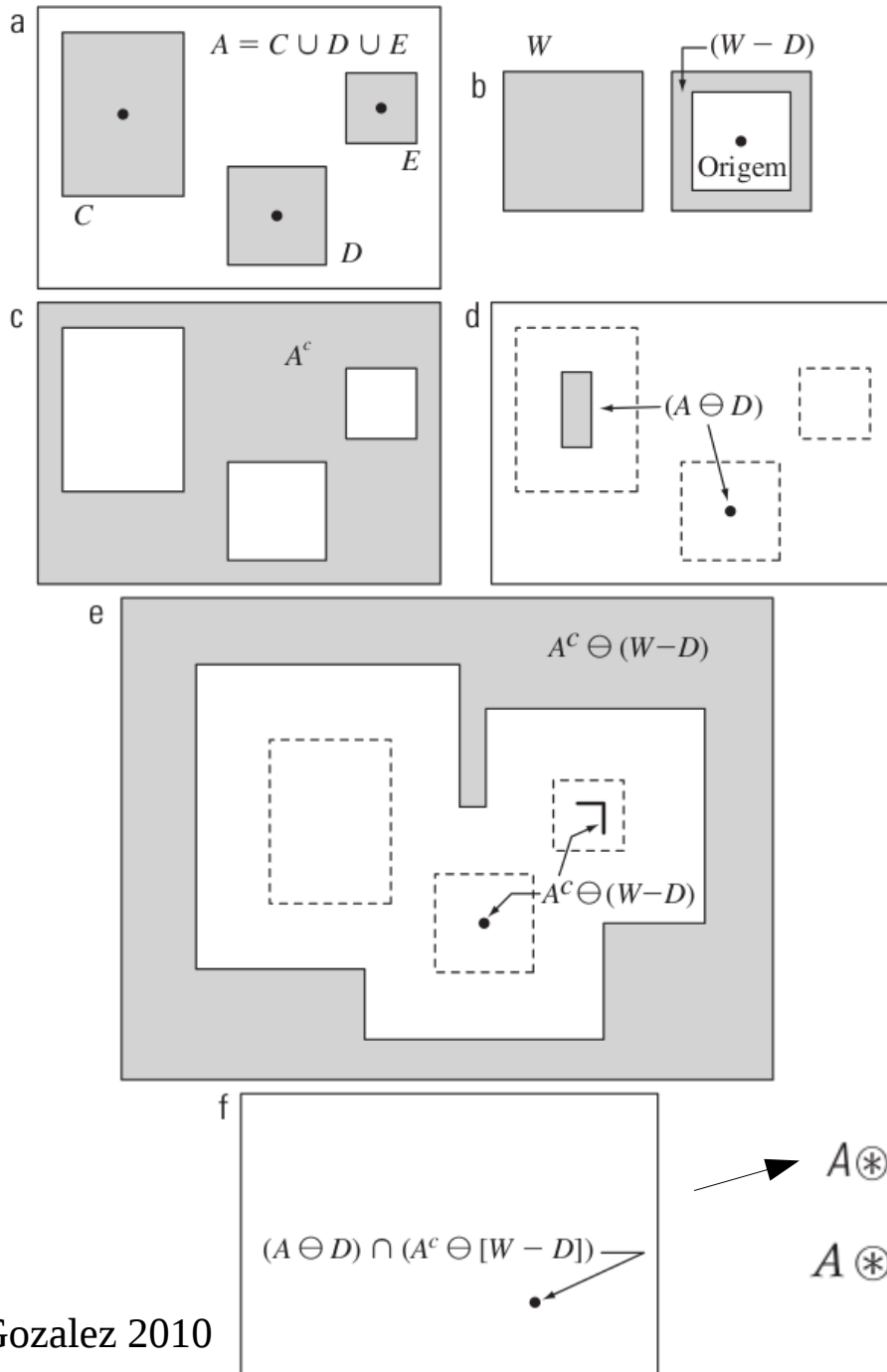


Fonte Gozalez 2010

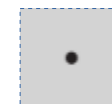
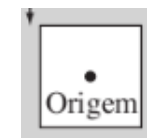


Extração de Fronteira

$$\beta(A) = A - (A \ominus B)$$



A transformada hit-or-miss



Considere:

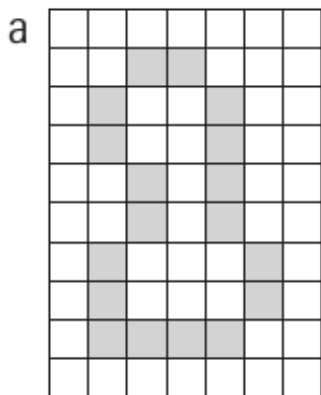
$$B_1 = D$$

$$B_2 = (W - D)$$

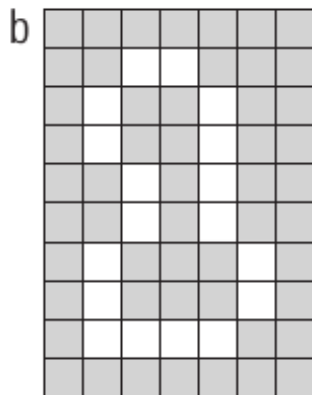
$$A \circledast B = (A \ominus B_1) \cap (A^c \ominus B_2)$$

$$A \circledast B = (A \ominus B_1) - (A \oplus \hat{B}_2)$$

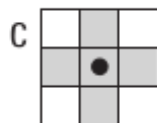
Preenchimento de Regiões



A



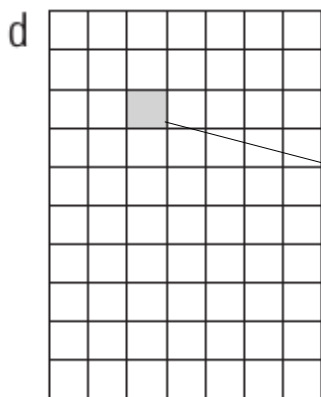
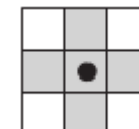
A^c



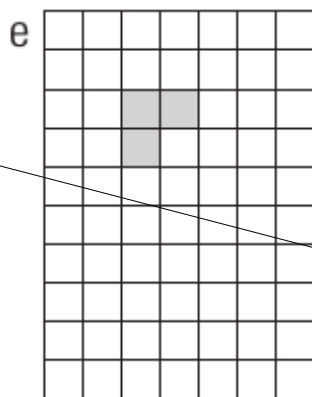
B

$$X_k = (X_{k-1} \oplus B) \cap A^c \quad k = 1, 2, 3, \dots$$

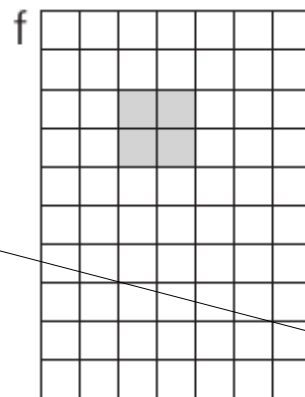
Elemento estruturante utilizado



X_0

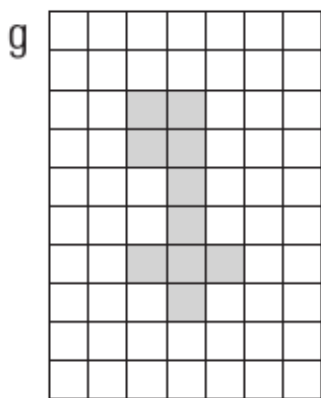


X_1

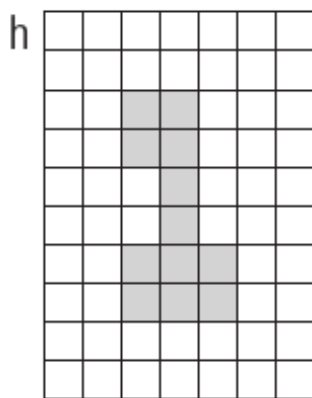


X_2

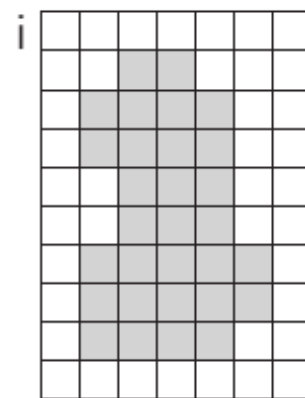
Dilatação começando por este elemento



X_6



X_8



$X_8 \cup A$

Objeto preenchido



Questões de implementação em OpenCV



Exemplo de Programa em OpenCV em c++

https://docs.opencv.org/3.3.0/d8/dc0/morphology2_8cpp-example.html

Documentação da rotina **morphologyEx** Opencv 3.3.0 :

https://docs.opencv.org/3.3.0/d4/d86/group__imgproc__filter.html#ga67493776e3ad1a3df63883829375201f

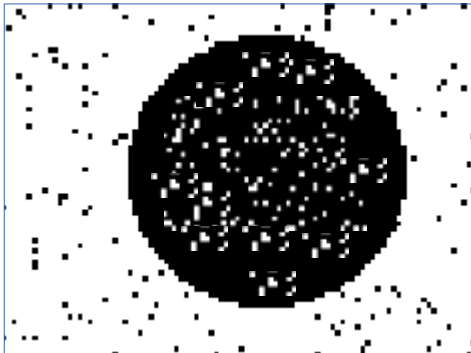
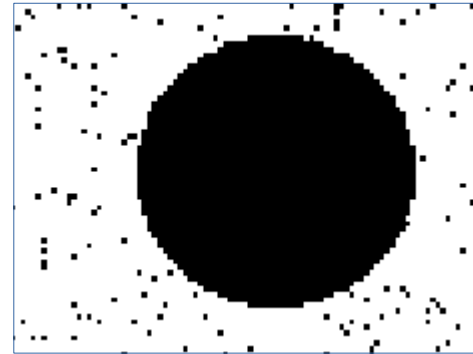
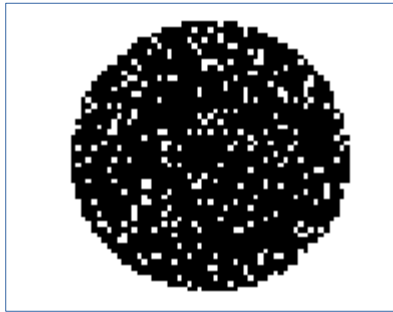
Documentação da rotina **morphologyEx** Opencv 2.4 :

<https://docs.opencv.org/2.4/modules/imgproc/doc/filtering.html?highlight=morphologyex#morphologyex>



Exercícios

1) Usando morfologia matemática retire os ruídos das imagens



Quais operações morfológicas aplicáveis ?

2) Dado uma imagem binária e os conceitos de processamento de imagens morfológicas, implemente um detector de bordas



Bibliografias

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- [Gonzalez (1993)] Gonzalez, R. F.; Woods, R. E. Digital Image Processing. Addison-Wesley, p 716. 1993.
- [Gonzalez (2010)] Gonzalez, R. F.; Woods, R. E. Processamento Digital de Imagens , 3ª edição, Pearson Prentice Hall, 624p. 2010.**
- [Hearn (1997)] Hearn, D; Baker, M. P. Computer Graphics, C Version. Prentice Hall, 2ª edição, p. 650. 1997.
- [FOLEY_90] Foley, James D. et al : Computer Graphics - Principles and Practice, Addison-Wesley Publishing Company, 1990.
- [PERSIANO_89] Persiano, R.C.M.; Oliveira, A.A.F. :Introdução à Computação Gráfica, Livros Técnicos e Científicos Editora Ltda., 1989.
- [Pratt (1991)] Pratt, Willian K. Digital Image Processing. A Wiley-Interscience Publication, 2ª edição. 698 p. 1991.