

Scale Space, Image Pyramids and Filter Banks

Vineeth N Balasubramanian

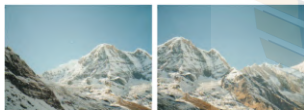
Department of Computer Science and Engineering
Indian Institute of Technology, Hyderabad



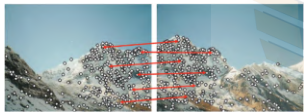
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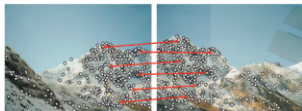
Review



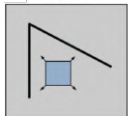
Review



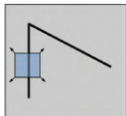
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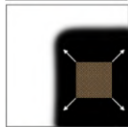
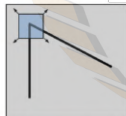
"flat" region:
no change in all
directions



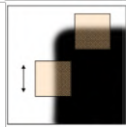
"edge":
no change along the
edge direction



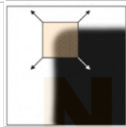
"corner":
significant change in
all directions



"flat" region
 λ_1 and λ_2 are
small;

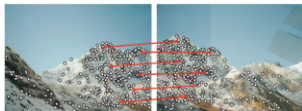


"edge":
 $\lambda_1 \gg \lambda_2$
 $\lambda_2 \gg \lambda_1$

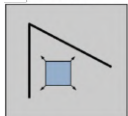


"corner":
 λ_1 and λ_2 are large,
 $\lambda_1 \sim \lambda_2$

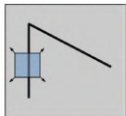
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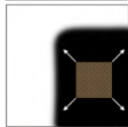
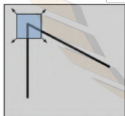
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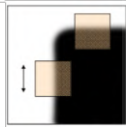
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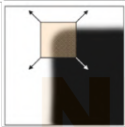
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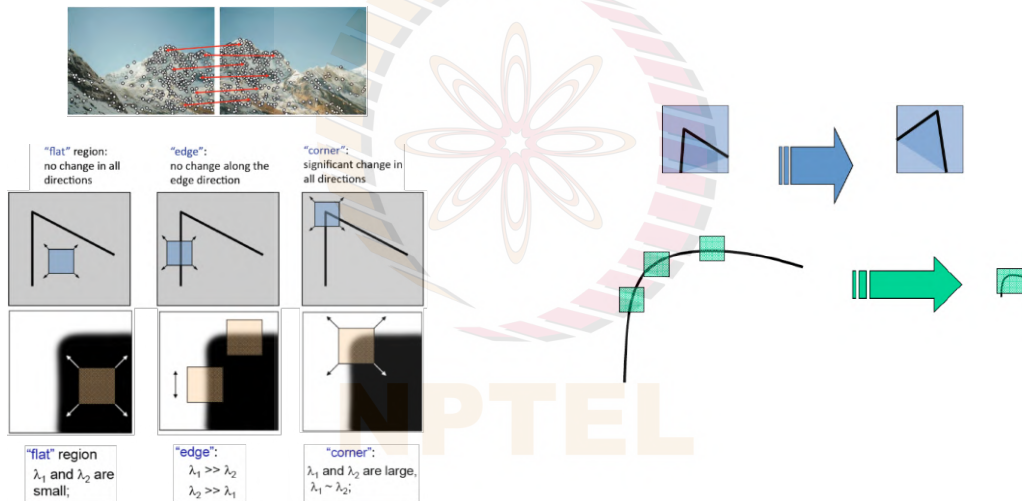
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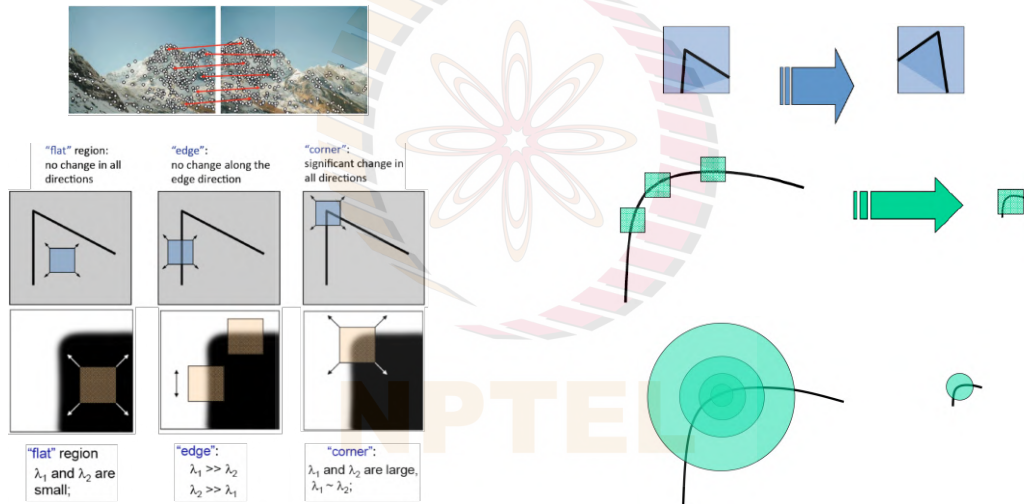
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Review

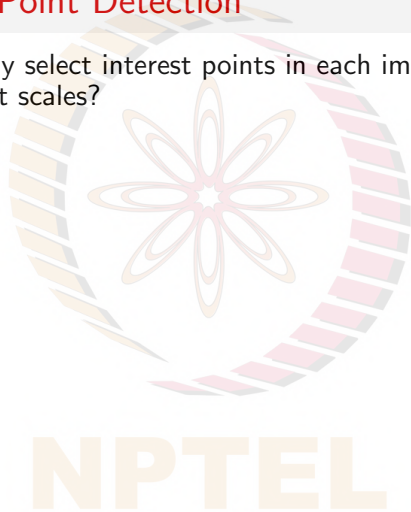


Review



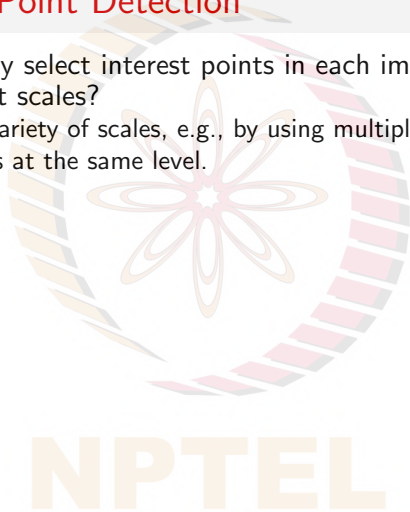
Scale-Invariant Interest Point Detection

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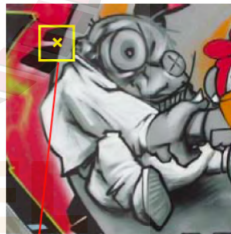
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 - More efficient to extract features stable in both location and scale.

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Scale-Invariant Interest Point Detection

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 - Extract features at a variety of scales, e.g., by using multiple resolutions in a pyramid, and then matching features at the same level.
 - When does this work?
 - More efficient to extract features stable in both location and scale.
 - Find scale that gives local maxima of a function f in both position and scale.



$$f(I_{i_1 \dots i_m}(x, \sigma)) = f(I_{i_1 \dots i_m}(x', \sigma'))$$

Automatic Scale Selection

Function responses for increasing scale (scale signature).



Credit: R Urtasun

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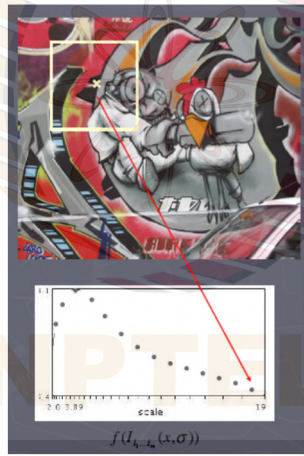
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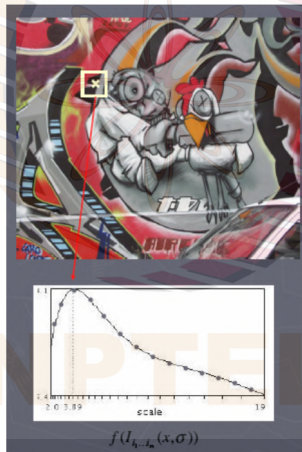
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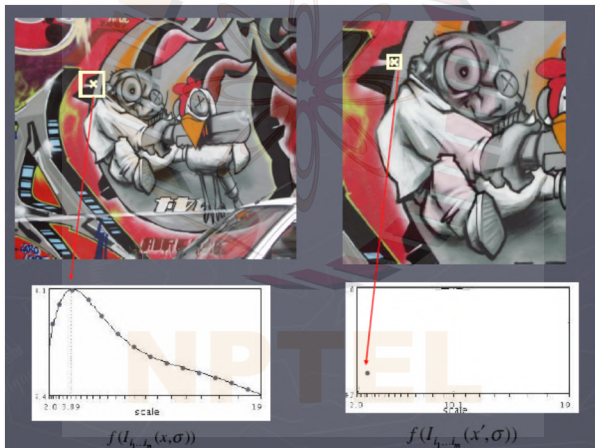
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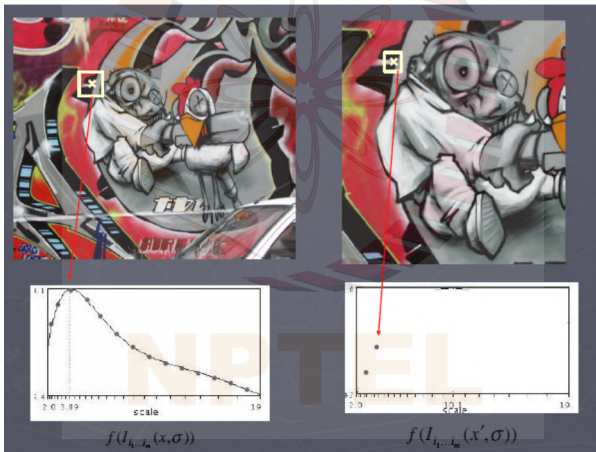
Function responses for increasing scale (scale signature).



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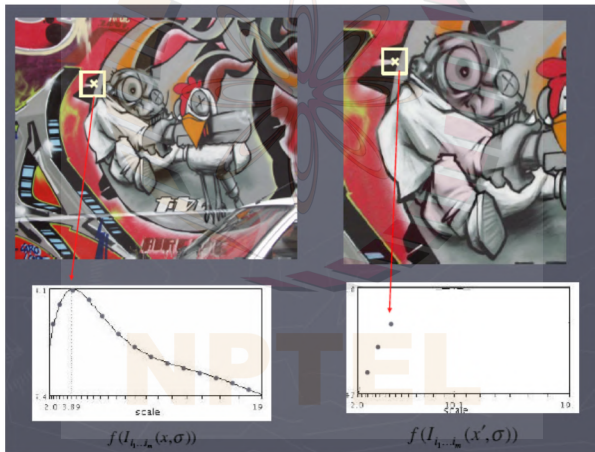
Function responses for increasing scale (scale signature).



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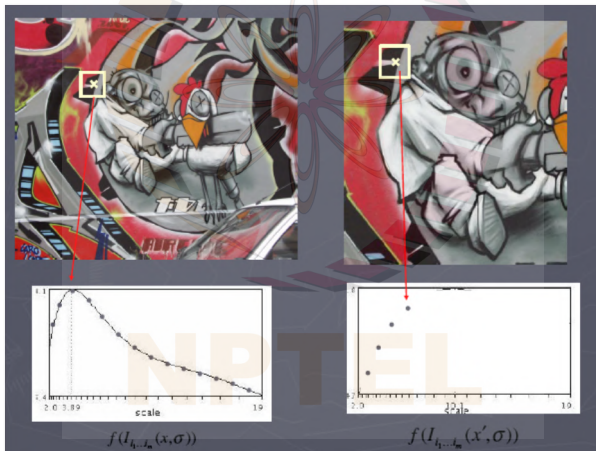
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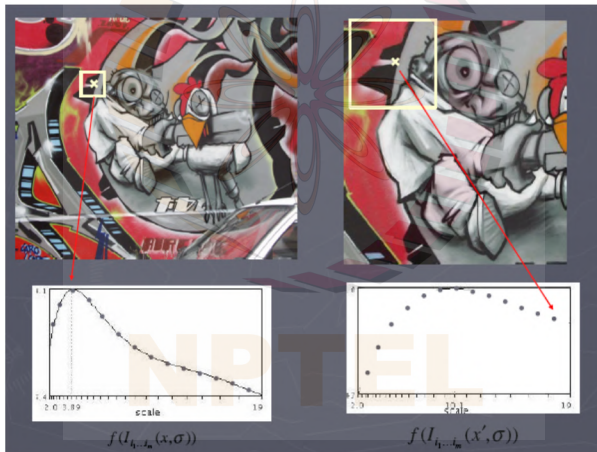
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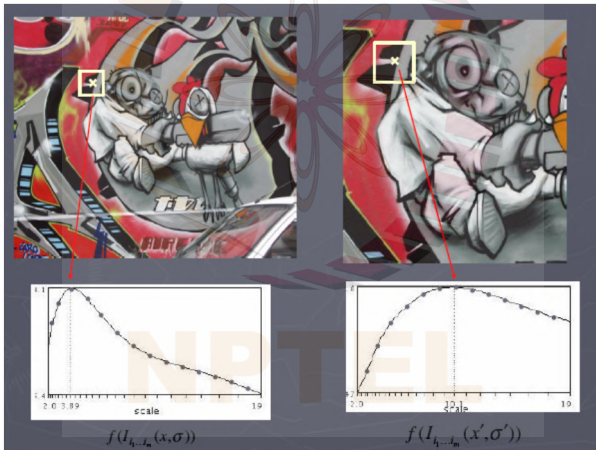
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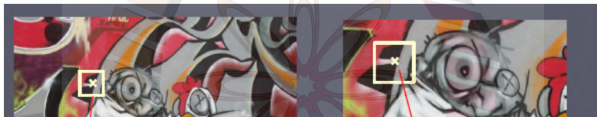
Function responses for increasing scale (scale signature).



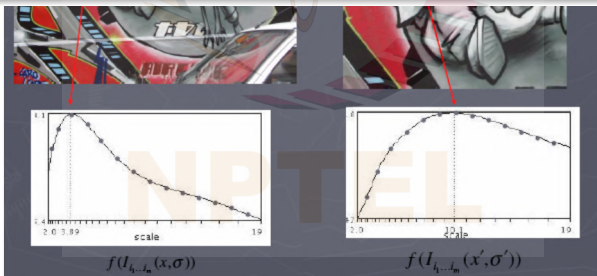
Credit: R Urtasun

Automatic Scale Selection

Function responses for increasing scale (scale signature).



Is there a better way to do this?



Automatic Scale Selection: Implementation

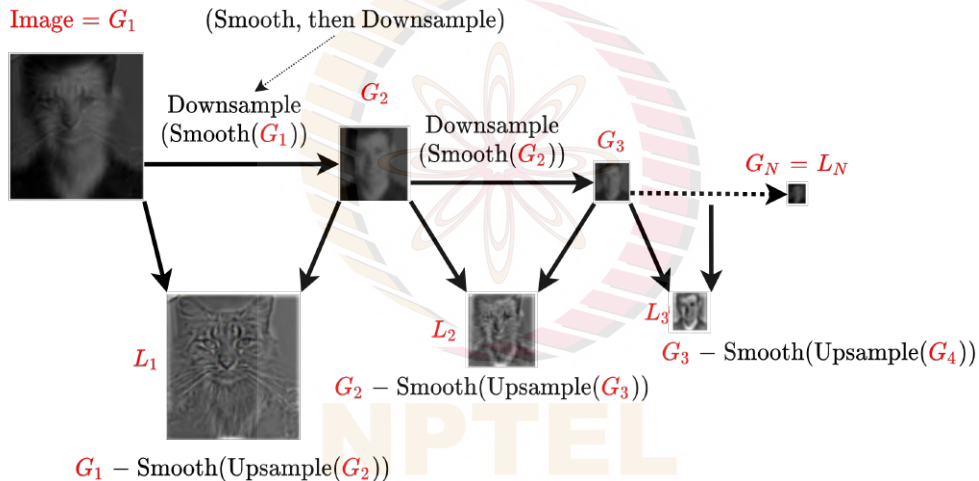
Instead of computing f for larger and larger windows, we can implement using a fixed window size with a Gaussian pyramid.



Sometimes need to create
in-between levels, e.g., a $\frac{3}{4}$ size image.

Credit: R Urtasun

Gaussian and Laplacian Pyramid



Credit: Derek Hoiem

Image Pyramids: Uses

- Compression



Image Pyramids: Uses

- Compression
- Object detection



Image Pyramids: Uses

- Compression
- Object detection
 - Scale search



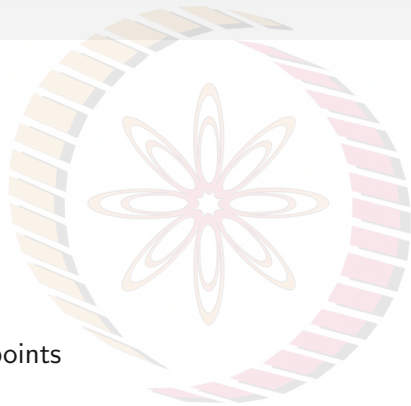
Image Pyramids: Uses

- Compression
- Object detection
 - Scale search
 - Features



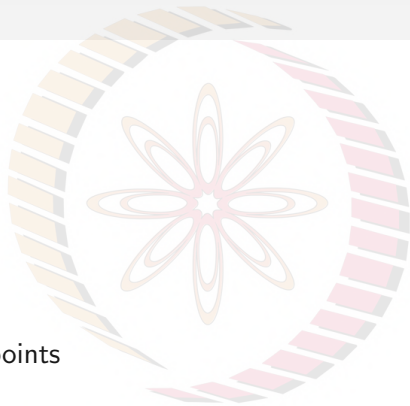
Image Pyramids: Uses

- Compression
- Object detection
 - Scale search
 - Features
- Detecting stable interest points



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Image Pyramids: Uses



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- Compression
- Object detection
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- Registration

Image Pyramids: Uses



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 - Coarse-to-fine Image Registration

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Coarse-to-fine Image Registration:

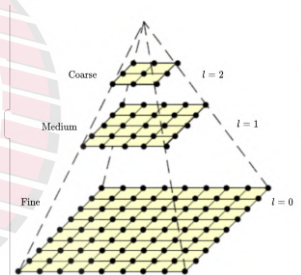
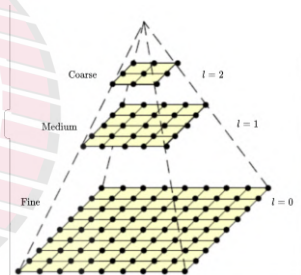


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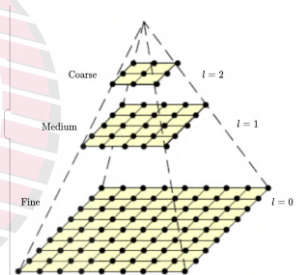


- Compute Gaussian pyramid.

Image Pyramids: Uses

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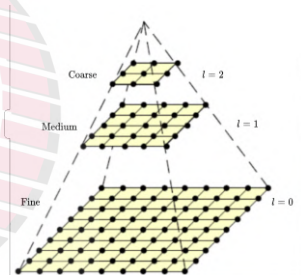


- Compute Gaussian pyramid.
- Align with coarse pyramid.

Image Pyramids: Uses

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Coarse-to-fine Image Registration:

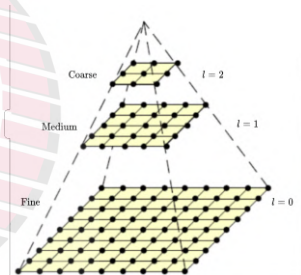


- Compute Gaussian pyramid.
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- Successively align with finer pyramids.

Image Pyramids: Uses

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 - Coarse-to-fine Image Registration

Coarse-to-fine Image Registration:



- Compute Gaussian pyramid.
- Align with coarse pyramid.
- Successively align with finer pyramids.
 - Search smaller range.

Credit: Derek Hoiem

Texture in Images

Textures:

- Regular or stochastic patterns caused by bumps, grooves and/or markings.

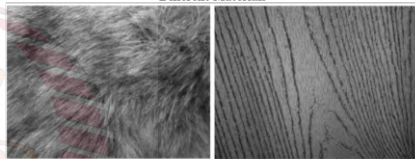


Texture in Images

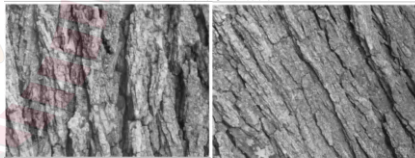
Textures:

- Regular or stochastic patterns caused by bumps, grooves and/or markings.
- Gives us information about spatial arrangement of colors or intensities in an image.

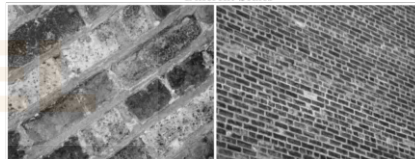
Different Materials



Different Orientation



Different Scales

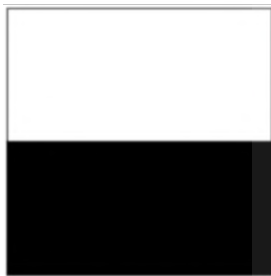


Credit: Derek Hoiem

Texture in Images

Conveys more information that can be exploited to match regions of interest in images.

Histogram conveys 50% white pixels and 50% black pixels



(Block Pattern)



(Checkerboard Pattern)



(Striped Pattern)

Drastically different textures

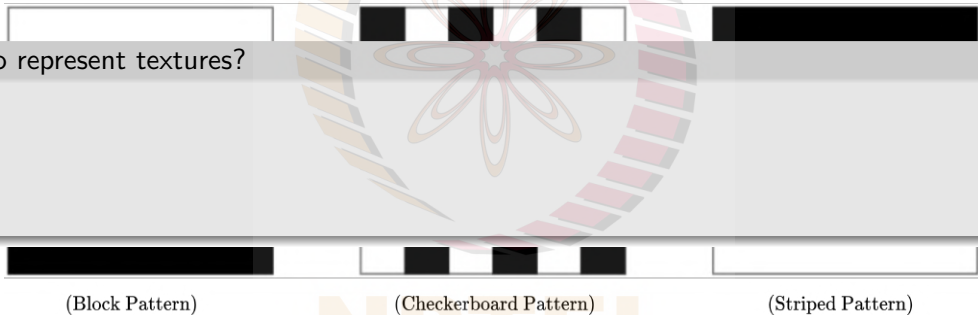
Credit: Linda G Shapiro

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How to represent textures?

- Compute responses of blobs and edges at various orientations and scales.



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How to represent textures?

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 - Record simple statistics (e.g., mean, std.) of absolute filter responses.



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How to represent textures?

- Compute responses of blobs and edges at various orientations and scales.
- Ways to process:
 - Record simple statistics (e.g., mean, std.) of absolute filter responses.
 - Take vectors of filter responses at each pixel and cluster them.



(Block Pattern)

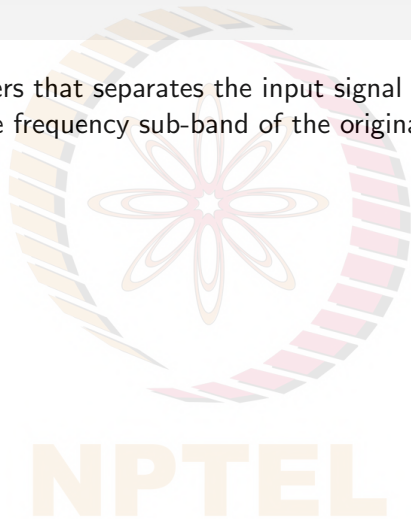
(Checkerboard Pattern)

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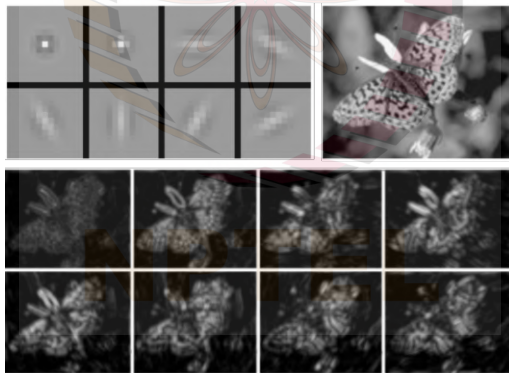
Filter Banks

- An array of bandpass filters that separates the input signal into multiple components, each one carrying a single frequency sub-band of the original signal.



Filter Banks

- An array of bandpass filters that separates the input signal into multiple components, each one carrying a single frequency sub-band of the original signal.
- Process image with each filter and keep responses (or squared/abs responses).



Credit: Derek Hoiem

Gabor Filters

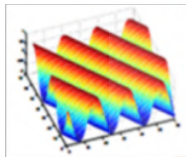
- Special classes of bandpass filters (i.e., they allow a certain 'band' of frequencies and reject the others).



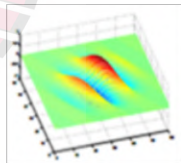
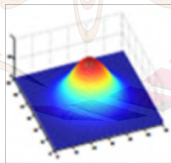
Gabor Filters

- Special classes of bandpass filters (i.e., they allow a certain 'band' of frequencies and reject the others).
- A Gabor filter can be viewed as a sinusoidal signal of particular frequency and orientation, modulated by a Gaussian wave.

A 2-D Gaussian



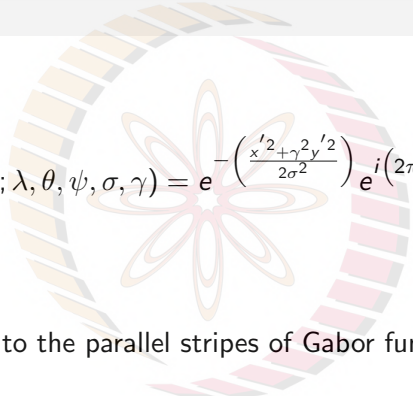
A sinusoid oriented 30° with x-axis



A corresponding 2-D Gabor Filter

A 2-D Gabor filter obtained by modulating the sine wave with a Gaussian

2-D Gabor Filter


$$g(x, y; \lambda, \theta, \psi, \sigma, \gamma) = e^{-\left(\frac{x'^2 + \gamma^2 y'^2}{2\sigma^2}\right)} e^{i\left(2\pi \frac{x'}{\lambda} + \psi\right)}$$

where:

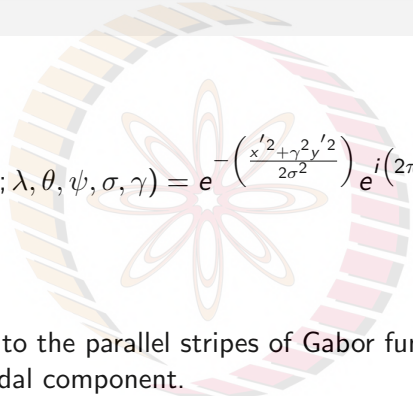
$$x' = x \cos \theta + y \sin \theta$$

$$y' = -x \sin \theta + y \cos \theta$$

θ – Orientation of the normal to the parallel stripes of Gabor function.

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2-D Gabor Filter


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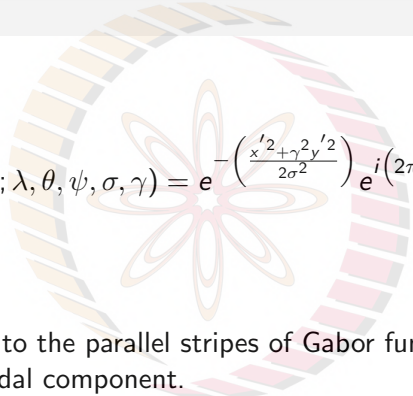
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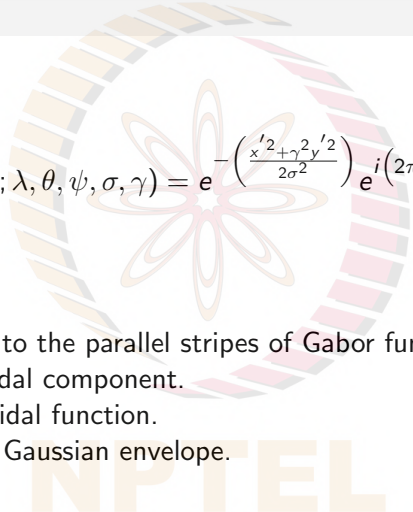
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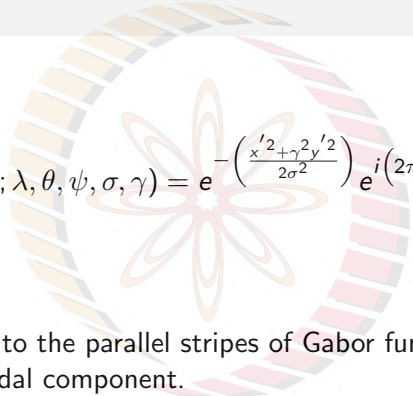
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where:

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θ – Orientation of the normal to the parallel stripes of Gabor function.

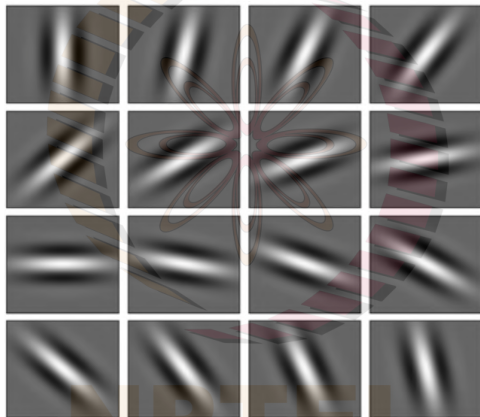
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ψ – Phase offset of the sinusoidal function.

σ – Standard deviation of the Gaussian envelope.

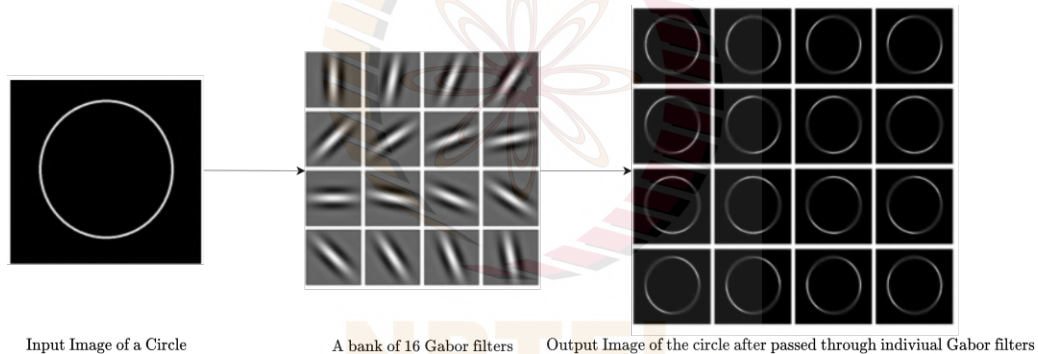
γ – Spatial aspect ratio and specifies the ellipticity of the support of Gabor function.

Gabor Filter Banks



Bank of 16 Gabor filters at an orientation of 11.250 (i.e. if the first filter is at 00.00, then the second will be at 11.25, the third will be at 22.50, and so on.)

Gabor Filter Banks



Steerable Filter Banks

Steerable Filters are a class of oriented filters that can be expressed as a linear combination of a set of basis filters.



Steerable Filter Banks

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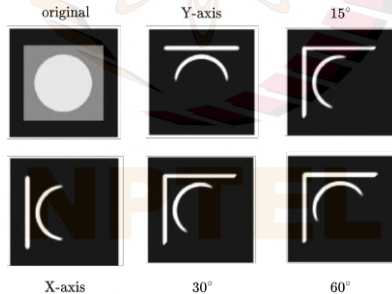
NPTEL

Steerable Filter Banks

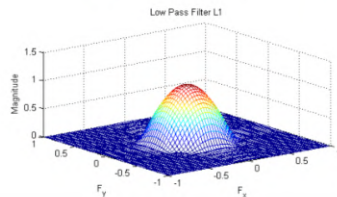
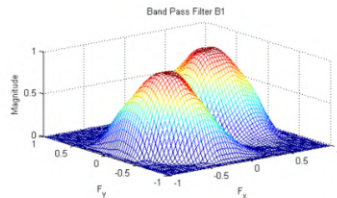
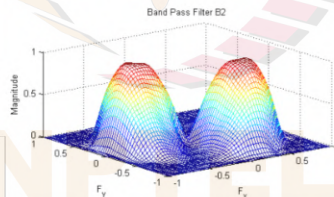
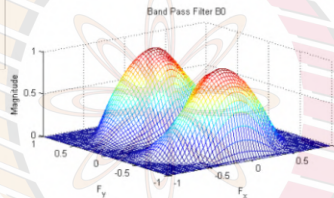
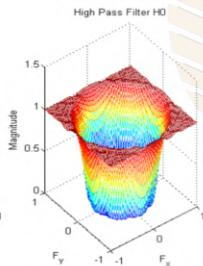
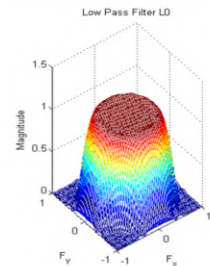
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where $G_1^{\theta^\circ}$ is the first derivative of G at angle θ .



Steerable Filter Banks



Homework

Readings

- Chapter 2, Szeliski, *Computer Vision: Algorithms and Applications*

Questions

- Why is camouflage attire effective? How?
- How is texture different from noise?
- Will scale-invariant filters be effective in matching pictures containing Matryoshka (or Russian nesting) dolls?

