

# Deep Learning for Data Science

## DS 542

<https://dl4ds.github.io/sp2026/>

Initialization

# Plan for Today

- Project 1
- The need for weights initialization
- Expectations Refresher
- The (Kaiming) He Initialization
- Lottery tickets

# Initialization

- Consider standard building block of NN in terms of pre-activations:

$$\begin{aligned}\mathbf{f}_k &= \boldsymbol{\beta}_k + \boldsymbol{\Omega}_k \mathbf{h}_k \\ &= \boldsymbol{\beta}_k + \boldsymbol{\Omega}_k \mathbf{a}[\mathbf{f}_{k-1}]\end{aligned}$$

- How do we initialize the biases and weights?
- Equivalent to choosing starting point in our gradient descent searches

# Forward Pass

- Consider standard building block of NN in terms of *pre-activations*:

$$\begin{aligned}\mathbf{f}_k &= \boldsymbol{\beta}_k + \boldsymbol{\Omega}_k \mathbf{h}_k \\ &= \boldsymbol{\beta}_k + \boldsymbol{\Omega}_k \mathbf{a}[\mathbf{f}_{k-1}]\end{aligned}$$

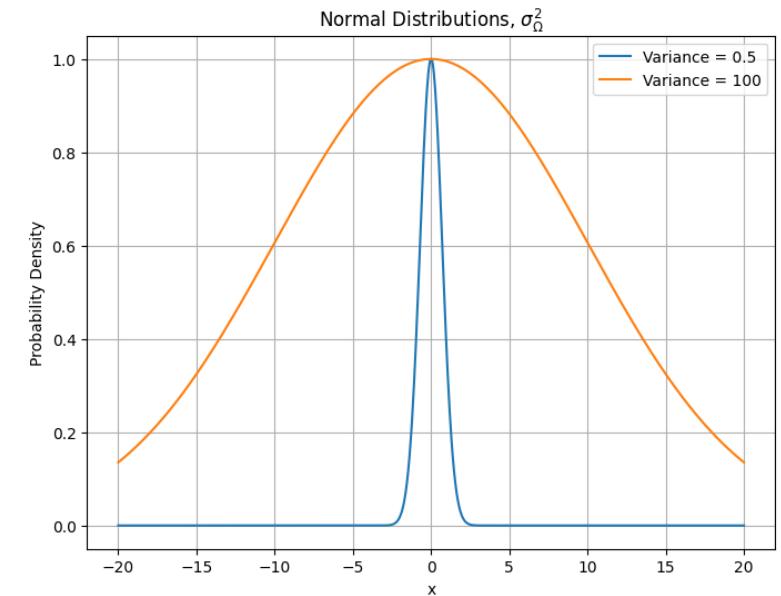
- Set all the biases to 0

$$\boldsymbol{\beta}_k = \mathbf{0}$$

- Set weights to be normally distributed

- mean 0
- variance  $\sigma_{\Omega}^2$

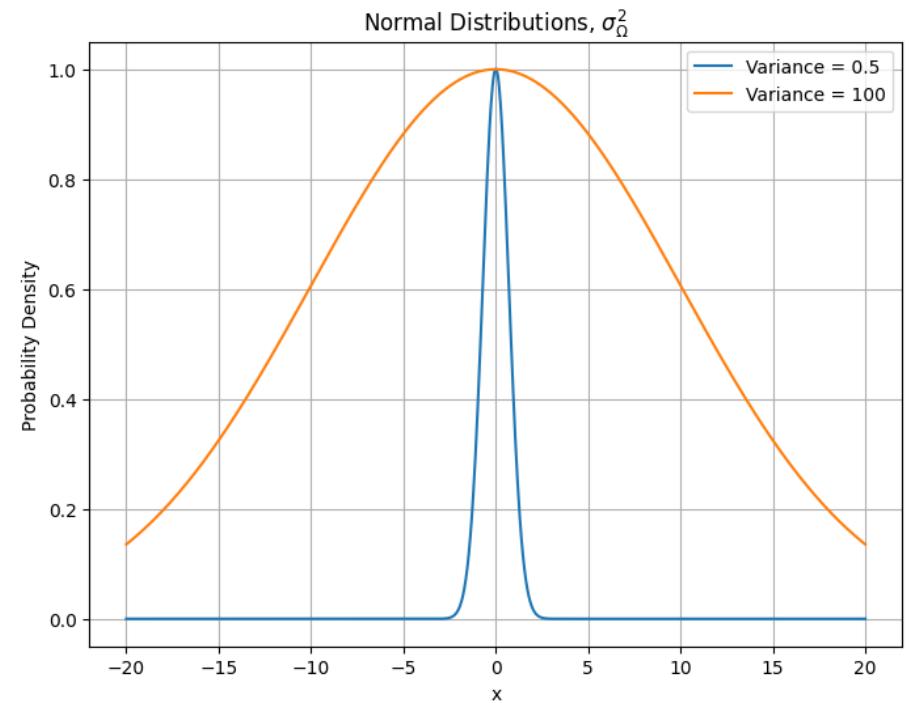
- What will happen as we move through the network if  $\sigma_{\Omega}^2$  is very small?
- What will happen as we move through the network if  $\sigma_{\Omega}^2$  is very large?



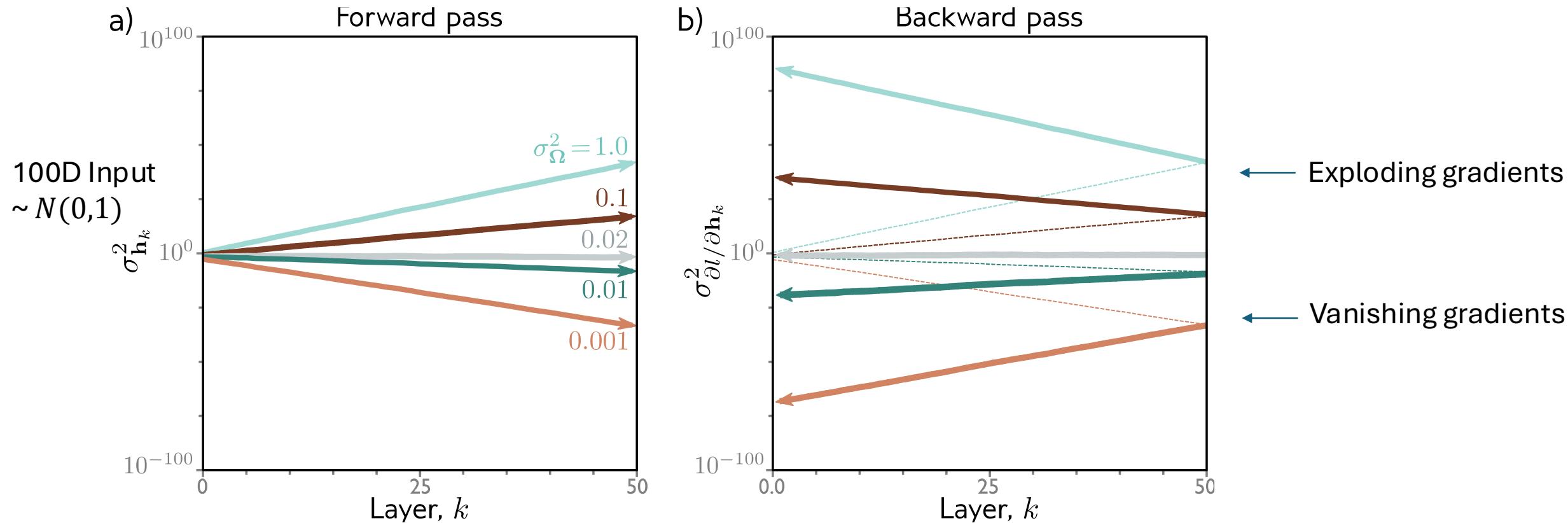
# Backward Pass

$$\frac{\partial \ell_i}{\partial \mathbf{f}_{k-1}} = \mathbb{I}[\mathbf{f}_{k-1} > 0] \odot \left( \boldsymbol{\Omega}_k^T \frac{\partial \ell_i}{\partial \mathbf{f}_k} \right), \quad k \in \{K, K-1, \dots, 1\} \quad (7.13)$$

- What will happen as we propagate backwards through the network if  $\sigma_\Omega^2$  is very small?
- What will happen as we propagate backwards through the network if  $\sigma_\Omega^2$  is very large?



# Initialize weights to different variances



**Figure 7.4** Weight initialization. Consider a deep network with 50 hidden layers and  $D_h = 100$  hidden units per layer. The network has a 100 dimensional input  $\mathbf{x}$  initialized with values from a standard normal distribution, a single output fixed at  $y = 0$ , and a least squares loss function. The bias vectors  $\beta_k$  are initialized to zero and the weight matrices  $\Omega_k$  are initialized with a normal distribution with mean zero and five different variances  $\sigma_{\Omega}^2 \in \{0.001, 0.01, 0.02, 0.1, 1.0\}$ . a)

How do we initialize weights to keep variance stable across layers?

Aim: keep variance same between two layers

$$\mathbf{f}' = \boldsymbol{\beta} + \boldsymbol{\Omega} \mathbf{h}$$

$$\mathbf{h} = \mathbf{a}[\mathbf{f}],$$

Definition of variance:

$$\sigma_{f'}^2 = \mathbb{E}[(f'_i - \mathbb{E}[f'_i])^2]$$

# Any Questions?

???

- The need for weights initialization
- Expectations Refresher
- The (Kaiming) He initialization
- Lottery tickets

# Expectations

$$\mathbb{E}[g[x]] = \int g[x] Pr(x) dx,$$

Interpretation: what is the average value of  $g[x]$  when taking into account the probability of  $x$ ?

Consider discrete case and assume uniform probability so calculating  $g[x]$  reduces to taking average:

$$\mathbb{E}[g[x]] \approx \frac{1}{N} \sum_{n=1}^N g[x_n^*] \quad \text{where} \quad x_n^* \sim Pr(x)$$

# Common Expectation Functions

Function $g[\bullet]$	Expectation
$x$	mean, $\mu$
$x^k$	$k$ th moment about zero
$(x - \mu)^k$	$k$ th moment about the mean
$(x - \mu)^2$	variance
$(x - \mu)^3$	skew
$(x - \mu)^4$	kurtosis

**Table B.1** Special cases of expectation. For some functions  $g[x]$ , the expectation  $\mathbb{E}[g[x]]$  is given a special name. Here we use the notation  $\mu_x$  to represent the mean with respect to random variable  $x$ .

# Rules for manipulating expectation

$$\mathbb{E}[k] = k$$

$$\mathbb{E}[k \cdot g[x]] = k \cdot \mathbb{E}[g[x]]$$

$$\mathbb{E}[f[x] + g[x]] = \mathbb{E}[f[x]] + \mathbb{E}[g[x]]$$

$$\mathbb{E}[f[x]g[y]] = \mathbb{E}[f[x]]\mathbb{E}[g[y]] \quad \text{if } x, y \text{ independent}$$

# Any Questions?

???

- The need for weights initialization
- Expectations Refresher
- The (Kaiming) He initialization
- Lottery tickets

Aim: keep variance same between two layers

$$\begin{aligned} \mathbf{h} &= \mathbf{a}[\mathbf{f}], \\ \mathbf{f}' &= \boldsymbol{\beta} + \boldsymbol{\Omega}\mathbf{h} \end{aligned}$$

Definition of variance:

$$\sigma_{f'_i}^2 = \mathbb{E}[(f'_i - \mathbb{E}[f'_i])^2]$$

Now let's prove:

$$\mathbb{E}[(x - \mu)^2] = \mathbb{E}[x^2] - \mathbb{E}[x]^2$$

Keeping in mind:

$$\mathbb{E}[x] = \mu$$

Rule 1:	$\mathbb{E}[k] = k$
Rule 2:	$\mathbb{E}[k \cdot g[x]] = k \cdot \mathbb{E}[g[x]]$
Rule 3:	$\mathbb{E}[f[x] + g[x]] = \mathbb{E}[f[x]] + \mathbb{E}[g[x]]$
Def'n	$\mathbb{E}[x] = \mu$

$$\mathbb{E}[(x - \mu^2)] = \mathbb{E}[x^2 - 2x\mu + \mu^2]$$

Rule 1:  $\mathbb{E}[k] = k$

Rule 2:  $\mathbb{E}[k \cdot g[x]] = k \cdot \mathbb{E}[g[x]]$

Rule 3:  $\mathbb{E}[f[x] + g[x]] = \mathbb{E}[f[x]] + \mathbb{E}[g[x]]$

Def'n  $\mathbb{E}[x] = \mu$



$$\begin{aligned}\mathbb{E}[(x - \mu^2)] &= \mathbb{E}[x^2 - 2x\mu + \mu^2] \\ &= \mathbb{E}[x^2] - \mathbb{E}[2x\mu] + \mathbb{E}[\mu^2]\end{aligned}$$

Rule 1:	$\mathbb{E}[k] = k$	←
Rule 2:	$\mathbb{E}[k \cdot g[x]] = k \cdot \mathbb{E}[g[x]]$	←
Rule 3:	$\mathbb{E}[f[x] + g[x]] = \mathbb{E}[f[x]] + \mathbb{E}[g[x]]$	
Def'n	$\mathbb{E}[x] = \mu$	

$$\begin{aligned}
 \mathbb{E}[(x - \mu^2)] &= \mathbb{E}[x^2 - 2x\mu + \mu^2] \\
 &= \mathbb{E}[x^2] - \mathbb{E}[2x\mu] + \mathbb{E}[\mu^2] \\
 &= \mathbb{E}[x^2] - 2\mu\mathbb{E}[x] + \mu^2
 \end{aligned}$$

Rule 1:	$\mathbb{E}[k] = k$
Rule 2:	$\mathbb{E}[k \cdot g[x]] = k \cdot \mathbb{E}[g[x]]$
Rule 3:	$\mathbb{E}[f[x] + g[x]] = \mathbb{E}[f[x]] + \mathbb{E}[g[x]]$
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 &= \mathbb{E}[x^2] - \mathbb{E}[2x\mu] + \mathbb{E}[\mu^2] \\
 &= \mathbb{E}[x^2] - 2\mu\mathbb{E}[x] + \mu^2 \\
 &= \mathbb{E}[x^2] - 2\mu^2 + \mu^2
 \end{aligned}$$

Rule 1:	$\mathbb{E}[k] = k$
Rule 2:	$\mathbb{E}[k \cdot g[x]] = k \cdot \mathbb{E}[g[x]]$
Rule 3:	$\mathbb{E}[f[x] + g[x]] = \mathbb{E}[f[x]] + \mathbb{E}[g[x]]$
Def'n	$\mathbb{E}[x] = \mu$

$$\begin{aligned}
\mathbb{E}[(x - \mu)^2] &= \mathbb{E}[x^2 - 2x\mu + \mu^2] \\
&= \mathbb{E}[x^2] - \mathbb{E}[2x\mu] + \mathbb{E}[\mu^2] \\
&= \mathbb{E}[x^2] - 2\mu\mathbb{E}[x] + \mu^2 \\
&= \mathbb{E}[x^2] - 2\mu^2 + \mu^2 \\
&= \mathbb{E}[x^2] - \mu^2
\end{aligned}$$

Rule 1:	$\mathbb{E}[k] = k$
Rule 2:	$\mathbb{E}[k \cdot g[x]] = k \cdot \mathbb{E}[g[x]]$
Rule 3:	$\mathbb{E}[f[x] + g[x]] = \mathbb{E}[f[x]] + \mathbb{E}[g[x]]$
Def'n	$\mathbb{E}[x] = \mu$



$$\begin{aligned}
\mathbb{E}[(x - \mu^2)] &= \mathbb{E}[x^2 - 2x\mu + \mu^2] \\
&= \mathbb{E}[x^2] - \mathbb{E}[2x\mu] + \mathbb{E}[\mu^2] \\
&= \mathbb{E}[x^2] - 2\mu\mathbb{E}[x] + \mu^2 \\
&= \mathbb{E}[x^2] - 2\mu^2 + \mu^2 \\
&= \mathbb{E}[x^2] - \mu^2 \\
&= \mathbb{E}[x^2] - E[x]^2
\end{aligned}$$

Aim: keep variance same between two layers

$$\mathbf{f}' = \boldsymbol{\beta} + \boldsymbol{\Omega} \mathbf{h}$$

$$\mathbf{h} = \mathbf{a}[\mathbf{f}],$$

$$\sigma_{f'}^2 = \mathbb{E}[(f'_i - \mathbb{E}[f'_i])^2]$$

$$\sigma_{f'}^2 = \mathbb{E}[f_i'^2] - \mathbb{E}[f_i']^2$$

$$\longrightarrow \mathbb{E}[(x - \mu)^2] = \mathbb{E}[x^2] - \mathbb{E}[x]^2$$

Aim: keep variance same between two layers

$$\mathbf{f}' = \boldsymbol{\beta} + \boldsymbol{\Omega} \mathbf{h}$$

$$\mathbf{h} = \mathbf{a}[\mathbf{f}],$$

$$\sigma_{f'}^2 = \mathbb{E}[(f'_i - \mathbb{E}[f'_i])^2]$$

$$\sigma_{f'}^2 = \mathbb{E}[f_i'^2] - \mathbb{E}[f_i']^2$$

Focus on this term.

Aim: keep variance same between two layers

$$\mathbf{f}' = \boldsymbol{\beta} + \boldsymbol{\Omega} \mathbf{h}$$

Consider the mean of the pre-activations:

$$\mathbb{E}[f'_i] = \mathbb{E} \left[ \beta_i + \sum_{j=1}^{D_h} \Omega_{ij} h_j \right]$$

$$\text{Rule 1: } \mathbb{E}[k] = k$$

$$\text{Rule 2: } \mathbb{E}[k \cdot g[x]] = k \cdot \mathbb{E}[g[x]]$$

$$\text{Rule 3: } \mathbb{E}[f[x] + g[x]] = \mathbb{E}[f[x]] + \mathbb{E}[g[x]]$$

$$\text{Rule 4: } \mathbb{E}[f[x]g[y]] = \mathbb{E}[f[x]]\mathbb{E}[g[y]] \quad \text{if } x, y \text{ independent}$$



$$\begin{aligned}\mathbb{E}[f'_i] &= \mathbb{E} \left[ \beta_i + \sum_{j=1}^{D_h} \Omega_{ij} h_j \right] \\ &= \mathbb{E} [\beta_i] + \sum_{j=1}^{D_h} \mathbb{E} [\Omega_{ij} h_j]\end{aligned}$$

$$\text{Rule 1: } \mathbb{E}[k] = k$$

$$\text{Rule 2: } \mathbb{E}[k \cdot g[x]] = k \cdot \mathbb{E}[g[x]]$$

$$\text{Rule 3: } \mathbb{E}[f[x] + g[x]] = \mathbb{E}[f[x]] + \mathbb{E}[g[x]]$$

$$\text{Rule 4: } \mathbb{E}[f[x]g[y]] = \mathbb{E}[f[x]]\mathbb{E}[g[y]] \quad \text{if } x, y \text{ independent}$$



$$\begin{aligned}\mathbb{E}[f'_i] &= \mathbb{E} \left[ \beta_i + \sum_{j=1}^{D_h} \Omega_{ij} h_j \right] \\ &= \mathbb{E} [\beta_i] + \sum_{j=1}^{D_h} \mathbb{E} [\Omega_{ij} h_j] \\ &= \mathbb{E} [\beta_i] + \sum_{j=1}^{D_h} \mathbb{E} [\Omega_{ij}] \mathbb{E} [h_j]\end{aligned}$$

Rule 1:	$\mathbb{E}[k] = k$
Rule 2:	$\mathbb{E}[k \cdot g[x]] = k \cdot \mathbb{E}[g[x]]$
Rule 3:	$\mathbb{E}[f[x] + g[x]] = \mathbb{E}[f[x]] + \mathbb{E}[g[x]]$
Rule 4:	$\mathbb{E}[f[x]g[y]] = \mathbb{E}[f[x]]\mathbb{E}[g[y]]$ if $x, y$ independent

$$\mathbb{E}[f'_i] = \mathbb{E} \left[ \beta_i + \sum_{j=1}^{D_h} \Omega_{ij} h_j \right]$$

Start making initialization choices.

- Set all the biases to 0
- Weights normally distributed
  - mean 0
  - variance  $\sigma_\Omega^2$

$$= \mathbb{E}[\beta_i] + \sum_{j=1}^{D_h} \mathbb{E}[\Omega_{ij} h_j]$$

$$= \mathbb{E}[\beta_i] + \sum_{j=1}^{D_h} \mathbb{E}[\Omega_{ij}] \mathbb{E}[h_j]$$

$$= 0 + \sum_{j=1}^{D_h} 0 \cdot \mathbb{E}[h_j] = 0$$

Aim: keep variance same between two layers

$$\mathbf{f}' = \boldsymbol{\beta} + \boldsymbol{\Omega} \mathbf{h}$$

$$\mathbf{h} = \mathbf{a}[\mathbf{f}],$$

$$\sigma_{f'}^2 = \mathbb{E}[(f'_i - \mathbb{E}[f'_i])^2]$$

$$\sigma_{f'}^2 = \mathbb{E}[f_i'^2] - \mathbb{E}[f_i']^2 = \mathbb{E}[f_i'^2]$$

↓  
0

- |         |   |
|---------|---|
| Rule 1: | $\mathbb{E}[k] = k$   |
| Rule 2: | $\mathbb{E}[k \cdot g[x]] = k \cdot \mathbb{E}[g[x]]$                           |
| Rule 3: | $\mathbb{E}[f[x] + g[x]] = \mathbb{E}[f[x]] + \mathbb{E}[g[x]]$                 |
| Rule 4: | $\mathbb{E}[f[x]g[y]] = \mathbb{E}[f[x]]\mathbb{E}[g[y]]$ if $x, y$ independent |

$$\begin{aligned}\sigma_{f'}^2 &= \mathbb{E}[f_i'^2] - \mathbb{E}[f_i']^2 \\ &= \mathbb{E} \left[ \left( \beta_i + \sum_{j=1}^{D_h} \Omega_{ij} h_j \right)^2 \right] - 0\end{aligned}$$

Set all the biases to 0

Weights normally distributed  
 mean 0  
 variance  $\sigma_\Omega^2$

- |         |   |
|---------|---|
| Rule 1: | $\mathbb{E}[k] = k$   |
| Rule 2: | $\mathbb{E}[k \cdot g[x]] = k \cdot \mathbb{E}[g[x]]$                           |
| Rule 3: | $\mathbb{E}[f[x] + g[x]] = \mathbb{E}[f[x]] + \mathbb{E}[g[x]]$                 |
| Rule 4: | $\mathbb{E}[f[x]g[y]] = \mathbb{E}[f[x]]\mathbb{E}[g[y]]$ if $x, y$ independent |

$$\sigma_{f'}^2 = \mathbb{E}[f_i'^2] - \mathbb{E}[f_i']^2$$

$$= \mathbb{E} \left[ \left( \beta_i + \sum_{j=1}^{D_h} \Omega_{ij} h_j \right)^2 \right] - 0$$

Initialization choices.

- Set all the biases to 0
- Weights normally distributed
  - mean 0
  - variance  $\sigma_\Omega^2$

$$= \mathbb{E} \left[ \left( \sum_{j=1}^{D_h} \Omega_{ij} h_j \right)^2 \right]$$

- |         |   |
|---------|---|
| Rule 1: | $\mathbb{E}[k] = k$   |
| Rule 2: | $\mathbb{E}[k \cdot g[x]] = k \cdot \mathbb{E}[g[x]]$                           |
| Rule 3: | $\mathbb{E}[f[x] + g[x]] = \mathbb{E}[f[x]] + \mathbb{E}[g[x]]$                 |
| Rule 4: | $\mathbb{E}[f[x]g[y]] = \mathbb{E}[f[x]]\mathbb{E}[g[y]]$ if $x, y$ independent |



$$\begin{aligned}
 \sigma_{f'}^2 &= \mathbb{E}[f_i'^2] - \mathbb{E}[f_i']^2 \\
 &= \mathbb{E} \left[ \left( \beta_i + \sum_{j=1}^{D_h} \Omega_{ij} h_j \right)^2 \right] - 0 \\
 &= \mathbb{E} \left[ \left( \sum_{j=1}^{D_h} \Omega_{ij} h_j \right)^2 \right] \\
 &= \sum_{j=1}^{D_h} \mathbb{E} [\Omega_{ij}^2] \mathbb{E} [h_j^2]
 \end{aligned}$$

## Initialization choices.

- Set all the biases to 0
- Weights normally distributed
  - mean 0
  - variance  $\sigma_\Omega^2$

For all the cross terms,  $E[\Omega_{ij}] = 0$  so only the squared terms are left, then use independence.

Rule 1:	$\mathbb{E}[k] = k$
Rule 2:	$\mathbb{E}[k \cdot g[x]] = k \cdot \mathbb{E}[g[x]]$
Rule 3:	$\mathbb{E}[f[x] + g[x]] = \mathbb{E}[f[x]] + \mathbb{E}[g[x]]$
Rule 4:	$\mathbb{E}[f[x]g[y]] = \mathbb{E}[f[x]]\mathbb{E}[g[y]]$ if $x, y$ independent

$$\sigma_{f'}^2 = \mathbb{E}[f_i'^2] - \mathbb{E}[f_i']^2$$

$$= \mathbb{E} \left[ \left( \beta_i + \sum_{j=1}^{D_h} \Omega_{ij} h_j \right)^2 \right] - 0$$

$$= \mathbb{E} \left[ \left( \sum_{j=1}^{D_h} \Omega_{ij} h_j \right)^2 \right]$$

$$= \sum_{j=1}^{D_h} \mathbb{E} [\Omega_{ij}^2] \mathbb{E} [h_j^2]$$

$$= \sum_{j=1}^{D_h} \sigma_\Omega^2 \mathbb{E} [h_j^2] = \sigma_\Omega^2 \sum_{j=1}^{D_h} \mathbb{E} [h_j^2]$$

## Initialization choices.

- Set all the biases to 0
- Weights normally distributed
  - mean 0
  - variance  $\sigma_\Omega^2$

Because the  $\Omega$ 's are zero mean, this is the variance.

$$\begin{aligned}
\sigma_{f'}^2 &= \sigma_\Omega^2 \sum_{j=1}^{D_h} \mathbb{E} [h_j^2] \\
&= \sigma_\Omega^2 \sum_{j=1}^{D_h} \mathbb{E} [\text{ReLU}[f_j]^2] \\
&= \sigma_\Omega^2 \sum_{j=1}^{D_h} \int_{-\infty}^{\infty} \text{ReLU}[f_j]^2 Pr(f_j) df_j \quad \xleftarrow{\text{From the definition of expectation.}} \\
&= \sigma_\Omega^2 \sum_{j=1}^{D_h} \int_{-\infty}^{\infty} (\mathbb{I}[f_j > 0] f_j)^2 Pr(f_j) df_j \\
&= \sigma_\Omega^2 \sum_{j=1}^{D_h} \int_0^{\infty} f_j^2 Pr(f_j) df_j \quad \xleftarrow{\text{Only positive integral limits because of ReLU}} \\
&= \sigma_\Omega^2 \sum_{j=1}^{D_h} \frac{\sigma_f^2}{2} = \frac{D_h \sigma_\Omega^2 \sigma_f^2}{2} \quad \xleftarrow{\text{1/2 of the variance for zero mean distribution}}
\end{aligned}$$

# Aim: keep variance same between two layers

Since:

$$\sigma_{f'}^2 = \frac{D_h \sigma_\Omega^2 \sigma_f^2}{2}$$

Should choose:

$$\sigma_\Omega^2 = \frac{2}{D_h}$$

To get:

$$\sigma_{f'}^2 = \sigma_f^2$$

Kaiming He 何恺明



<https://people.csail.mit.edu/kaiming/>

This is called **He initialization** or **Kaiming initialization**.

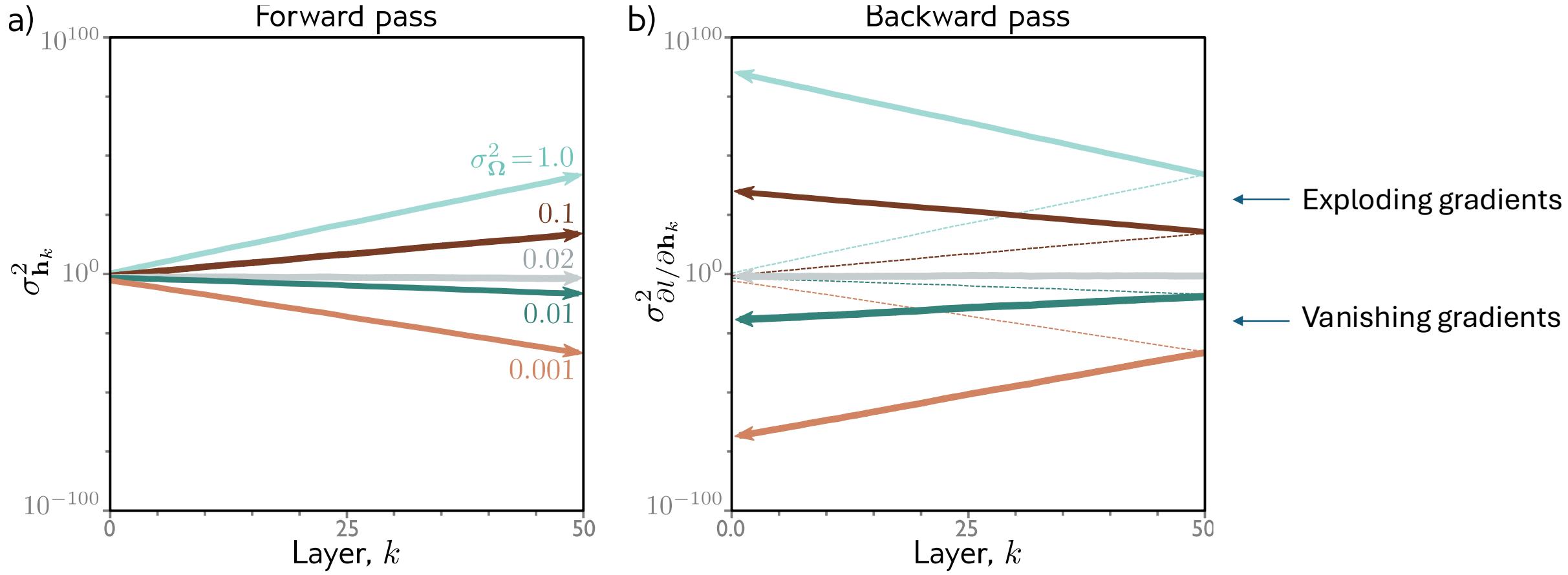
# He initialization (assumes ReLU)

- Forward pass: want the variance of hidden unit activations in layer  $k+1$  to be the same as variance of activations in layer  $k$ :

$$\sigma_{\Omega}^2 = \frac{2}{D_h} \quad \longleftarrow \quad \text{Number of units at layer } k$$

- Backward pass: want the variance of gradients at layer  $k$  to be the same as variance of gradient in layer  $k+1$ :

$$\sigma_{\Omega}^2 = \frac{2}{D_{h'}} \quad \longleftarrow \quad \text{Number of units at layer } k+1$$



**Figure 7.4** Weight initialization. Consider a deep network with 50 hidden layers and  $D_h = 100$  hidden units per layer. The network has a 100 dimensional input  $\mathbf{x}$  initialized with values from a standard normal distribution, a single output fixed at  $y = 0$ , and a least squares loss function. The bias vectors  $\beta_k$  are initialized to zero and the weight matrices  $\Omega_k$  are initialized with a normal distribution with mean zero and five different variances  $\sigma_\Omega^2 \in \{0.001, 0.01, 0.02, 0.1, 1.0\}$ . a)

$$\sigma_\Omega^2 = \frac{2}{D_h} = \frac{2}{100} = 0.02$$

# Default Initialization in PyTorch

[https://pytorch.org/docs/stable/nn.init.html#torch.nn.init.kaiming\\_uniform\\_](https://pytorch.org/docs/stable/nn.init.html#torch.nn.init.kaiming_uniform_)

```
torch.nn.init.kaiming_uniform_(tensor, a=0, mode='fan_in', nonlinearity='leaky_relu',
generator=None) [SOURCE]
```

Fill the input *Tensor* with values using a Kaiming uniform distribution.

The method is described in *Delving deep into rectifiers: Surpassing human-level performance on ImageNet classification* - He, K. et al. (2015). The resulting tensor will have values sampled from  $\mathcal{U}(-\text{bound}, \text{bound})$  where

$$\text{bound} = \text{gain} \times \sqrt{\frac{3}{\text{fan\_mode}}}$$

Also known as He initialization.

# Any Questions?

???

- The need for weights initialization
- Expectations Refresher
- The (Kaiming) He initialization
- Lottery tickets

# Initialization Note

A good initialization does not prevent gradient descent from changing the weights a lot.

- A good initialization keeps the initial gradients modestly sized,
- And modest gradients reduce wild swings in parameters with gradient descent
- Smaller learning rates also help with this.
- Next week's topic, regularization, will directly address this.

# Limitations of Initialization

- No guarantees that the model will train to low losses
- No guarantees that training process won't lead to large values or gradients
- No guarantees that the model won't have lots of inactive units
  - In fact, the estimates adjusted for half being inactive!
- In fact, much of the network is often useless, and could be pruned away!

# The Lottery Ticket Hypothesis: Finding Sparse, Trainable Neural Networks

Neural network pruning techniques can **reduce the parameter counts** of trained networks **by over 90%**, decreasing storage requirements and improving computational performance of inference **without compromising accuracy**. However, contemporary experience is that the sparse architectures produced by pruning are difficult to train from the start, which would similarly improve training performance.

We find that a standard pruning technique naturally uncovers subnetworks whose initializations made them capable of training effectively. Based on these results, we articulate the "lottery ticket hypothesis:" **dense, randomly-initialized, feed-forward networks contain subnetworks ("winning tickets") that - when trained in isolation - reach test accuracy comparable to the original network in a similar number of iterations**. The winning tickets we find have won the initialization lottery: their connections have initial weights that make training particularly effective.

We present an algorithm to identify winning tickets and a series of experiments that support the lottery ticket hypothesis and the importance of these fortuitous initializations. **We consistently find winning tickets that are less than 10-20% of the size of several fully-connected and convolutional feed-forward architectures for MNIST and CIFAR10. Above this size, the winning tickets that we find learn faster than the original network and reach higher test accuracy.**

# Any Questions?

???

- The need for weights initialization
- Expectations Refresher
- The (Kaiming) He initialization
- Lottery tickets

# Disclaimer

- Just because variance of gradients starts the same does not mean that the variance of gradients stays the same.
- You should still check the gradients if you are having training difficulties...

# Bonus Tip

- If you are trying to implement a model based on a paper, and you are having trouble training, check if they shared their code.
  - Many papers omit important initialization details.



- Especially if they say that their method is not sensitive to initialization.



- Also, some paper descriptions of initialization don't match their code.

