



Privacy-preserving Generative Modeling

Presenter:

Dingfan Chen

Supervisor:

Prof. Dr. Mario Fritz

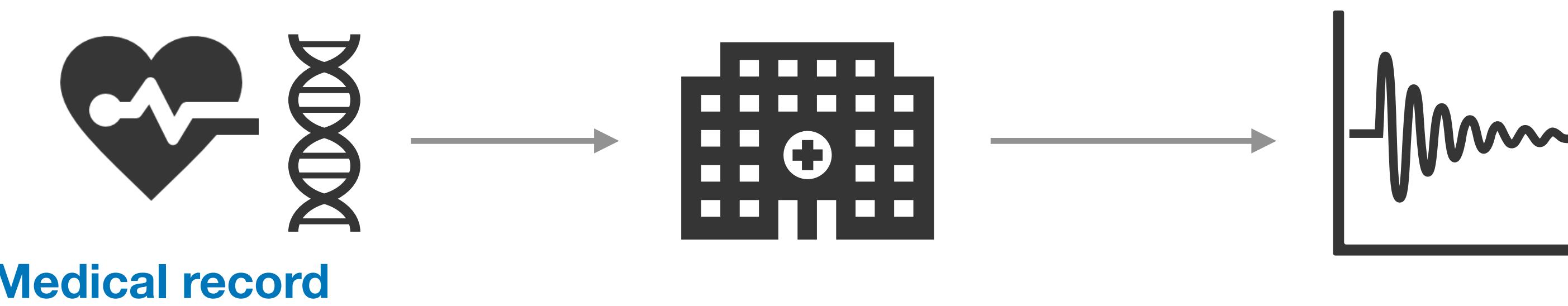
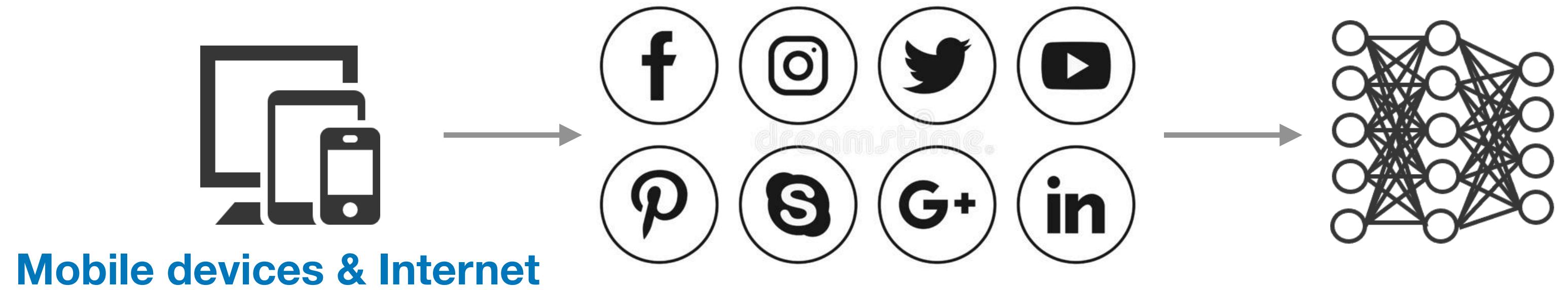
Affiliation:

CISPA – Helmholtz Center for Information Security

Privacy-preserving Generative Modeling

Data Privacy in ML:

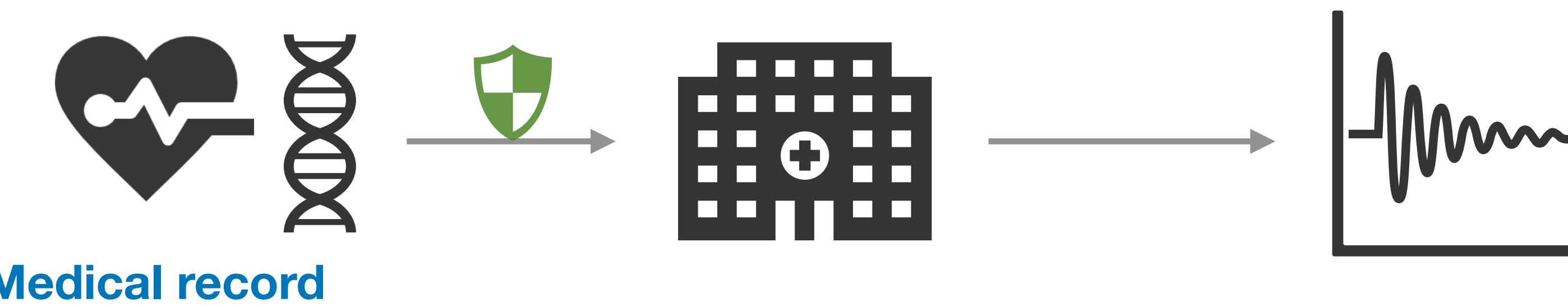
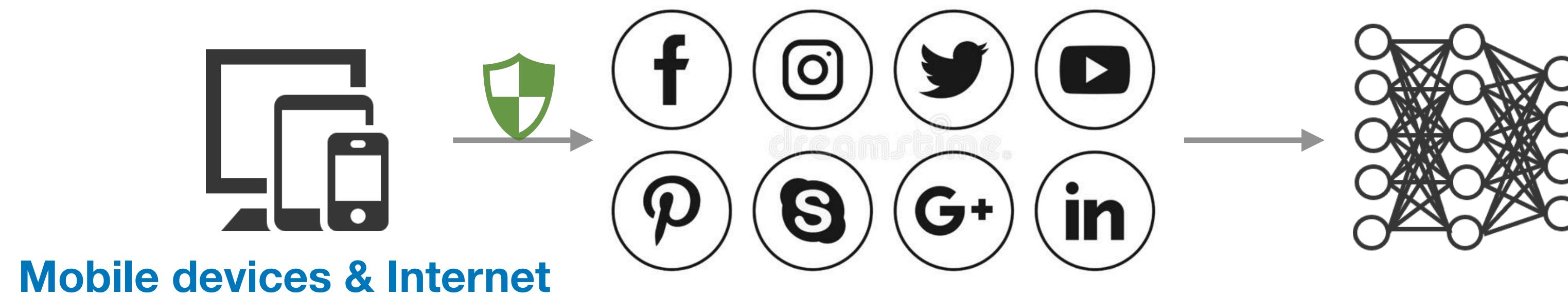
- Sensitive data is **ubiquitous**



Data Privacy in ML:

- Sensitive data is **ubiquitous**

Our task: **Data sanitization**



Data Privacy in ML:

- Protecting privacy is **non-trivial**
 - **Anonymization** vs. **Deidentification**
 (ZIP code, date of birth, gender) is sufficient to identify 87% of US population^{1,2}

Anonymous medical data

ID	QID			SA
	Name	ZIP code	Age	
				Disease
Alice	47677	29	F	Ovarian Cancer
Betty	47602	22	F	Ovarian Cancer
Charles	47678	27	M	Prostate Cancer
David	47905	43	M	Flu
Emily	47909	52	F	Heart Disease
Fred	47906	47	M	Heart Disease

Voter registration data

Name	ZIP code	Age	Sex
Alice	47677	29	F
Bob	47983	65	M
Carol	47677	22	F
Dan	47532	23	M
Ellen	46789	43	F
Fabian	47905	30	M

¹ Golle, Philippe. "Revisiting the uniqueness of simple demographics in the US population.", *Proceedings of the 5th ACM Workshop on Privacy in Electronic Society*, 2006.

² Sweeney, L., "K-anonymity: A model for protecting privacy.", *International Journal of Uncertainty, Fuzziness and Knowledge-Based Systems*, 2002

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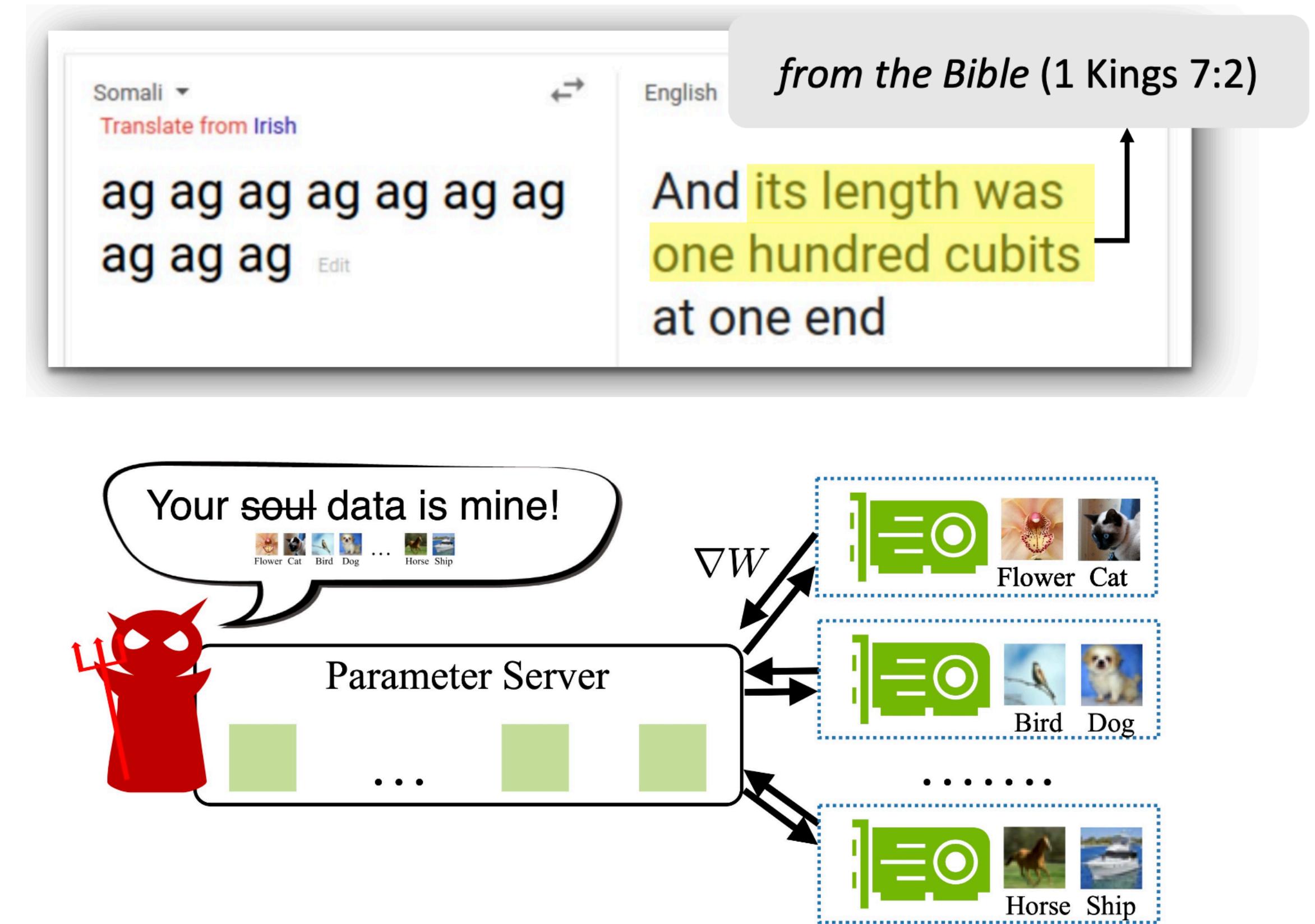
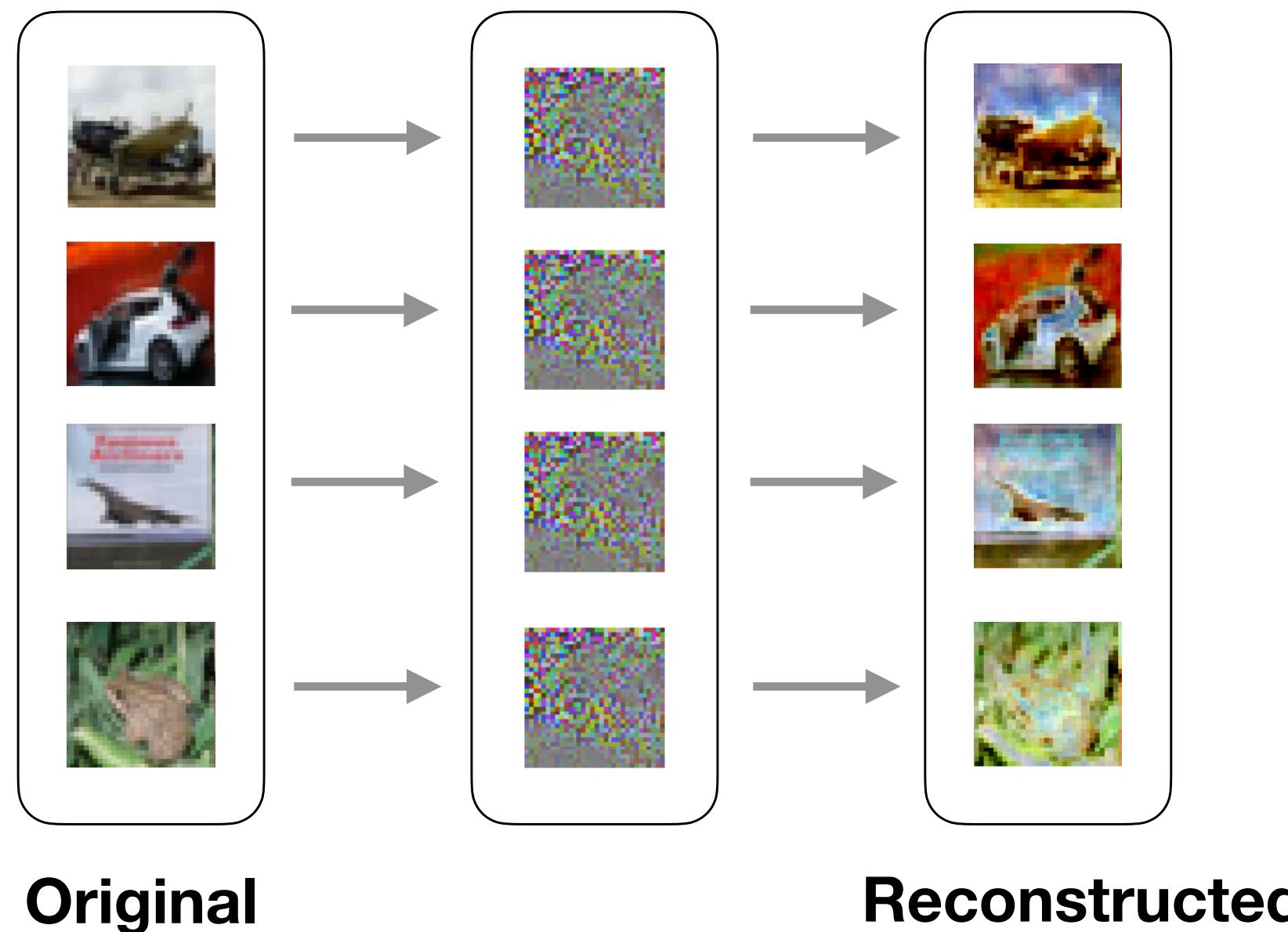
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Data Privacy in ML:

- Protecting privacy is **non-trivial**
 - **Reconstruction** from features, models, gradients, etc.



¹ Carlini, Nicholas, et al. "Is Private Learning Possible with Instance Encoding?." *IEEE Security & Privacy*, 2021.

² Carlini, Nicholas, et al. "Extracting training data from large language models." *USENIX Security 21*, 2021.

³ Zhu, Ligeng, et al. "Deep leakage from gradients.", *NeurIPS*, 2019.

Rigorous Privacy Guarantee

¹ Dwork. “Differential privacy.”, Automata, languages and programming, 2006

² Mironov, Ilya, “Renyi Differential Privacy”, CSF, 2017

Rigorous Privacy Guarantee

Differential privacy (DP)¹

- Belonging to a dataset \approx Not belonging to it
- A mechanism \mathcal{A} is (ε, δ) -DP iff for any **neighboring datasets** D and D' differing in a single data point, and any $S \subseteq \text{range}(\mathcal{A})$, we have:

$$\Pr[\mathcal{A}(D) \in S] \leq e^\varepsilon \cdot \Pr[\mathcal{A}(D') \in S] + \delta$$

- **Bound the maximal influence** of each individual, introduce **randomness**
- Currently, people always turn it into bounding the divergence²:

$$D_\alpha(\mathcal{A}(D) \| \mathcal{A}(D')) \leq \varepsilon$$

Properties

- Allows **quantifying** the privacy risk
- Compose gracefully for iterative methods
- Closed under **post-processing**

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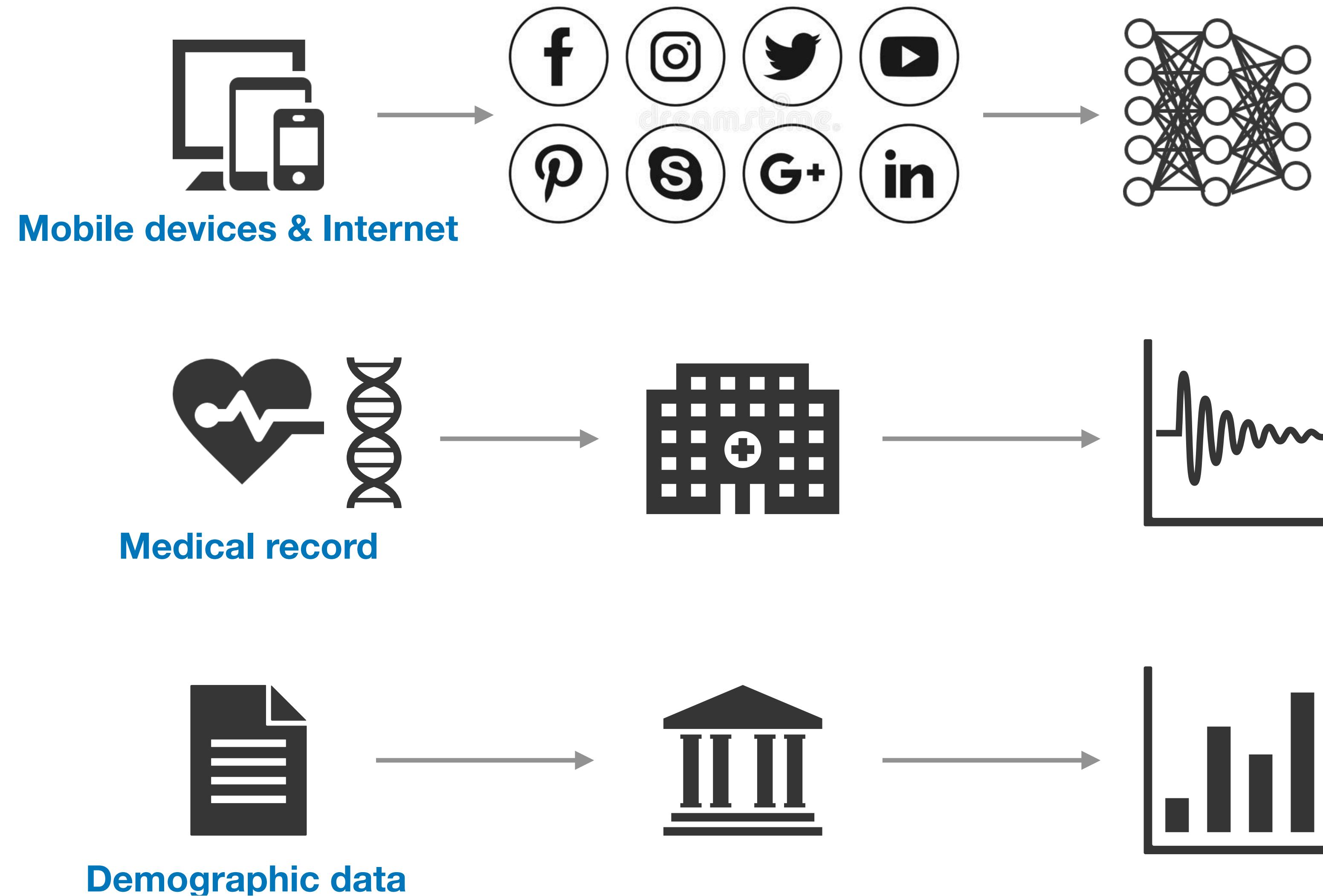
- Allows **quantifying** the privacy risk
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Sanitized data can be freely used for downstream analysis

¹ Dwork. "Differential privacy.", Automata, languages and programming, 2006

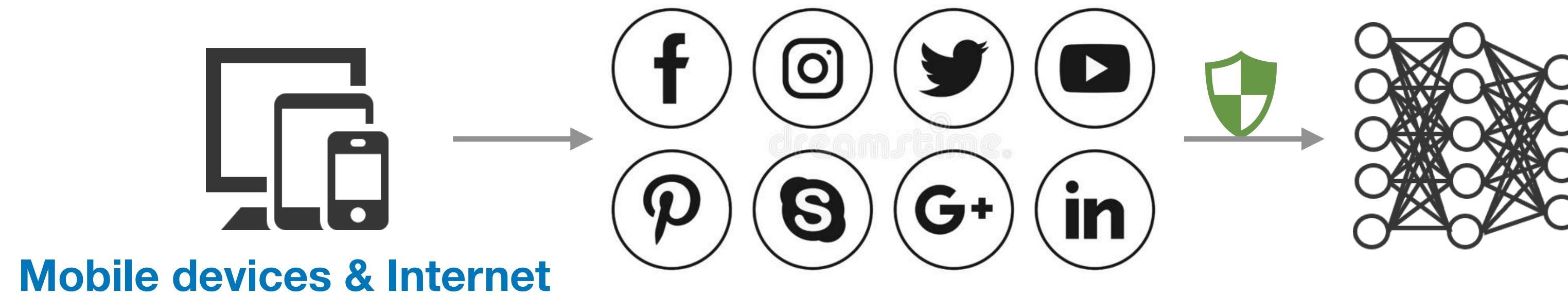
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Privacy-preserving Generation vs. Analysis



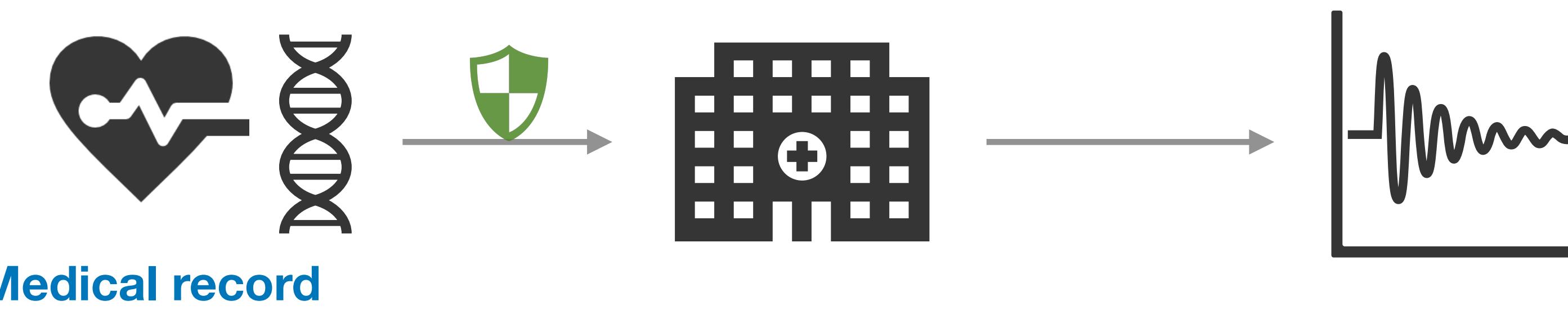
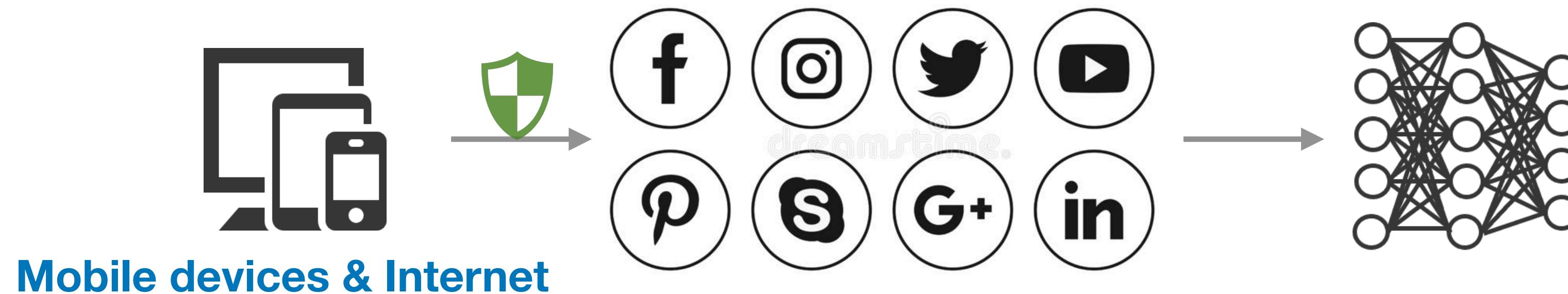
Privacy-preserving Generation vs. Analysis

Privacy-preserving analysis



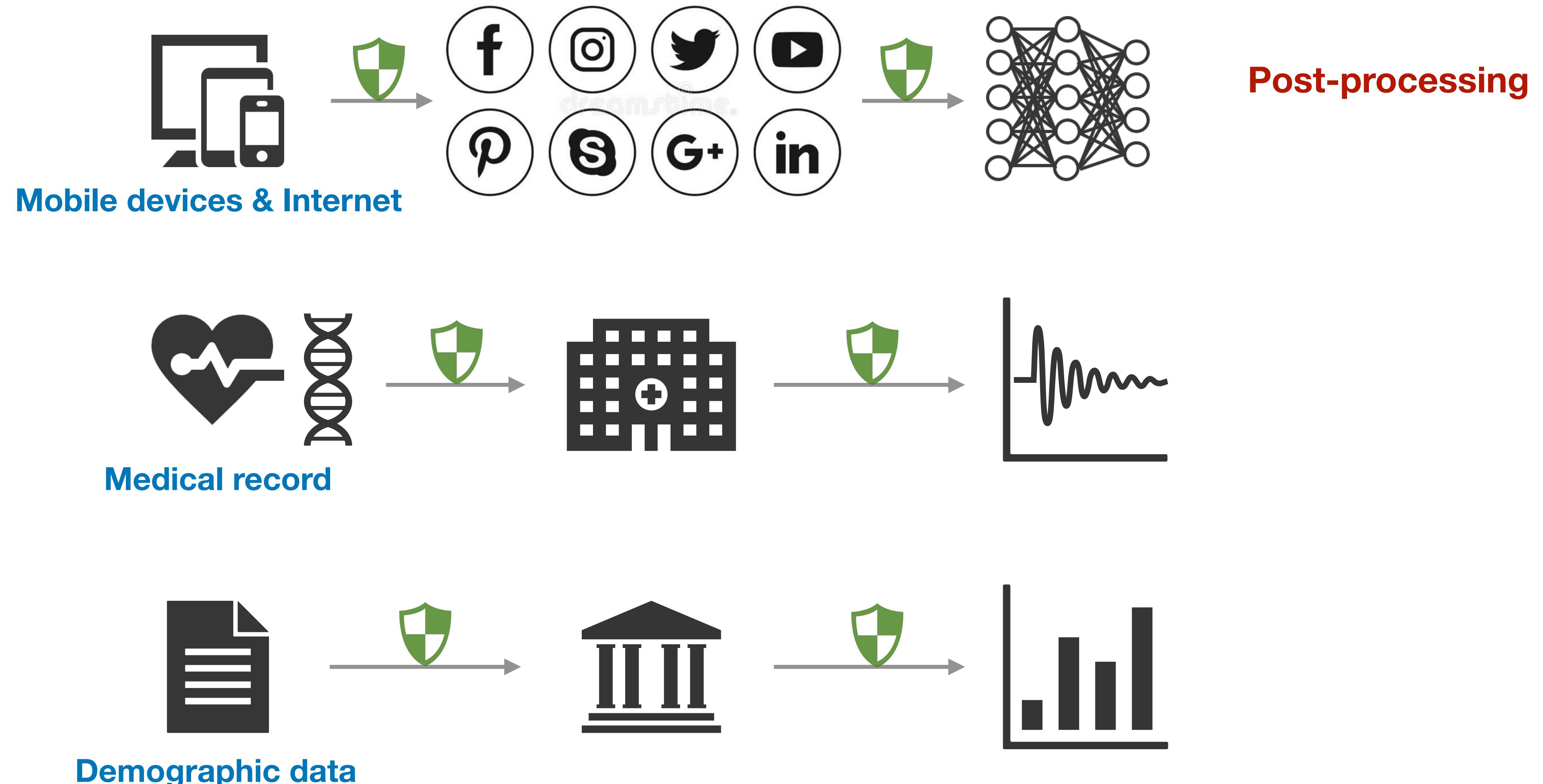
Privacy-preserving Generation vs. Analysis

Our task: Data sanitization



Privacy-preserving Generation vs. Analysis

Our task: **Data sanitization**



How to Train a Model under DP?

Algorithm 1 Differentially private SGD (Outline)

Input: Examples $\{x_1, \dots, x_N\}$, loss function $\mathcal{L}(\theta) = \frac{1}{N} \sum_i \mathcal{L}(\theta, x_i)$. Parameters: learning rate η_t , noise scale σ , group size L , gradient norm bound C .

Initialize θ_0 randomly

for $t \in [T]$ **do**

 Take a random sample L_t with sampling probability L/N

Compute gradient

 For each $i \in L_t$, compute $\mathbf{g}_t(x_i) \leftarrow \nabla_{\theta_t} \mathcal{L}(\theta_t, x_i)$

Clip gradient

$\bar{\mathbf{g}}_t(x_i) \leftarrow \mathbf{g}_t(x_i) / \max(1, \frac{\|\mathbf{g}_t(x_i)\|_2}{C})$

Add noise

$\tilde{\mathbf{g}}_t \leftarrow \frac{1}{L} (\sum_i \bar{\mathbf{g}}_t(x_i) + \mathcal{N}(0, \sigma^2 C^2 \mathbf{I}))$

Descent

$\theta_{t+1} \leftarrow \theta_t - \eta_t \tilde{\mathbf{g}}_t$

Output θ_T and compute the overall privacy cost (ε, δ) using a privacy accounting method.

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$$\mathcal{M}(D) \triangleq f(D) + \mathcal{N}(0, S_f^2 \cdot \sigma^2)$$

\mathcal{M} : Gaussian Mechanism

D : Dataset

f : Real-valued function

S_f : Sensitivity

σ : Noise scale

$$S_f = \max_{D, D'} \|f(D) - f(D')\|_2$$

Sensitivity

$$S_f = \max_{x_i} \|\bar{\mathbf{g}}_t(x_i)\|_2 = C$$

Privacy-preserving Generative Modeling

Generative Models

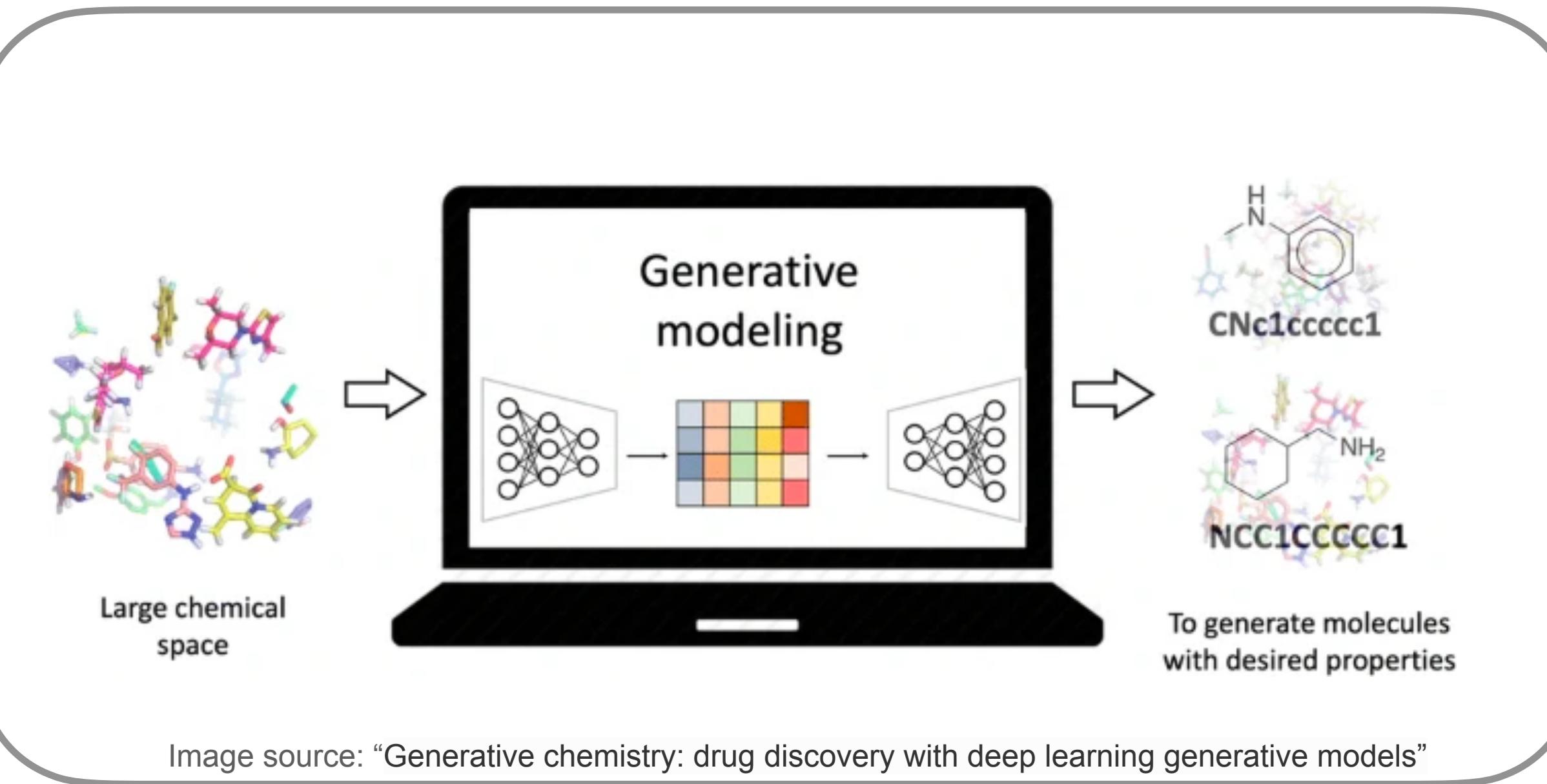
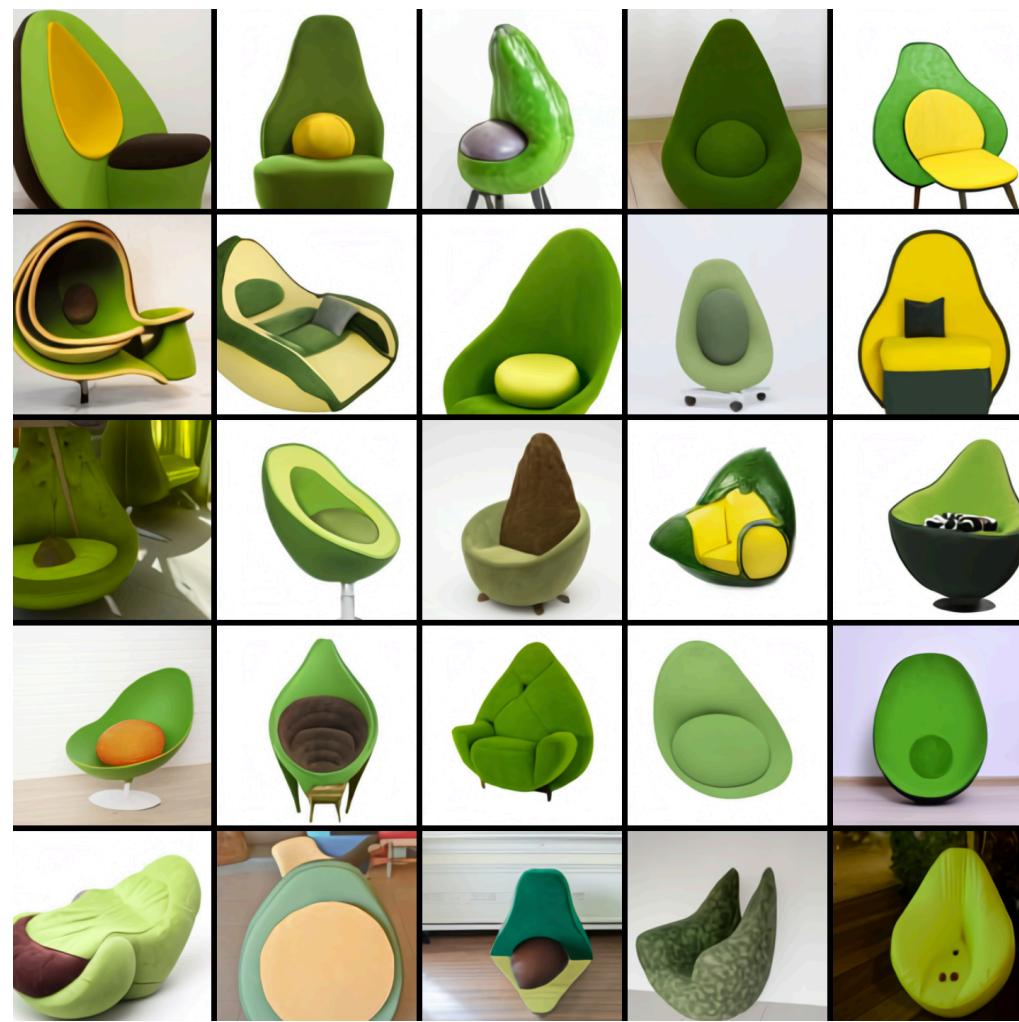


Image source: "Generative chemistry: drug discovery with deep learning generative models"

"An armchair in the shape of an avocado"



"A snail made of a harp"



Image source: <https://openai.com/blog/dall-e/>

a) Real structures



e) Torsion GAN



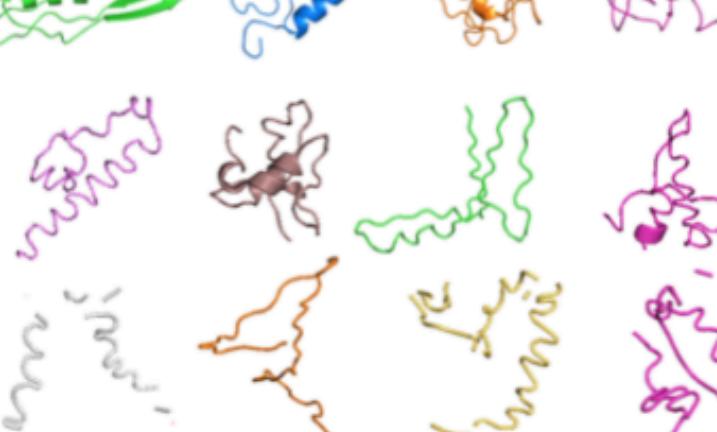
b) GAN, folded by fragment sampling



f) TorusDBN



c) GAN, folded by ADMM



g) FB5-HMM, folded by fragment sampling

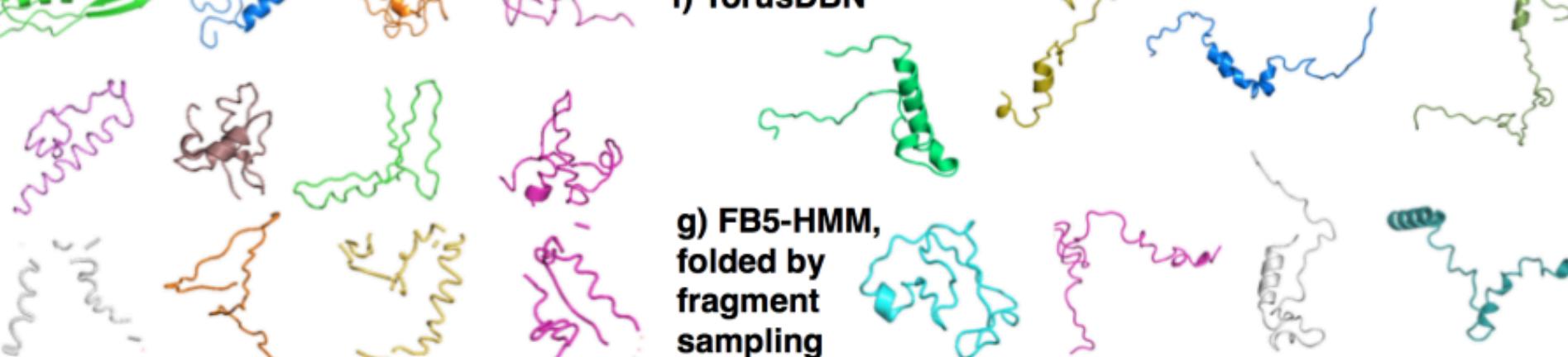
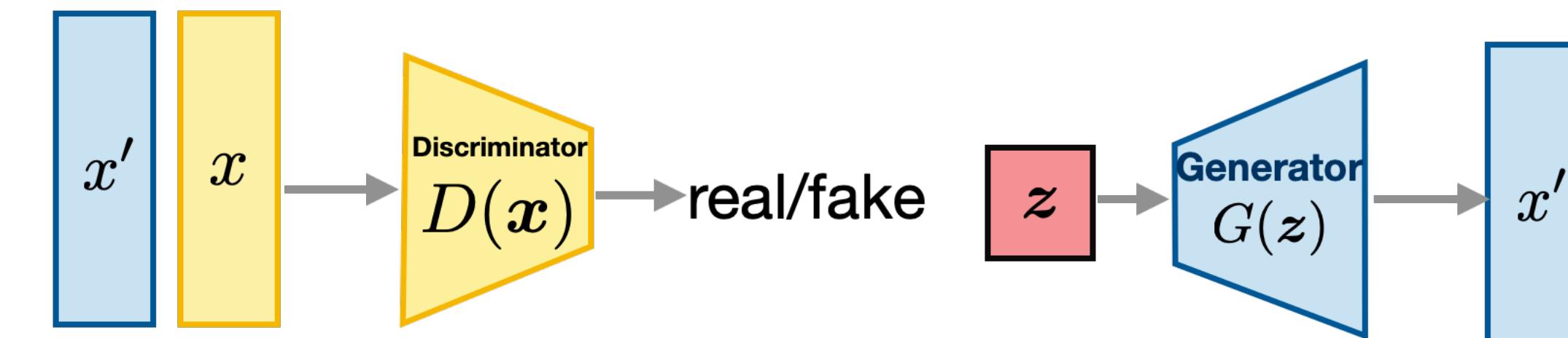


Image source: "Generative Modeling for Protein Structures"

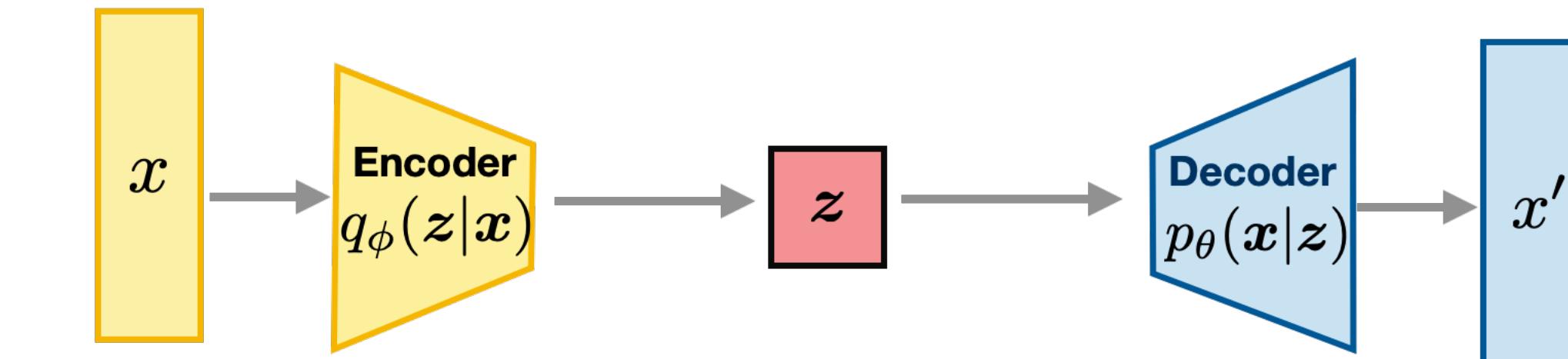
Generative Models

- **Overview:**

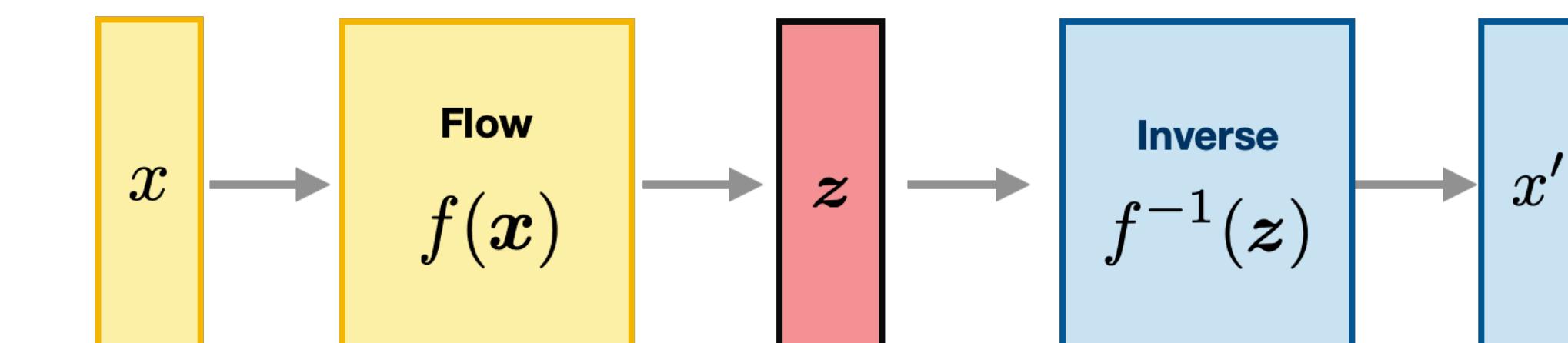
- **GAN:** Adversarial training



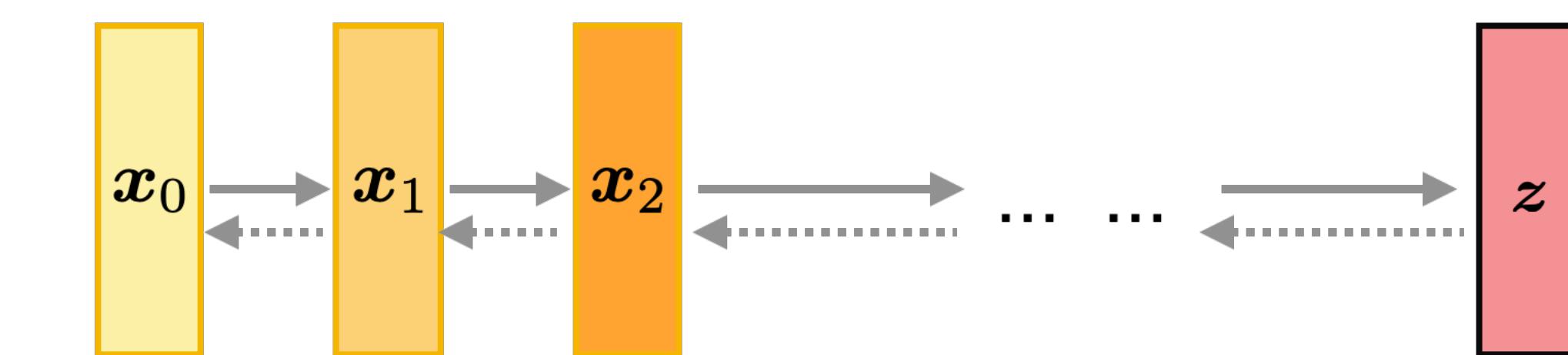
- **VAE:** Maximize variational lower bound



- **Flow-based:** Invertible transforms of distributions



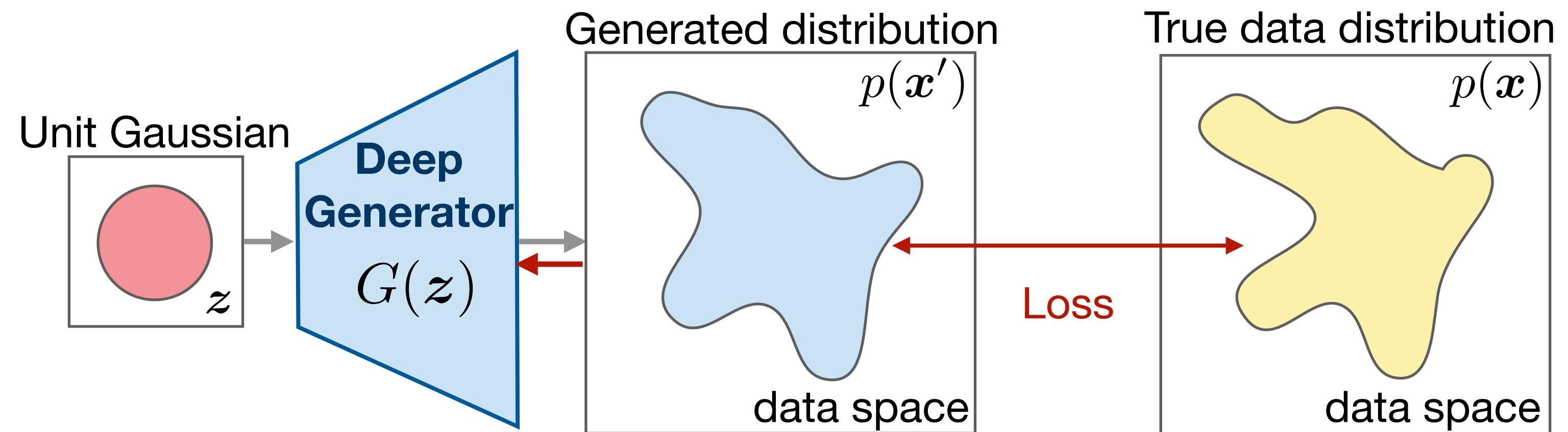
- **Diffusion models:** Gradually add Gaussian noise and reverse



Generative Models

- **Overview:**

- Latent variable model $z \rightarrow x$
- Learn a mapping from simple distribution $p(z)$ to complex data distribution

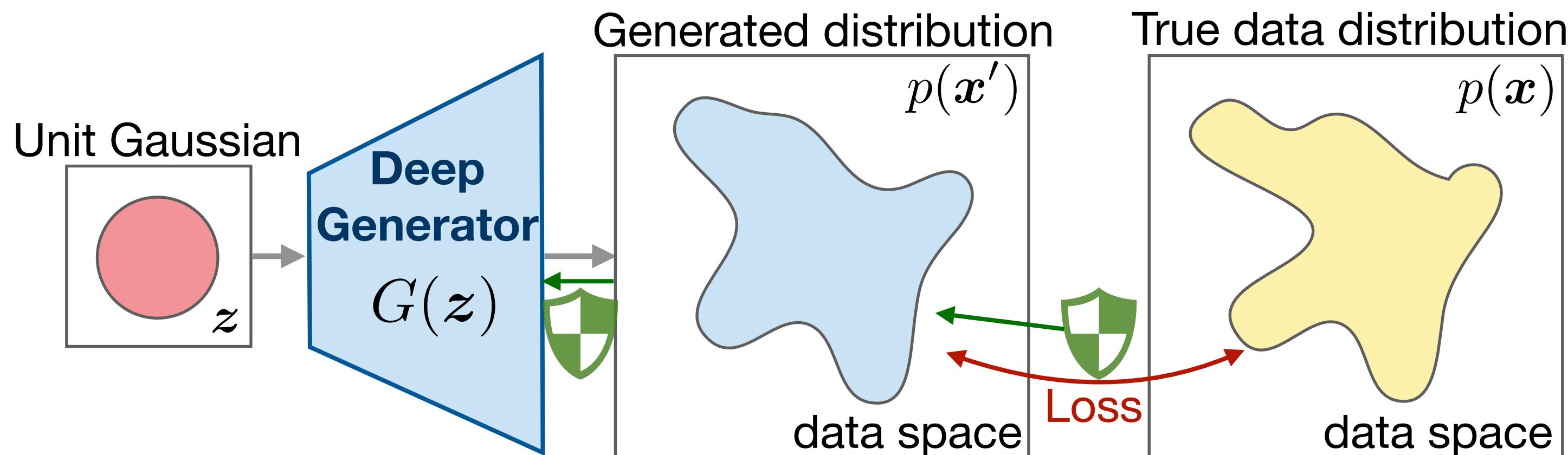


Privacy-preserving Data Generation

- **Task:**
 - Learn to generate high-dimensional **sanitized data**

- **Key:**
 - Rigorous privacy guarantee → Differential Privacy
 - High-dimensional data → Deep Neural Networks
 - General purpose → Generality & Expressiveness

- **Overview:**



Existing Solutions

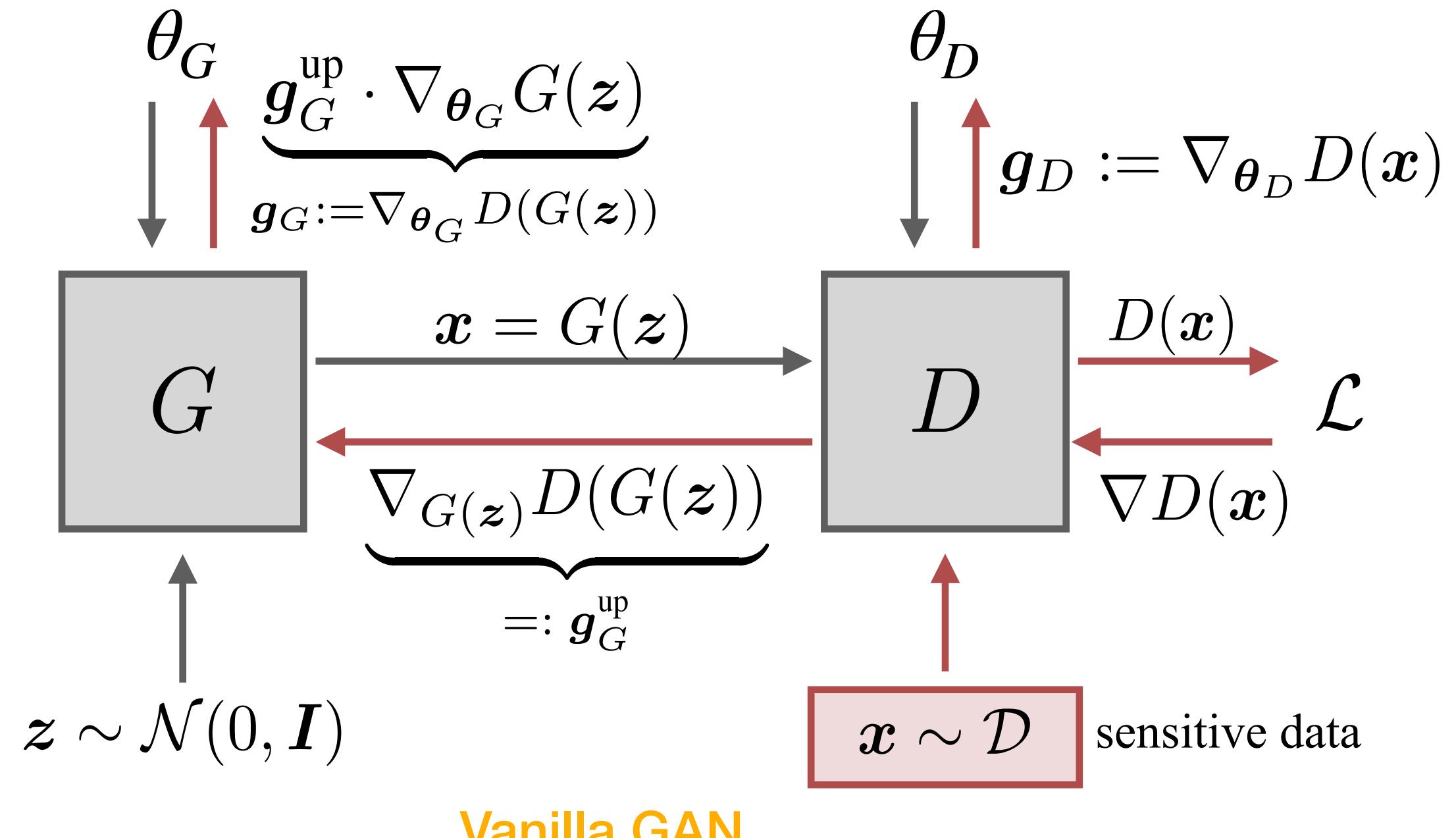
- **Generative adversarial networks (GANs):**

- Gradient

$$\mathbf{g}^{(t)} := \nabla_{\theta} \mathcal{L}(\theta_D, \theta_G)$$

- Gradient descent step

$$\theta^{(t+1)} := \theta^{(t)} - \eta \cdot \mathbf{g}^{(t)}$$



Vanilla GAN

→ non-private	→ sensitive	→ (ε, δ) -private
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Existing Solutions

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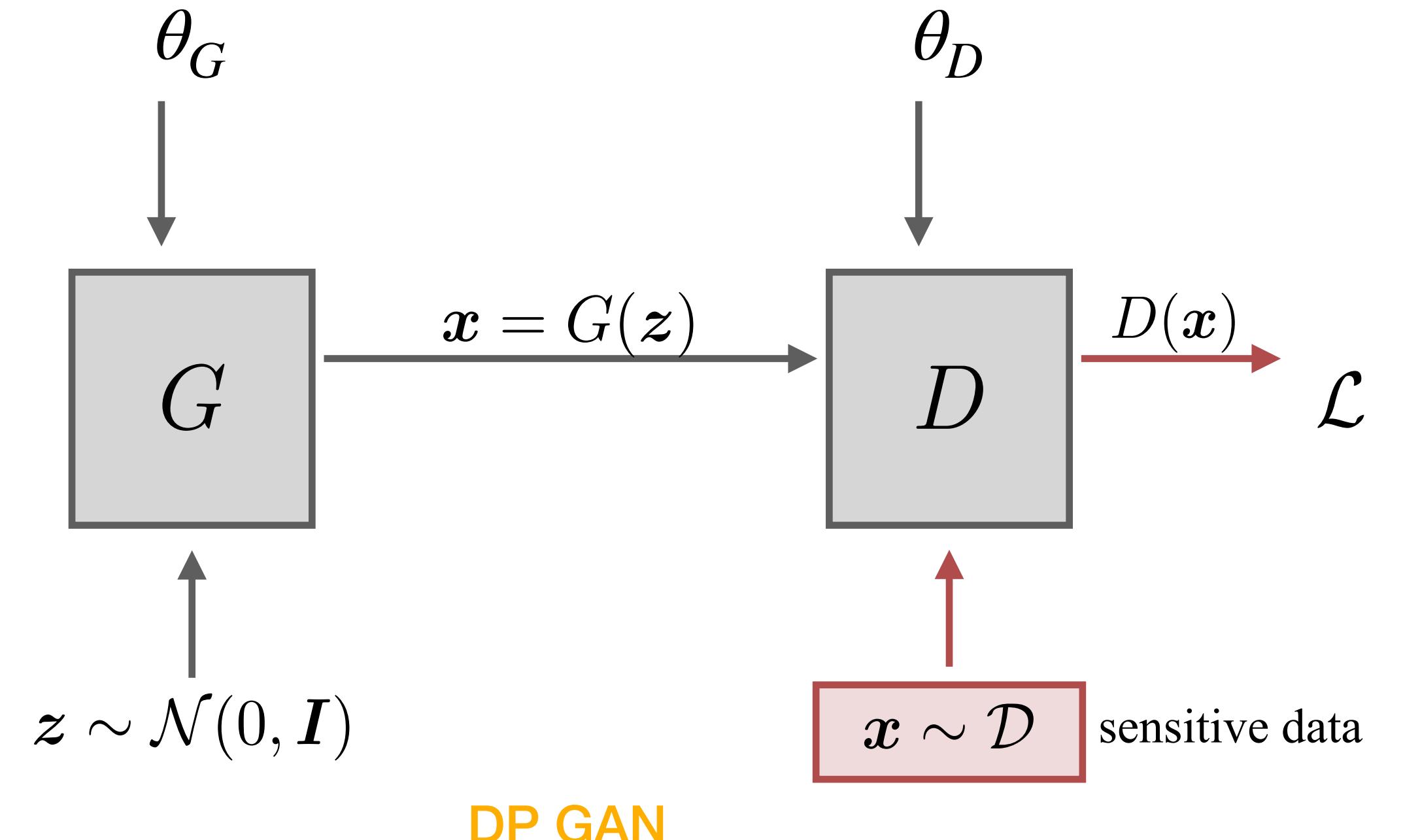
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- Sanitization mechanism

$$\begin{aligned}\hat{\mathbf{g}}^{(t)} &:= \mathcal{M}_{\sigma, C}(\mathbf{g}^{(t)}) \\ &= \text{clip}(\mathbf{g}^{(t)}, C) + \mathcal{N}(0, \sigma^2 C^2 \mathbf{I})\end{aligned}$$

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Existing Solutions

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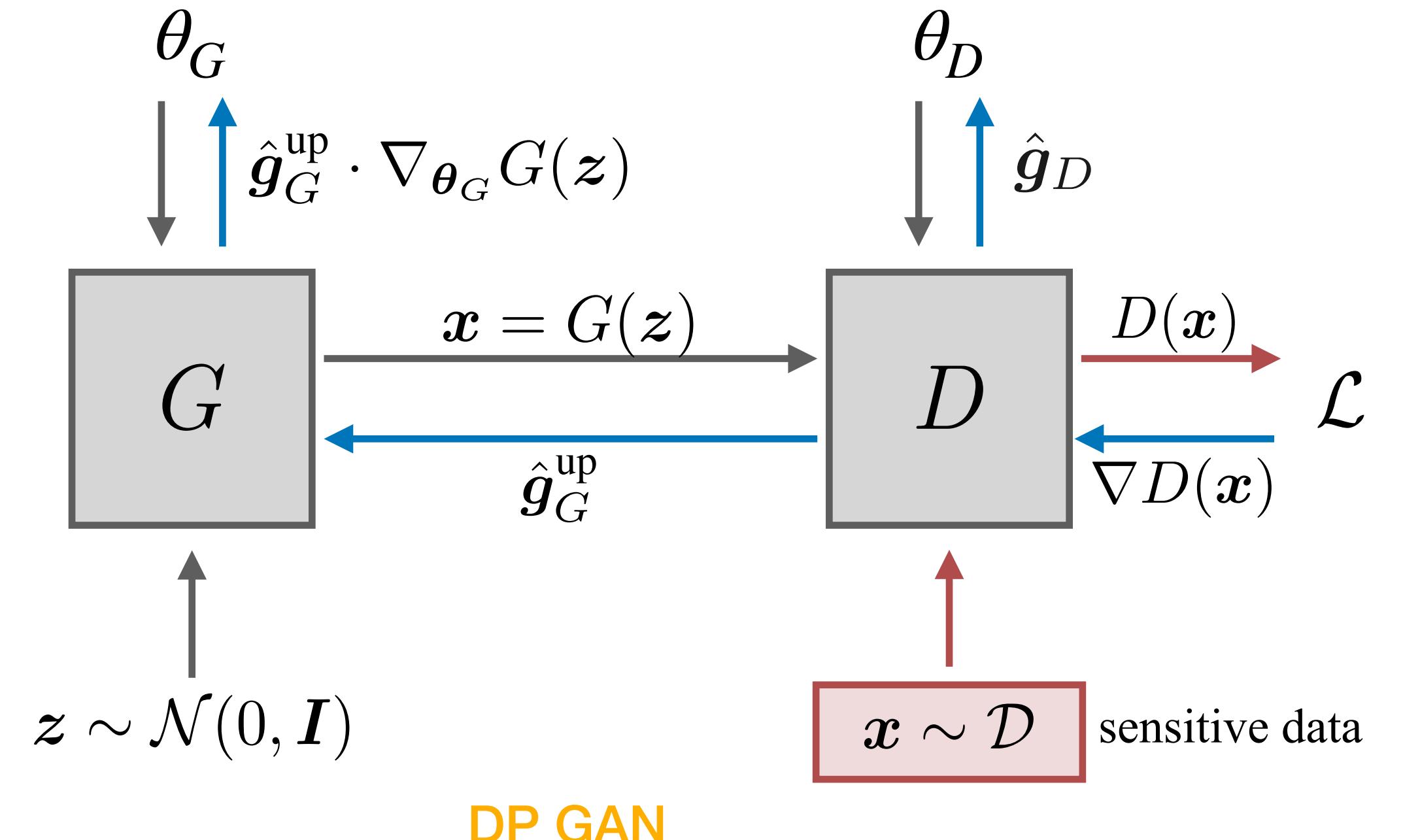
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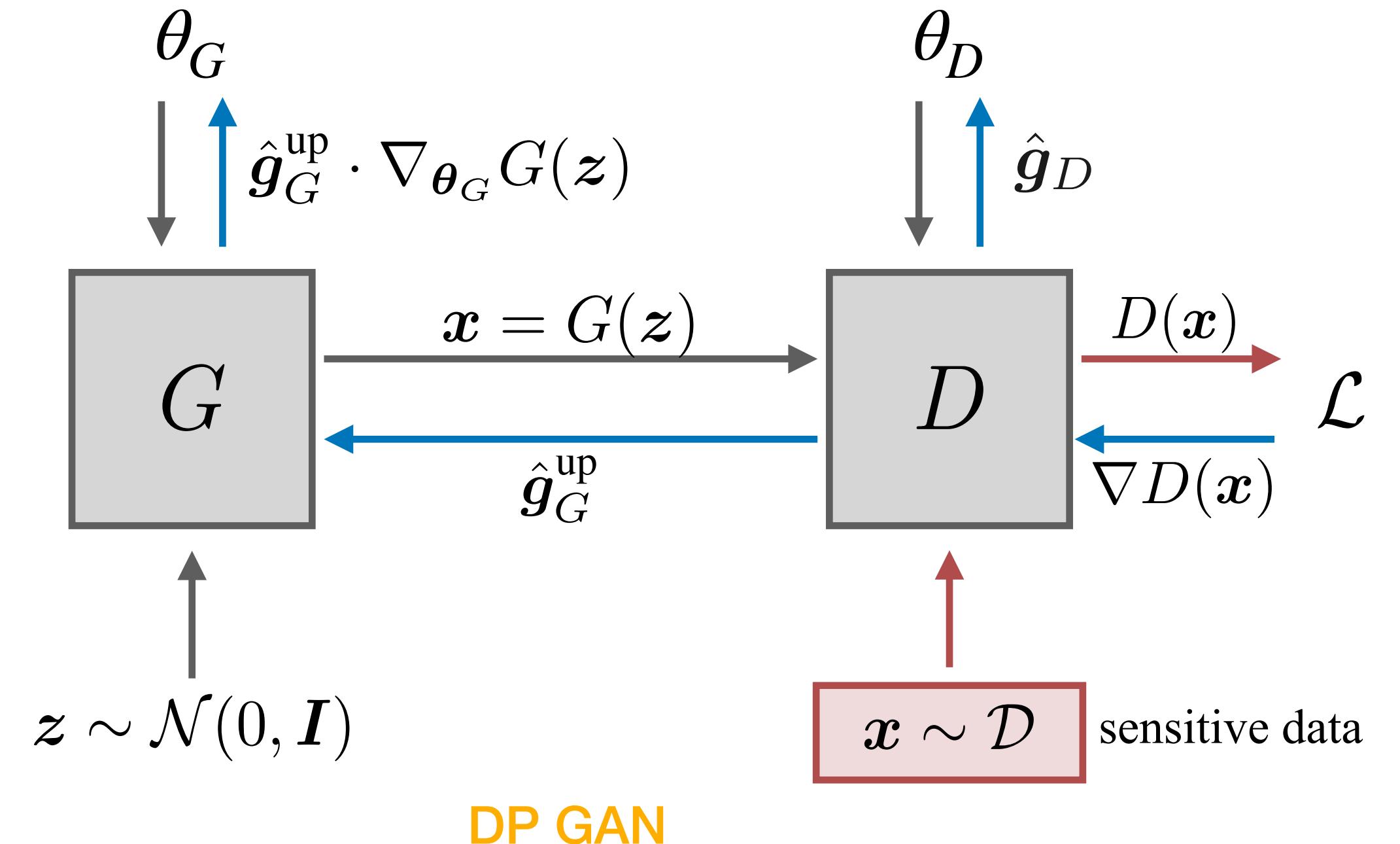
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clipping bound

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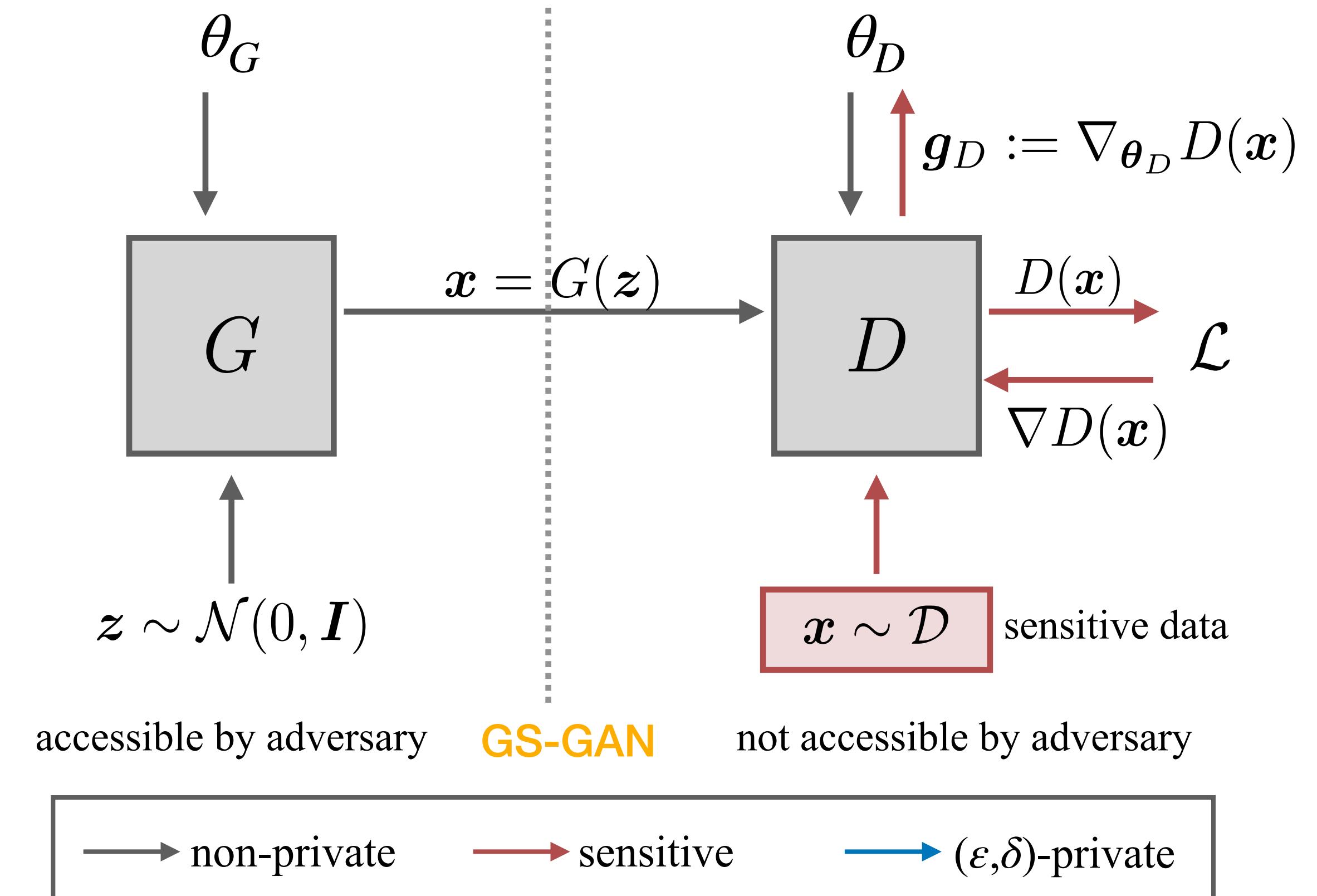
DP GAN

→ non-private → sensitive → (ε, δ) -private

GS-WGAN: A Gradient-Sanitized Approach for Learning Differentially Private Generators (NeurIPS 2020)

- **Insight:**

- Only the *generator* need to be publicly-released



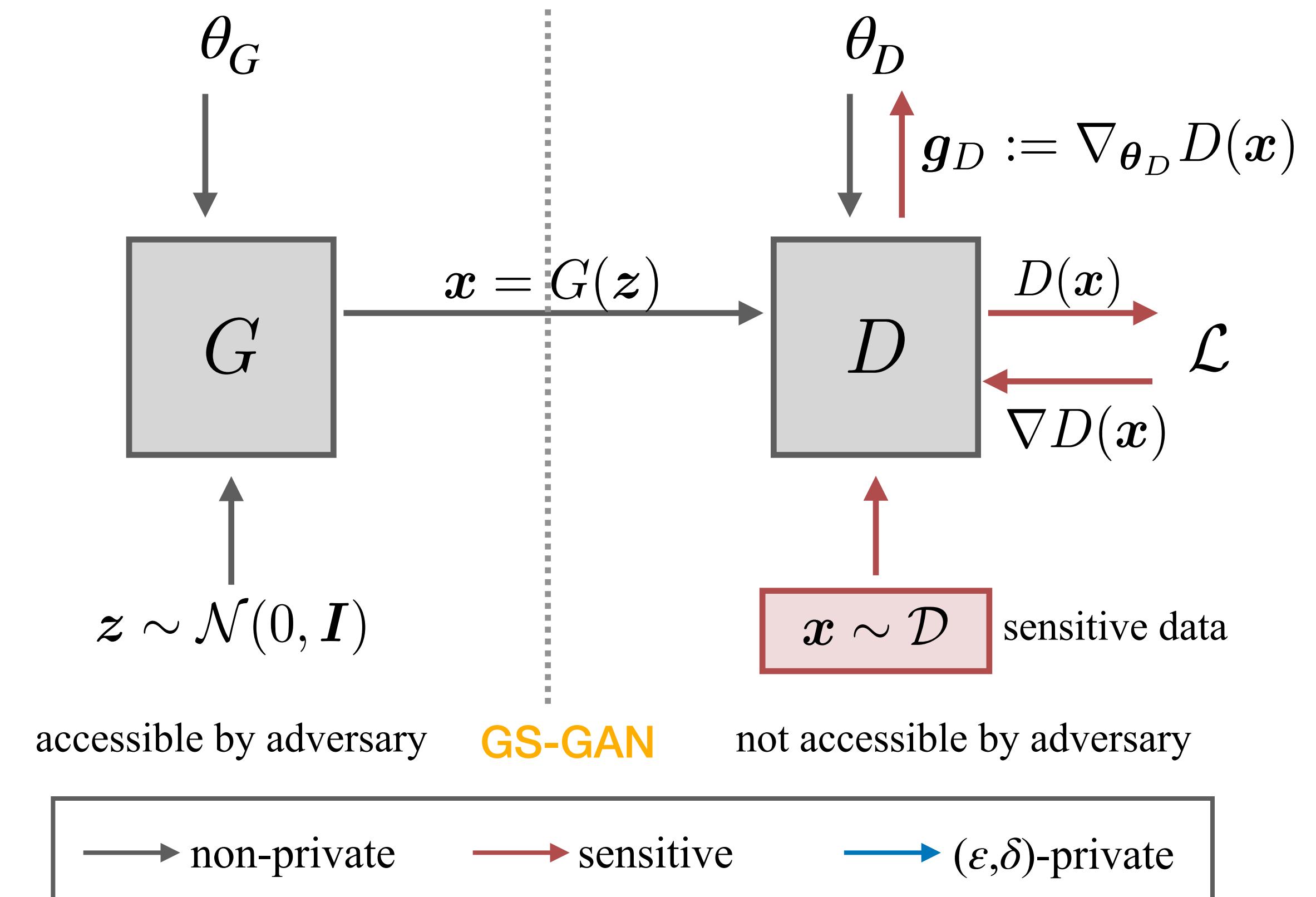
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- **Our framework:**

1. Selectively applying sanitization mechanism



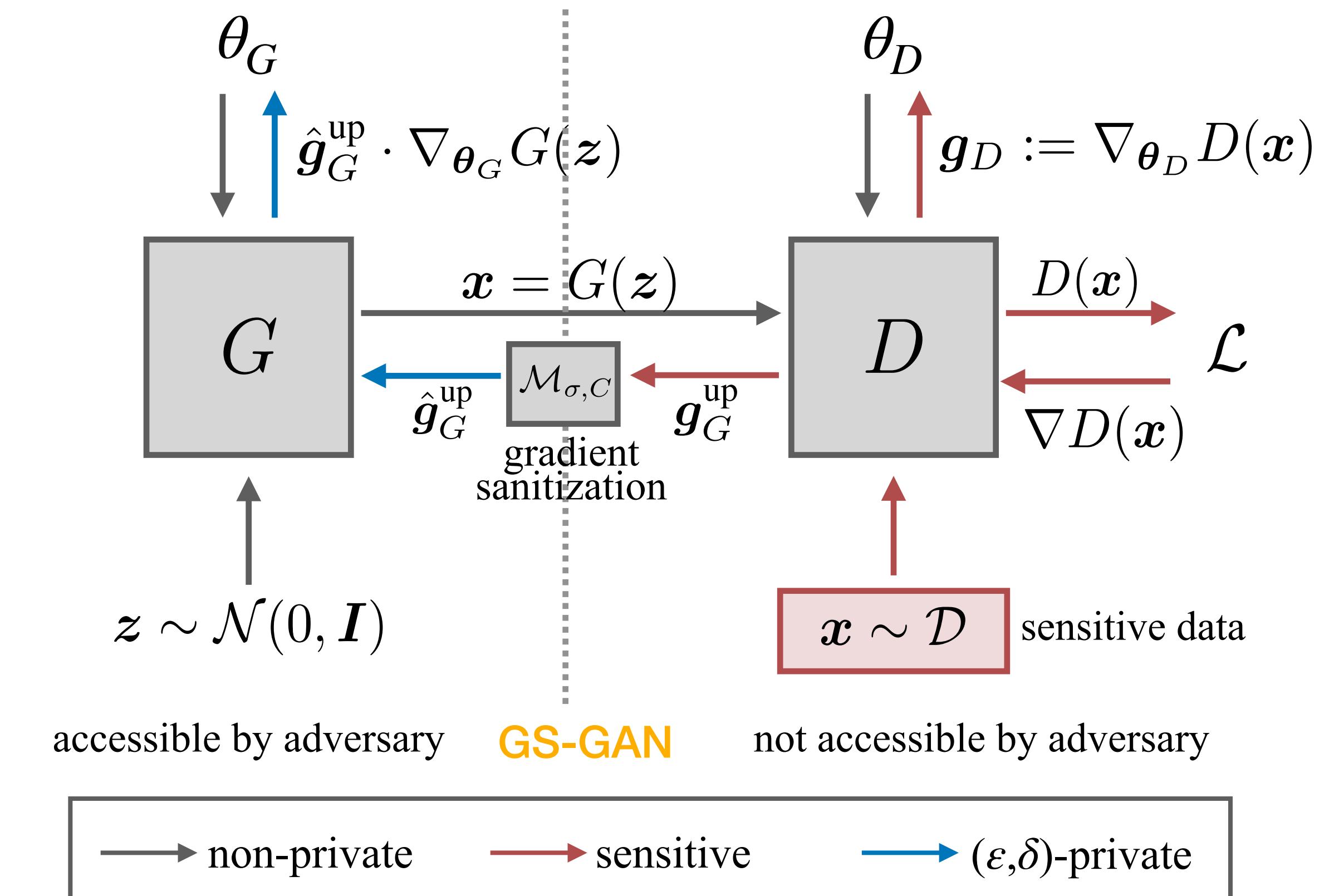
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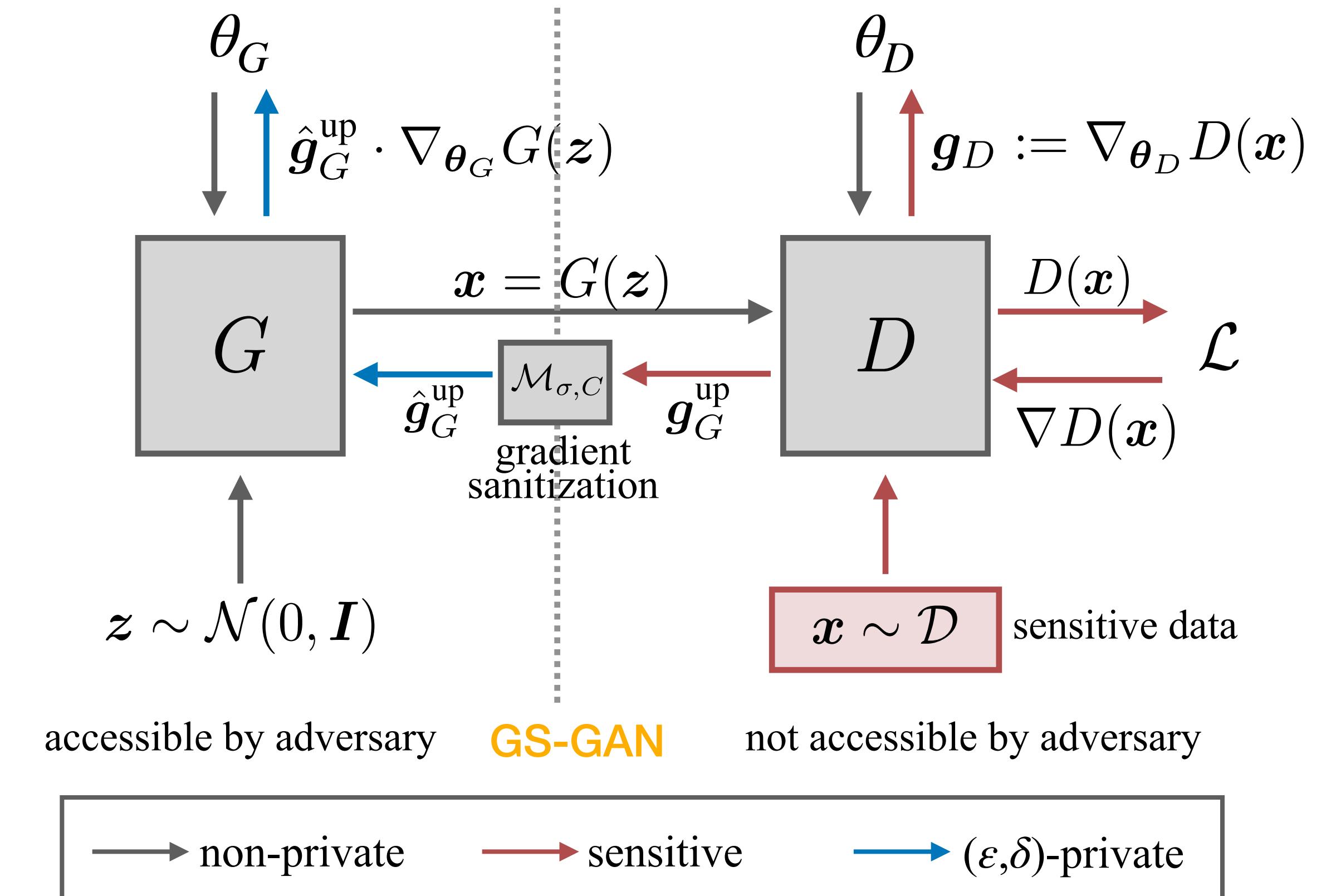
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- **Advantages:**

1. Maximally preserve the true gradient direction



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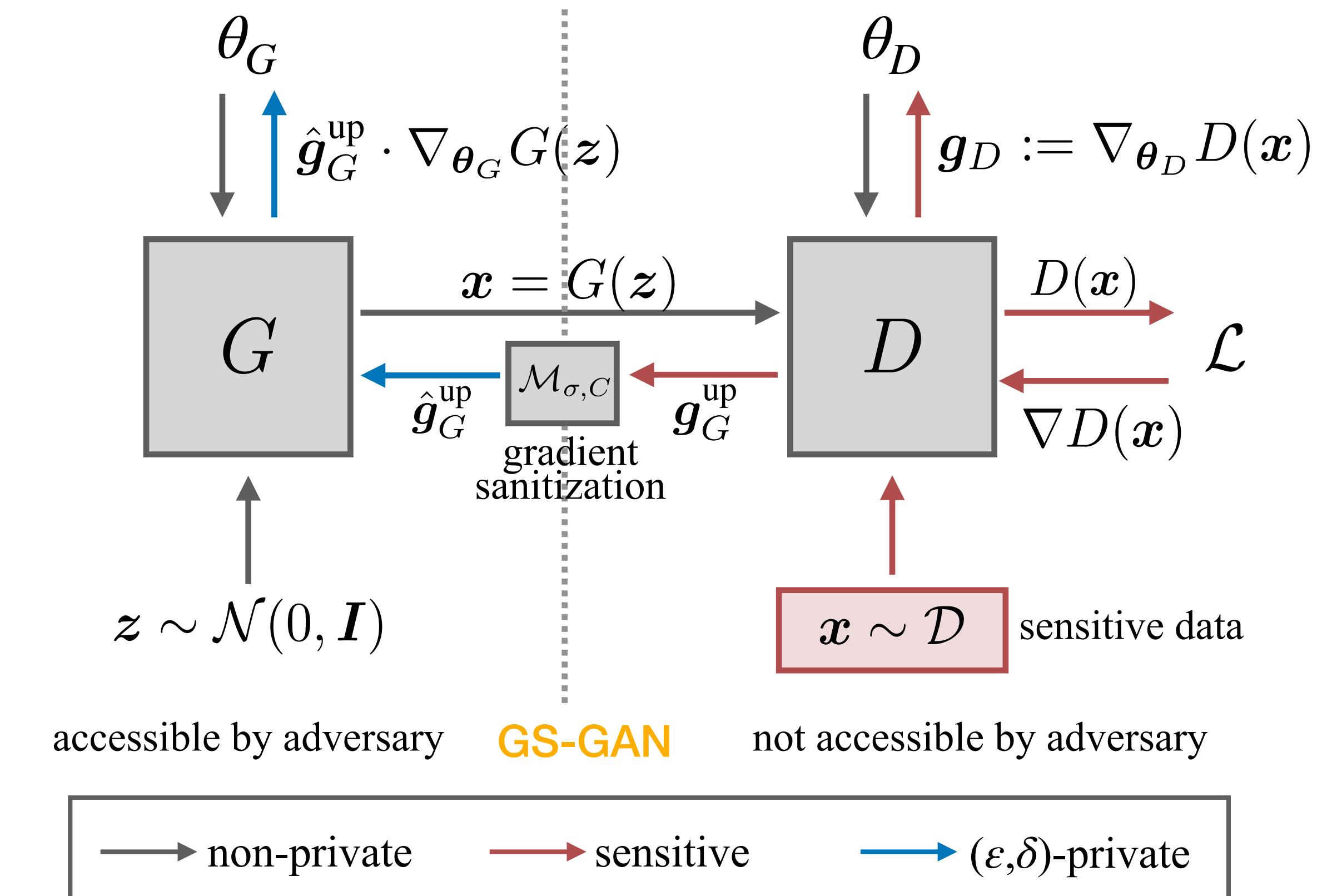
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2. Bounding sensitivity using Wasserstein distance

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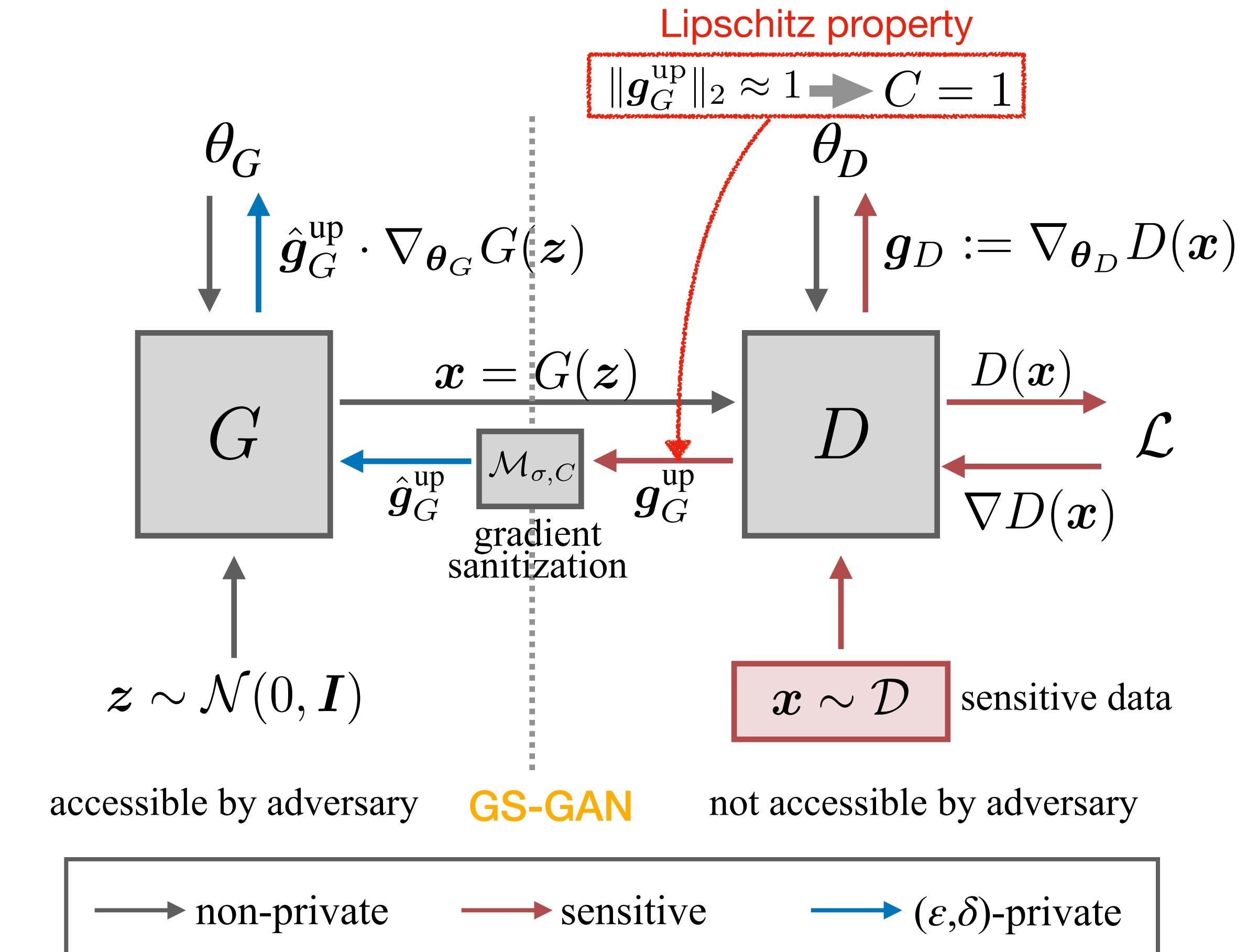
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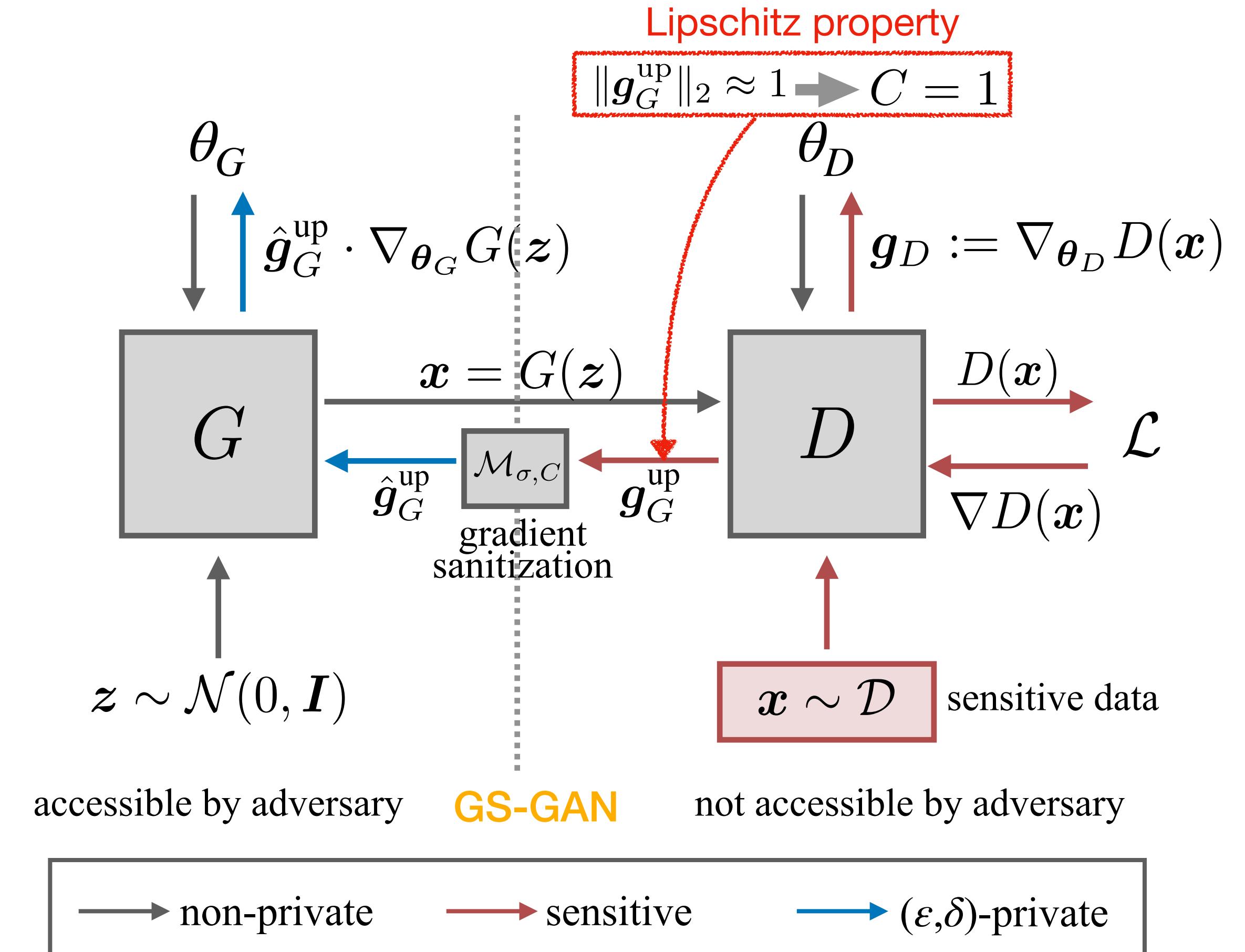
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1. Maximally preserve the true gradient direction
2. Bypass an intensive and fragile hyper-parameter search for clipping value
3. Small clipping bias



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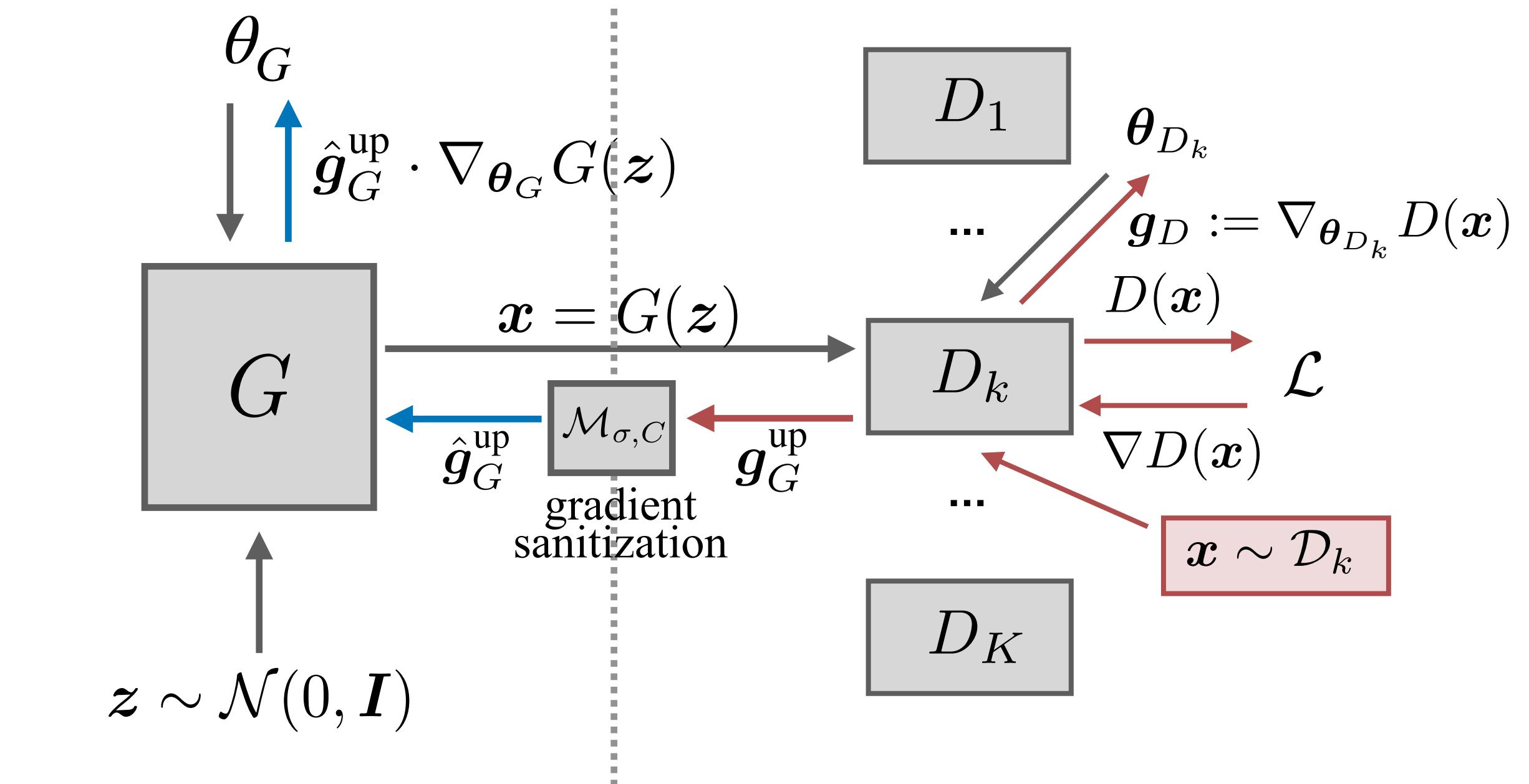
- Decentralized (Federated) setting:

- Each user train a discriminator on its sensitive dataset locally
- Communicate the sanitized gradient

- Advantages:

- User-level DP guarantee under an *untrusted* server
- Communication-efficient (gradients w.r.t. generated samples are *more compact* than gradients w.r.t model parameters¹)

$$\dim(\hat{g}_G^{\text{up}}) \ll \dim(\theta_G) \ll \dim(\theta_G) + \dim(\theta_D)$$



accessible by adversary **Fed-GS-GAN** not accessible by adversary

GS-WGAN: A Gradient-Sanitized Approach for Learning Differentially Private Generators (NeurIPS 2020)

Session 7A: Privacy Attacks and Defenses for ML

CCS '21, November 15–19, 2021, Virtual Event, Republic of Korea

- Adopted and extended by SOTA following works:

- Long, Yunhui, et al., "G-PATE: Scalable Differentially Private Data Generator via Private Aggregation of Teacher Discriminators." (*NeurIPS*, 2021)
- Cao, Tianshi, et al., "Don't Generate Me: Training Differentially Private Generative Models with Sinkhorn Divergence.", (*NeurIPS*, 2021)
- Wang, Boxin et al., "DataLens: Scalable privacy preserving training via gradient compression and aggregation." (*CCS*, 2021)

DataLens: Scalable Privacy Preserving Training via Gradient Compression and Aggregation

Don't Generate Me: Training Differentially Private Generative Models

G-PATE: Scalable Differentially Private Data Generator via Private Aggregation of Teacher Discriminators

Yunhui Long^{1*} Boxin Wang^{1*} Zhuolin Yang¹ Bhavya Kailkhura² Aston Zhang¹

Carl A. Gunter¹

Bo Li¹

¹ University of Illinois, Urbana Champaign ² Lawrence Livermore National Laboratory
(ylong4, boxinw2, zhuolin8, lzhang74, cgunter, lbo}@illinois.edu

Abstract

Recent advances in machine learning have largely benefited from the massive accessible training data. However, large-scale data sharing has raised great privacy concerns. In this work, we propose a novel privacy-preserving data Generative model based on the PATE framework (G-PATE), aiming to train a scalable differentially private data generator which preserves high generated data utility. Our approach leverages generative adversarial nets to generate data, combined with private aggregation among different discriminators to ensure strong privacy guarantees. Compared to existing approaches, G-PATE significantly improves the use of privacy budgets. In particular, we train a student data generator with an ensemble of teacher discriminators and propose a novel private gradient aggregation mechanism to ensure differential privacy on all information that flows from teacher discriminators to the student generator. In addition, with random projection and gradient discretization, the proposed gradient aggregation mechanism is able to effectively deal with high-dimensional gradient vectors. Theoretically, we prove that G-PATE ensures differential privacy for the data generator. Empirically, we demonstrate the superiority of G-PATE over prior work through extensive experiments. We show that G-PATE is the first work being able to generate high-dimensional image data with high data utility under limited privacy budgets ($\epsilon \leq 1$). Our code is available at <https://github.com/AI-secure/G-PATE>.

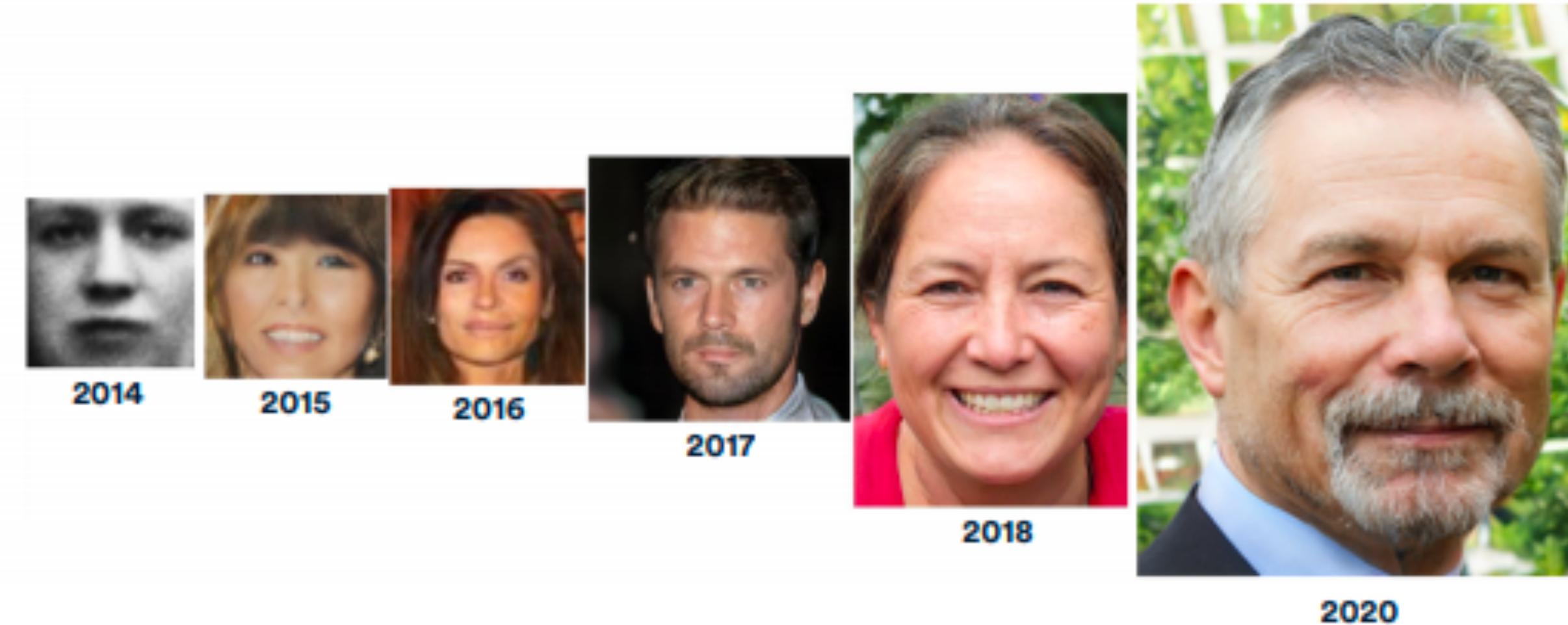
1 Introduction

Machine learning has been applied to a wide range of applications such as face recognition [30, 39, 21], autonomous driving [26], and medical diagnoses [8, 20]. However, most learning methods rely on the availability of large-scale training datasets containing sensitive information such as personal photos or medical records. Therefore, such sensitive datasets are often hard to share due to privacy concerns [40]. To handle this challenge, data providers sometimes release synthetic datasets produced by generative models learned on the original data. Though recent studies show that generative models such as generative adversarial networks (GAN) [14] can generate synthetic records that are indistinguishable from the original data distribution, there is no theoretical guarantee on the privacy protection. While privacy definitions such as differential privacy [9] and Rényi differential privacy [27] provide rigorous privacy guarantee, applying them to synthetic data generation is nontrivial.

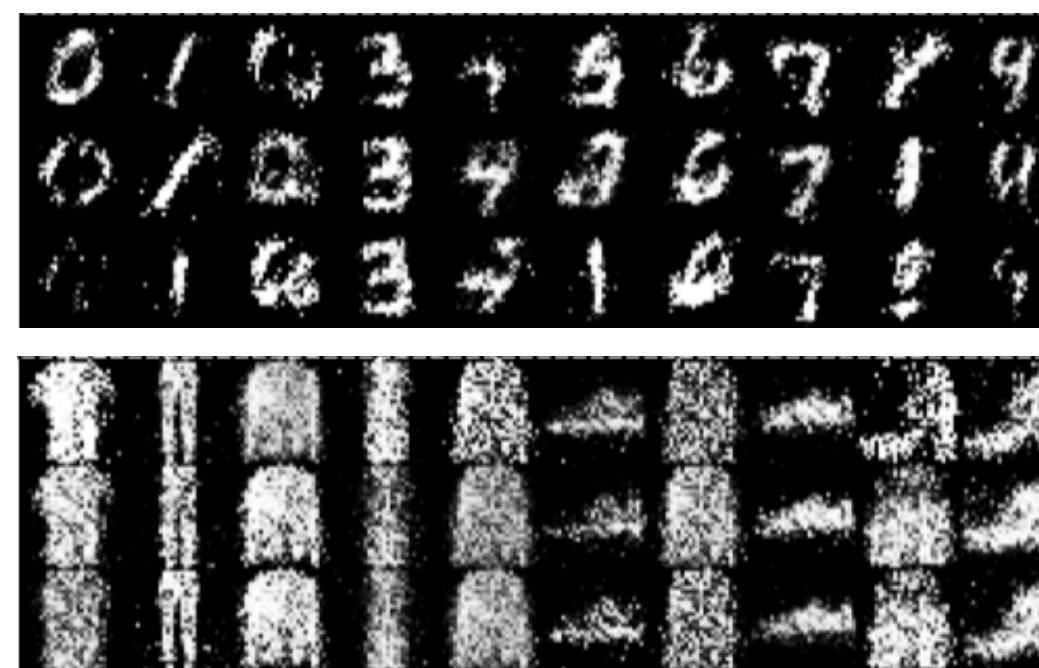
Recently, two approaches have been proposed to combine differential privacy with synthetic data generation: DP-GAN [15] and PATE-GAN [37]. DP-GAN modifies GAN by training the discriminator using differentially private stochastic gradient descent. Though it achieves privacy guarantee due to

*Equal contribution.

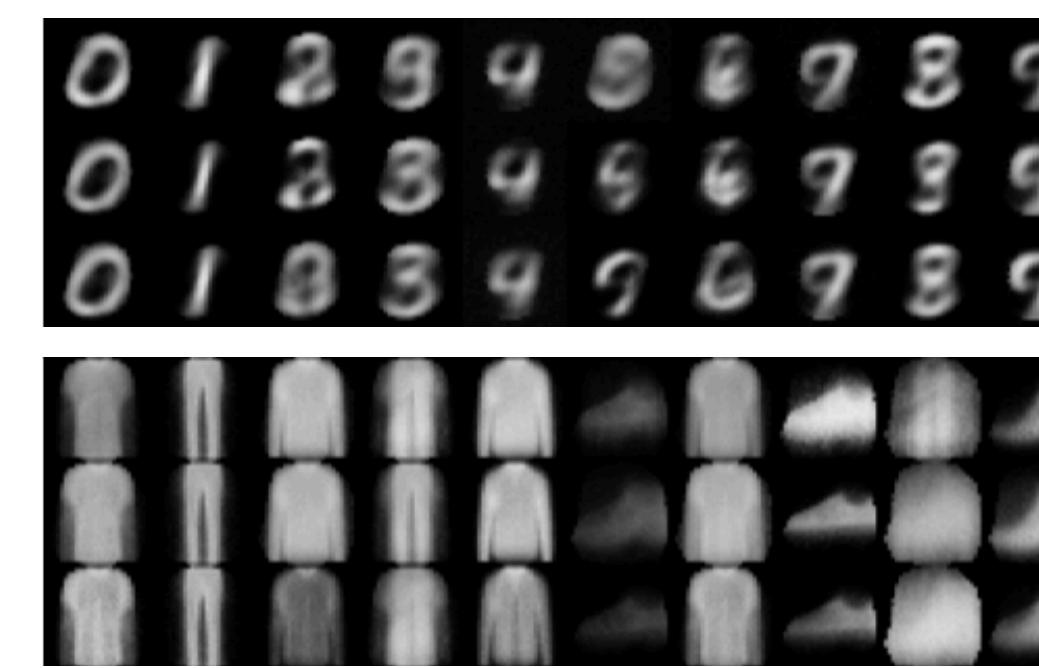
Challenges



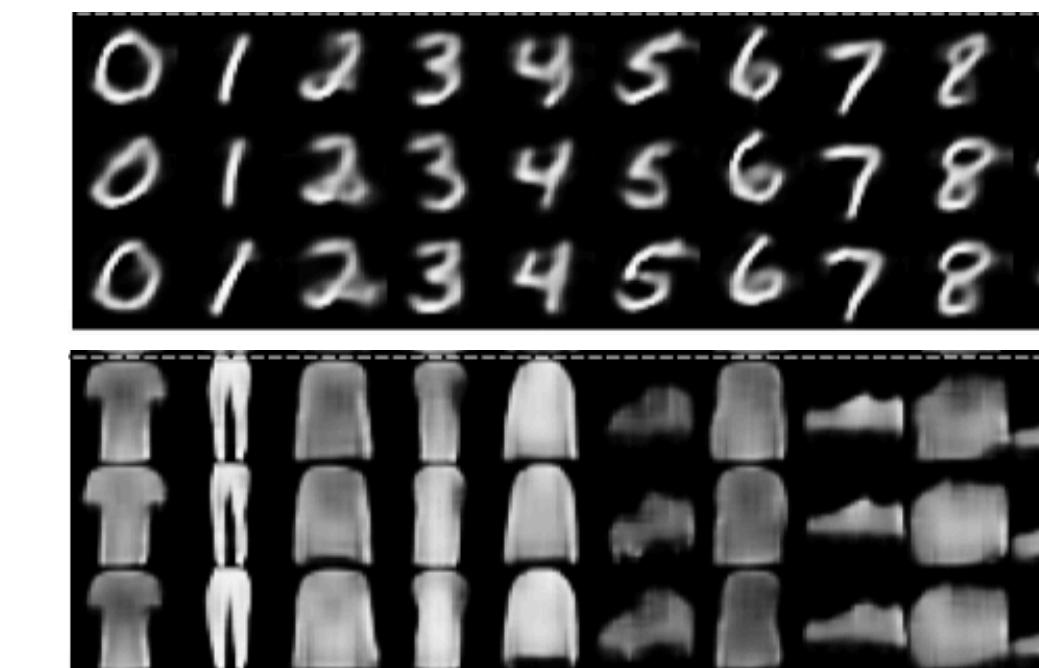
Progress of **non-private** generation



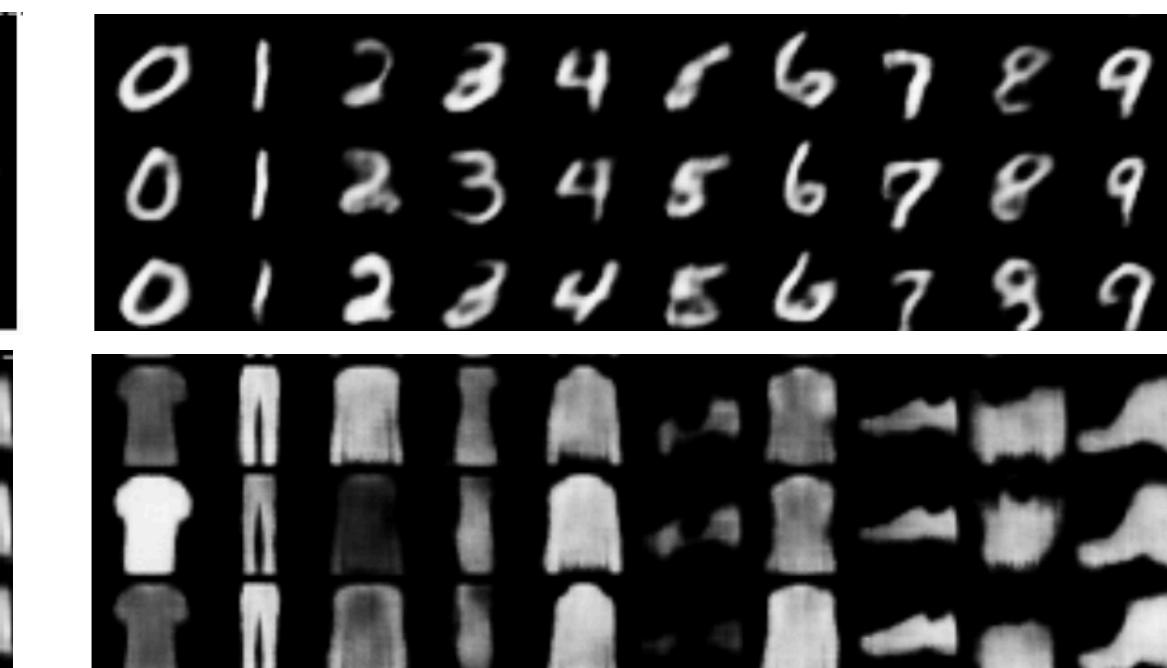
2018



2019



2020



2021

Progress of **private** generation $(\varepsilon, \delta) = (10, 10^{-5})$

Saturated? Problem too hard?

Challenges

- Fitting the complete high-dimensional data distribution is complicated
 - Deep generative models are **data demanding**
 - Privacy constraints
- No enough data to solve such a difficult problem 

Private Set Generation with Discriminative Information

(NeurIPS 2022)

- **Existing approaches:**

- Aim at fitting the complete data distribution
- Optimize deep generative models
- Suboptimal utility: <85% for MNIST with $(\varepsilon, \delta) = (10, 10^{-5})$

- **Our approach:**

- Target at common downstream tasks (e.g., classification)
- Directly optimize a set of representative samples
- ~10% downstream test accuracy improvement over SOTA

Generally easier

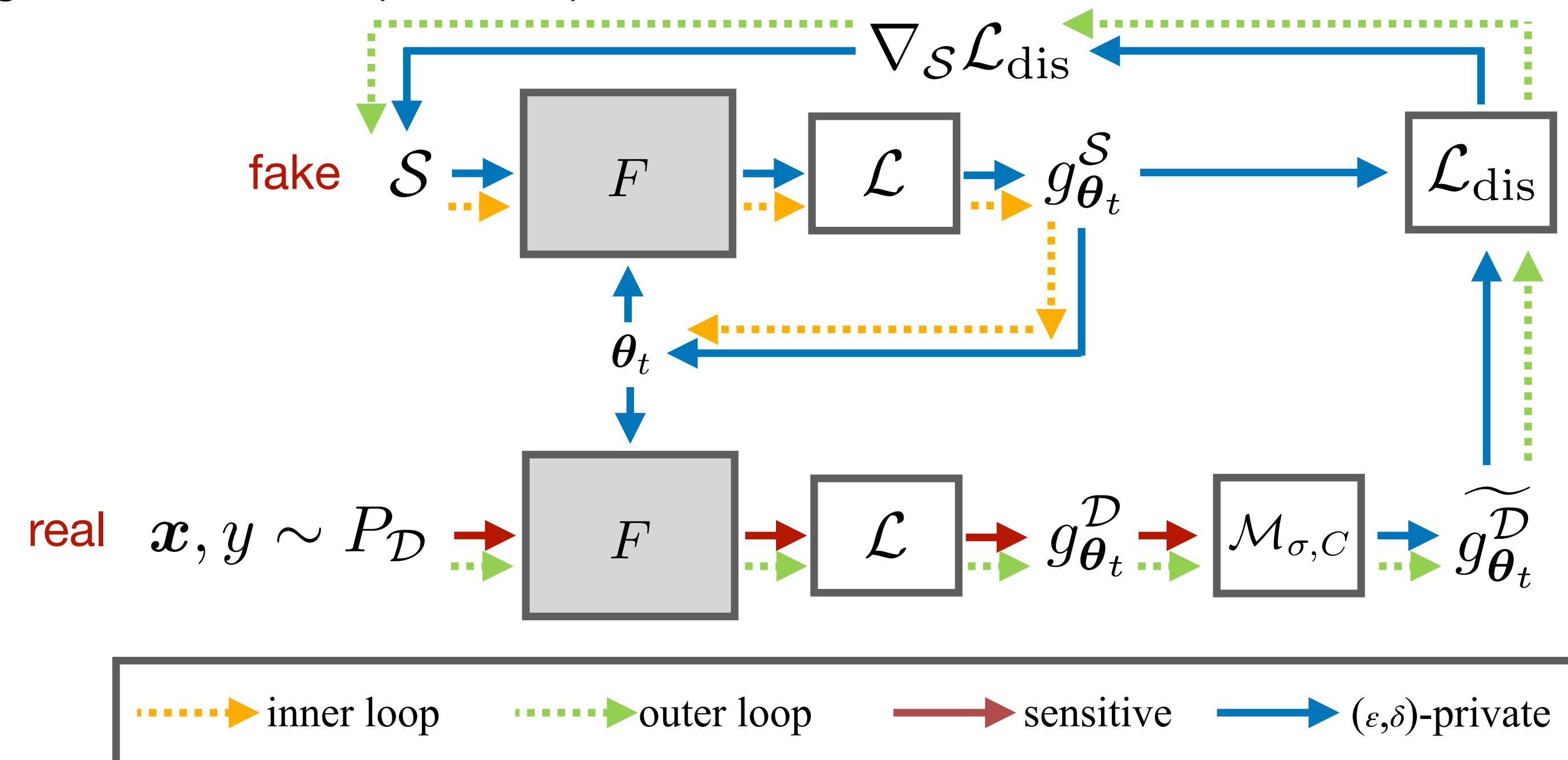
Better convergence

Useful samples

Private Set Generation with Discriminative Information

(NeurIPS 2022)

- **Target:**
 - Optimize for training downstream Neural Network classifier
- **Basic idea:**
 - Gradient-based **coreset generation**^{1,2}
 - DP stochastic gradient descent (DP-SGD)



¹ Zhao, Bo, et al., “Dataset condensation with gradient matching.”, *ICLR*, 2021.

² Zhao, Bo, et al., “Dataset condensation with differentiable siamese augmentation.”, *ICML*, 2021

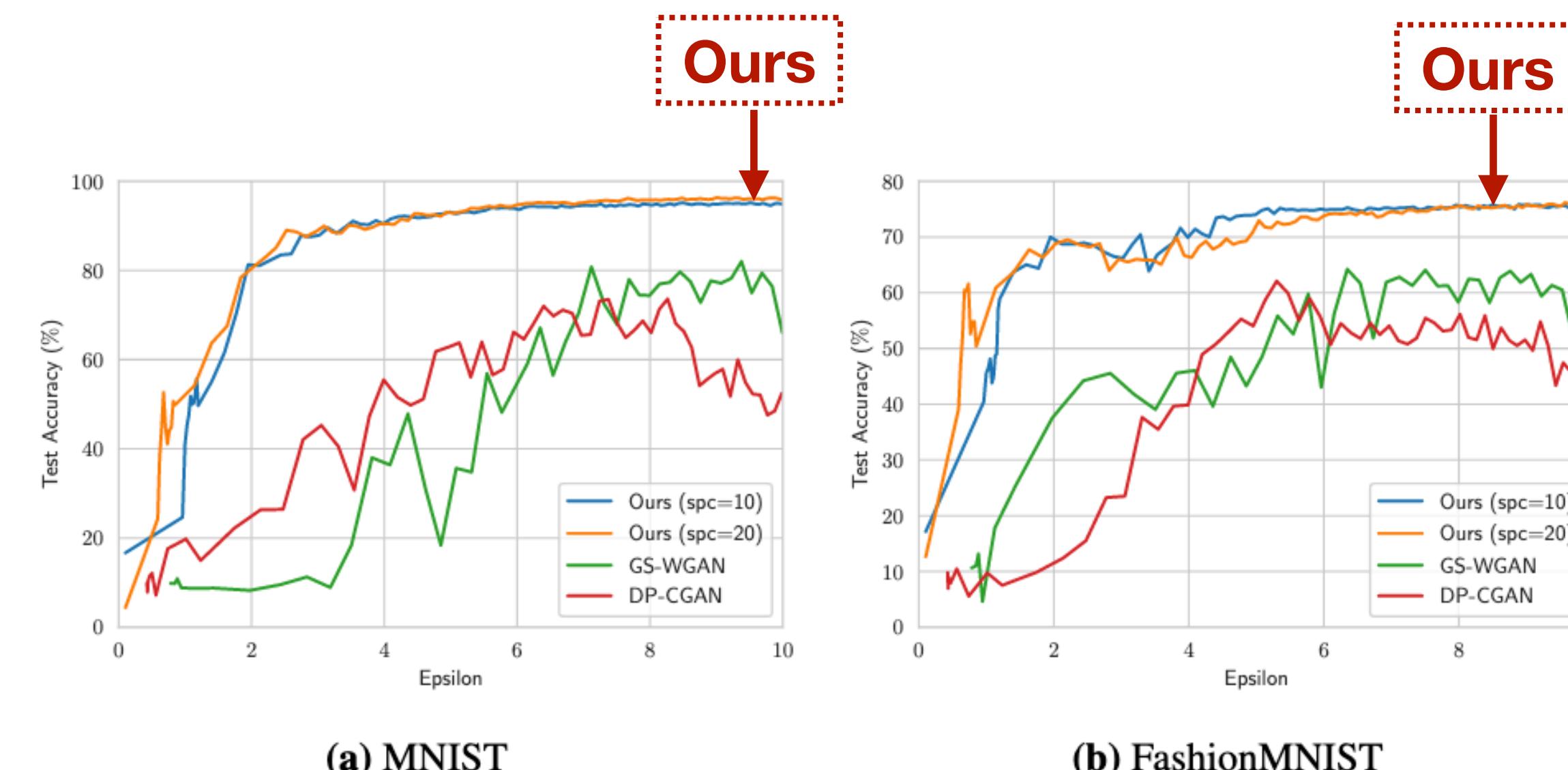
Private Set Generation with Discriminative Information

(NeurIPS 2022)

- Comparison to SOTA:

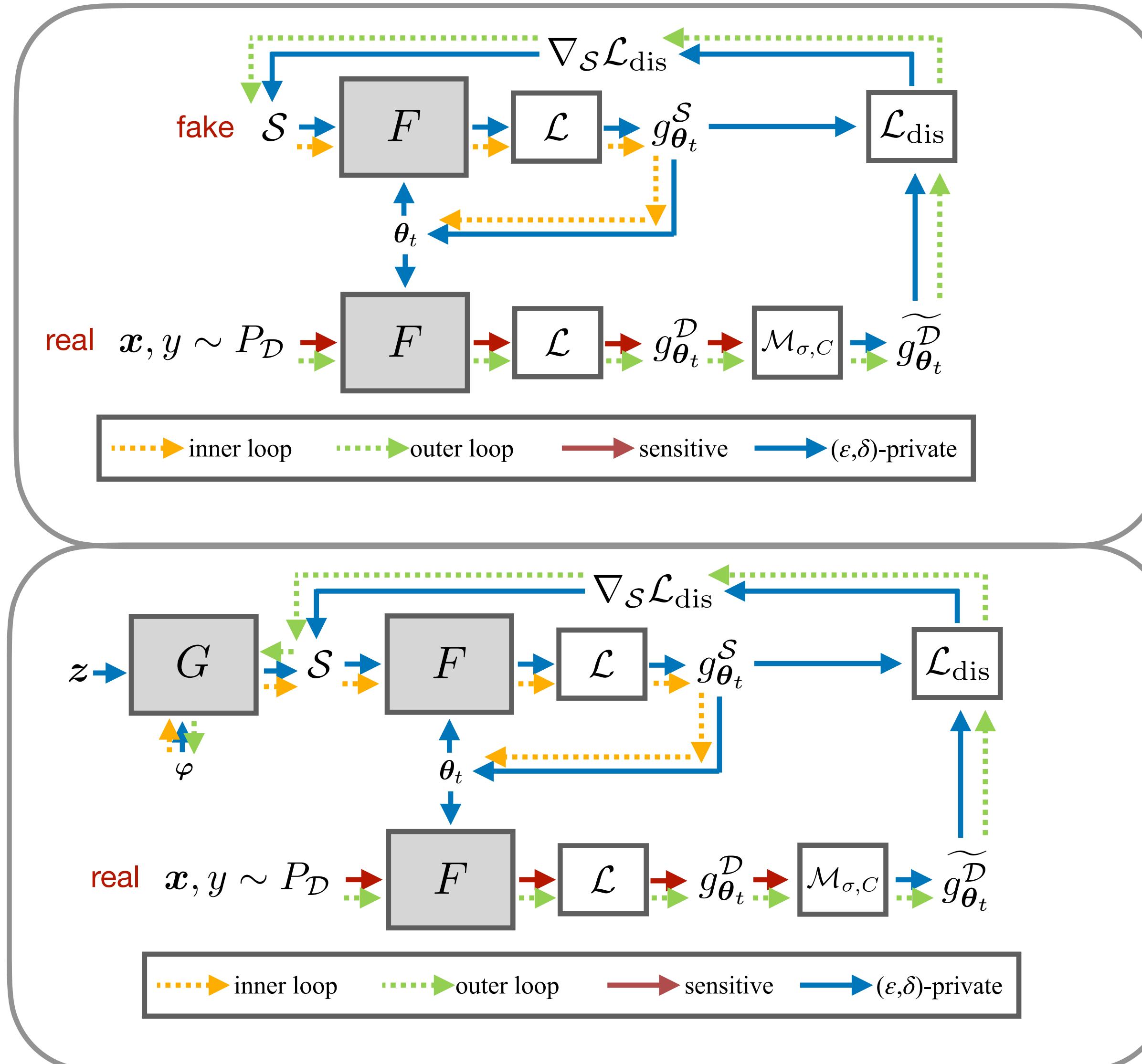
- Utility for downstream classification task (train on synthetic; test on real)
- Convergence rate

	MNIST						FashionMNIST					
	ConvNet	LeNet	AlexNet	VGG11	ResNet18	MLP	ConvNet	LeNet	AlexNet	VGG11	ResNet18	MLP
Real	99.6	99.2	99.5	99.6	99.7	98.3	93.5	88.9	91.5	93.8	94.5	86.9
DP-CGAN	50.2	52.6	52.1	54.7	51.8	54.3	50.2	52.6	52.1	54.7	51.8	54.3
GS-WGAN	84.9	83.2	80.5	87.9	89.3	74.7	54.7	62.7	55.1	57.3	58.9	65.4
DP-Merf	85.7	87.2	84.4	81.7	81.3	85.0	72.4	67.9	64.9	70.1	66.7	73.1
Ours (spc=10)	94.9	91.3	90.3	93.6	94.3	86.1	75.6	68.0	66.2	74.7	72.1	62.8
Ours (spc=20)	95.6	93.0	92.3	94.5	94.1	87.1	77.7	68.0	59.1	76.8	70.8	62.2

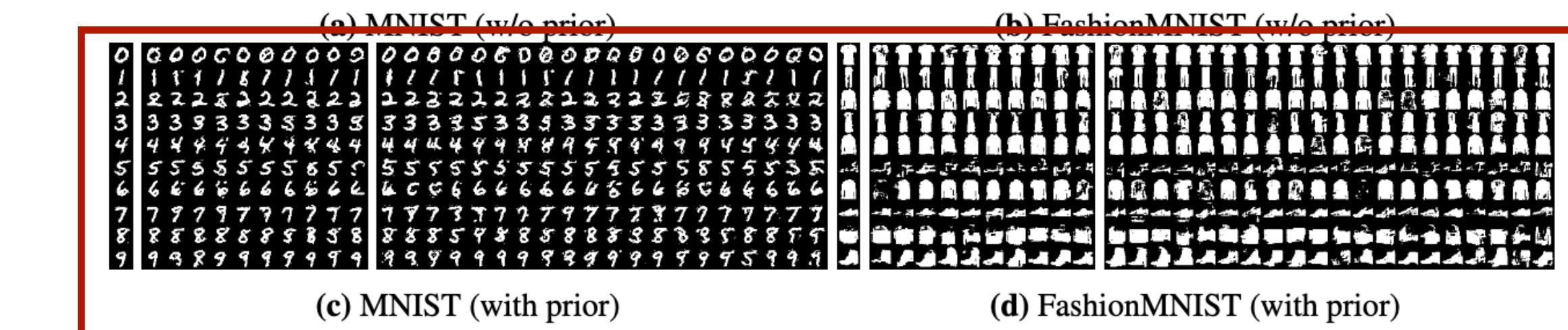


Private Set Generation with Discriminative Information

(NeurIPS 2022)



- Deep generator structure result in:
 - Better visual quality
 - Slow convergence
 - Sub-optimal downstream utility

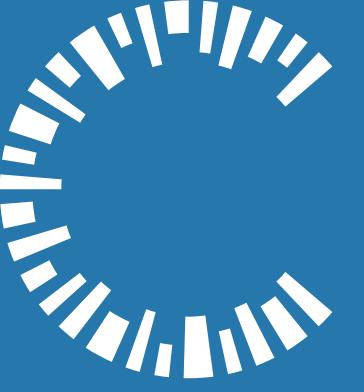


with generative model

	MNIST			FashionMNIST		
	1	10	20	1	10	20
w/o prior	81.4	94.9	95.6	66.7	75.6	77.7
with prior	88.2	92.2	90.6	63.0	70.2	70.7

In summary:

- **Privacy-preserving Generation is important**
 - Flexibility & Transparency: downstream analysis, reproducible research
 - Applications: federated learning
- **Privacy-preserving Generation is non-trivial:**
 - Exploit the progress in general generative modeling
 - Co-design of private- and non-private models
 - Make better usage of “prior knowledge”
 - Task (downstream model)
 - Data distribution



Thanks for your attention!

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