

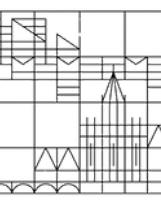


11 | Reinforcement Learning

Giordano De Marzo

<https://giordano-demarzo.github.io/>

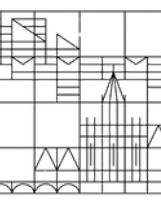
Deep Learning for the Social Sciences



Course Evaluation

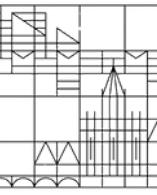
Please scan the QR code and fill the form! We have two forms,
one for me and one for Max (this is mine)





Recap

- Generative Deep Learning
- Variational Autoencoders
- Generative Adversarial Networks
- Applications



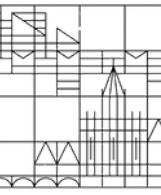
Outline

1. A New Learning Paradigm

2. Reinforcement Learning

3. Q-Learning and Policy Gradient

4. Applications



A New Learning Paradigm



Supervised vs Unsupervised Learning

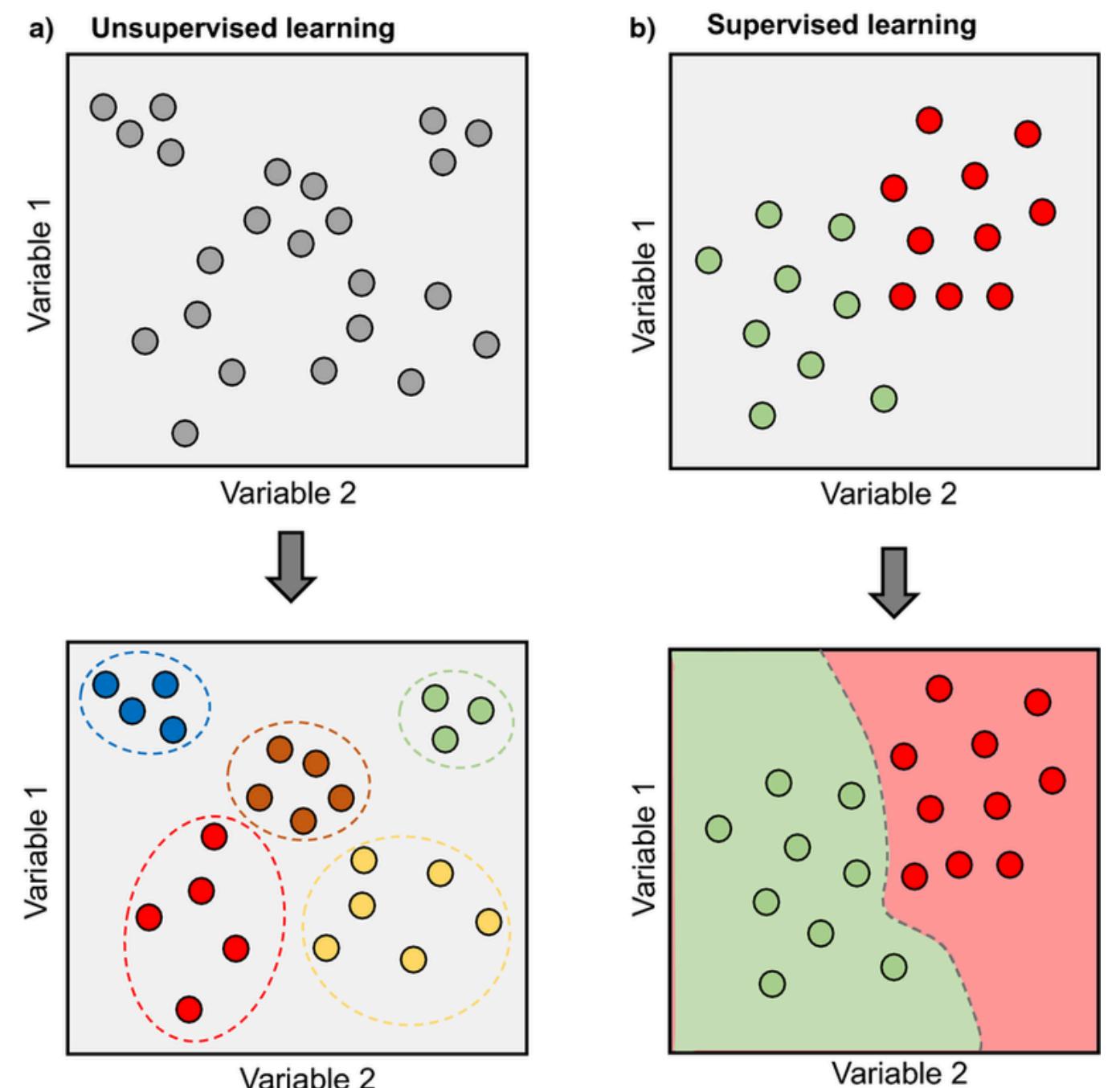
Up to now we mostly consider supervised deep learning models:

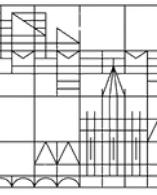
- MLP for classification and regression
- CNN for classification
- GNN for classification

We only considered one architecture that performs unsupervised learning, the Autoencoder.

Unsupervised learning tasks include

- clustering
- dimensionality reduction
- data generation



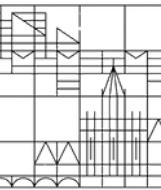


Limits of (Un)Supervised Learning

When we introduced Generative Deep Learning we discussed some of the limits of traditional learning paradigms

- supervised learning need a lot of labelled data
- with unsupervised learning we can't train the model to perform a specific task
- both frameworks are based on offline training, they struggle with new data or scenarios
- supervised learning rely on humans, how can we train a model better than humans?

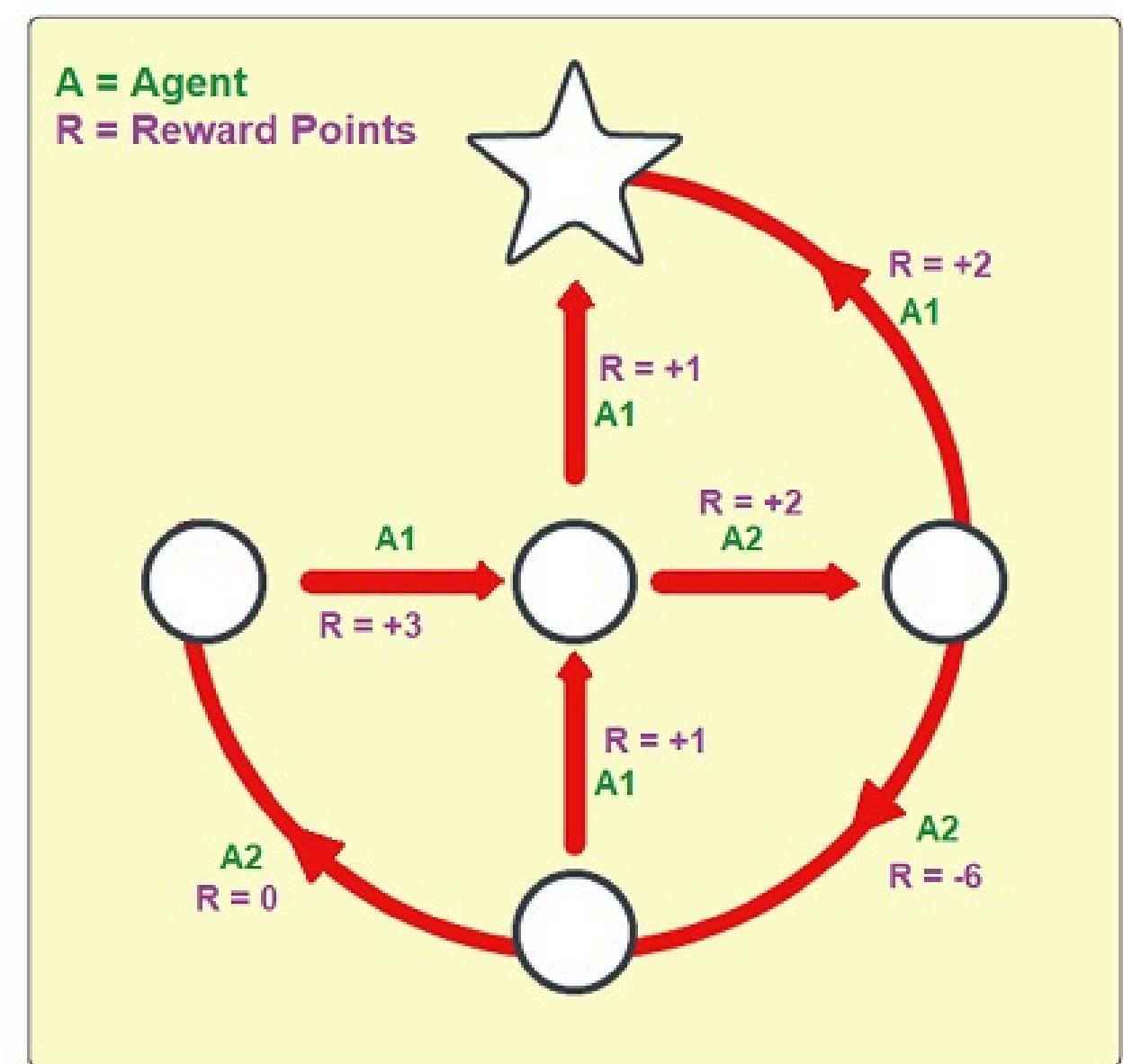
All these problems are solved by Reinforcement Learning (RL). It combines the benefits of the two approaches.

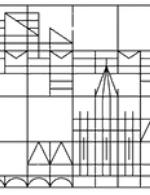


Reinforcement Learning

Reinforcement Learning (RL) is in-between supervised and unsupervised learning:

- The agent begins with little to no knowledge of the environment
- Agents learn to make decisions by interacting with a dynamic environment
- The goal is learning a strategy to perform actions that result in the highest long-term rewards
- Humans only need to set the environment and the rewards, then the agent learns autonomously





Strengths of Reinforcement Learning

Beyond Supervision

RL learns optimal behaviors through trial and error directly from raw experience without needing pre-labeled data. This capability is critical in environments where prior knowledge is limited or the solution space is complex.

Decision Making

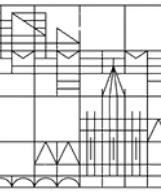
RL excels in scenarios requiring a series of decisions, where each choice impacts future outcomes, making it ideal for strategic planning and operations management.

Adaptability

An RL agent can adapt to changes in an unpredictable environment in real-time, continually updating its strategy based on new experiences. This adaptability is essential for applications such as dynamic pricing or autonomous driving.



Reinforcement Learning

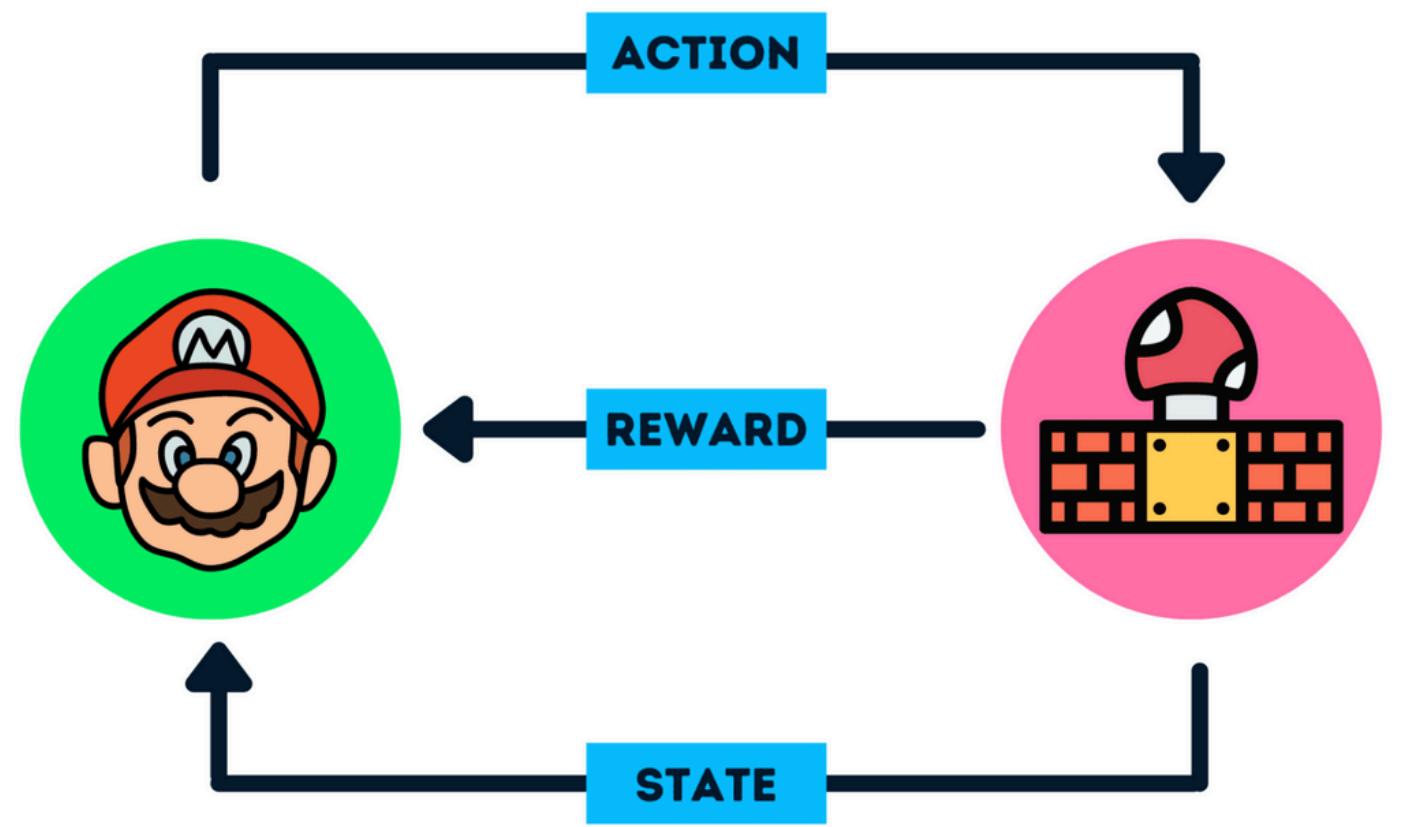


Reinforcement Learning Framework

The RL framework is structured around a set of key elements:

- **State:** The representation of the environment at any given time.
- **Action:** A set of possible moves the agent can make.
- **Reward:** Immediate feedback given to the agent to evaluate its last action.
- **Policy:** A strategy that the agent follows to determine its action at each state.

The goal of RL is to follow a policy or strategy that maximizes the reward

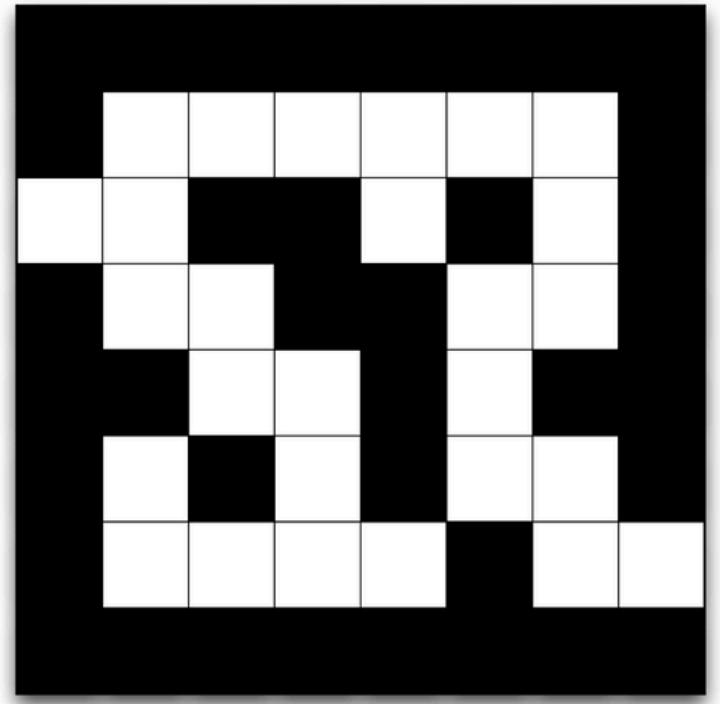




Environment and Actions

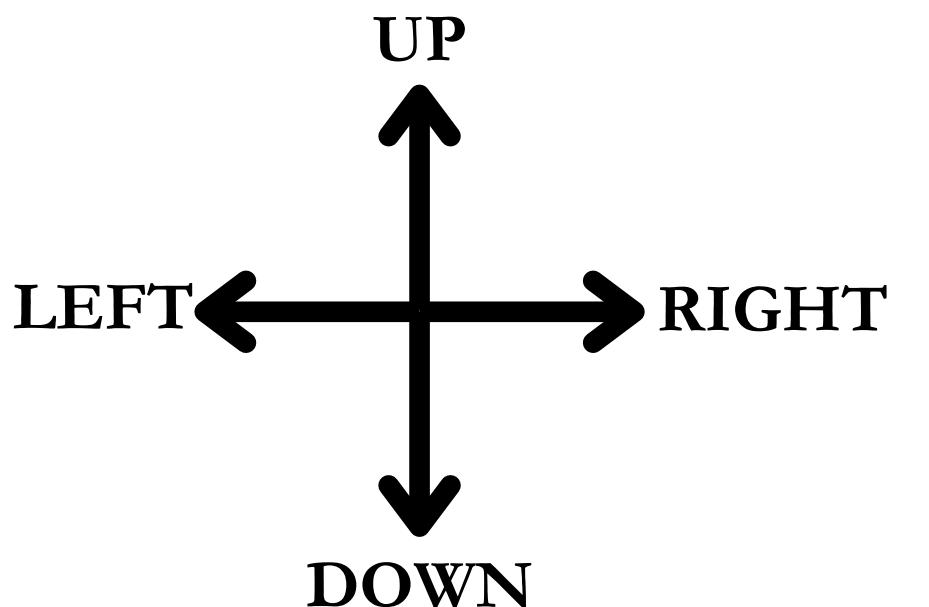
Environment:

- The setting or context within which the agent operates.
- It can be physical (like a robot navigating a room) or virtual (like a video game or simulation).
- Characteristically dynamic, potentially complex, and initially unknown to the agent.



Actions:

- Actions represent the choices available to the agent at each state.
- The set of all possible actions available in a given environment constitutes the action space, which can be discrete or continuous





Reward and Discounted Reward

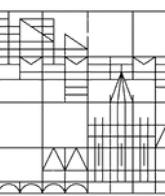
Whenever the agent performs something good, we should give it a reward r_t

- Rewards are signals sent from the environment to the agent
- They indicate the effectiveness of the action relative to achieving the goal.

To prioritize immediate rewards over distant ones and to handle the uncertainty of future rewards, RL uses a concept known as discounting.

- The value of future rewards is multiplied by a discount factor γ . This teaches the agent to prefer receiving rewards sooner rather than later, which is crucial in environments with changing conditions
- The total discounted reward starting from time t is then defined as

$$R_t = r_t + \gamma r_{t+1} + \gamma^2 r_{t+2} + \gamma^3 r_{t+3} + \dots = \sum_{k=0}^{\infty} \gamma^k r_{t+k}$$



Types of Reinforcement Learning



Policy Based Methods:

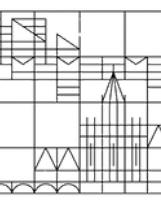
- They find the optimal policy, which defines the agent's way of behaving at a given time. A policy maps states to actions the agent should take, either deterministically or stochastically.

Value Function Methods:

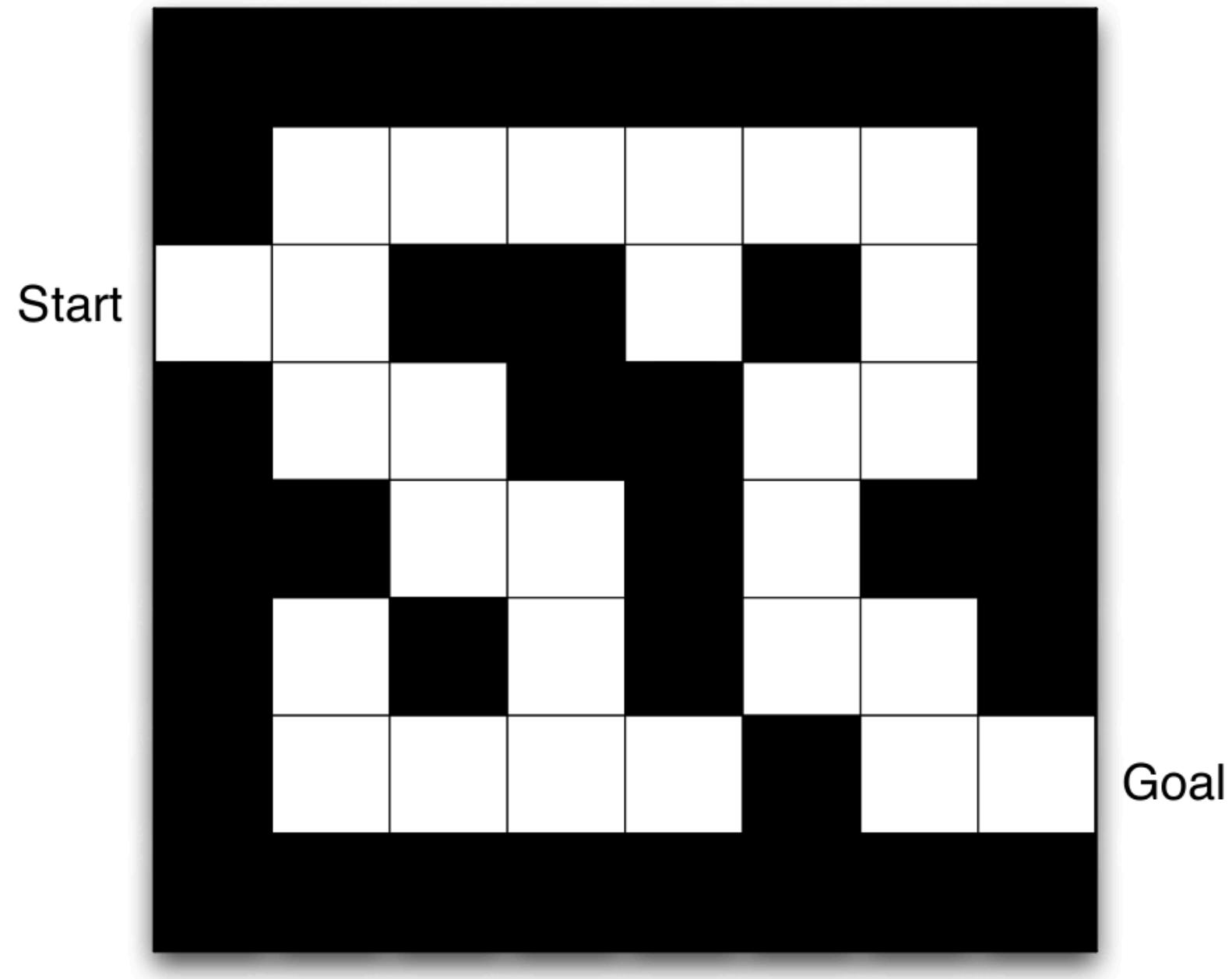
- They derive a function that gives the expected future rewards from each state. It is used to guide policy decisions and helps assess the potential of different states under a particular policy.

Model Based Methods:

- They allow the agent to get an understanding of the environment. In model-based RL, the agent uses the model to predict how the environment will respond to its actions.



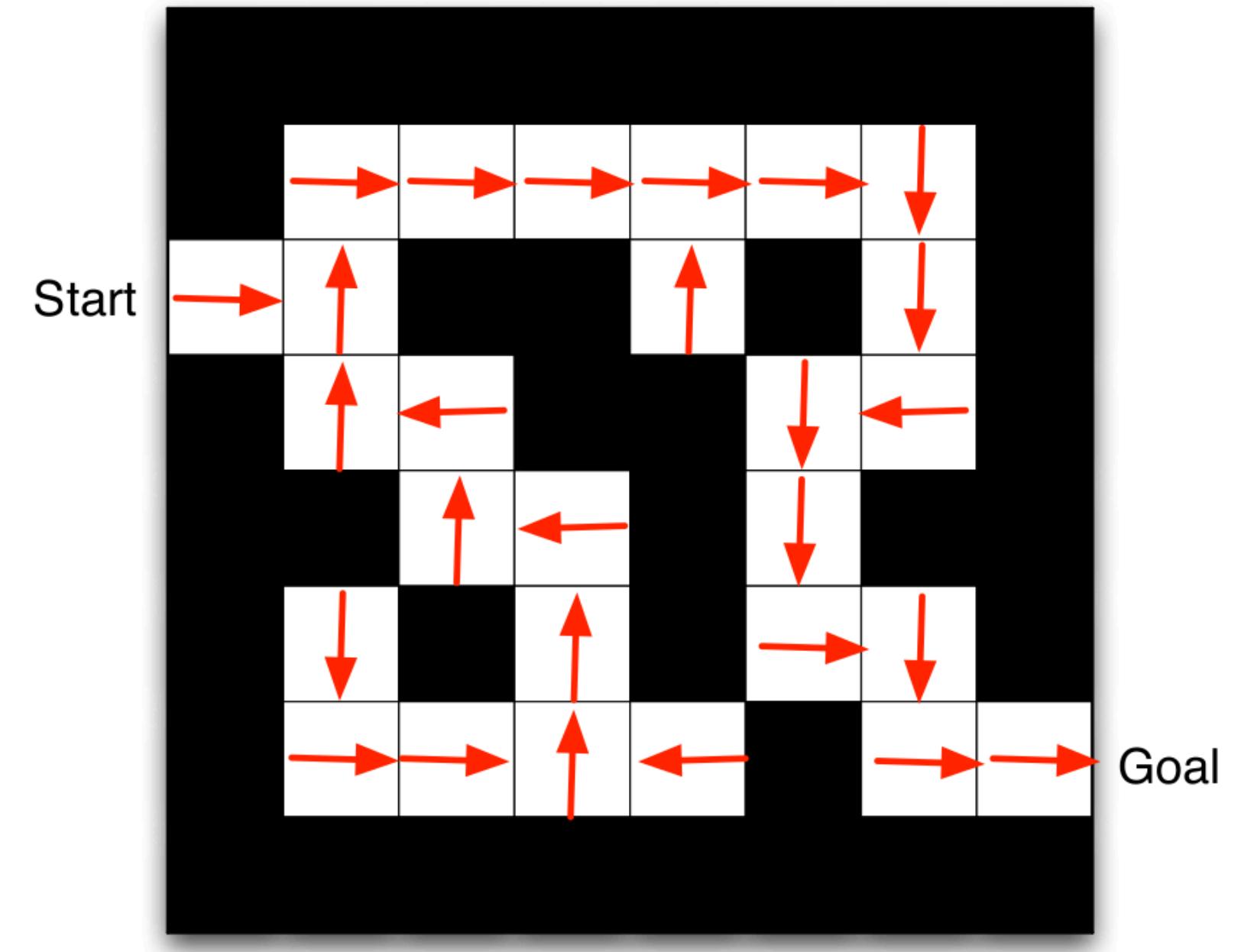
Example: Maze

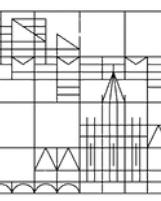


- **Rewards:** -1 per time-step
- **Actions:** up, down, left, right
- **States:** Agent's location in the maze

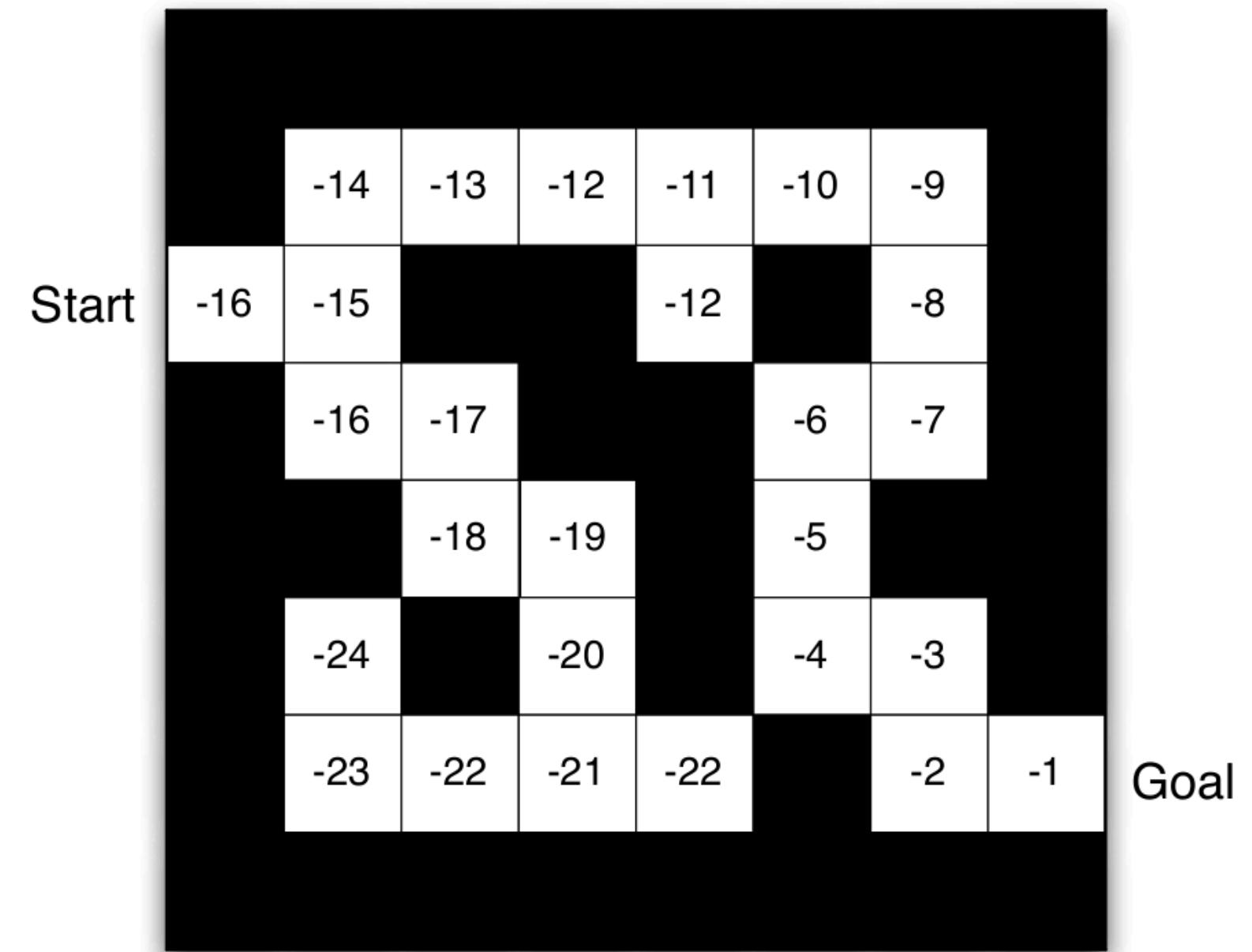


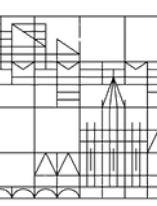
Example: Policy



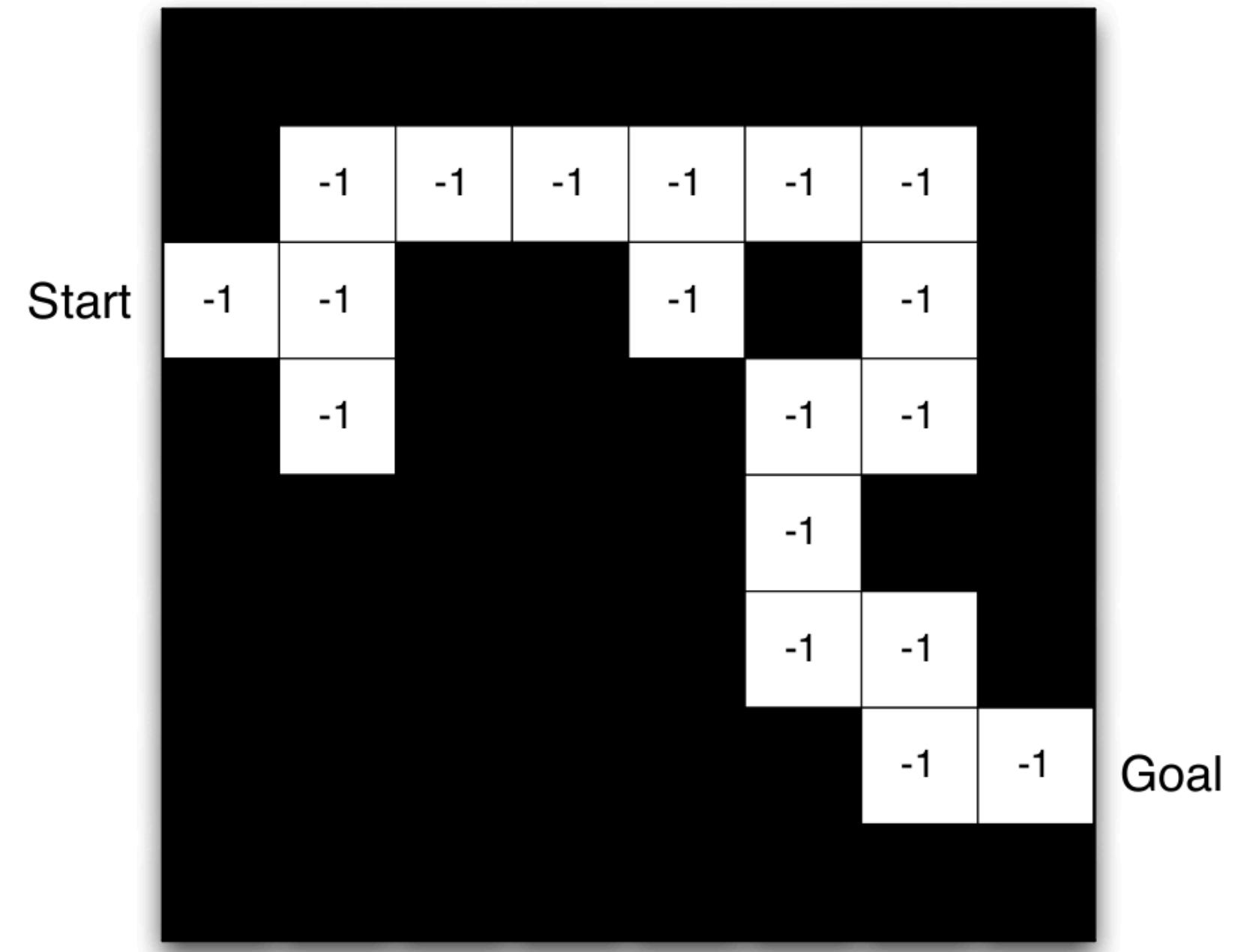


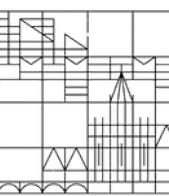
Example: Value Function





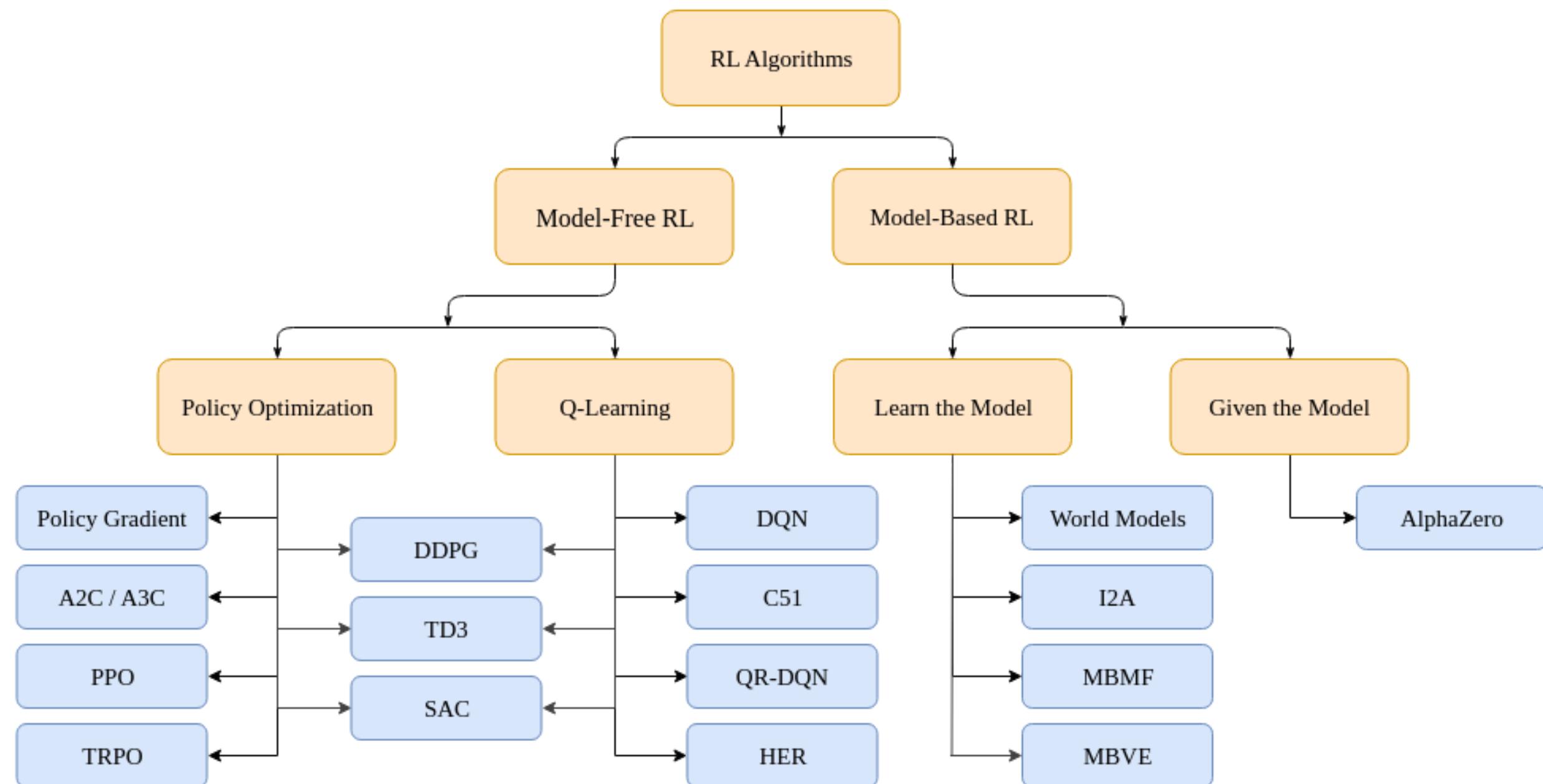
Example: Model

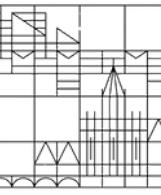




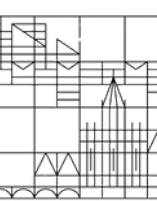
Taxonomy of Reinforcement Learning

We will focus on Deep Q-Learning Networks (DQNs) and on Policy Gradient.





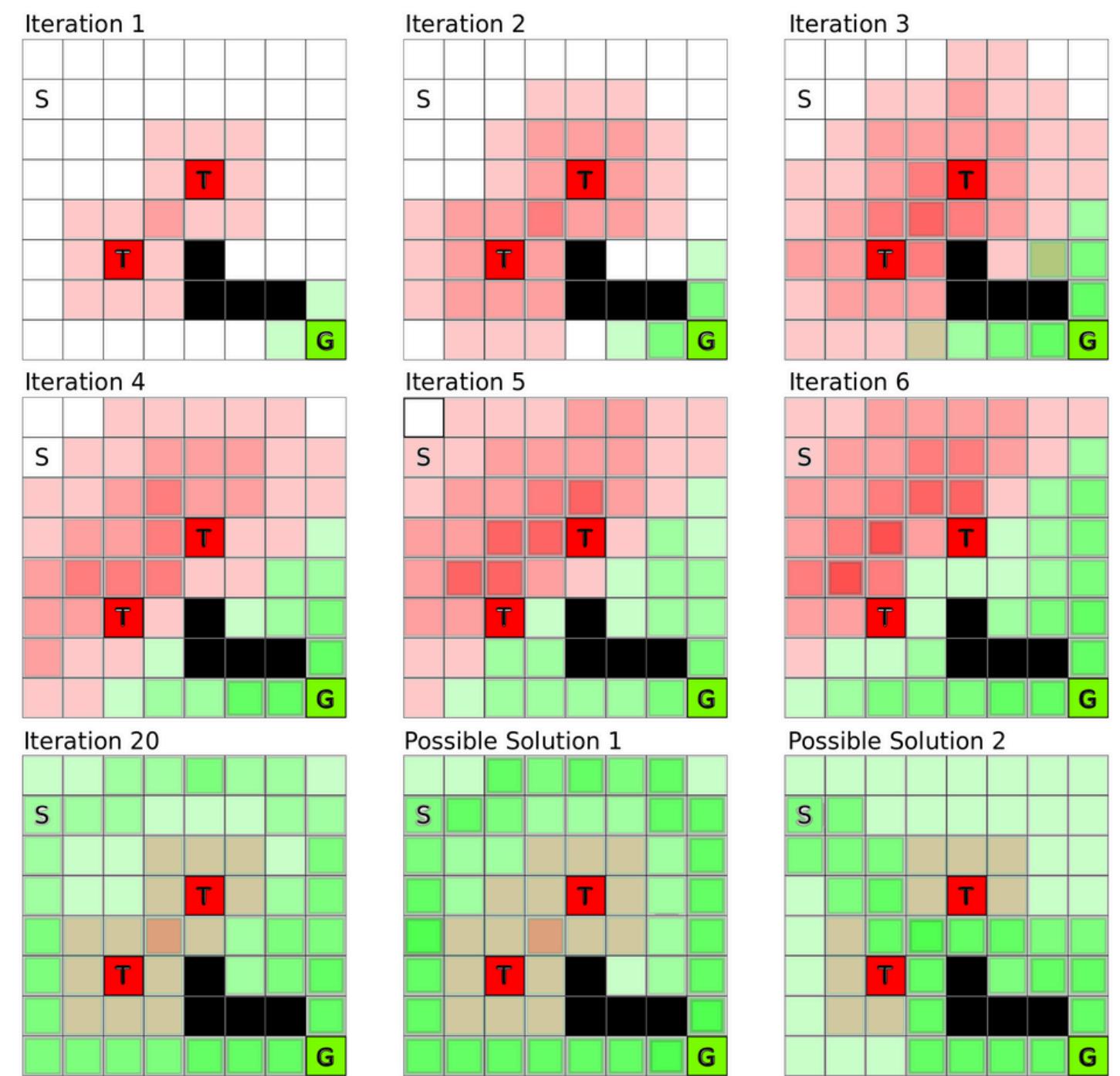
Deep Q-Learning and Policy Gradient

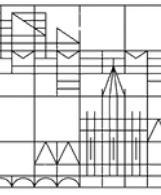


Q-Learning

Q-Learning is an off-policy reinforcement learning algorithm that seeks to find the best action to take given the current state.

- The algorithm uses a Q-function to evaluate the quality of a particular action taken from a particular state.
- The goal is to learn the Q-function and then to use it to get the maximal possible discounted reward.
- The agent observes the outcomes of actions taken, and iteratively updates the Q-values based on the rewards





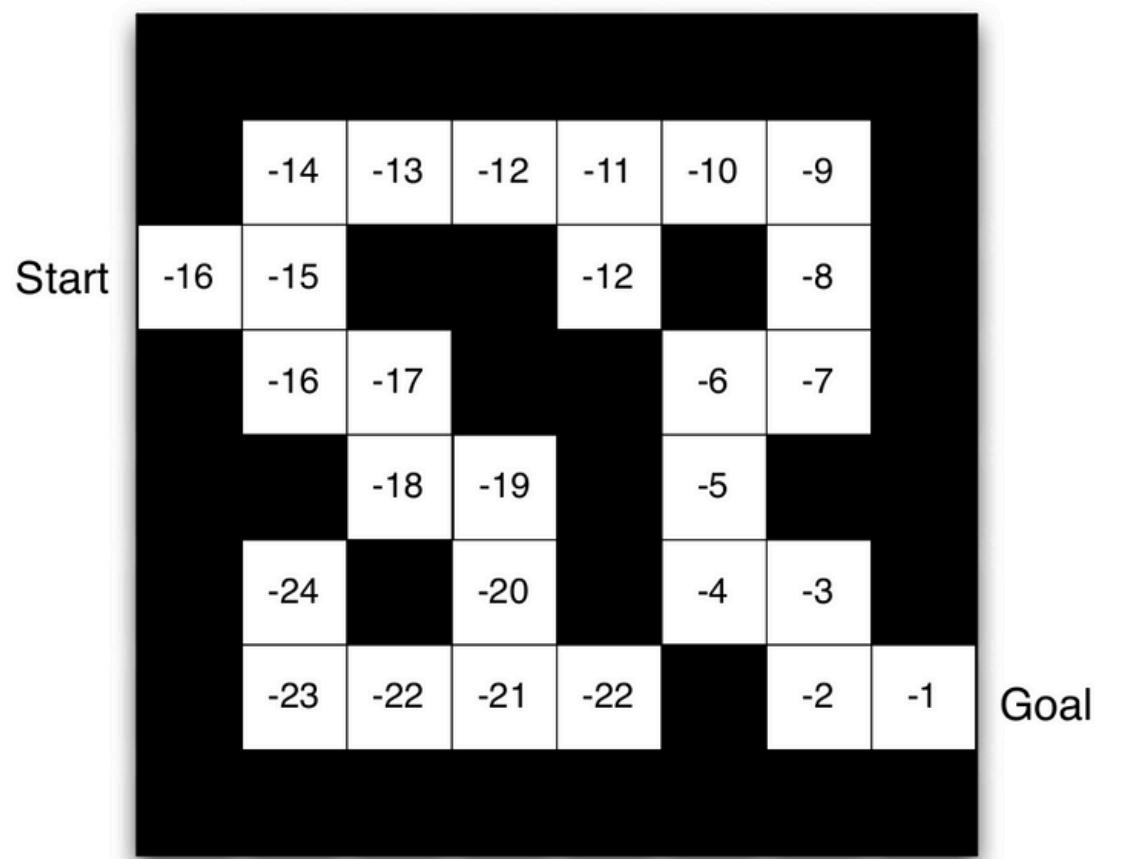
Q-Value Function

The Q-value function $Q(s,a)$ quantifies the expected total payoff starting from state s , taking an action a , and thereafter following an optimal policy, as given by the Q-value function itself.

- The Q-value function is defined as:

$$Q(s, a) = \mathbb{E} \left[\sum_{k=0}^{\infty} \gamma^k r_{t+k+1} \mid S_t = s, A_t = a \right]$$

- It allows the agent to evaluate the expected utility of its actions at each state without knowing the full dynamics of the environment.
- As the agent explores its environment, the Q-value function is continually updated to better approximate the true expected returns.





Bellman's Formula

The Bellman equation allows to define the optimal Q-value function $Q^*(s, a)$ as:

$$Q^*(s, a) = r + \gamma \max_{a'} Q^*(s', a')$$

In practice $Q^*(s, a)$ is approximated using the Q-learning algorithm, which iteratively updates the Q-values based on experience:

$$Q(s, a) \leftarrow Q(s, a) + \alpha \left[r + \gamma \max_{a'} Q(s', a') - Q(s, a) \right]$$

Here's how it works:

1. **Initialization:** Q-values are typically set to zero for all state-action pairs.
2. **Experience:** For each action taken, observe the immediate reward r and the next state s' .
3. **Update:** Adjust the Q-value of the state-action pair based on Bellman equation
4. **Repeat:** Iterate until the Q-values converge.



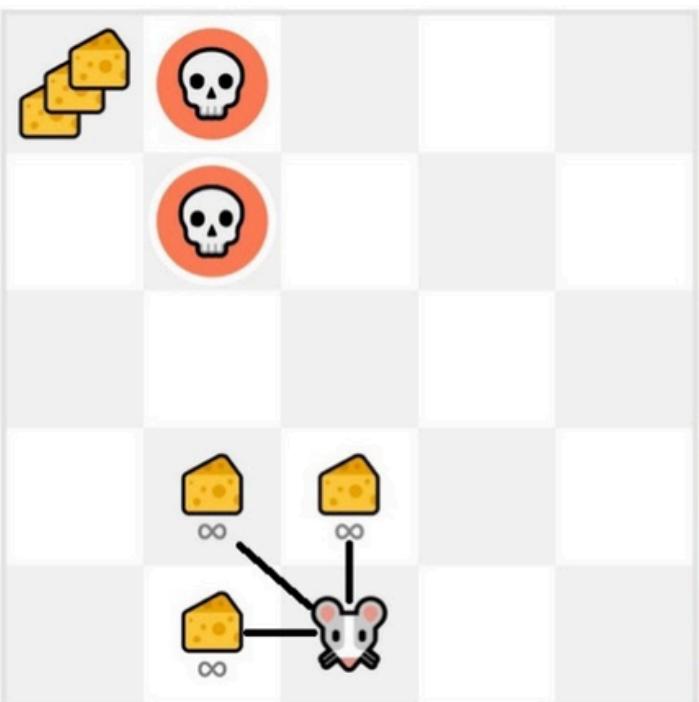
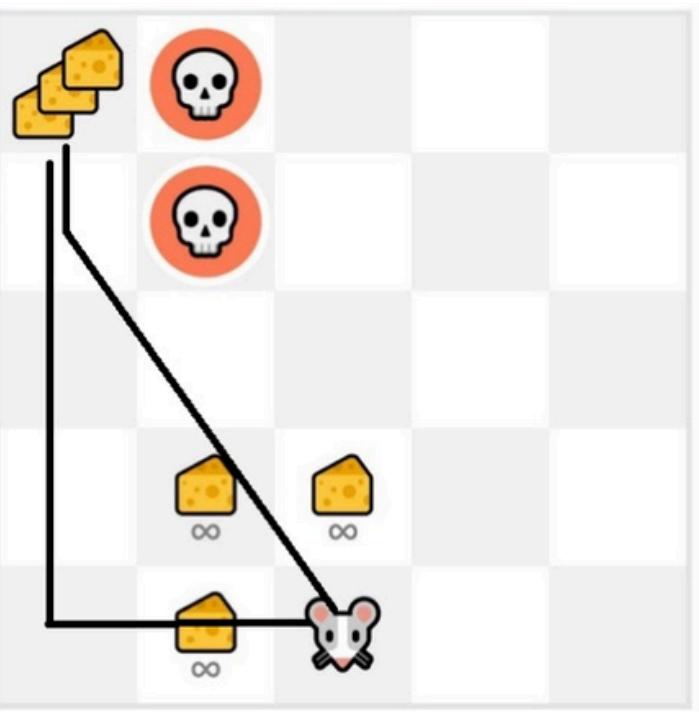
Exploration vs Exploitation

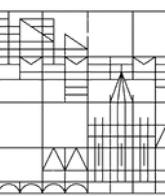
Balancing exploration and exploitation is a central point in RL

- Exploration is crucial in early learning stages or if conditions change over time. It prevents the algorithm from getting stuck in local optima.
- Exploitation is important for utilizing the learned behaviors to achieve the best results.

A common approach to this problem is the ϵ -greedy algorithm

- ϵ set the likelihood of taking a random action (exploration) versus the best-known action (exploitation).
- ϵ decreases gradually as learning progresses, allowing more exploration initially and more exploitation later.





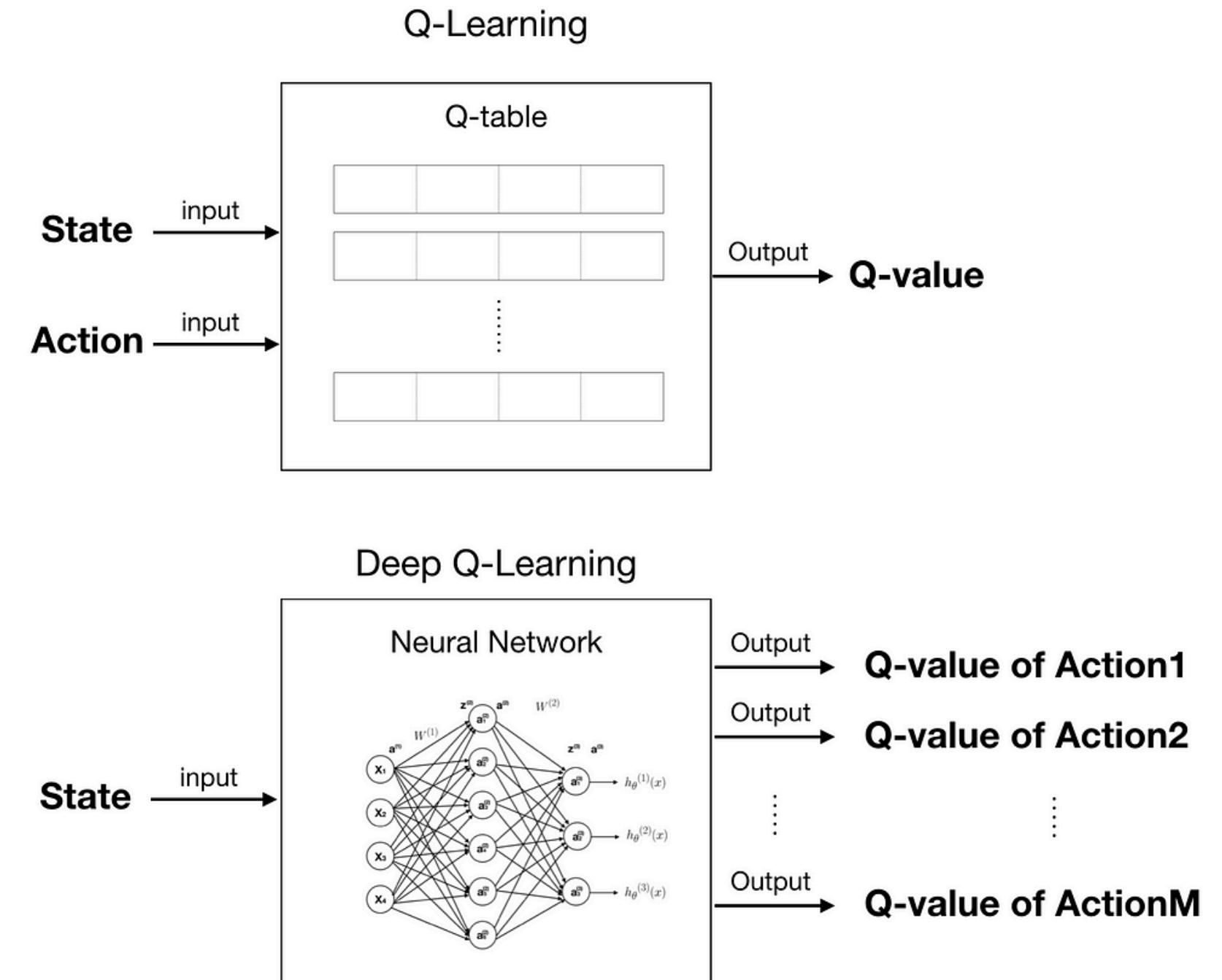
Deep Q-Learning Networks

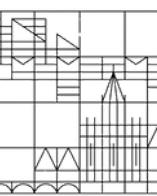
Traditional Q-Learning has many limitations

- It relies on a Q-table, which becomes impractical in environments with vast numbers of state-action pairs.
- In high-dimensional state spaces it requires exponential data to adequately cover the state-action space.

Deep Q-Networks (DQN) utilize a neural network to approximate the Q-value function

$$Q(s, a; \theta) \approx r + \gamma \max_{a'} Q(s', a'; \theta)$$





DQN Loss Function and Training

The loss function for DQN is typically framed as the Mean Squared Error (MSE) between the predicted Q-values and the target Q-values computed using the Bellman equation:

$$L(\theta) = \mathbb{E} \left[\left(r + \gamma \max_{a'} Q(s', a'; \theta') - Q(s, a; \theta) \right)^2 \right]$$

Training data in DQN is generated through the agent's interactions with the environment

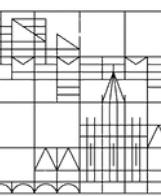
- At each timestep, the agent observes the current state s , selects and executes an action a , and observes the outcome, which includes the next state s' and reward r .
- All this information is stored in memory and they are later used to update the weights of the neural network with the standard optimization procedure.
- The updated neural network is used to gather new data and the process is iterated.



DQNs Training Tricks

Training DQNs is not trivial and several tricks have been devised to make the process more stable

- **Experience Replay:**
 - instead of learning directly from consecutive experiences, the algorithm randomly samples a small batch of experiences from the buffer.
 - this random sampling helps to break the correlation and allows the network to learn from a more diverse set of experiences, thus stabilizing the update steps.
- **Target Network:**
 - the Target Network is a less frequently updated neural network that is added to the algorithm
 - the Target Network is used to estimate the target Q-values
 - this addresses the "moving target" problem, where continuous updates can make the training process unstable and inefficient.



Policy Gradient

Policy Gradient methods directly optimize the policy function π . They work by adjusting the policy parameters θ directly in response to an estimator of the long-term reward.

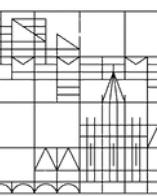
- It is effective in high-dimensional or continuous action spaces.
- It can learn stochastic policies, allowing for more exploration.

The policy function is approximated by a neural network and the objective is to maximize the expected reward $J(\theta)$

$$J(\theta) = \mathbb{E}_{\pi_\theta}[R_t]$$

Policy gradient updates parameters via a standard gradient ascent:

$$\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$$



REINFORCE Algorithm

REINFORCE, is a simple policy gradient method. Policy parameters are updated as

$$\theta \leftarrow \theta + \alpha \sum_{t=0}^T R_t \nabla_\theta \log \pi_\theta(a_t | s_t)$$

Training is done as detailed below

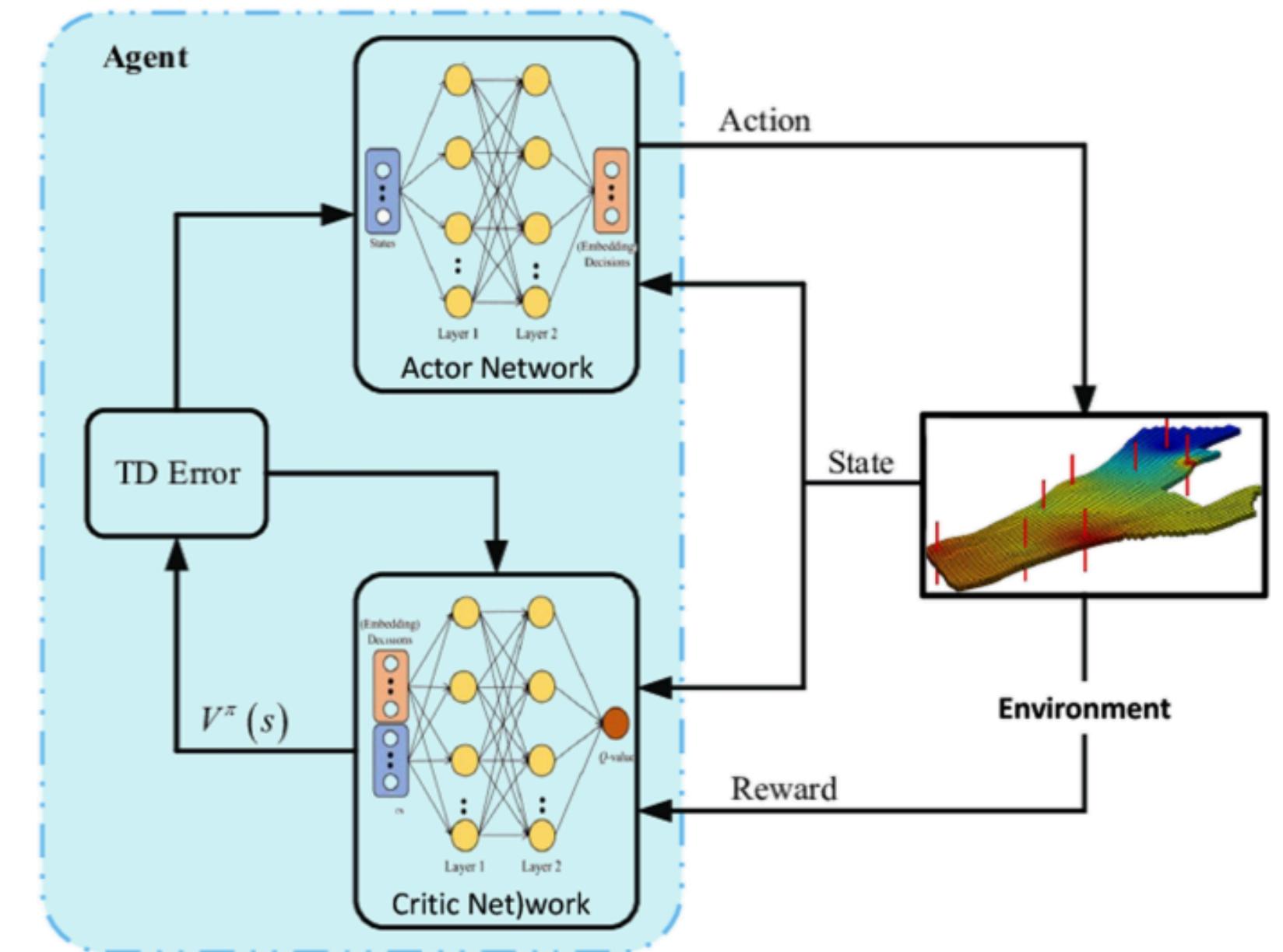
- The agent observes the current state s , selects an action a based on its current policy, and observes the outcome, which includes the reward r and the next state s' .
- This sequence of states, actions, and rewards is collected until the episode ends. The returns R_t for each timestep are calculated post-episode.
- These returns are used to update the policy parameters θ via gradient ascent
- The updated policy is then employed to gather new data in subsequent episodes, repeating the process.

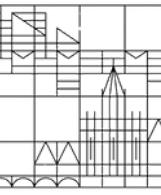


The Actor-Critic Framework

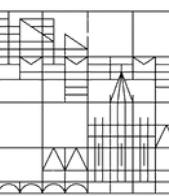
The Actor-Critic framework combines the benefits of both policy-based and value-based approaches in reinforcement learning.

- This method uses two models: the Actor, which proposes actions given the current state, and the Critic, which evaluates these actions by estimating the value function.
- By providing constant feedback after every action, the Critic helps the Actor adjust its policy in a more timely and informed manner.



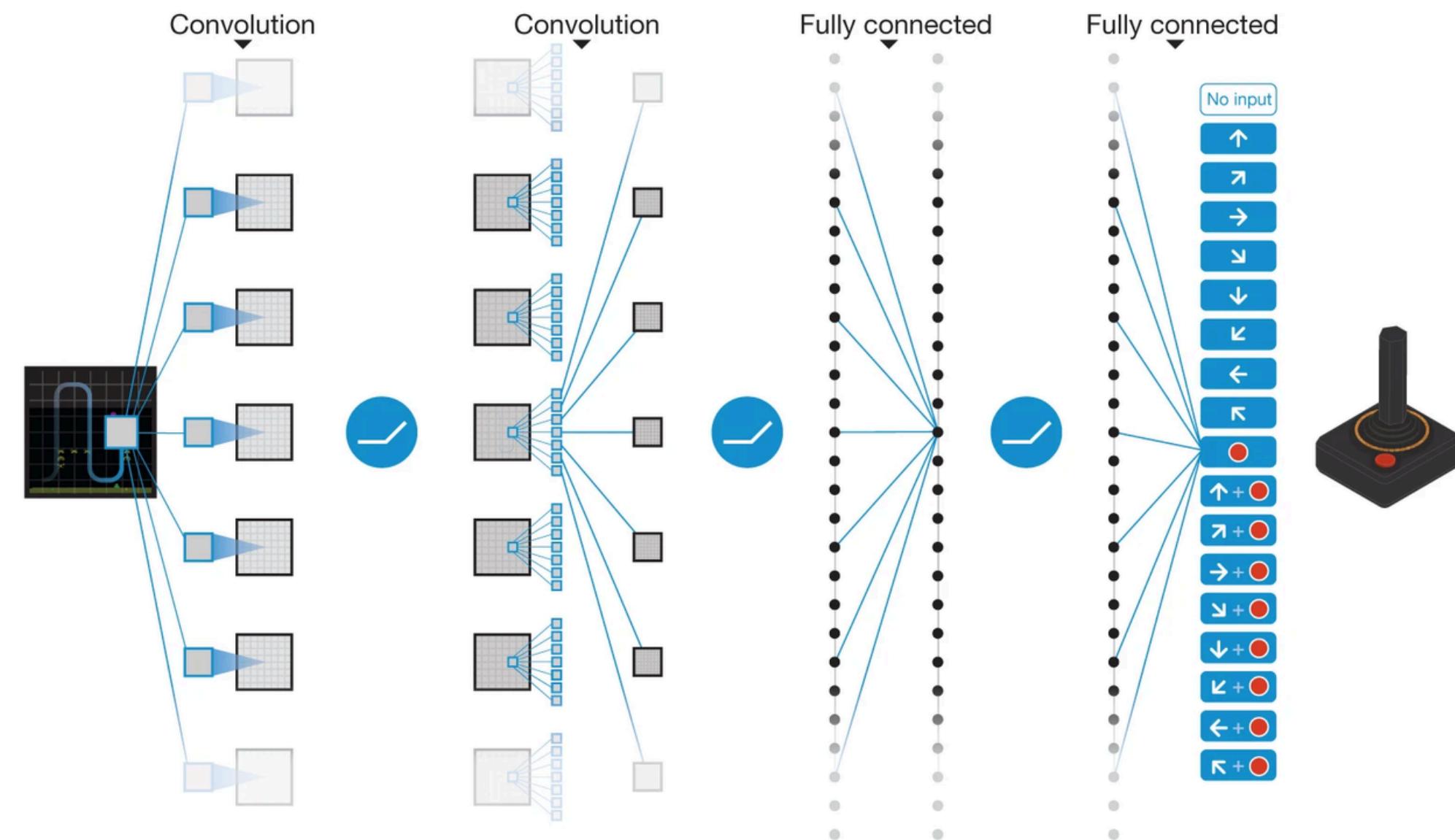


Applications of Reinforcement Learning



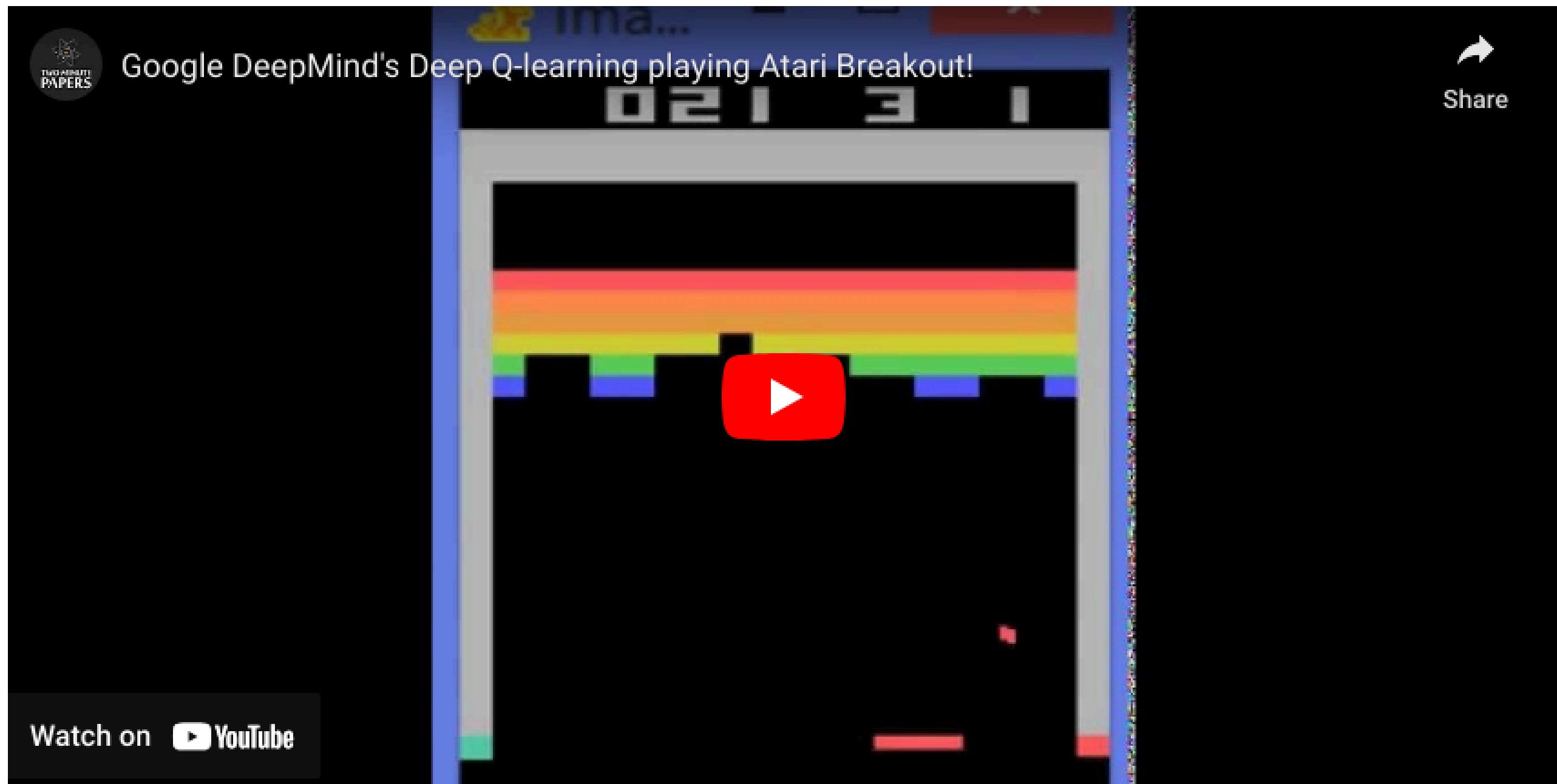
DQNs Beating Atari Games

The first big breakthrough in RL has been a famous [paper](#) by Google Deep Mind using DQNs and CNNs to play Atari games with RL (2013)





DQN Playing Atari





Other Games

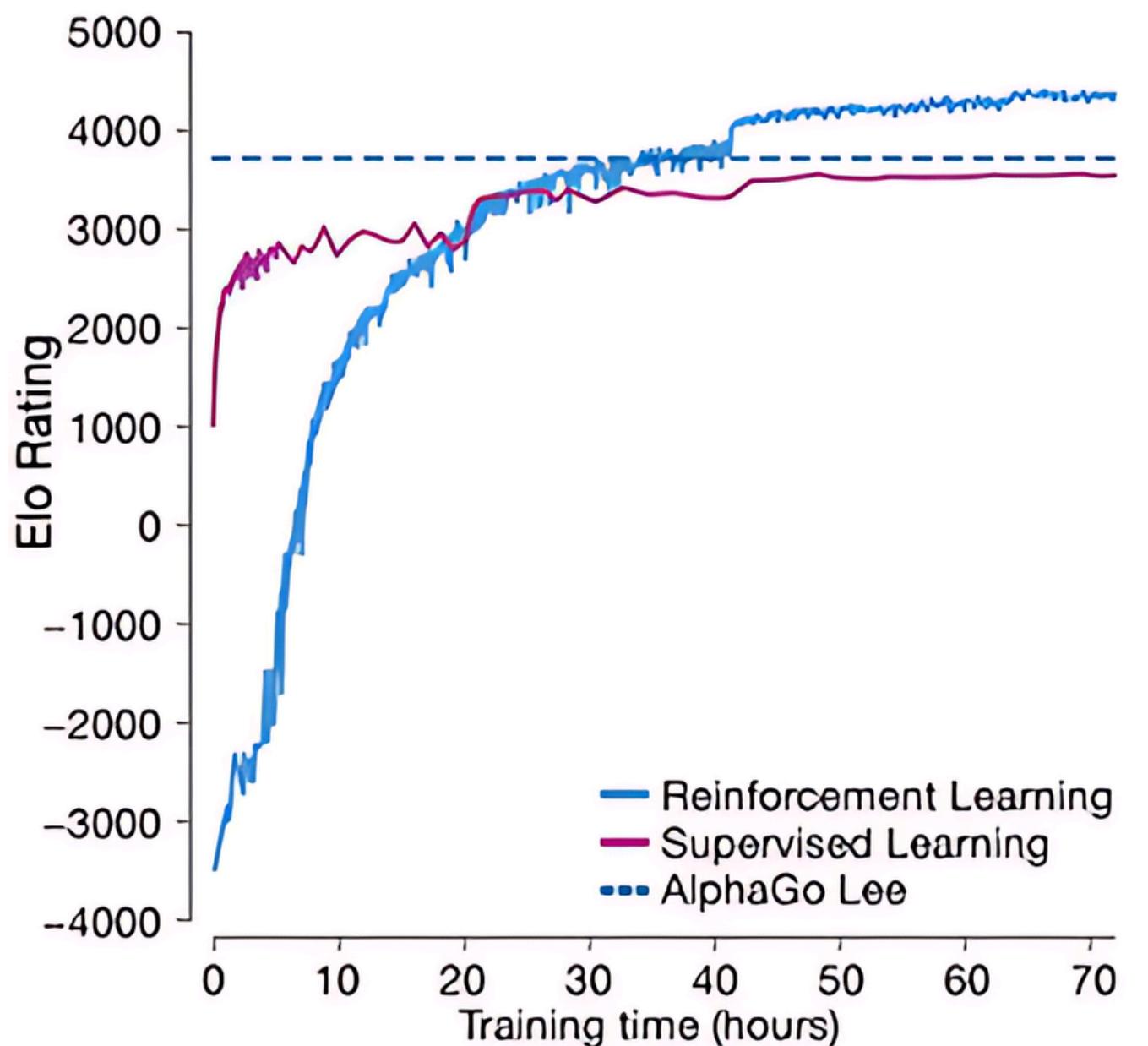




AlphaGo and AlphaZero

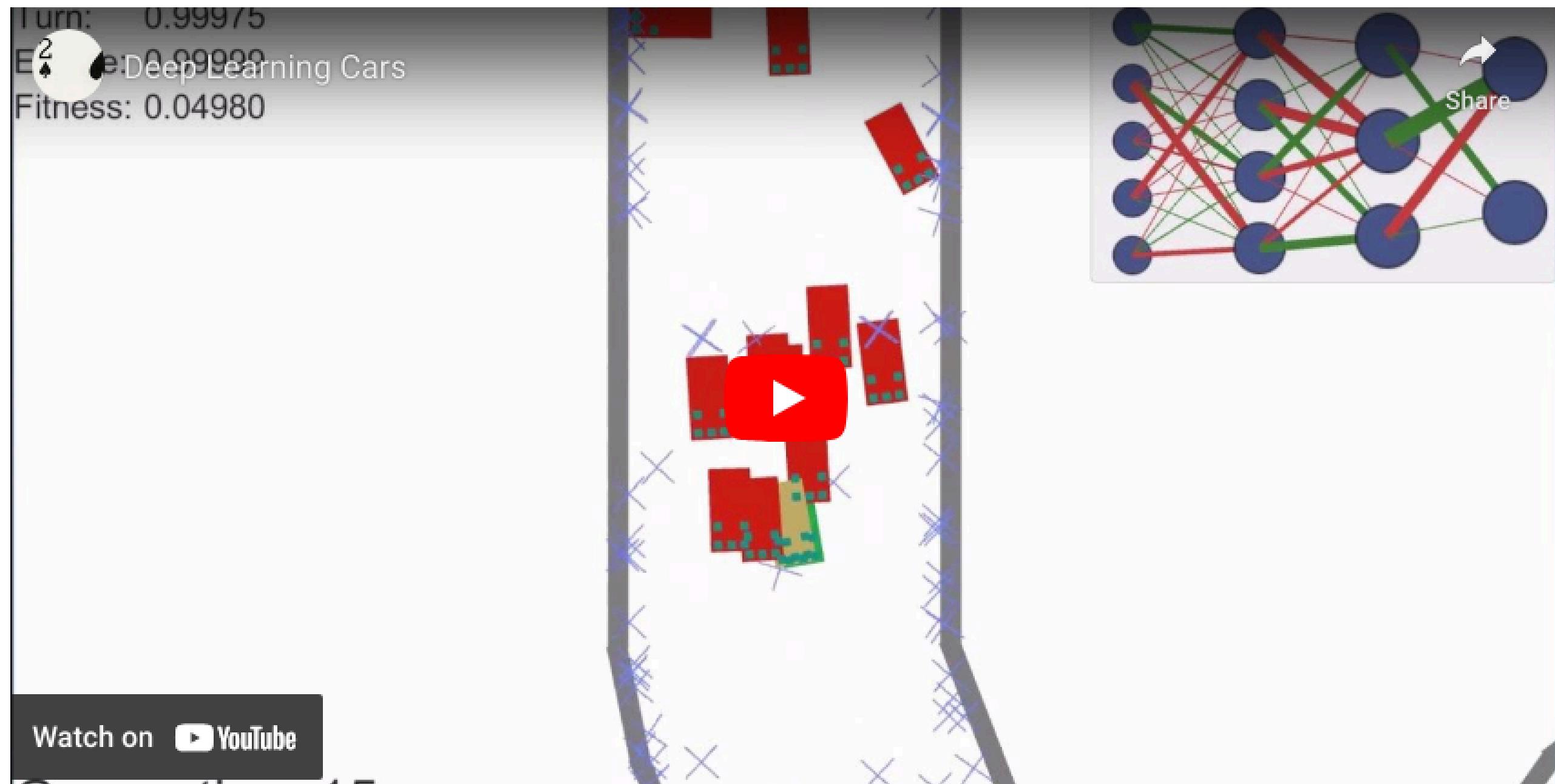
In 2016 Deep Mind makes another breakthrough with AlphaGo, beating the go world champion

- AlphaGo was initially trained on professional human games to learn winning patterns and then improved through self-play, refining its policy and value networks.
- AlphaZero enhances this approach by using purely self-play reinforcement learning without any human data, starting from random play. It learns optimal strategies in games like Go, chess, and Shogi by playing millions of games against itself.





Self-Driving Cars?





Summary

A New Learning Paradigm

Reinforcement learning solves the problems of supervised and unsupervised learning, combining their benefits.

Reinforcement Learning

In reinforcement learning agents learn by interacting with an environment and performing actions. They learn optimal strategies by maximizing the reward they receive.

Deep Q-Learning and Policy Gradient

DQNs are neural networks that learn the Q-value function, providing the agent an optimal policy. Policy gradient instead directly optimize the policy.

Applications of Reinforcement Learning

Reinforcement learning has found applications especially in games such as chess or go. At present days the most relevant application is probably in LLMs.