#### DM561 / DM562 Linear Algebra with Applications

#### Intoduction to Python - Part 2

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#### Outline

- 1. Exception Handling
- 2. File Input and Output
- 3. Numpy

Data Access Numerical Computing with NumPy

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Numerical Computing with NumPy

#### **Exceptions**

An exception formally indicates an error and terminates the program early.

```
>>> print(x)
Traceback (most recent call last):
   File "<stdin>", line 1, in <module>
NameError: name 'x' is not defined

>>> [1, 2, 3].fly()
Traceback (most recent call last):
   File "<stdin>", line 1, in <module>
AttributeError: 'list' object has no attribute 'fly'
```

### **Built-in Exceptions**

| Exception           | Indication  |
|---------------------|---|
| AttributeError      | An attribute reference or assignment failed.                    |
| ${\tt ImportError}$ | An import statement failed.                                     |
| ${\tt IndexError}$  | A sequence subscript was out of range.                          |
| NameError           | A local or global name was not found.                           |
| TypeError           | An operation or function was applied to an object of            |
|                     | inappropriate type.   |
| ValueError          | An operation or function received an argument that had          |
|                     | the right type but an inappropriate value.                      |
| ZeroDivisionError   | The second argument of a division or modulo operation was zero. |

See  ${\tt https://docs.python.org/3/library/exceptions.html} \ \ for \ the \ complete \ list \ of \ built-in \ exception$ 

#### Raising Exceptions

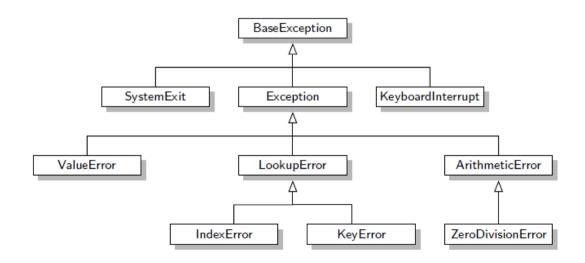
```
>>> if 7 is not 7.0:
                                    # Raise an exception with an error message.
       raise Exception("ints and floats are different!")
. . .
Traceback (most recent call last):
 File "<stdin>", line 2, in <module>
Exception: ints and floats are different!
>>> for x in range(10):
\dots if x > 5:
                                    # Raise a specific kind of exception.
           raise ValueError("'x' should not exceed 5.")
. . .
    print(x, end=' ')
. . .
0 1 2 3 4 5
Traceback (most recent call last):
 File "<stdin>", line 3, in <module>
ValueError: 'x' should not exceed 5.
```

### **Handling Exceptions**

To prevent an exception from halting the program, it must be handled by placing the problematic lines of code in a try block.

```
>>> trv:
        print("Entering try block...", end='')
        house_on_fire = False
... except ValueError as e: # Skipped because there was no exception.
       print("caught a ValueError.")
. . .
    house_on_fire = True
... except TypeError as e: # Also skipped (if just ``except:'' then always caught)
       print("caught a TypeError.")
       house_on_fire = True
else
       print("no exceptions raised.")
... finally: # always executed, even if a return statement or an uncaught \leftrightarrow
    exception occurs
        print("The house is on fire:", house_on_fire)
. . .
Entering try block...no exceptions raised.
The house is on fire: False
```

### **Exeception Hierarchy**



#### **Custom Exception Classes**

```
>>> class TooHardError(Exception):
...    pass
...
>>> raise TooHardError("This lab is impossible!")
Traceback (most recent call last):
    File "<stdin>", line 1, in <module>
    __main__.TooHardError: This lab is impossible!
```

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### File Reading

```
>>> myfile = open("hello_world.txt", 'r')  # Open a file for reading.
>>> print(myfile.read())  # Print the contents of the file.
Hello,  # (it's a really small file.)
World!
>>> myfile.close()  # Close the file connection.
```

the 'mode' can be 'r', 'w', 'x', 'a'

#### A More Secure Way

# Reading and Writing

| Attribute               | Description  |  |
|-------------------------|--|--|
| closed                  | True if the object is closed.  |  |
| mode                    | The access mode used to open the file object.                                  |  |
| name                    | The name of the file.  |  |
|                         |  |  |
| Method                  | Description  |  |
| close()                 | Close the connection to the file.  |  |
| read()                  | Read a given number of bytes; with no input, read the entire file.             |  |
| readline()              | Read a line of the file, including the newline character at the end.           |  |
| readlines()             | Call readline() repeatedly and return a list of the resulting lines.           |  |
| seek()                  | Move the cursor to a new position.   |  |
| tell()                  | Report the current position of the cursor.                                     |  |
| write()                 | Write a single string to the file (spaces are <b>not</b> added).               |  |
| <pre>writelines()</pre> | Write a list of strings to the file (newline characters are <b>not</b> added). |  |

## Writing

```
>>> with open("out.txt", 'w') as outfile:  # Open 'out.txt' for writing.
... for i in range(10):
... outfile.write(str(i**2)+' ')  # Write some strings (and spaces).
...
>>> outfile.closed  # The file is closed automatically.
True
```

# **String Methods**

| Method               | Returns  |
|----------------------|--|
| count()              | The number of times a given substring occurs within the string.        |
| find()               | The lowest index where a given substring is found.                     |
| isalpha()            | True if all characters in the string are alphabetic (a, b, c,).        |
| <pre>isdigit()</pre> | True if all characters in the string are digits (0, 1, 2,).            |
| isspace()            | True if all characters in the string are whitespace (" ", '\t', '\n'). |
| <pre>join()</pre>    | The concatenation of the strings in a given iterable with a            |
|                      | specified separator between entries.                                   |
| lower()              | A copy of the string converted to lowercase.                           |
| upper()              | A copy of the string converted to uppercase.                           |
| replace()            | A copy of the string with occurrences of a given substring             |
|                      | replaced by a different specified substring.                           |
| split()              | A list of segments of the string, using a given character or string    |
|                      | as a delimiter.  |
| strip()              | A copy of the string with leading and trailing whitespace removed.     |

#### **String Methods**

```
# str.join() puts the string between the entries of a list.
>>> words = ["state", "of", "the", "art"]
>>> "-".join(words)
'state-of-the-art'
# str.split() creates a list out of a string, given a delimiter.
>>> "One fish\nTwo fish\nRed fish\nBlue fish\n".split('\n')
['One fish', 'Two fish', 'Red fish', 'Blue fish', '']
# If no delimiter is provided, the string is split by whitespace characters.
>>> "One fish\nTwo fish\nRed fish\nBlue fish\n".split()
['One', 'fish', 'Two', 'fish', 'Red', 'fish', 'Blue', 'fish']
```

#### **Format**

```
# Join the data using string concatenation.
>>> day, month, year = 10, "June", 2017
>>> print("Is today", day, str(month) + ',', str(year) + "?")
Is today 10 June, 2017?

# Join the data using str.format().
>>> print("Is today {} {}, {}?".format(day, month, year))
Is today 10 June, 2017?
```

```
# From version 3.6
>>> print(f'Is today {day} {month}, {year}?')
Is today 10 June, 2017?
```

```
>>> iters = int(1e7)
>>> chunk = iters // 20
>>> for i in range(iters):
... print("\r[{:<20}] i = {}".format('='*((i//chunk)+1), i),
... end='', flush=True)

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```

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#### Numpy

Module implementing multi-dimensional vectors useful for applied and computational mathematics.

```
>>> import numpy as np
# Create a 1-D array by passing a list into NumPy's array() function.
>>> np.array([8, 4, 6, 0, 2])
array([8, 4, 6, 0, 2])
```

ndarray object. Each dimension is called an axis: For a 2-D array, the 0-axis indexes the rows and the 1-axis indexes the columns.

```
# Create a 2-D array by passing a list of ←
    lists into array().
>>> A = np.array( [ [1, 2, 3],[4, 5, 6] ] )
>>> print(A)
[[1 2 3]
  [4 5 6]]
```

### **Basic Array Operations**

Operators + and \* for built-in lists (and strings too) :

```
# Addition concatenates lists together.
>>> [1, 2, 3] + [4, 5, 6]
[1, 2, 3, 4, 5, 6]

# Multiplication concatenates a list with itself a given number of times.
>>> [1, 2, 3] * 4
[1, 2, 3, 1, 2, 3, 1, 2, 3, 1, 2, 3]
```

#### **Basic Array Operations**

```
>>> x, y = np.array([1, 2, 3]), np.array([4, 5, 6])
# Addition or multiplication by a scalar acts on each element of the array.
>>> x + 10
                                    # Add 10 to each entry of x.
array([11, 12, 13])
>>> x * 4
                                    # Multiply each entry of x by 4.
array([4, 8, 12])
# Add two arrays together (component-wise).
>>> x + v
array([5, 7, 9])
# Multiply two arrays together (component-wise).
>>> x * v
array([ 4, 10, 18])
```

## **Array Attributes**

An ndarray object has several attributes, some of which are listed below.

| Attribute | Description  |
|-----------|--|
| dtype     | The type of the elements in the array.                     |
| ndim      | The number of axes (dimensions) of the array.              |
| shape     | A tuple of integers indicating the size in each dimension. |
| size      | The total number of elements in the array.                 |

### Data Types

All elements of a NumPy array must have the same data type!!

| Data type  | Description   |
|------------|---|
| bool_      | Boolean   |
| int8       | 8-bit integer   |
| int16      | 16-bit integer  |
| int32      | 32-bit integer  |
| int64      | 64-bit integer  |
| uint8      | Unsigned 8-bit integer                                      |
| uint16     | Unsigned 16-bit integer                                     |
| uint32     | Unsigned 32-bit integer                                     |
| uint64     | Unsigned 64-bit integer                                     |
| float16    | Half-precision float  |
| float32    | Single-precision float                                      |
| float64    | Double-precision float (default type for most computations) |
| complex64  | Complex number represented by two single-precision floats   |
| complex128 | Complex number represented by two double-precision floats   |

#### Change Data Types

To change an existing array's type, use the array's astype() method.

```
# A list of integers becomes an array of integers.
>>> x = np.array([0, 1, 2, 3, 4])
>>> print(x)
[0 1 2 3 4]
>>> x.dtvpe
dtype('int64')
# Change the data type to one of NumPy's float types.
>>> x = x.astype(np.float64)
>>> print(x)
[0. 1. 2. 3. 4.]
>>> x.dtype
dtype('float64')
```

### **Array Creation Routines**

| Function               | Returns   |
|------------------------|---|
| arange()               | Array of sequential integers (like list(range())).            |
| eye()                  | 2-D array with ones on the diagonal and zeros elsewhere.      |
| ones()                 | Array of given shape and type, filled with ones.              |
| ones_like()            | Array of ones with the same shape and type as a given array.  |
| zeros()                | Array of given shape and type, filled with zeros.             |
| zeros_like()           | Array of zeros with the same shape and type as a given array. |
| full()                 | Array of given shape and type, filled with a specified value. |
| <pre>full_like()</pre> | Full array with the same shape and type as a given array.     |

Each of these functions accepts the keyword argument dtype to specify the data type. Common types include np.bool\_, np.int64, np.float64, and np.complex128.

### **Array Creation Routines**

```
# A 1-D array of 5 zeros.
>>> np.zeros(5)
array([ 0., 0., 0., 0., 0.])
# A 2x5 matrix (2-D array) of integer ones.
>>> np.ones((2,5), dtype=np.int) # The shape is specified as a tuple.
array([[1, 1, 1, 1, 1],
      [1, 1, 1, 1, 1]]
# The 2x2 identity matrix.
>>> I = np.eve(2)
>>> print(I)
[[ 1. 0.]
[ 0. 1.]]
# Array of 3s the same size as 'I'.
>>> np.full_like(I, 3)  # Equivalent to np.full(I.shape, 3).
array([[ 3., 3.],
      [3., 3.]])
```

### **Array Creation Routines**

| Function | Description  |  |
|----------|--|--|
| diag()   | Extract a diagonal or construct a diagonal array.  |  |
| tril()   | Get the lower-triangular portion of an array by replacing entries above  |  |
| triu()   | the diagonal with zeros.  Get the upper-triangular portion of an array by replacing entries below the diagonal with zeros. |  |

## Random Sampling

Similar to standard library's 'Random' module but more efficient

| Function                         | Description   |
|----------------------------------|---|
| choice()                         | Take random samples from a 1-D array.                     |
| random()                         | Uniformly distributed floats over [0, 1).                 |
| randint()                        | Random integers over a half-open interval.                |
| random_integers()                | Random integers over a closed interval.                   |
| randn()                          | Sample from the standard normal distribution.             |
| <pre>permutation()</pre>         | Randomly permute a sequence / generate a random sequence. |
| Function                         | Distribution  |
| beta()                           | Beta distribution over [0, 1].                            |
| binomial()                       | Binomial distribution.                                    |
| exponential()                    | Exponential distribution.                                 |
| gamma()                          | Gamma distribution.                                       |
| <pre>geometric()</pre>           | Geometric distribution.                                   |
| <pre>multinomial()</pre>         | Multivariate generalization of the binomial distribution. |
| <pre>multivariate_normal()</pre> | Multivariate generalization of the normal distribution.   |
| normal()                         | Normal / Gaussian distribution.                           |
| poisson()                        | Poisson distribution.                                     |
| uniform()                        | Uniform distribution.                                     |

### Random Sampling

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$$exttt{A[1:-1,1:-1]} = egin{bmatrix} imes & imes & imes & imes \\ imes & imes & imes & imes \\ imes & imes & imes & imes \\ imes & imes & imes & imes & imes \end{bmatrix}$$

```
>>> x = np.arange(10); x
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
>>> x[3]
                                     # The element at index 3.
3
>>> x[:3]
                                     # Everything up to index 3 (exclusive).
array([0, 1, 2])
>>> x[3:]
                                     # Everything from index 3 on.
array([3, 4, 5, 6, 7, 8, 9])
>>> x[3:8]
                                     # The elements from index 3 to 8.
array([3, 4, 5, 6, 7])
>>> A = np.array([[0,1,2,3,4],[5,6,7,8,9]])
>>> A
array([[0, 1, 2, 3, 4],
       [5, 6, 7, 8, 9]])
>>> A[1, 2]
                                     # The element at row 1, column 2.
>>> A[:, 2:]
                                     # All of the rows, from column 2 on.
array([[2, 3, 4],
       [7, 8, 9]])
```

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- Indexing and slicing operations return a view of the array.
- Changing a view of an array also changes the original array.
- That is, arrays are mutable.
- To create a copy of an array, use np.copy() or the array's copy() method.
- Changes to a copy of an array does not affect the original array
- Copying is less efficient than getting a view.

### **Fancy Indexing**

Via either an array of indices or an array of boolean values (mask) to extract specific elements.

```
>>> x = np.arange(0, 50, 10) # The integers from 0 to 50 by tens.
>>> x
array([ 0, 10, 20, 30, 40])
# An array of integers extracts the entries of 'x' at the given indices.
>>> index = np.array([3, 1, 4])  # Get the 3rd, 1st, and 4th elements.
>>> x[index]
                                   # Same as np.arrav([x[i] for i in index]).
array([30, 10, 40])
# A boolean array extracts the elements of 'x' at the same places as 'True'.
>>> mask = np.array([True, False, False, True, False])
>>> x[mask]
                                   # Get the Oth and 3rd entries.
array([ 0, 30])
```

### **Fancy Indexing**

```
\Rightarrow y = np.arange(10, 20, 2) # Every other integers from 10 to 20.
>>> v
array([10, 12, 14, 16, 18])
# Extract the values of 'y' larger than 15.
>>> mask = v > 15
                   # Same as np.array([i > 15 \text{ for i in y}]).
>>> mask
array([False, False, False, True, True], dtype=bool)
>>> y[mask]
                                   # Same as y[y > 15]
array([16, 18])
# Change the values of 'y' that are larger than 15 to 100.
>>> y[mask] = 100
>>> print(y)
[10 12 14 100 100]
```

# **Shaping**

```
>>> A = np.arange(12)
                                 # The integers from 0 to 12 (exclusive).
>>> print(A)
[0 1 2 3 4 5 6 7 8 9 10 11]
# 'A' has 12 entries, so it can be reshaped into a 3x4 matrix.
>>> A.reshape((3,4))
                           # The new shape is specified as a tuple.
array([[ 0, 1, 2, 3],
      [4, 5, 6, 7],
      [8, 9, 10, 11]])
# Reshape 'A' into an array with 2 rows and the appropriate number of columns.
>>> A.reshape((2,-1))
array([[ 0, 1, 2, 3, 4, 5],
      [6, 7, 8, 9, 10, 11]])
```

# **Shaping**

```
>>> A = np.arange(12).reshape((3,4))
>>> A
array([[ 0, 1, 2, 3],
      [4, 5, 6, 7],
      [8, 9, 10, 11]])
# Flatten 'A' into a one-dimensional array.
>>> np.ravel(A)
                          # Equivalent to A.reshape(A.size)
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11])
# Transpose the matrix 'A'.
>>> A.T
                                # Equivalent to np.transpose(A).
array([[ 0, 4, 8],
      [1, 5, 9],
      [2, 6, 10],
     [3, 7, 11]])
```

• Caution: reshape is just a view on the array, it does not copy the data. Beware: the following does shallow copy:

```
>>> N=A

>>> N[0,0] = 0 # now A[0,0] has become 0

>>> M=A.reshape(1,9)

>>> M[0,7]=10 # now A[2,1] has become 10

>>> A

array([[ 0., 2., 3.],

       [ 4., 5., 6.],

       [ 7., 10., 9.]])
```

• We can see the base object by:

• To implement a deep copy you must use np.copy(A)

## Note on Vector Shape

- By default, all NumPy 1D arrays (including column slices) are automatically reshaped into "flat" (ie, row) 1D arrays.
- This contrasts with mathematical notation where vectors are represented vertically
- NumPy methods such as dot() are implemented to purposefully work well with 1D "row arrays".
- np.transpose() does not alter 1D arrays.
- Do not force a 1D vector to be a column vector unless necessary.
- To force a "column array" use np.reshape(), np.vstack()

# Stacking

| Function                  | Description  |
|---------------------------|--|
| concatenate()             | Join a sequence of arrays along an existing axis     |
| hstack()                  | Stack arrays in sequence horizontally (column wise). |
| vstack()                  | Stack arrays in sequence vertically (row wise).      |
| <pre>column_stack()</pre> | Stack 1-D arrays as columns into a 2-D array.        |
| row_stack()               | Stack 1-D arrays as rows into a 2-D array.           |

# Stacking

```
>>> A = np.arange(6).reshape((2,3))
>>> B = np.zeros((4,3))
>>> np.vstack((A,B,A)) # same as np.concatenate([A,B,A],axis=0) and row_stack()
                                 # A
array([[ 0., 1., 2.],
      [3., 4., 5.],
      [0., 0., 0.],
                                # B
      [ 0., 0., 0.],
      [ 0., 0., 0.],
      [ 0., 0., 0.],
      [0., 1., 2.],
                                 # A
      [3., 4., 5.]])
```

# Stacking

You need to use column\_stack() to stack arrays horizontally 1-D arrays.

http://docs.scipy.org/doc/numpy-1.10.1/reference/routines.array-manipulation.html

#### **Broadcasting**

NumPy tries to automatically align arrays for component-wise operations whenever possible.

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 1 & 2 & 3 \\ 1 & 2 & 3 \end{bmatrix}$$
  $x = \begin{bmatrix} 10 & 20 & 30 \end{bmatrix}$ 

$$A + x = \begin{bmatrix} 1 & 2 & 3 \\ 1 & 2 & 3 \\ 1 & 2 & 3 \end{bmatrix} = \begin{bmatrix} 11 & 22 & 33 \\ 11 & 22 & 33 \\ 11 & 22 & 33 \end{bmatrix}$$

A + x.reshape((3,-1)) = 
$$\begin{bmatrix} 1 & 2 & 3 \\ 1 & 2 & 3 \\ 1 & 2 & 3 \end{bmatrix} + \begin{bmatrix} 10 \\ 20 \\ 30 \end{bmatrix} = \begin{bmatrix} 11 & 12 & 13 \\ 21 & 22 & 23 \\ 31 & 32 & 33 \end{bmatrix}$$

http://docs.scipy.org/doc/numpy/user/basics.broadcasting.html

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#### **Universal Functions**

Universal function: operates on an entire array element-wise. More efficent than looping.

| Function                         | Description                                     |
|----------------------------------|---|
| <pre>«abs()» or absolute()</pre> | Calculate the absolute value element-wise.      |
| exp() / log()                    | Exponential $(e^x)$ / natural log element-wise. |
| <pre>maximum() / minimum()</pre> | Element-wise maximum / minimum of two arrays.   |
| sqrt()                           | The positive square-root, element-wise.         |
| sin(), cos(), tan(), etc.        | Element-wise trigonometric operations.          |

```
>>> x = np.arange(-2,3)
>>> print(x, np.abs(x))  # Like np.array([abs(i) for i in x]).

[-2 -1 0 1 2] [2 1 0 1 2]

>>> np.sin(x)  # Like np.array([math.sin(i) for i in x]).

array([-0.90929743, -0.84147098, 0. , 0.84147098, 0.90929743])
```

#### **Universal Functions**

- Some functions from the module math do not work with array.
- It is possible to make them element-wise via vectorize.

# Operations along an Axis

Most array methods have an axis argument that allows an operation to be done along a given axis.

$$A = \begin{bmatrix} 1 & 2 & 3 & 4 \\ 1 & 2 & 3 & 4 \\ 1 & 2 & 3 & 4 \\ 1 & 2 & 3 & 4 \end{bmatrix}$$

A.sum(axis=0) = 
$$\begin{bmatrix} 1 & 2 & 3 & 4 \\ 1 & 2 & 3 & 4 \\ 1 & 2 & 3 & 4 \\ 1 & 2 & 3 & 4 \end{bmatrix} = \begin{bmatrix} 4 & 8 & 12 & 16 \end{bmatrix}$$

A.sum(axis=1) = 
$$\begin{bmatrix} 1 & 2 & 3 & 4 \\ 1 & 2 & 3 & 4 \\ 1 & 2 & 3 & 4 \end{bmatrix} = \begin{bmatrix} 10 & 10 & 10 & 10 \end{bmatrix}$$

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