

# Unifying Data, Model and Hybrid Parallelism in Deep Learning via Tensor Tiling

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[ARXIV18]

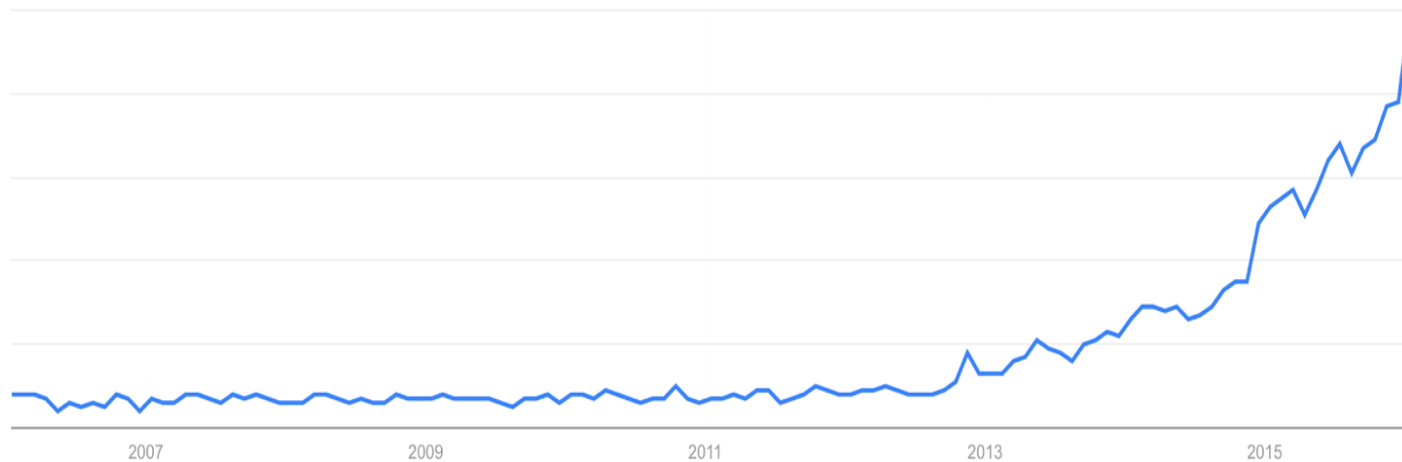


Adapted From Minjie Wang

# Outline

- Background & Motivation
- Problem Setup & Challenge
- Tofu solution
  - Single Operator
  - Whole Graph
- Experiments

# Deep Learning



“Deep Learning” trend in the past 10 years

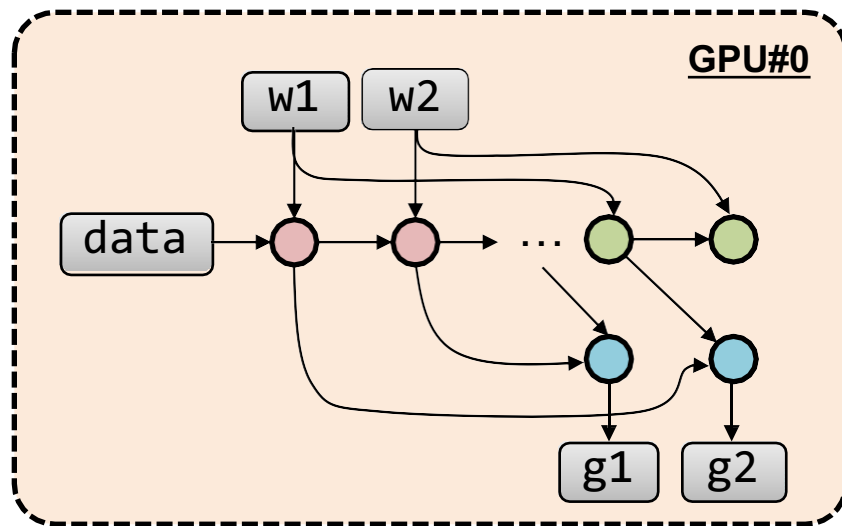
Caffe




theano



# State-of-art DL system is based on dataflow

```
import tensorflow as tf
... # generate data and weight
act1 = tf.matmul(data, w1)
act2 = tf.matmul(act1, w2)
...
grad_act2 = tf.matmul(w3.T, grad_act3)
grad_act1 = tf.matmul(w2.T, grad_act2)
...
grad_w2 = tf.matmul(act1.T, grad_act2)
grad_w1 = tf.matmul(data.T, grad_act1)
... # update weights using gradients
```



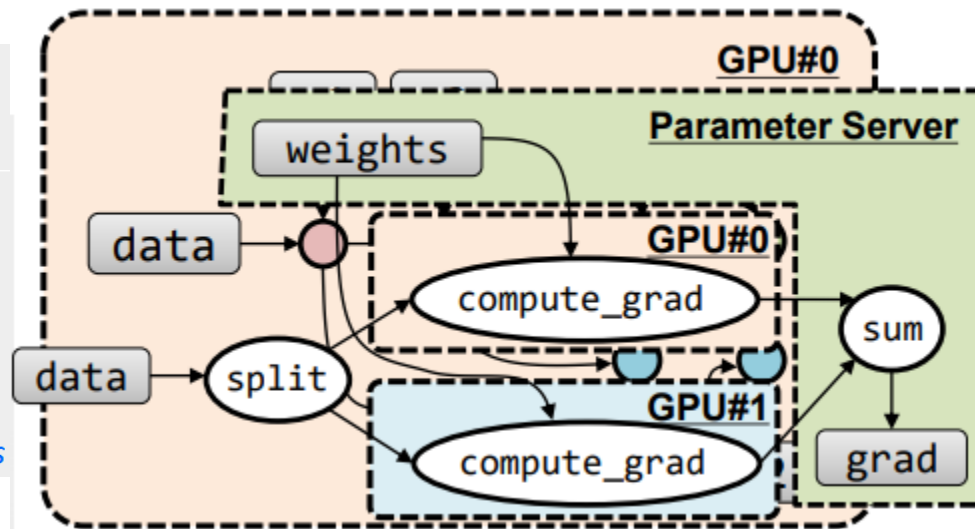
-  *Forward propagation*
-  *Backward propagation (input gradients)*
-  *Backward propagation (weight gradients)*

# What if I have many GPUs?



# Data parallelism with manual distribution

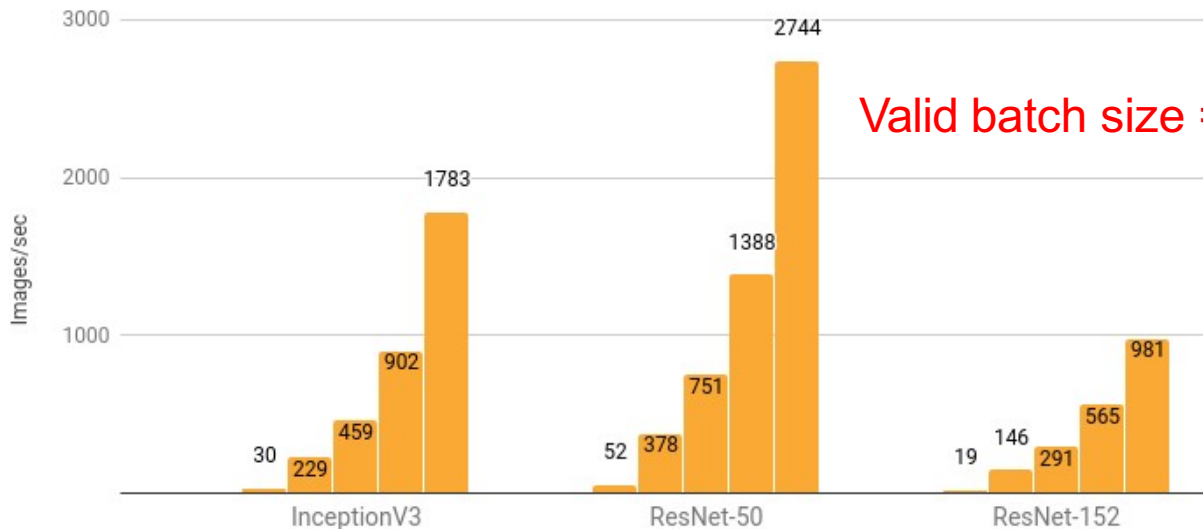
```
import tensorflow as tf
... # generate data and weight
data1, data2 = tf.split(data, axis=0)
with tf.device('/gpu:0'):
    grad1 = compute_grad(data1, weights)
with tf.device('/gpu:1'):
    grad2 = compute_grad(data2, weights)
with tf.device('/ps'):
    grad = aggregate(grad1, grad2)
... # update weights using gradients
```



**Manual Distribution &  
Device assignment**

# Scalability secret of data parallelism

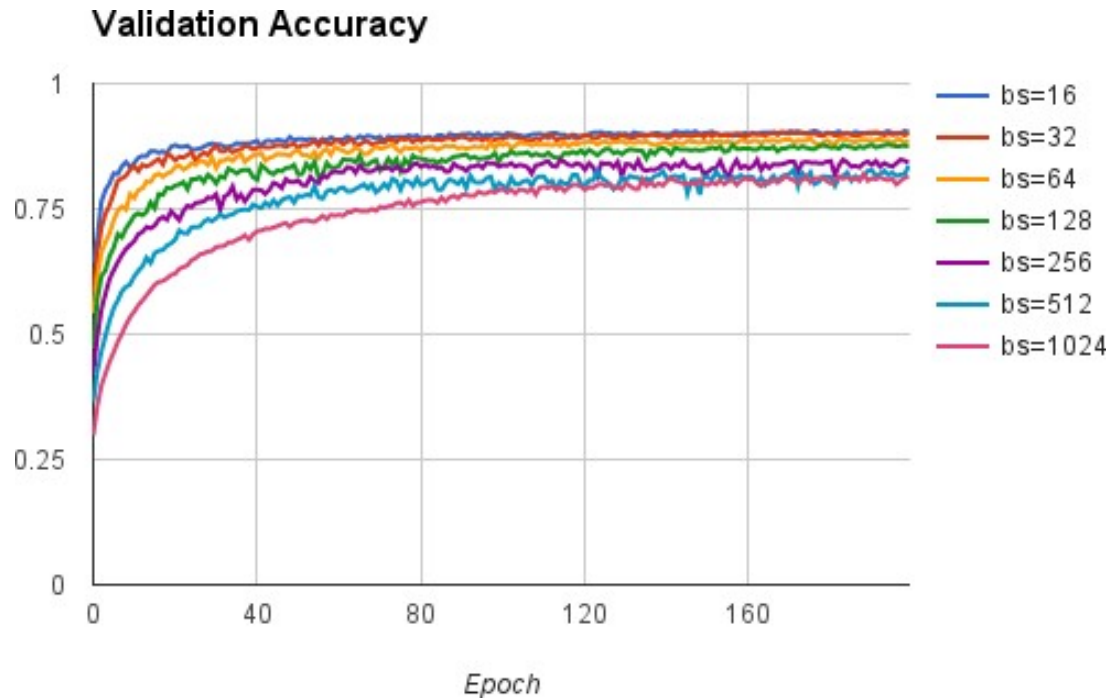
Training: NVIDIA® Tesla® K80 synthetic data (1,8,16,32, and 64)



Options	InceptionV3	ResNet-50	ResNet-152	Alexnet	VGG16
Batch size per GPU	64	64	64	512	64
Optimizer	sgd	sgd	sgd	sgd	sgd

\* Numbers from <https://www.tensorflow.org/performance/benchmarks>

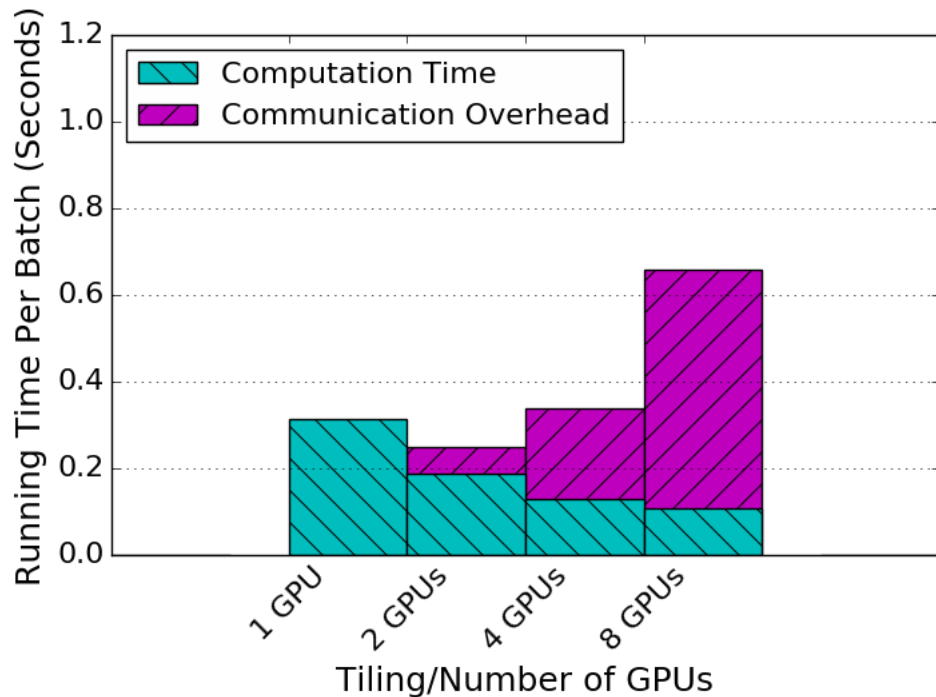
# Large batch size harms model accuracy



Inception Network on Cifar-10 dataset



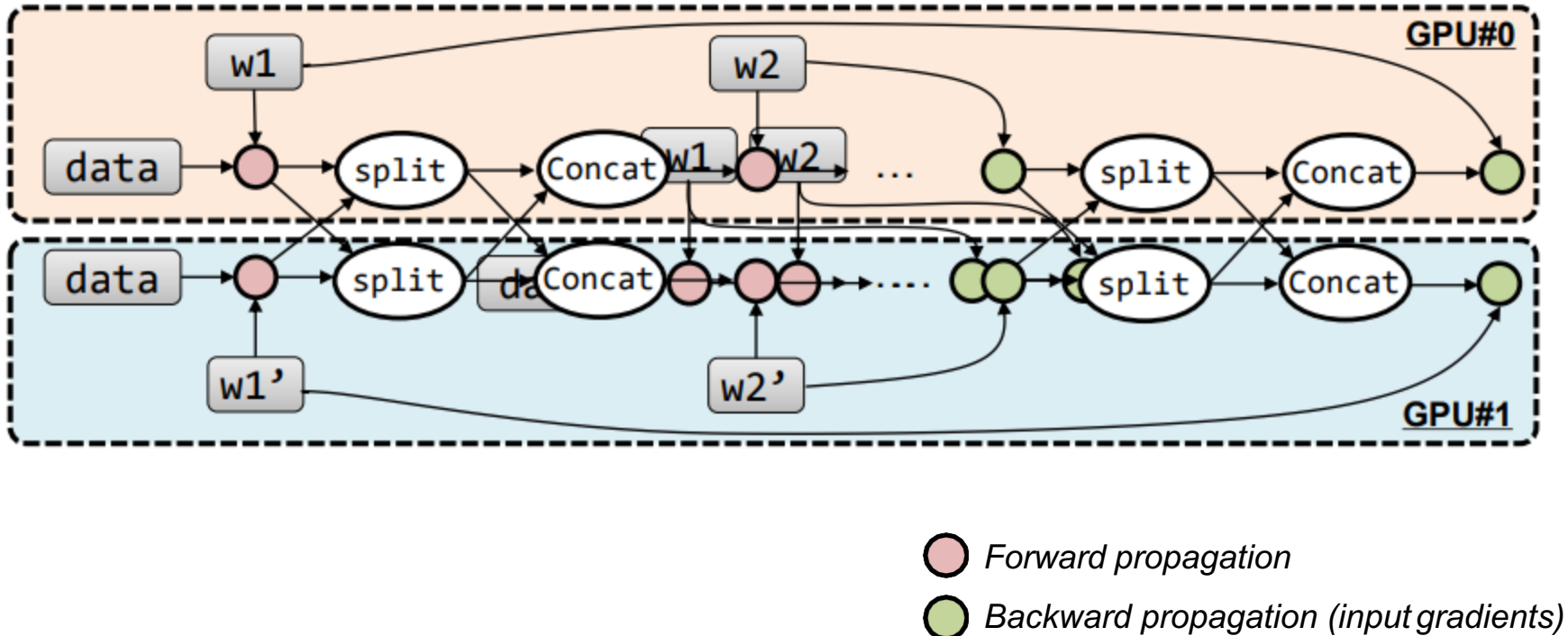
# Data parallelism bottlenecked by communication



>80% of the total running time is for communication on 8 cards

5-layer MLP; Hidden Size = 8192; Batch Size = 512

# An alternative way: Model Parallelism



# MP is hard to program

```
1 # Original MLP code.
2* def mlp(data, weights):
3     # Forward Propagation.
4     fwd = [data]
5     for i in xrange(FLAGS.num_layers):
6         fwd.append(tf.matmul(fwd[-1], weights[i])) # forward matmult
7     # Backward Propagation.
8     targets = []
9     last = fwd[-1]
10*    for i in reversed(xrange(FLAGS.num_layers)):
11        dw = tf.matmul(fwd[i], last, transpose_a=True) # matmult: grad
12        last = tf.matmul(last, w[i], transpose_b=True) # matmult: bp
13        # update
14        targets.append(dw)
15    return targets
```



```
1 # Manual Model Parallelism implementation for a MLP network.
2 def model_par_mlp(data, weights):
3     # Partition weights on row.
4     w = []
5     for i in xrange(FLAGS.num_layers):
6         w.append([])
7         for j in xrange(FLAGS.num_workers):
8             with tf.device('/job:worker/task:%d' % j):
9                 w[i].append(tf.get_variable(
10                     name='w%d' % j,
11                     shape=[slice_size, feature_size],
12                     trainable=True))
13     # Forward Propagation.
14     fwd = []
15     last = data
16     for i in xrange(FLAGS.num_layers):
17         with tf.name_scope('fc_ff%d' % i):
18             fwd.append(last)
19             tmp = []
20             for j in xrange(FLAGS.num_workers):
21                 with tf.device('/job:worker/task:%d' % j):
22                     y = tf.matmul(last[j], w[i][j]) # forward matmult
23                     # split the result so we can do balanced reduction.
24                     tmp.append(tf.split(split_dim=1, num_split=FLAGS.num_workers, value=y))
25             # Reduce the result.
26             red = []
27             for j in xrange(FLAGS.num_workers):
28                 with tf.device('/job:worker/task:%d' % j):
29                     red.append(tf.accumulate_n([s[j] for s in tmp]))
30             last = red
31     # Backward Propagation.
32     targets = []
33     for i in reversed(xrange(FLAGS.num_layers)):
34         with tf.name_scope('fc_bp%d' % i):
35             # Concatenate input tensors.
36             tmp = []
37             for j in xrange(FLAGS.num_workers):
38                 with tf.device('/job:worker/task:%d' % j):
39                     tmp.append(tf.concat(concat_dim=1, values=last))
40             last = []
41             for j in xrange(FLAGS.num_workers):
42                 with tf.device('/job:worker/task:%d' % j):
43                     dy = tf.matmul(tmp[j], w[i][j], transpose_b=True) # matmult: bp
44                     last.append(dy)
45                     dw = tf.matmul(fwd[i][j], tmp[j], transpose_a=True) # matmult: grad
46                     targets.append(dw) # update
47    return targets
```

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# What is the best strategy for distribution?

- No one-size-fits-all
  - DP and MP suit different situations (parameter shapes, batch sizes).
  - Different layers might be suited for different strategies (**hybrid parallelism**).
    - Use data parallelism for convolution layers; use model parallelism for fully-connected layers.
- *Can we find an optimal distributed execution plan?*

# Parallelism in Deep Learning

- Exploring Hidden Dimensions in Parallelizing Convolutional Neural Networks [ICML18, Stanford & MSR]
- Unifying Data, Model and Hybrid Parallelism in Deep Learning via Tensor Tiling [NYU, May 10]
- PipeDream: Fast and Efficient Pipeline Parallel DNN Training [MSR&Stanford&CMU, June 8]
- Beyond Data and Model Parallelism for Deep Neural Networks [Stanford, July 14]
- GPipe: Efficient Training of Giant Neural Networks using Pipeline Parallelism [Google Brain, Nov 20]

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# Tofu automatically distributes DL training

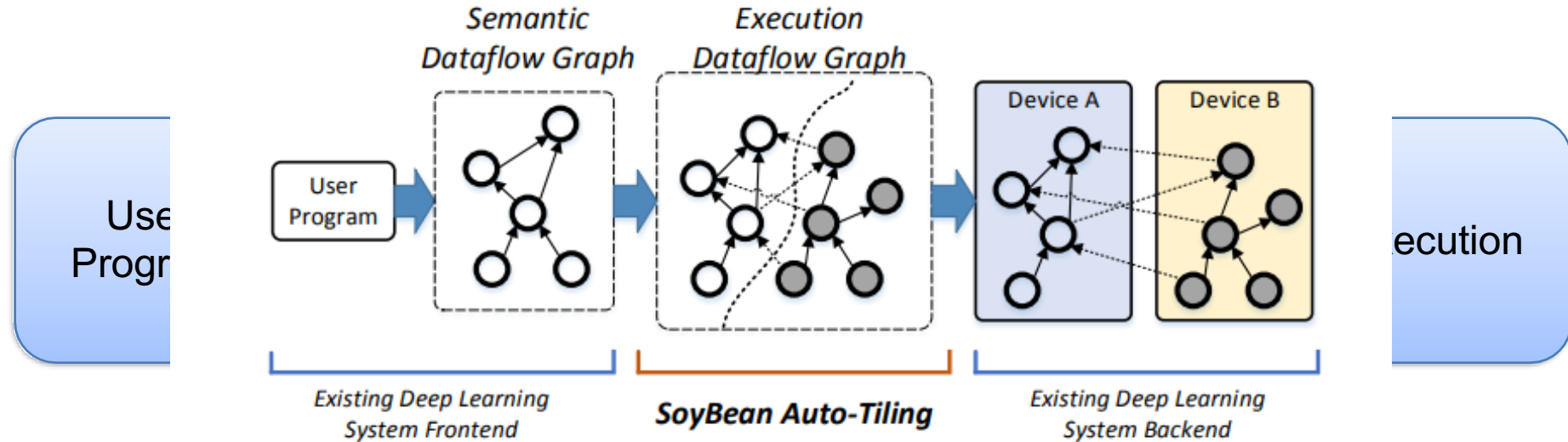


Figure 3: Overview of SOYBEAN's design.

**Tofu**





# Parallelism unified as tensor tiling:

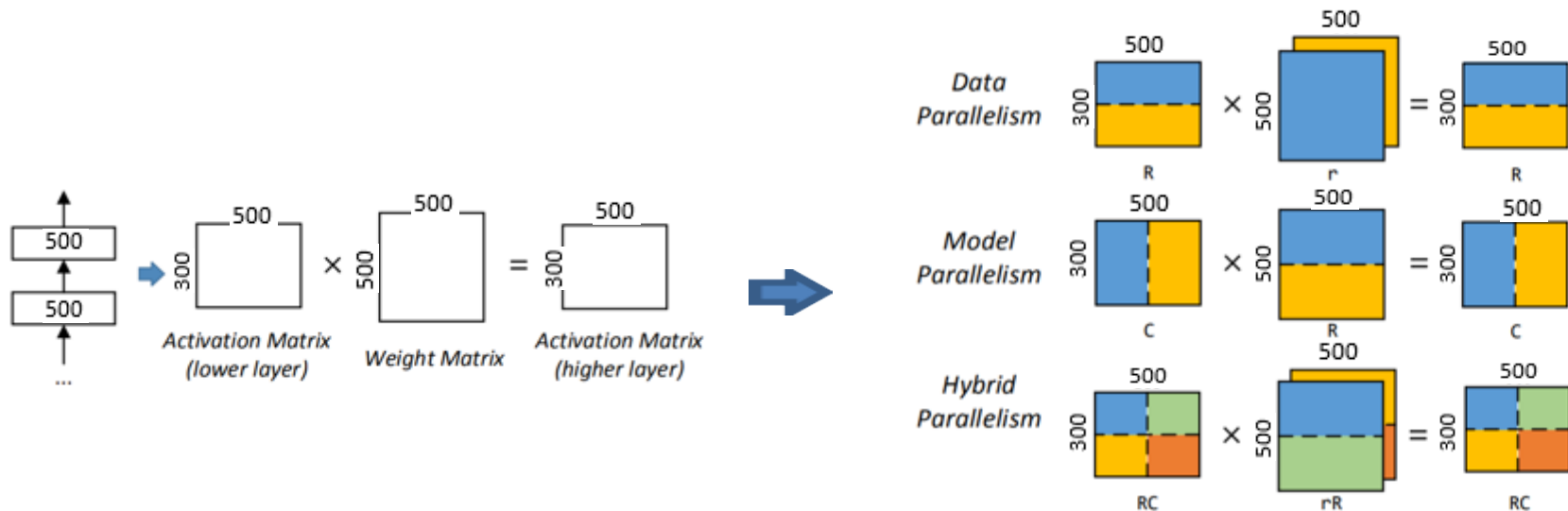


Figure 5: Top: forward propagation of one layer in a MLP model. Bottom: how matrices are tiled in the forward propagation for different parallelisms.

# Aligned Tilings

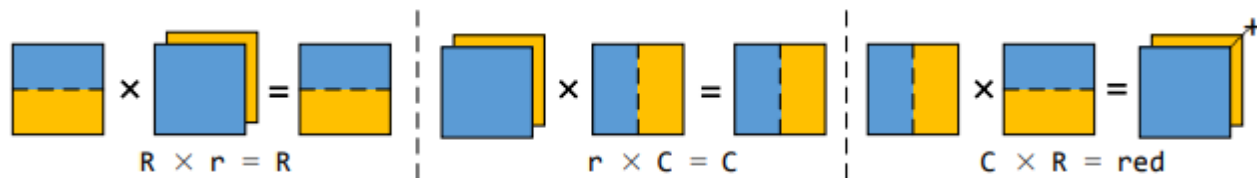
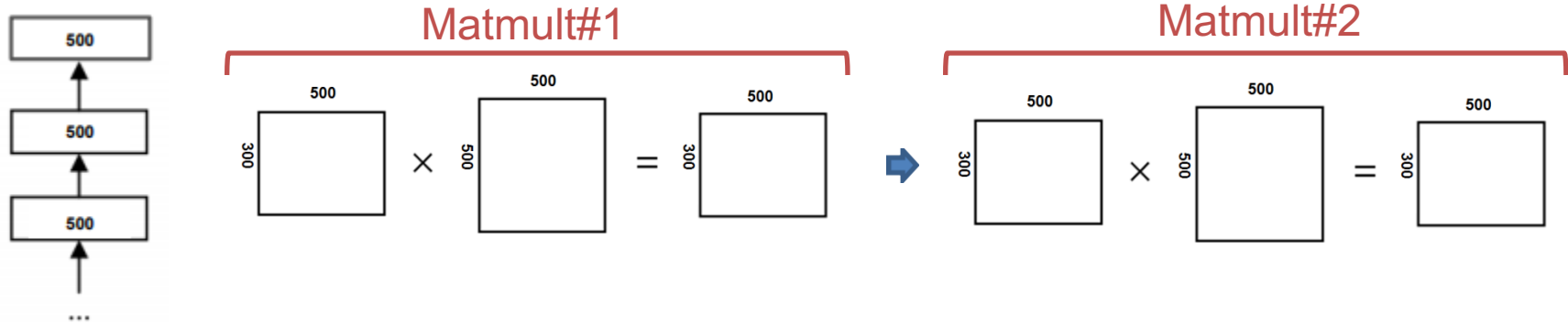


Figure 6: Three forms of aligned tilings for matrix multiplication. The resulting partition of the third form is an intermediate one red, and requires an extra reduction.

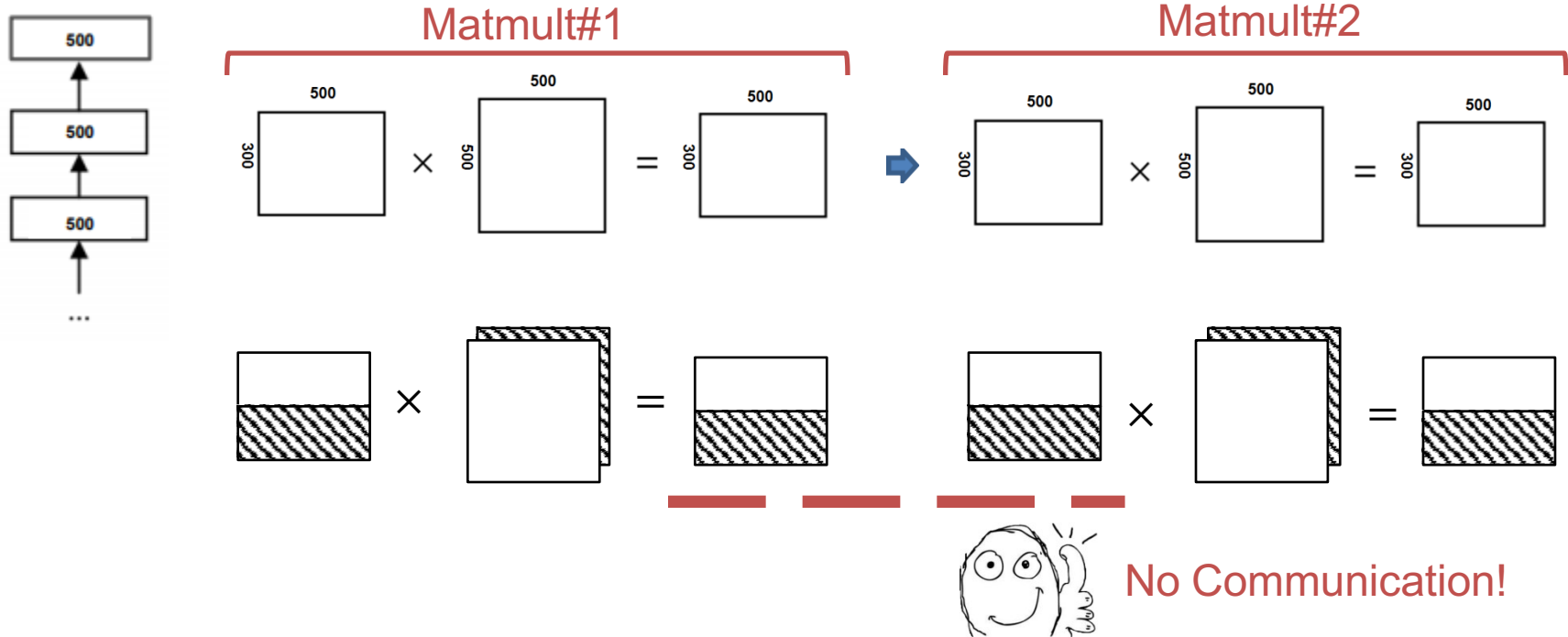
# Example of different strategies

- Different matrix multiplications may choose different strategies.



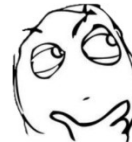
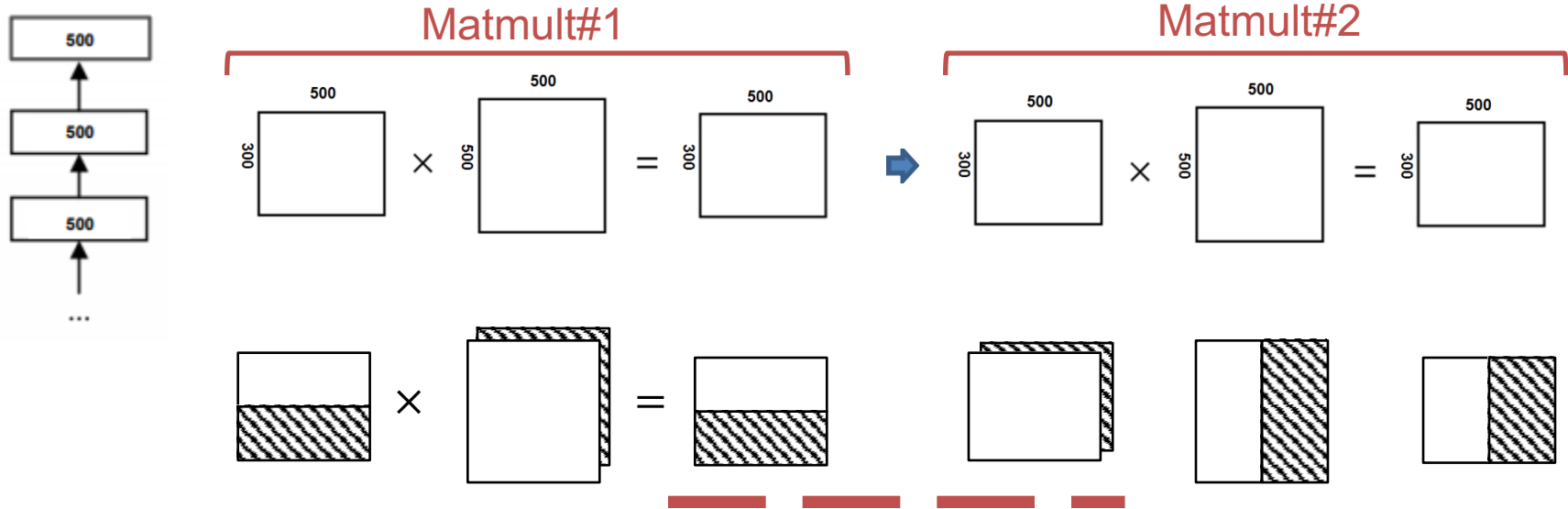
# Example of different strategies

- No communication if the output matrix satisfies the input partition.



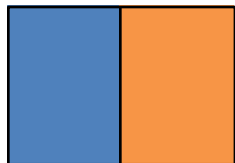
# Example of different strategies

- Communication happens when matrices need to be re-partitioned.

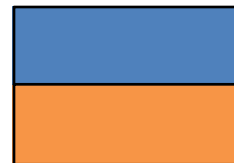


# Communication Cost

- Communication happens when matrices need to be re-partitioned.
- Communication cost == partition conversion cost.



C



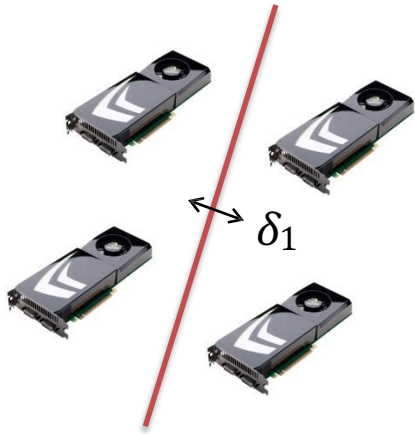
R

# Finding optimal strategy with minimal communication

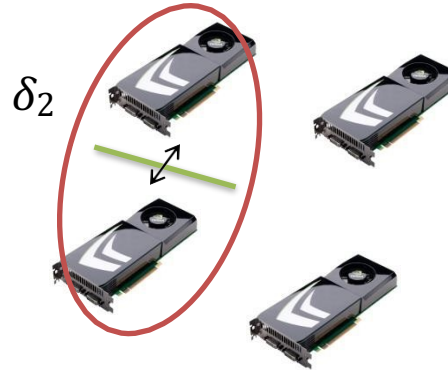
- Each operator has several distribution decisions.
  - DP and MP are one of them.
- Looking at one operator at a time is **not** optimal.
- Finding strategy with minimal communication cost for a general graph is NP-Complete.
- Tofu finds optimal strategy for deep learning in polynomial time:
  - “Layer-by-layer” propagations → graph with long diameter.
  - Use dynamic programming algorithm to find optimal strategy.

# Find combined strategies

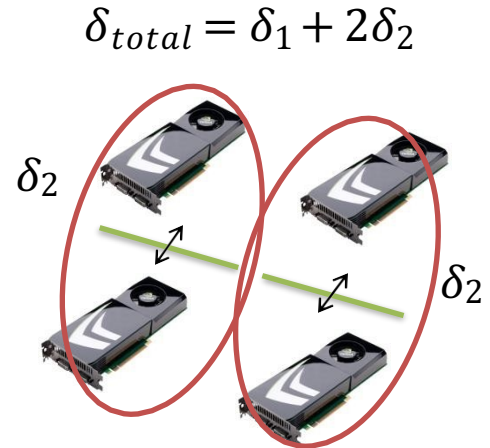
- Solve the problem recursively.
- Proved to be optimal.



Step 1: Partition to two groups



Step 2: Apply the algorithm again on one of the group

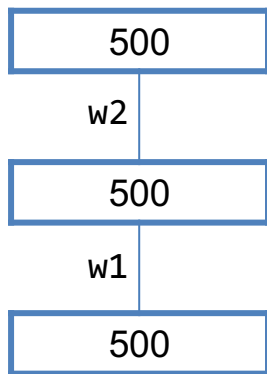


Step 3: Apply the same strategy to the other group due to symmetry.



# Which One is Better?

## ToyNet Configuration



nGPUs: 16

Batch size: 300

Parameter (gradients) size:

$$500 * 500 * 2 = 500K$$

Activation (gradients) size:

$$500 * 300 * 2 = 300K$$

- ✓ Data Parallelism
  - $500K * 2 * 4B * 16 = 64MB$
- ✓ Model Parallelism
  - $300K * 2 * 4B * 16 = 38.4MB$
- ✓ Hybrid Parallelism
  - 4 groups of GPUs, each group has 4 GPUs
  - Model Parallelism among groups
    - $300K * 2 * 4B * 4 = 9.6MB$
  - Data Parallelism within each group
    - $500K / 4 * 2 * 4B * 4 = 4MB$
  - $9.6MB + 4 * 4MB = 25.6MB$
  - **Save 33.3% communications!**

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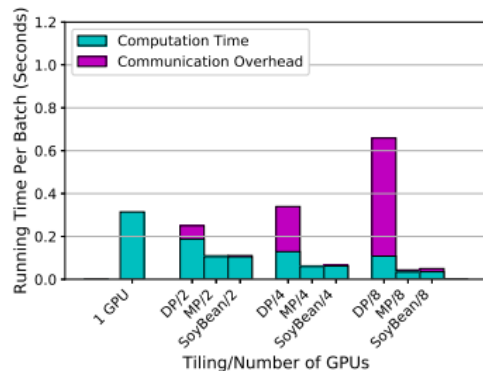
# Tofu Evaluation Setup

- Implemented in MXNet's NNVM dataflow optimization library.
- Multi-GPU evaluation
  - Amazon p2.8xlarge instance
  - 8 NVIDIA GK210 GPUs (4 K80)
  - 12GB memory per card
  - Connected by PCI-e (160Gbps bandwidth)

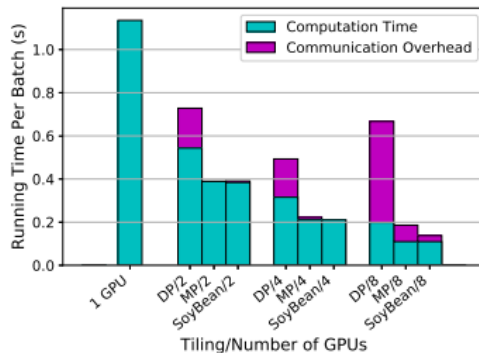
Under submission. Contact [wmjlyjemaine@gmail.com](mailto:wmjlyjemaine@gmail.com) for more details.

# Communication Overhead Evaluation

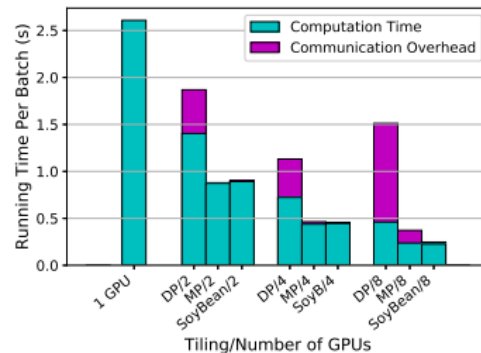
- Per batch running time of a 4-layer MLP for DP, MP and TOFU.
- Hidden layer size: 8K/12K; Batch size: 512/2K



(a) Batch size = 512; Hidden Size = 8K



(b) Batch size = 2K; Hidden Size = 8K

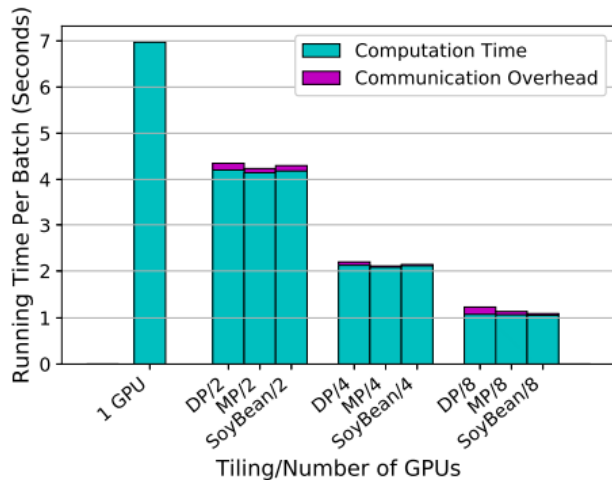


(c) Batch size = 2K; Hidden Size = 12K

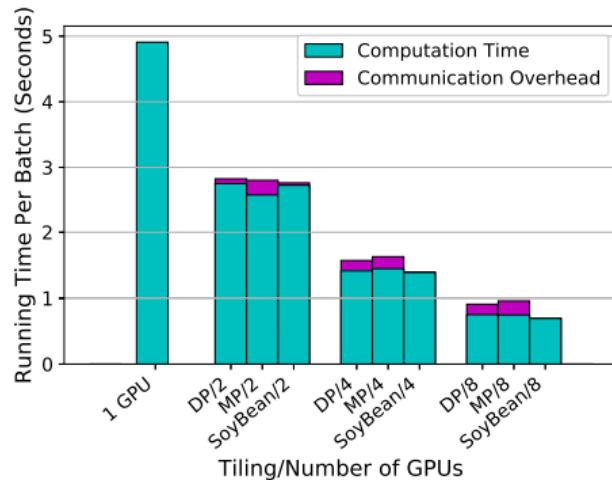
Figure 8: Runtime comparison of a 4-layer MLP for DP, MP, and SOYBEAN with different batch sizes and hidden sizes.

# Communication Overhead Evaluation

- Per batch running time of a 5-layer CNN for DP and TOFU.
- Filter size: 2048/512



(a) Image Size = 6x6, Filter Size = 2048

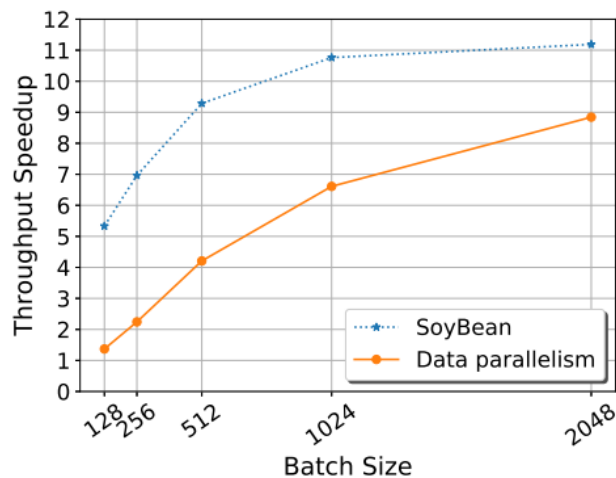


(b) Image Size = 24x24, Filter Size = 512

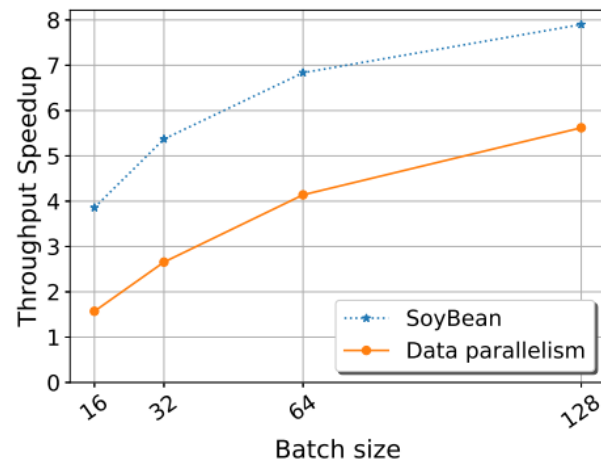
Figure 9: Runtime comparison of training a 5-layer convolutional neural network using DP, MP, and SOYBEAN. The batch size is 256.

# Real Deep Neural Networks Evaluation

- Experimental setup: 1 machine, 8 cards.
- Baseline: 1 card



(a) AlexNet throughput speedup.

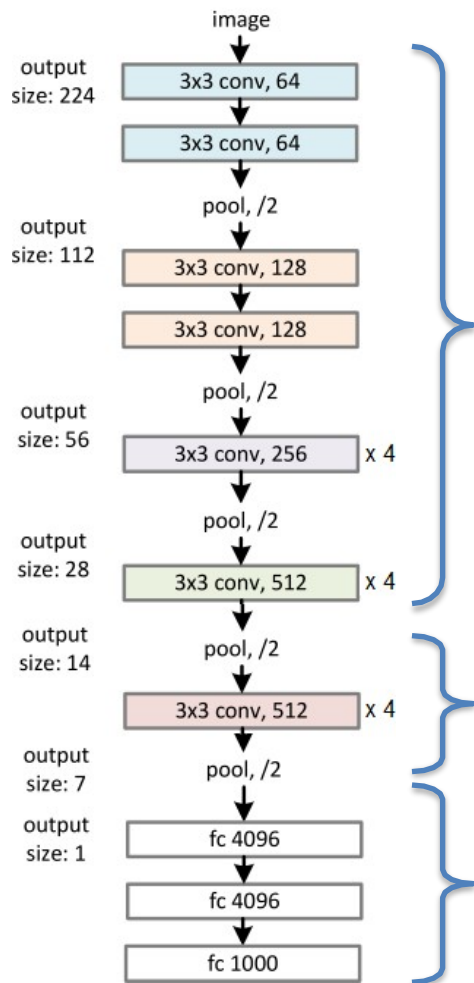


(b) VGG throughput speedup.

Figure 10: Throughput comparison of SOYBEAN and data parallelism on 8 GPUs.

Batch Size: 64

VGG-19



## Tofu's tiling for VGG-19 on 8 GPUs

### Data Parallelism

### Hybrid Parallelism

- 8 GPUs into 4 groups
- Data parallelism among groups
- Model parallelism within each group (tile on channel)

### Model Parallelism

- Tile on both row and column for weight matrices

# Recap

- Data parallelism suffers from *batch-size-dilemma*.
- Other parallelisms exist but are hard to program.
  - Model parallelism, hybrid parallelism, combined parallelism, etc.
- Tofu automatically parallelizes deep learning training
  - Figure out distributed strategies for each operator.
  - Combine strategies recursively.
  - Proved to have least communication cost.
- Implemented in TVM (we may use 😊)



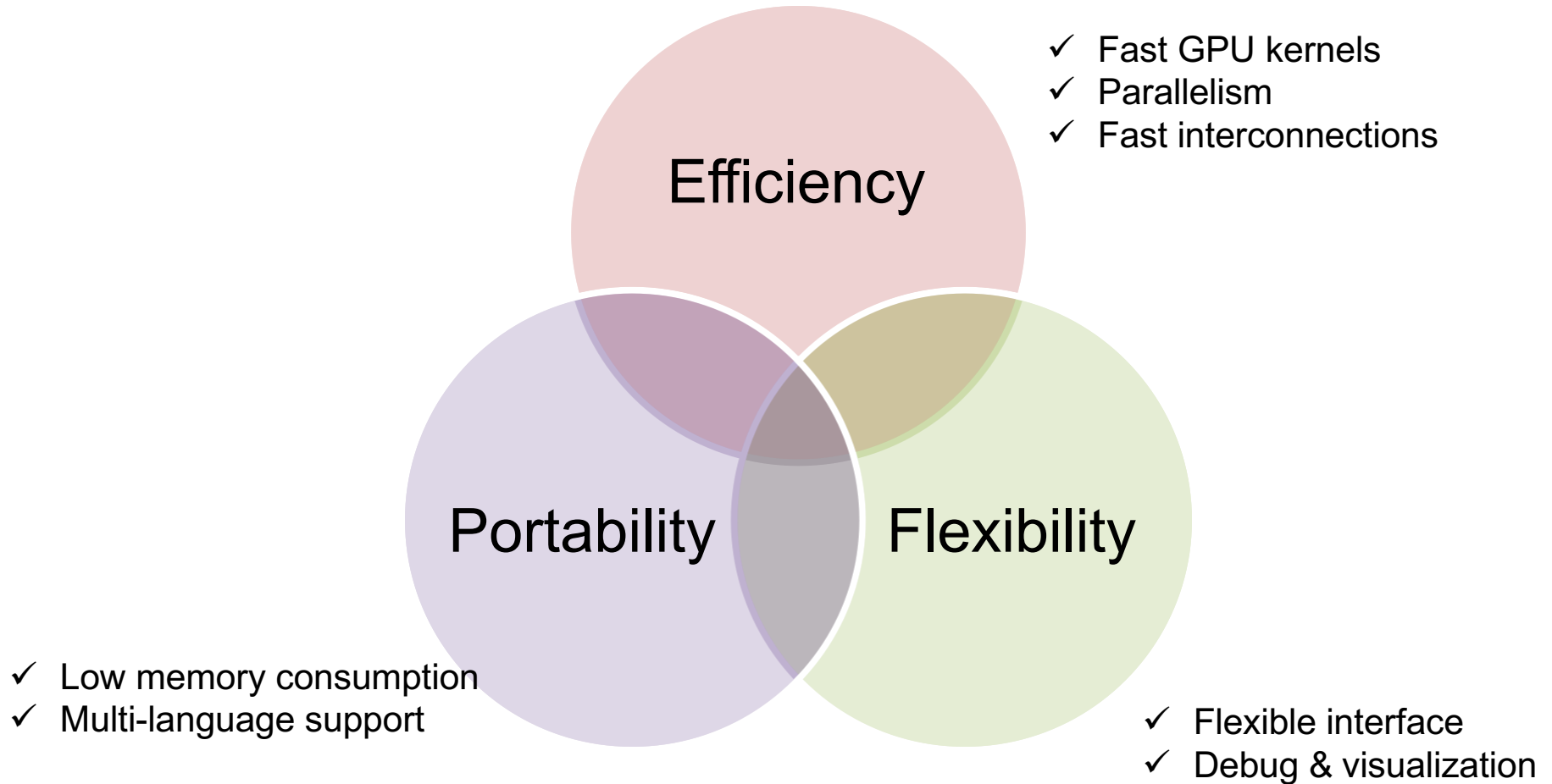
Q & A



# Single Card Different Tilings

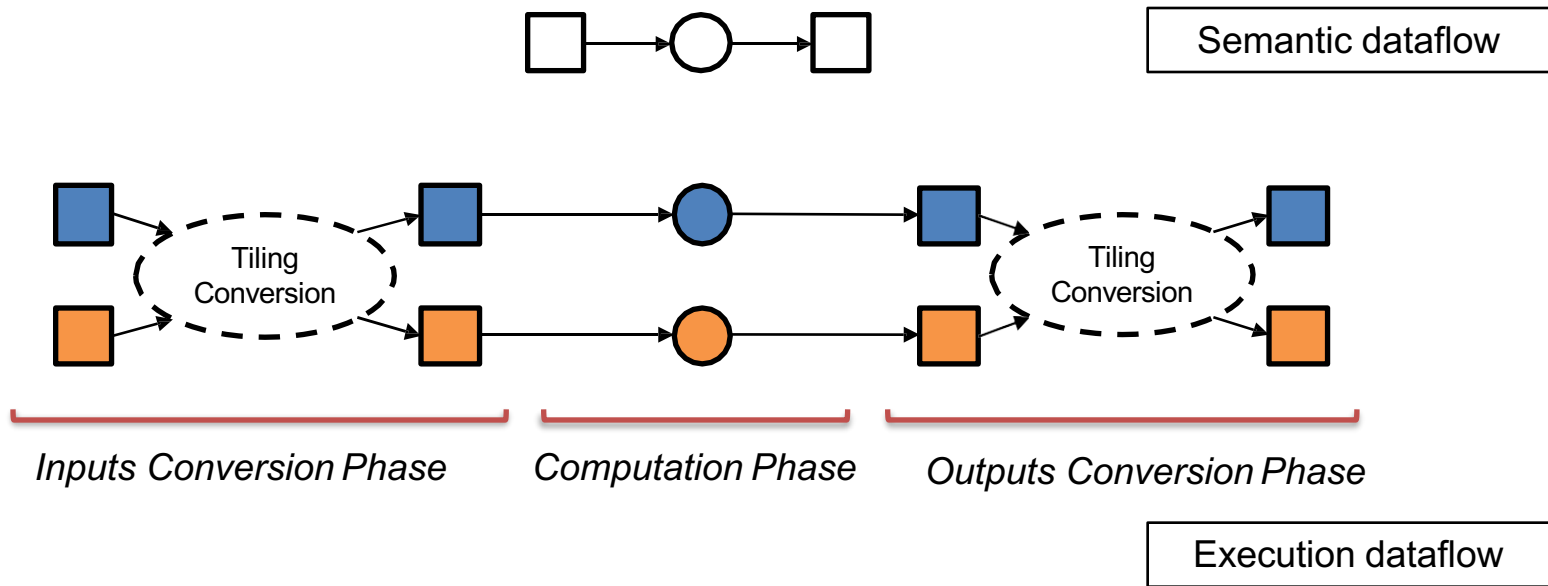
- Per batch running time for a 4-layers MLP network.
- Hidden layer size: 8192
- Partition dataflow to 8 workers but put them on the same GPU.

Batch Size	Single GPU	Single GPU w/ Tofu partitions
512	0.31s	0.19s
1024	0.56s	0.39s
2048	1.13s	0.73s



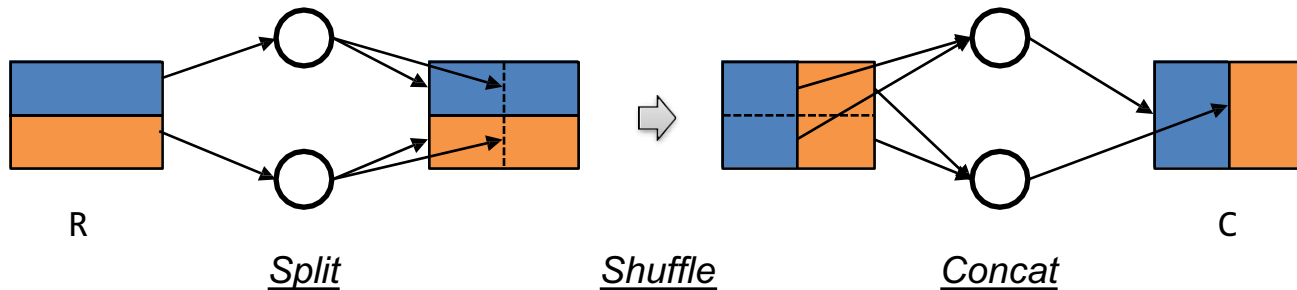
# Construct Parallel Execution Graph

- Three-phase computation



# Construct Parallel Execution Graph

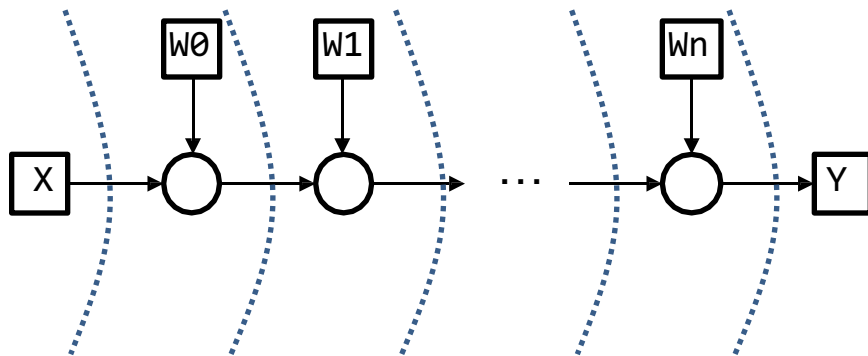
- Dataflow graph for tiling conversion.



# One-cut Tiling Algorithm

- Given a dataflow graph  $G$ , find  $\mathcal{T}_{min}: M_G \mapsto \{R, C, r\}$  such that the communication cost of *all* matrix multiplications are minimized.
- Case #1:

$$XW_0W_1 \dots W_n = Y$$

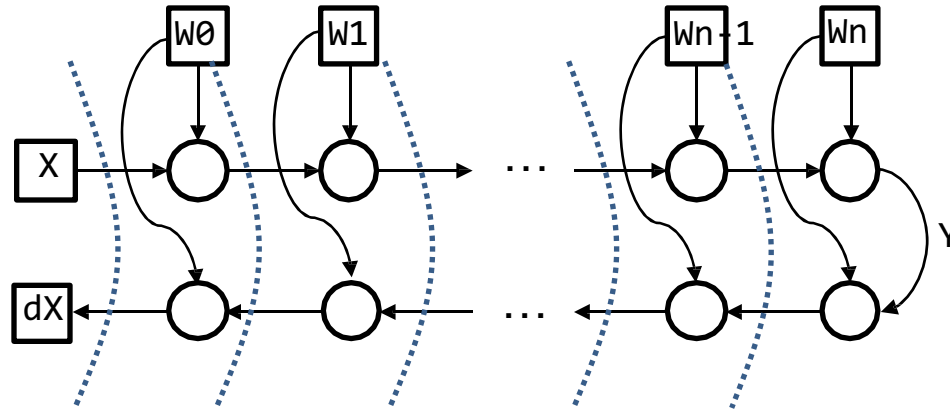


Dynamic Programming

# One-cut Tiling Algorithm

- Case #2:

$$XW_0W_1\dots W_n=Y$$
$$dX = Y \underset{n}{W^T} \underset{n-1}{W^T} \dots \underset{0}{W^T}$$



Dynamic Programming



# One-cut Tiling Algorithm

- Organize nodes in the dataflow graph into levels, such that for any node, **all** its neighbors are contained in the adjacent levels.
- BFS is one way to produce such levels.
- Dynamic Programming:

*Initial condition:*

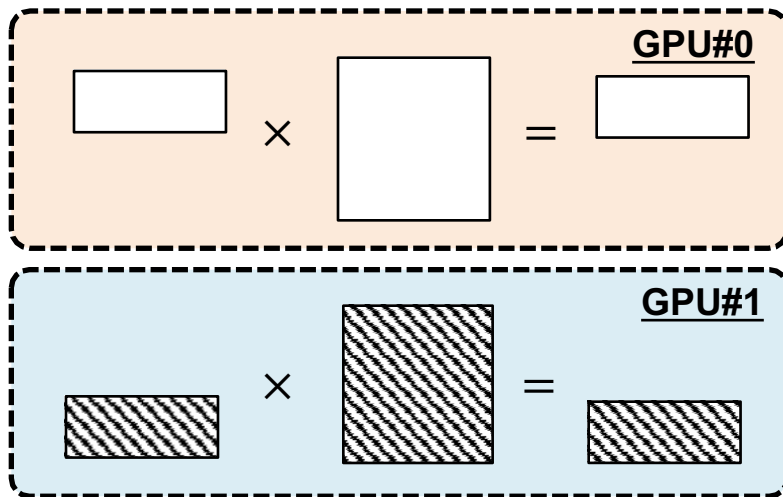
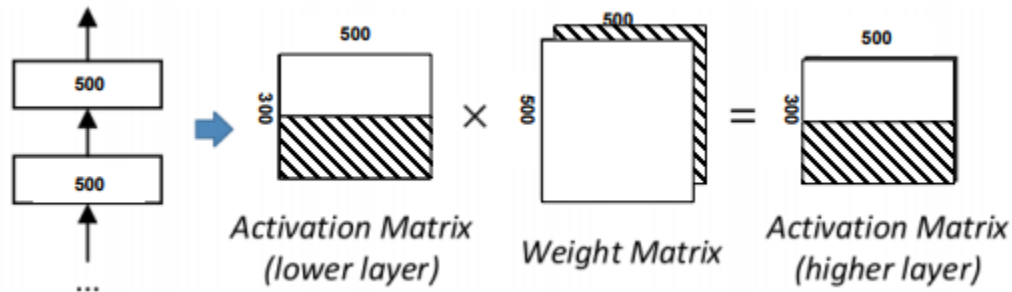
$$g_0(\tau_0) = \text{level\_cost}_0(\phi, \tau_0)$$

*DP equation ( $l \geq 1$ ):*

$$g_l(\tau_l) = \min_{\tau_{l-1}} \{ \text{level\_cost}_l(\tau_{l-1}, \tau_l) + g_{l-1}(\tau_{l-1}) \}$$

# Different ways of distributing matrix multiplication

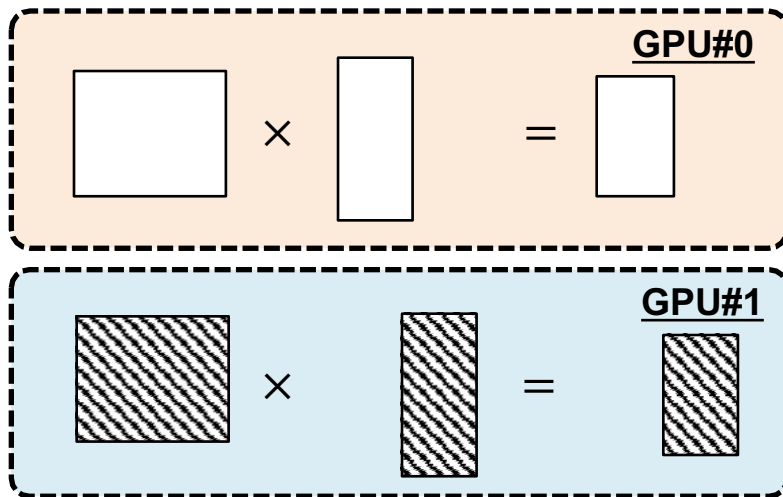
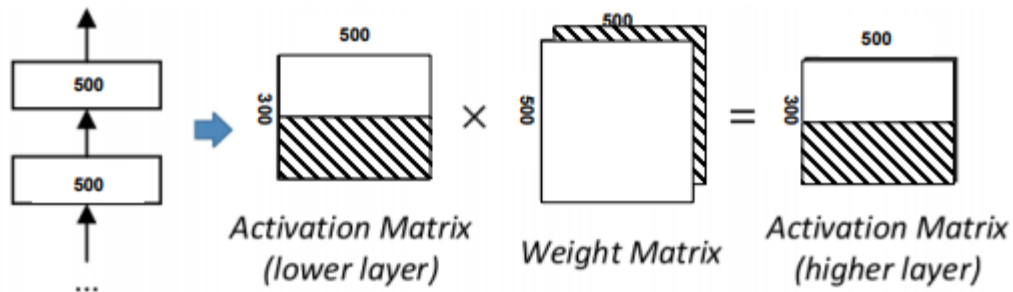
Batch size: 300



- Activation Matrix (lower layer) is **row-partitioned**
- Weight Matrix is **replicated**
- Activation Matrix (higher layer) is **row-partitioned**
- Data parallelism

# Different ways of distributing matrix multiplication

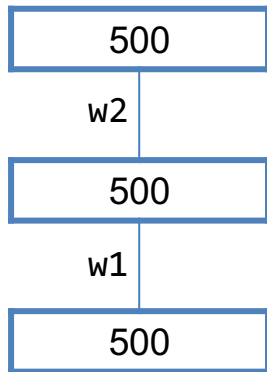
Batch size: 300



- Activation Matrix (lower layer) is **replicated**
- Weight Matrix is **column-partitioned**
- Activation Matrix (higher layer) is **column-partitioned**
- Model Parallelism

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- ✓ Model Parallelism
  - $300K * 2 * 4B * 16 = 38.4MB$
- ✓ Hybrid Parallelism?