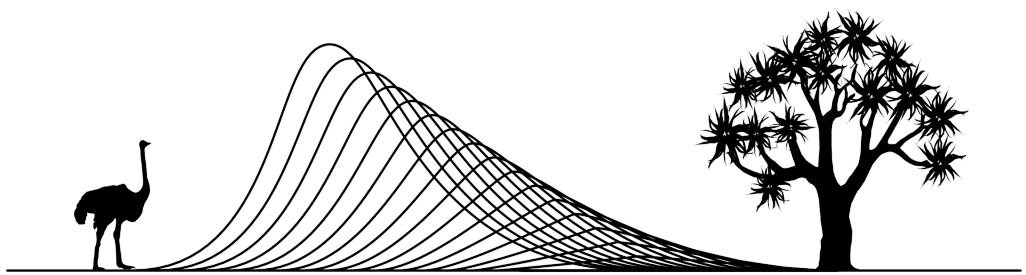
Ensemble methods: Bagging, boosting, random forests

Machine Learning for Ecology workshop

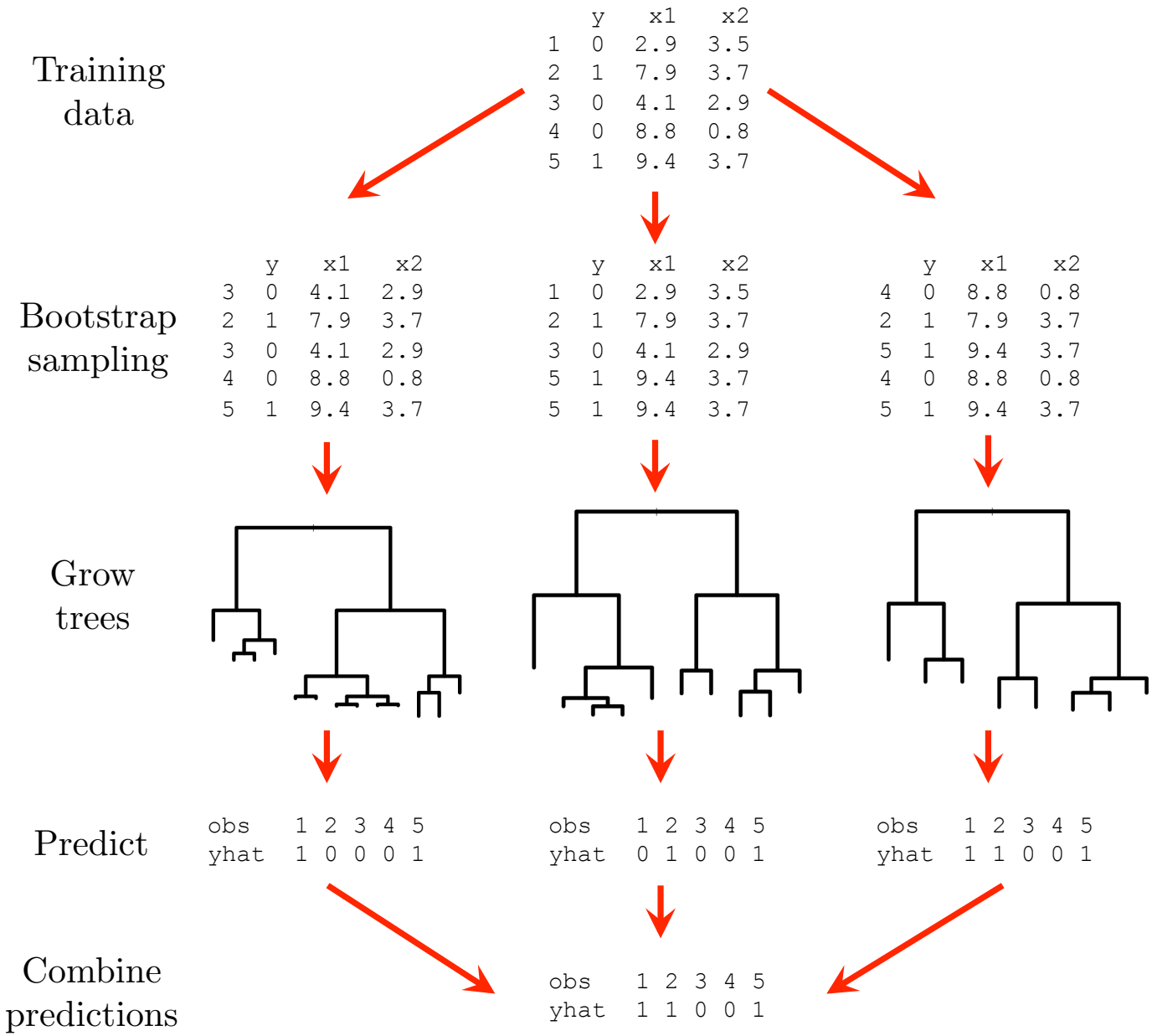


SEEC - Statistics in Ecology, Environment and Conservation

The Problem of High Variance

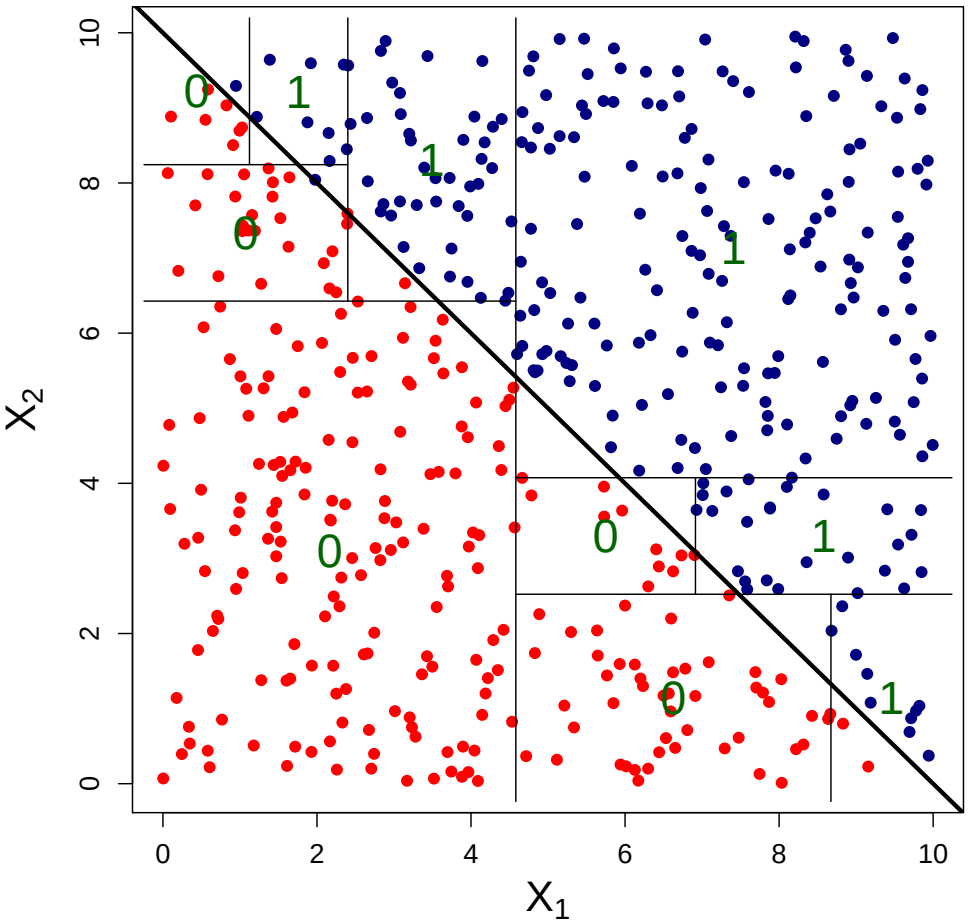
- Trees suffer from *high sampling variability*
- Small changes to sample $\Rightarrow$ Large changes in fitted tree
- Bootstrap aggregation or *bagging* is a general purpose procedure for variance reduction
- General idea: averaging reduces variance ($var(\bar{X}) = \sigma^2/n$)

Bagged regression trees

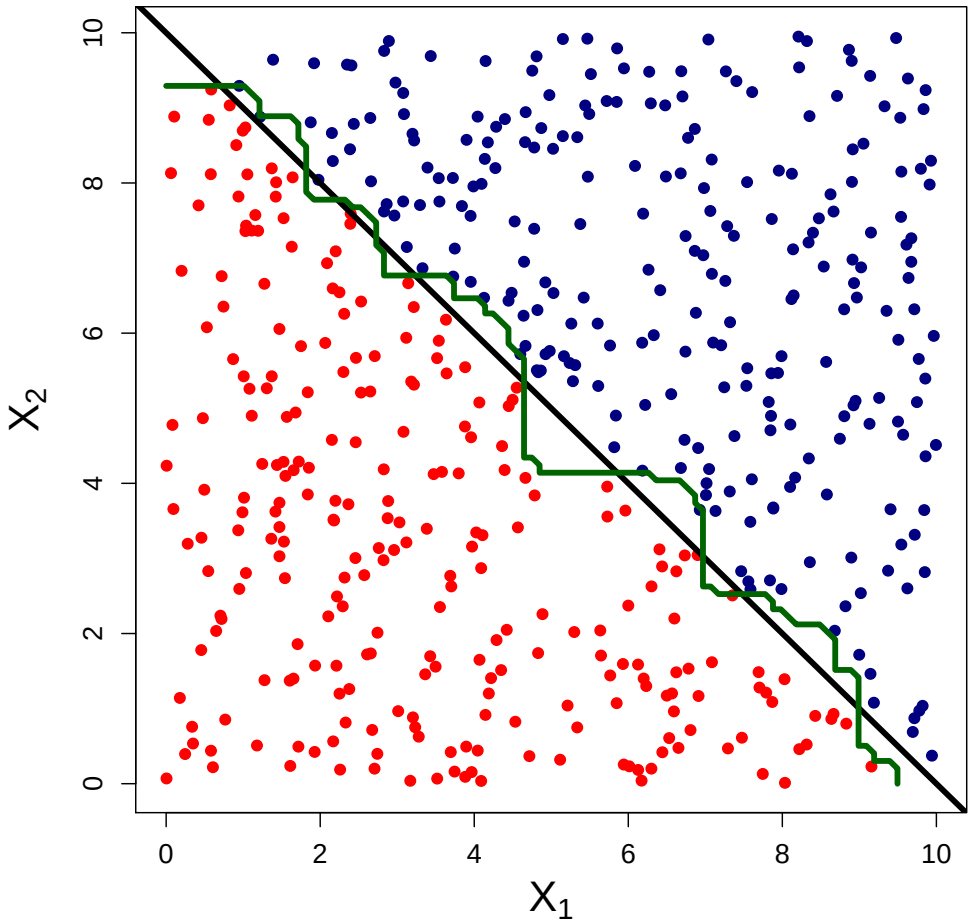


Why does bagging help?

Single Classification Tree

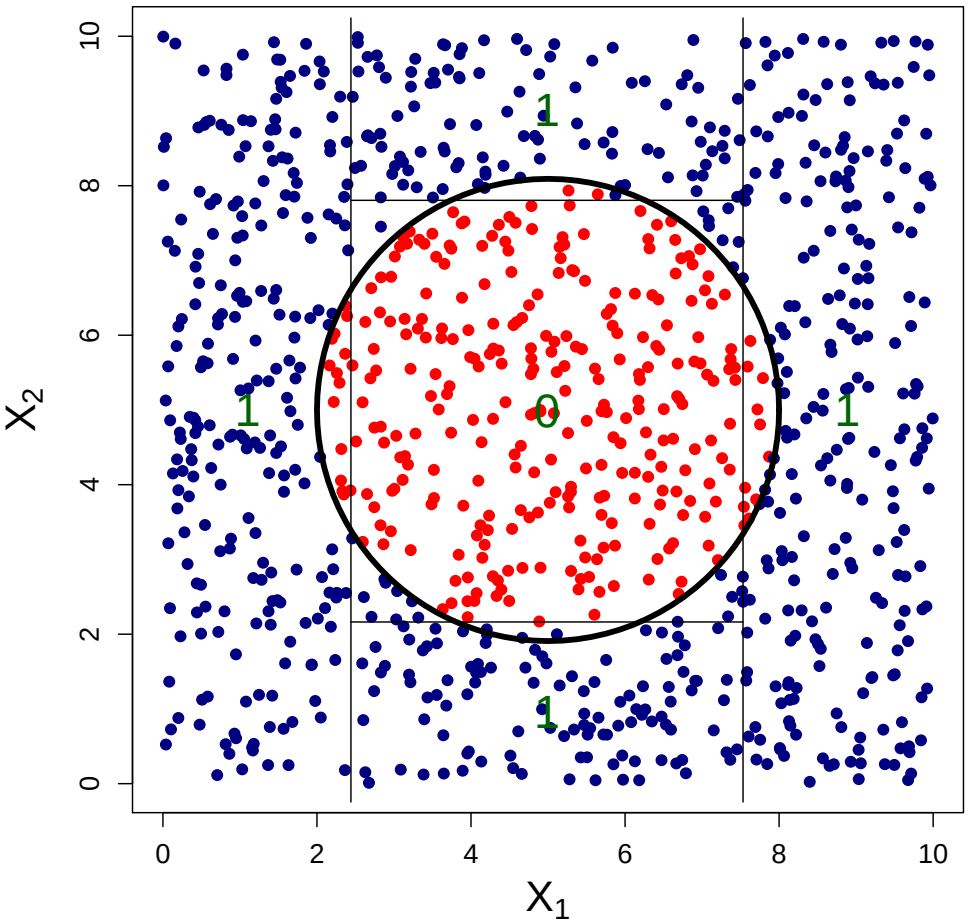


Bagging

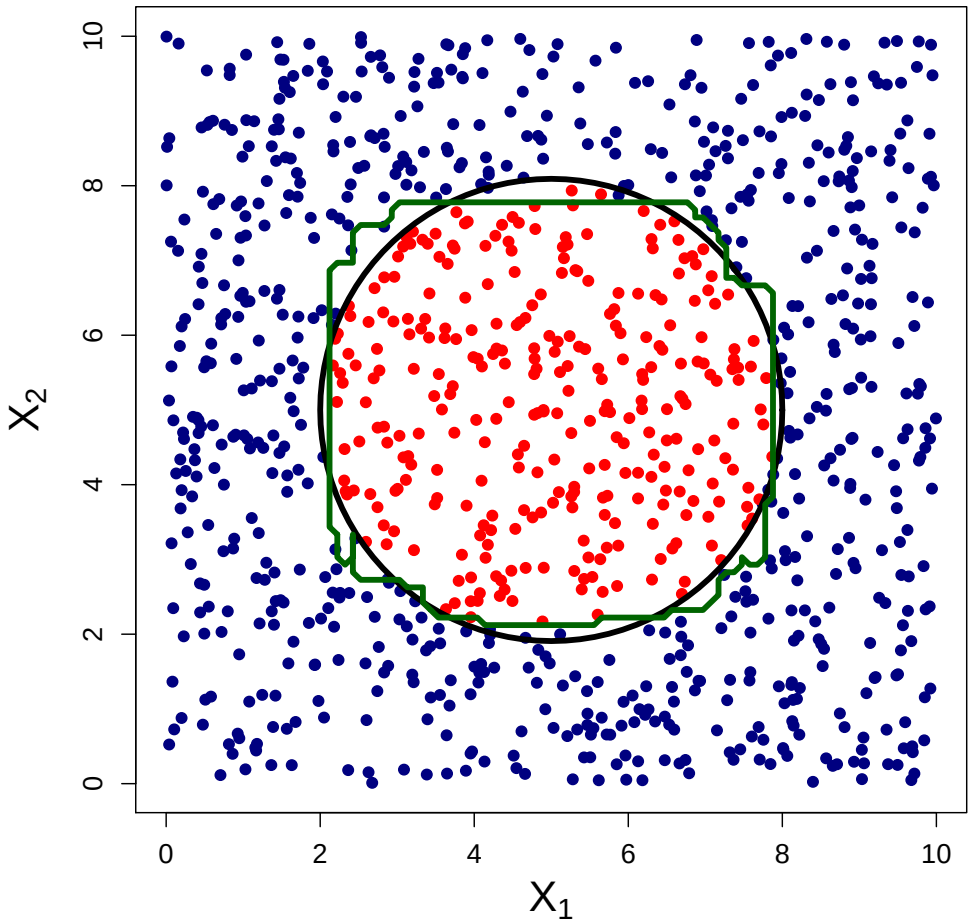


Why does bagging help?

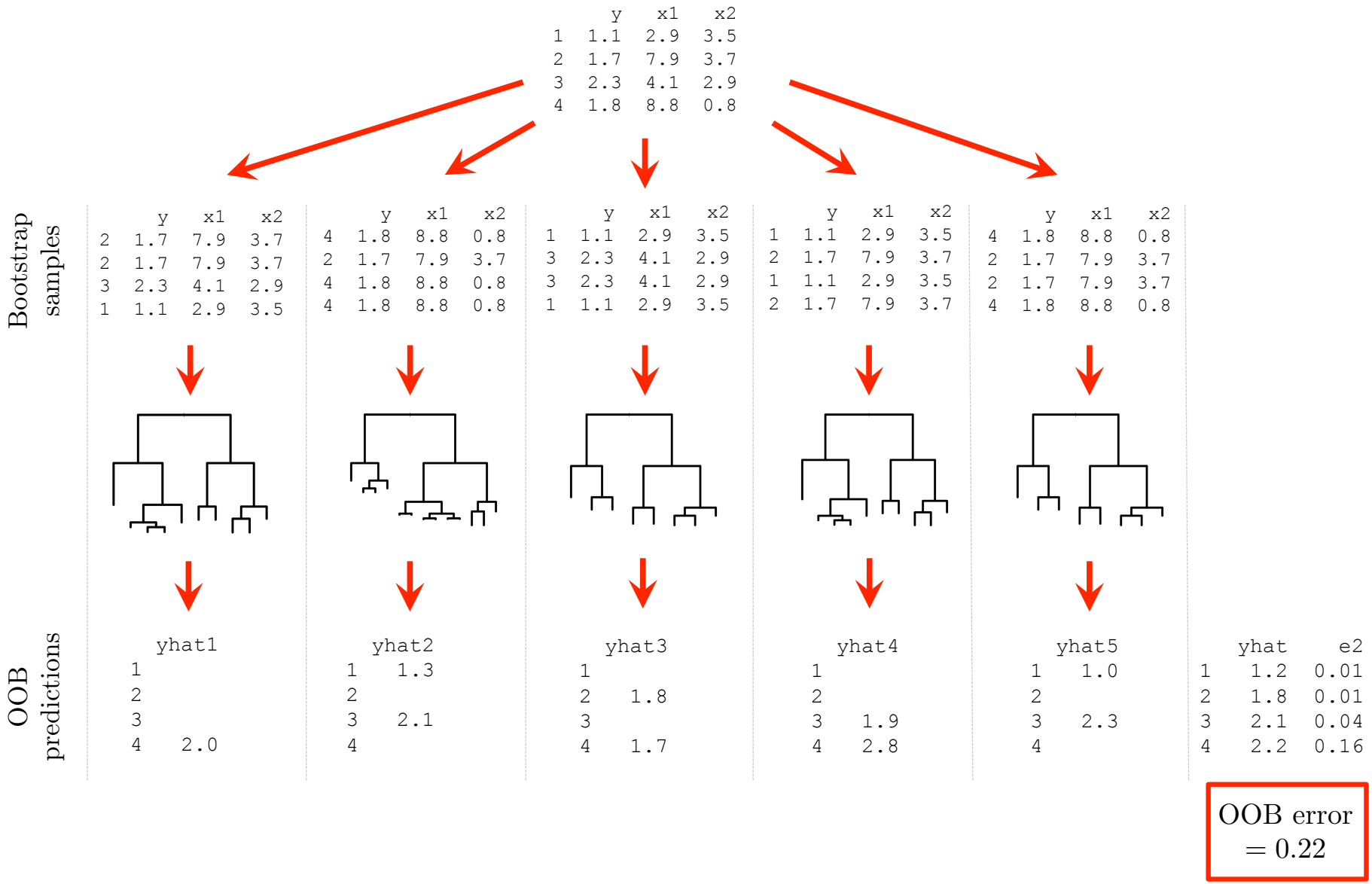
Single Classification Tree



Bagging

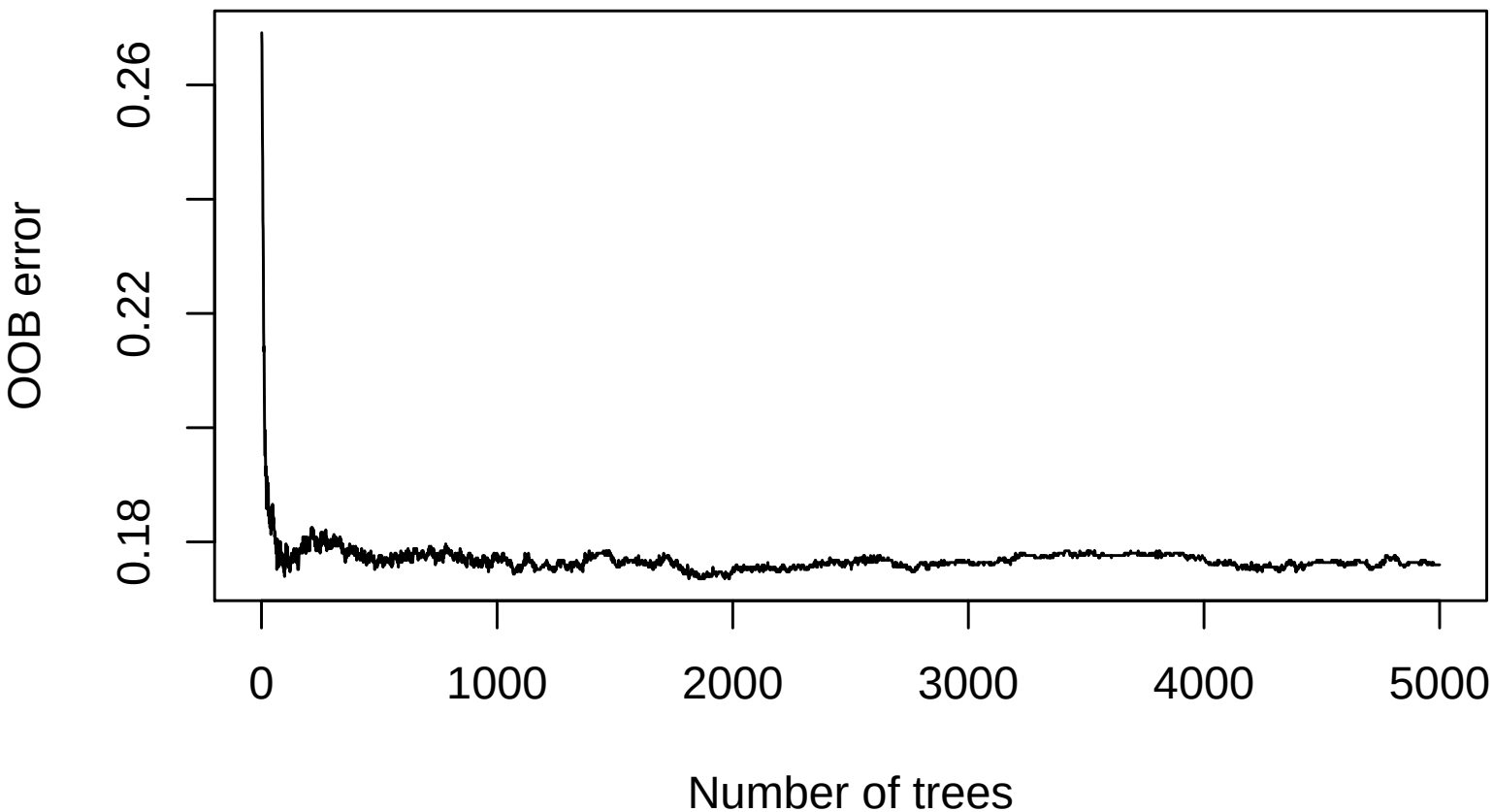


Cross-validation for bagging: Out-of-Bag Error



OOB error $= 0.22$

Out-of-Bag Error Estimation



Variable Importance

- The key advantage of a decision tree is ease of interpretation
- When we bag a large number of trees, it is no longer possible to represent the model with a single tree
- Variable importance: for each tree, record improvement in splitting criterion due to each predictor, and average over all trees
- More on this later

Random forests

- A small tweak that *decorrelates* the trees produced by bagging
- Each time a split is considered, *a random sample of* $m < p$ *predictors* are chosen as split candidates
- Bagging is a special case with $m = p$

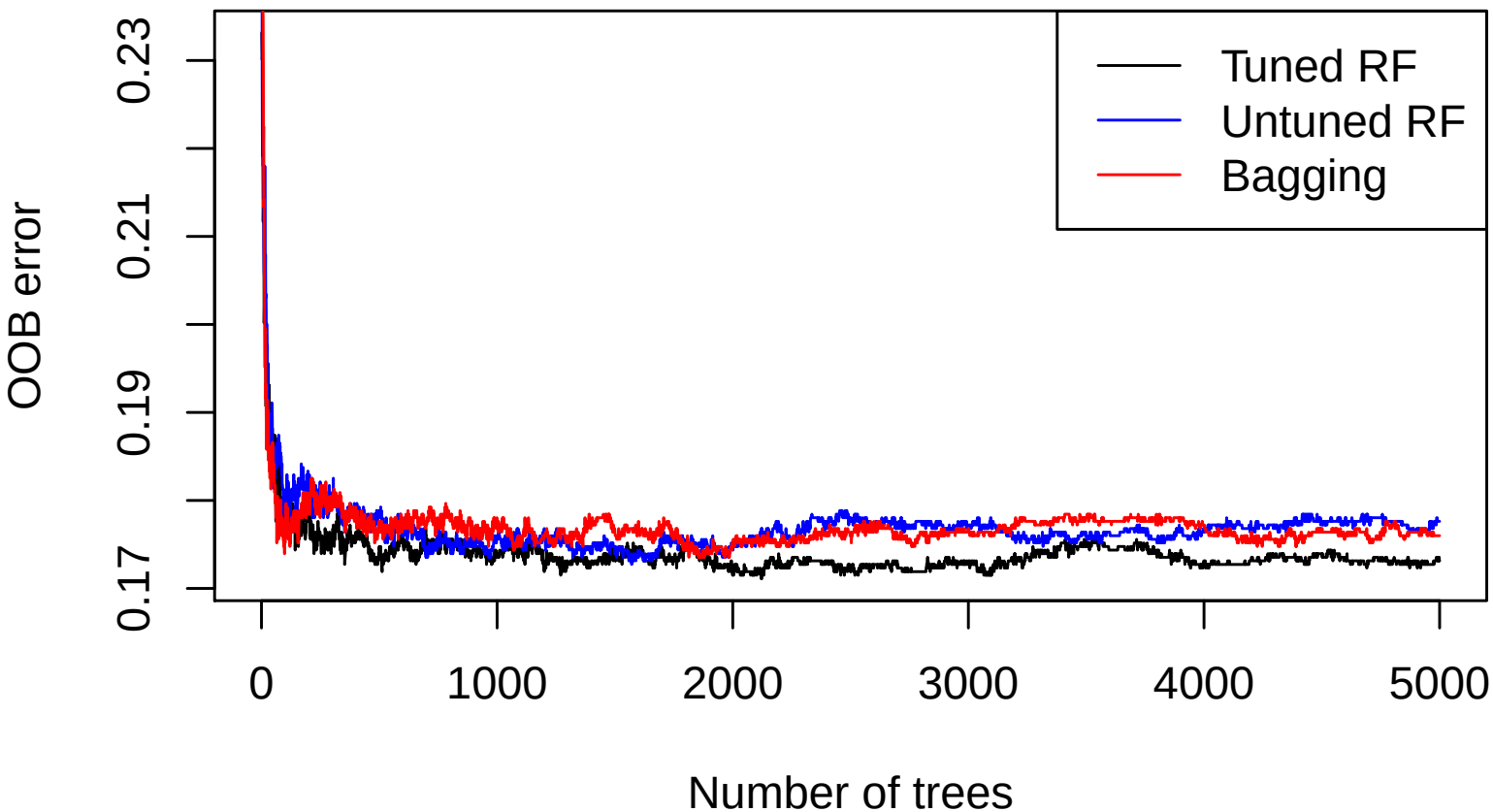
Why random forests work

- Bagging reduces the sampling variability of predictions by averaging over many trees
- Correlated trees are bad for variance reduction

$$\text{Var}[\bar{Z}] = \frac{\sigma^2}{n} + \frac{2\sigma^2}{n^2} \sum_{i \neq j} \rho_{ij}$$

- In practice bagged trees often are correlated (one strong predictor)
- Default is $m \approx \sqrt{p}$ for classification and $m \approx p/3$ for regression trees

Out-of-Bag Error Estimation



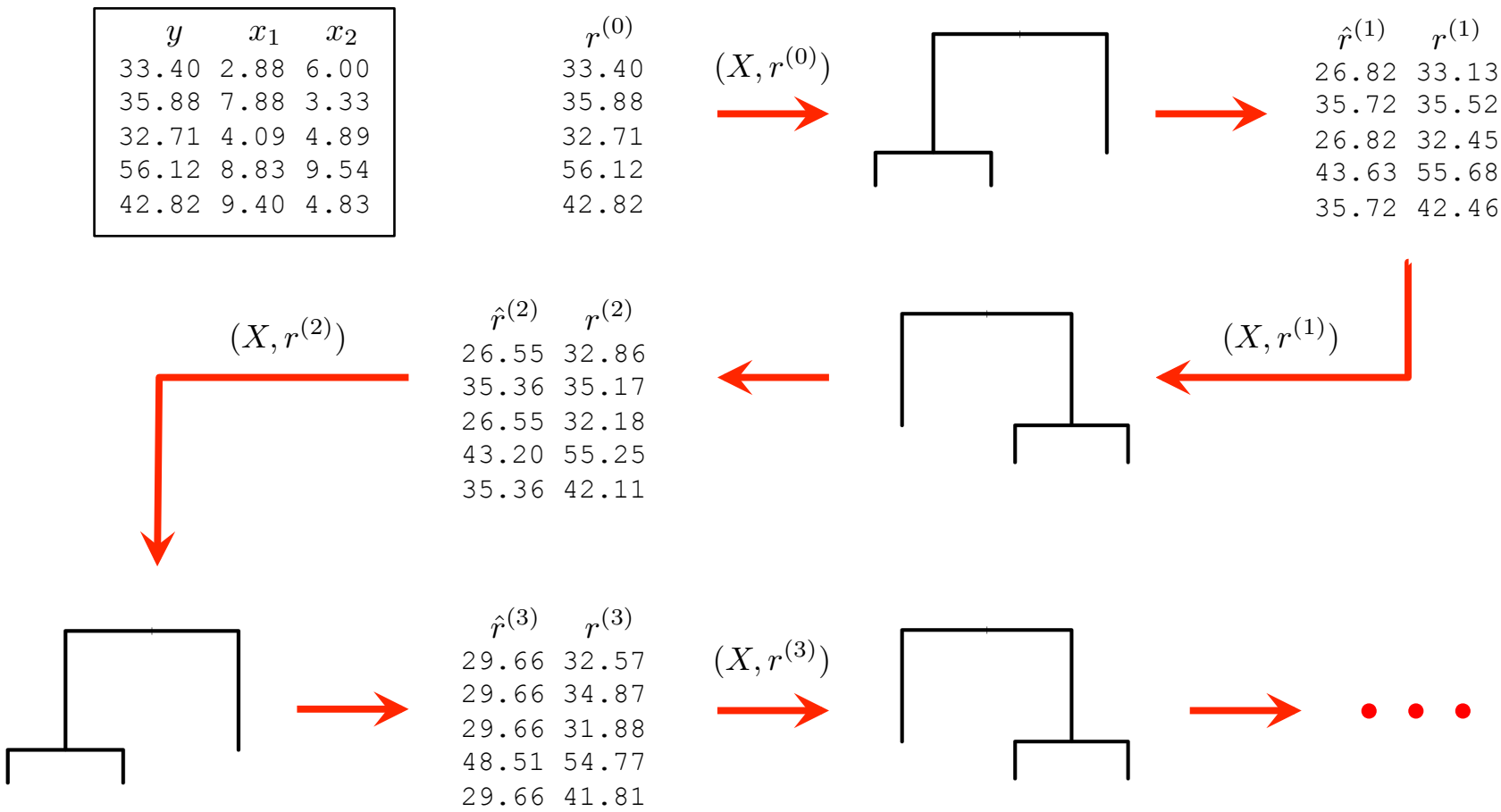
Boosting

- Bagging and RFs: each tree is grown independently of all other trees
- Boosting: grows trees *sequentially* using information from previously trees

Boosting

- First, grow a regression tree with a small number of splits, d
- The residuals of this tree are then treated as the response variable and used to grow another tree
- And so on...
- Yields a sequence of B trees, each accounting for some variation not explained by the previous trees

Boosting



Boosting algorithm with
$d = 2$ and $\lambda = 0.01$

$$\hat{y} = \lambda \sum_{b=1}^{B} \hat{r}^{(b)}$$

Why boosting works

- **Slow learning**: methods that learn slowly tend to perform well
- Small trees give slow improvement (small d)
- Slow learning by down-weighting contribution of each tree

$$\hat{y} = \lambda \sum_{b=1}^{B} \hat{r}^{(b)}$$

- Slow learning $\Rightarrow$ many trees

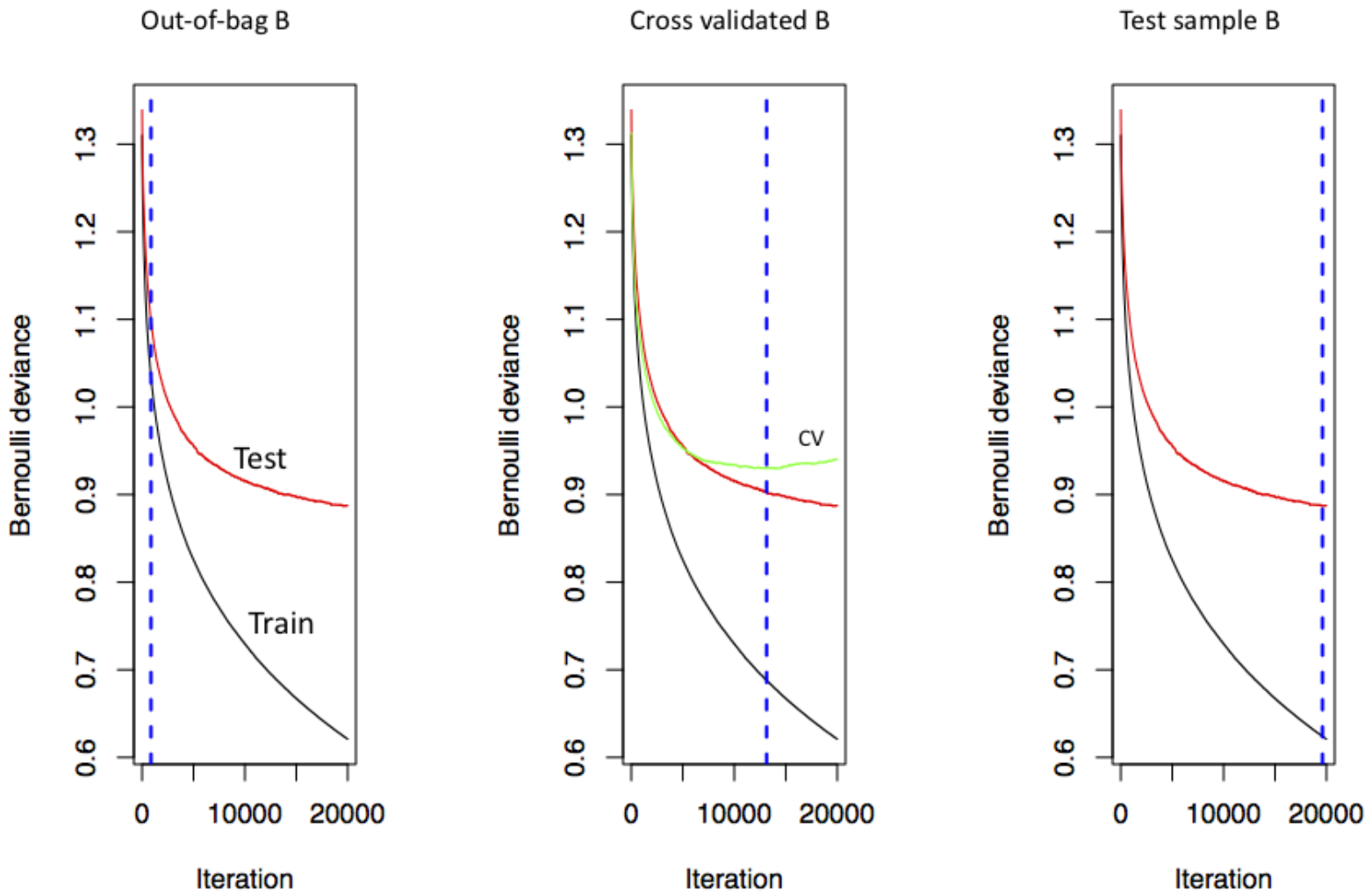
Tuning Parameters

1. The number of trees, B
   Unlike bagging and random forests, boosting can lead to overfitting if B is too large (why?). We use cross-validation to select B.

2. The shrinkage parameter or learning rate, λ
   Typical values are 0.01 or 0.001 (default in R package `gbm`). Smaller values require more trees.

3. Number of splits in each tree, d
   d is also called the *interaction depth* of the boosted model, since d splits can involve at most d variables. Often $d = 1$ works well.

Selecting number of trees B



Summary

- Bagging to reduce variance
- Random forests to reduce correlation (and hence variance)
- Boosting and the power of slow learning
- Out-of-bag but still need test sample if tuning

- **Next:** Variable importance and interpretation