

$$\text{In}[*]:= \text{lb1[q]} := \sigma[q] \text{Log}[\text{Exp}[\epsilon] - (1 - q)] / q - 1 / (2 \sigma[q])$$

$$\text{In}[*]:= \text{lb2[q]} := \sigma[q] \text{Log}[\text{Exp}[\epsilon] - (1 - q)] / q + 1 / (2 \sigma[q])$$

$$\text{In}[*]:= \text{delta[q]} := q (1 - \text{CDF}[\text{NormalDistribution}[0, 1], \text{lb1[q]}]) + (1 - q - \text{Exp}[\epsilon]) (1 - \text{CDF}[\text{NormalDistribution}[0, 1], \text{lb2[q]}])$$

$$\text{In}[*]:= \text{D}[\text{delta[q]}, \{q, 1\}]$$

$$\begin{aligned} \text{Out}[*]= & \frac{1}{2} \text{Erfc}\left[\frac{-\frac{1}{2\sigma[q]} - \text{Log}\left[\frac{-1+\text{Exp}[\epsilon]+q}{q}\right]\sigma[q]}{\sqrt{2}}\right] - \frac{1}{2} \text{Erfc}\left[\frac{\frac{1}{2\sigma[q]} - \text{Log}\left[\frac{-1+\text{Exp}[\epsilon]+q}{q}\right]\sigma[q]}{\sqrt{2}}\right] + \\ & \frac{e^{-\frac{1}{2}\left(-\frac{1}{2\sigma[q]} - \text{Log}\left[\frac{-1+\text{Exp}[\epsilon]+q}{q}\right]\sigma[q]\right)^2} q \left(-\frac{q\left(\frac{1}{q} - \frac{-1+\text{Exp}[\epsilon]+q}{q^2}\right)\sigma[q]}{-1+\text{Exp}[\epsilon]+q} - \text{Log}\left[\frac{-1+\text{Exp}[\epsilon]+q}{q}\right]\sigma'[q] - \frac{\sigma'[q]}{2\sigma[q]^2}\right)}{\sqrt{2\pi}} + \\ & \frac{e^{-\frac{1}{2}\left(-\frac{1}{2\sigma[q]} - \text{Log}\left[\frac{-1+\text{Exp}[\epsilon]+q}{q}\right]\sigma[q]\right)^2} (1 - e^\epsilon - q) \left(-\frac{q\left(\frac{1}{q} - \frac{-1+\text{Exp}[\epsilon]+q}{q^2}\right)\sigma[q]}{-1+\text{Exp}[\epsilon]+q} - \text{Log}\left[\frac{-1+\text{Exp}[\epsilon]+q}{q}\right]\sigma'[q] + \frac{\sigma'[q]}{2\sigma[q]^2}\right)}{\sqrt{2\pi}} \end{aligned}$$

$$\text{In}[*]:= \text{Simplify}[\%4]$$

$$\text{Out}[*]= \frac{1}{2} \left(-\text{Erfc}\left[\frac{1 - 2 \text{Log}\left[\frac{-1+\text{Exp}[\epsilon]+q}{q}\right]\sigma[q]^2}{2\sqrt{2}\sigma[q]}\right] + \text{Erfc}\left[-\frac{1 + 2 \text{Log}\left[\frac{-1+\text{Exp}[\epsilon]+q}{q}\right]\sigma[q]^2}{2\sqrt{2}\sigma[q]}\right] - \frac{e^{-\frac{1+4 \text{Log}\left[\frac{-1+\text{Exp}[\epsilon]+q}{q}\right]^2\sigma[q]^4}{8\sigma[q]^2}} \sqrt{\frac{2}{\pi}} q \sqrt{\frac{-1+\text{Exp}[\epsilon]+q}{q}} \sigma'[q]}{\sigma[q]^2} \right)$$

$$\text{In}[*]:= \text{Solve}[\%5 == 0, \sigma'[q]]$$

$$\text{Out}[*]= \left\{ \left\{ \sigma'[q] \rightarrow -\frac{e^{\frac{1}{8\sigma[q]^2} + \frac{1}{2} \text{Log}\left[\frac{-1+\text{Exp}[\epsilon]+q}{q}\right]^2\sigma[q]^2} \sqrt{\frac{\pi}{2}} \left(\text{Erfc}\left[\frac{1-2 \text{Log}\left[\frac{-1+\text{Exp}[\epsilon]+q}{q}\right]\sigma[q]^2}{2\sqrt{2}\sigma[q]}\right] - \text{Erfc}\left[-\frac{1+2 \text{Log}\left[\frac{-1+\text{Exp}[\epsilon]+q}{q}\right]\sigma[q]^2}{2\sqrt{2}\sigma[q]}\right] \right) \sigma[q]^2}{q \sqrt{\frac{-1+\text{Exp}[\epsilon]+q}{q}}} \right\} \right\}$$