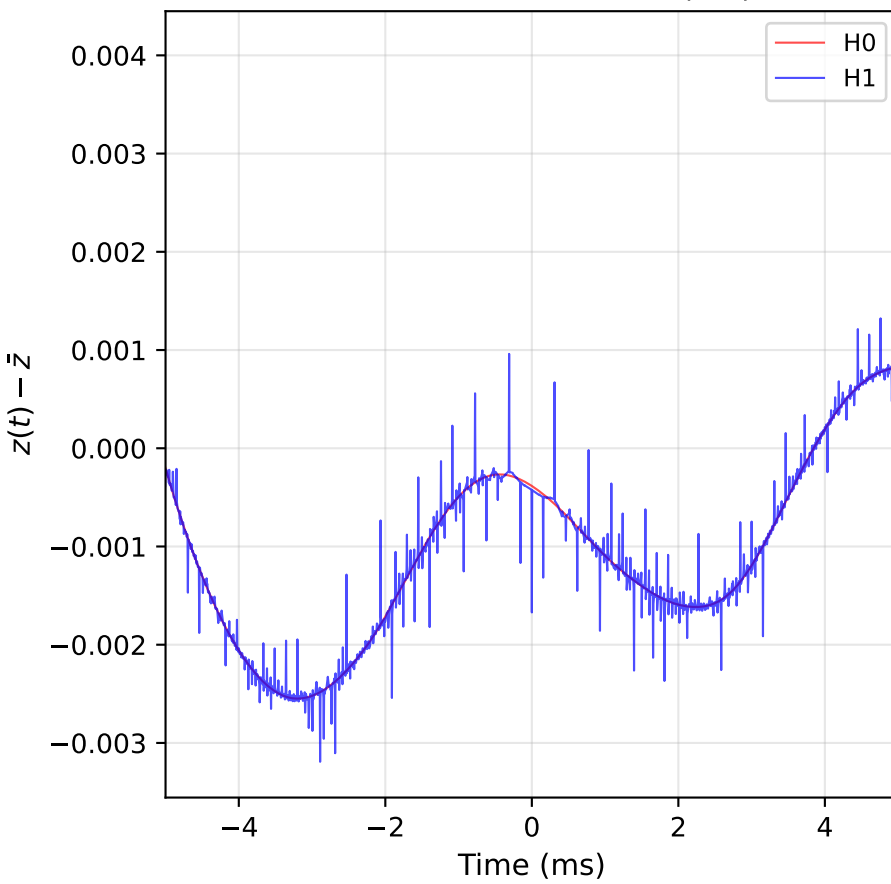
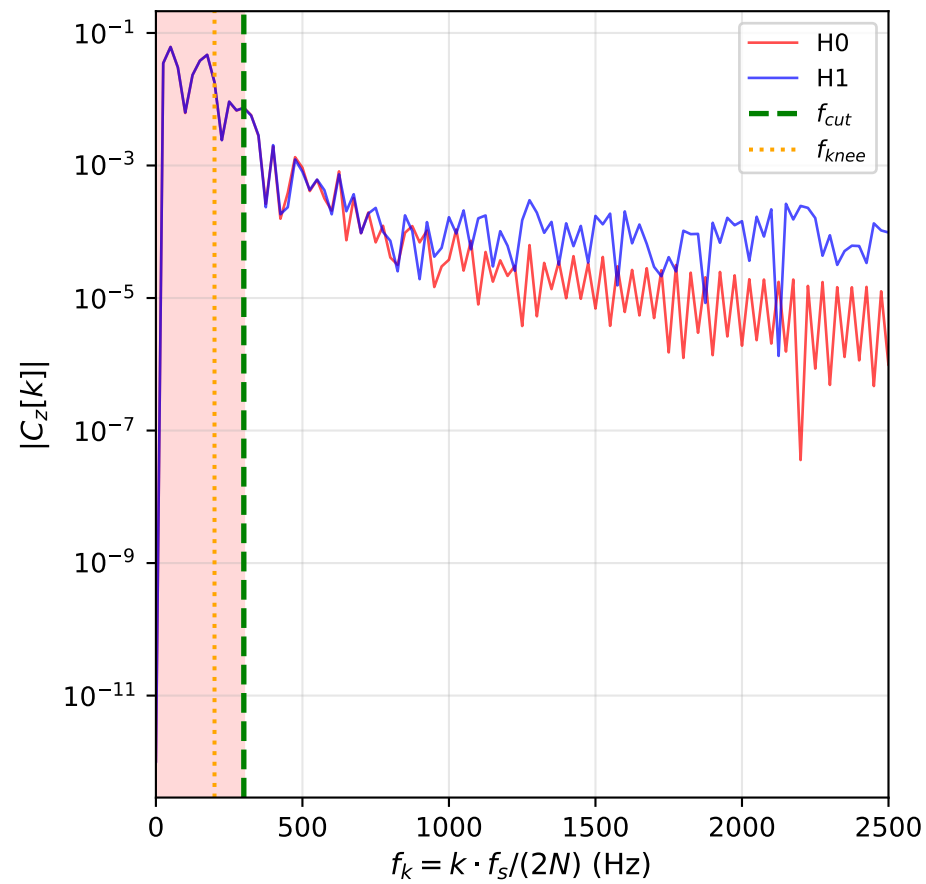
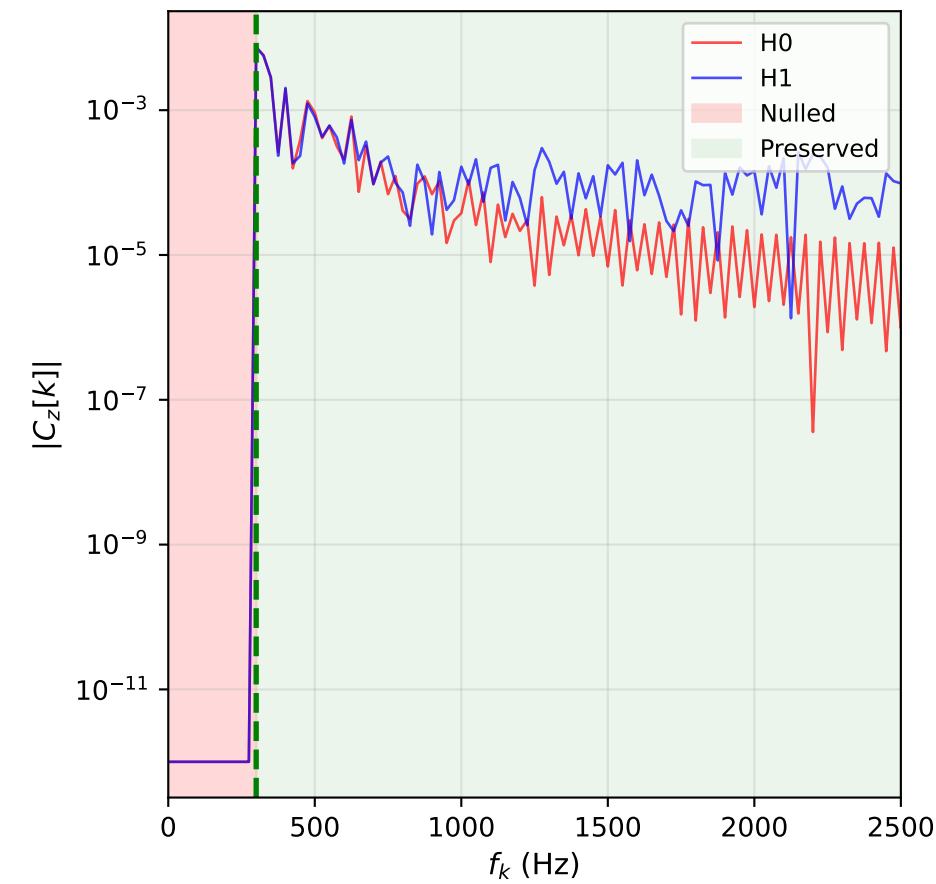
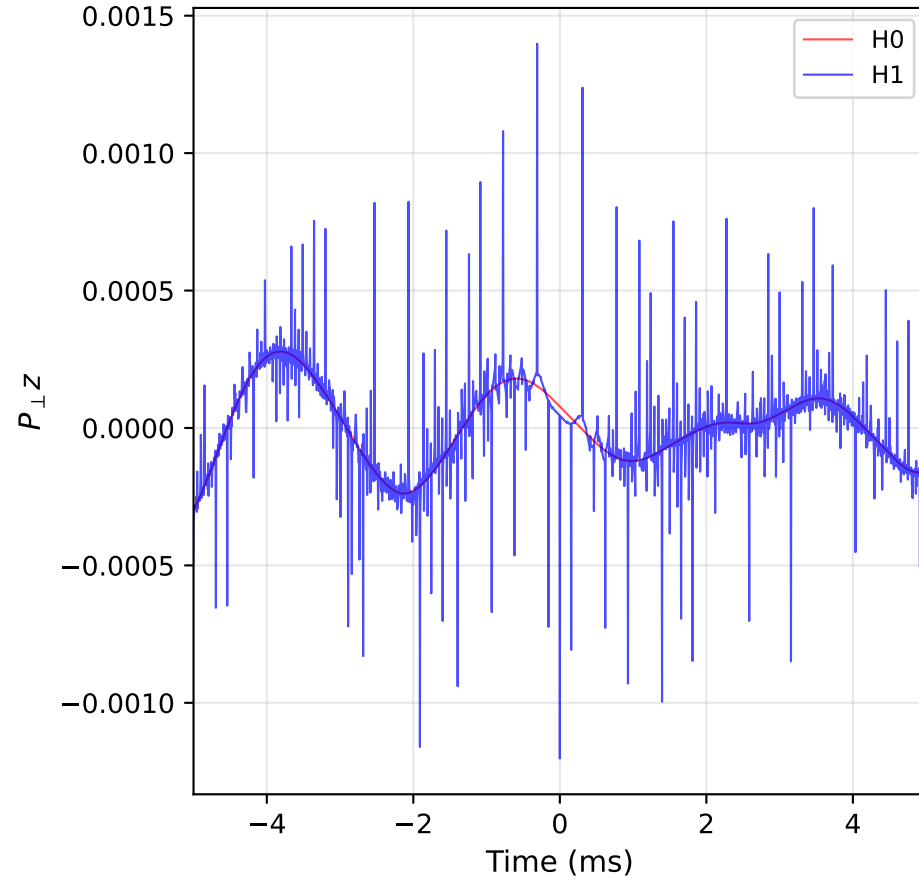
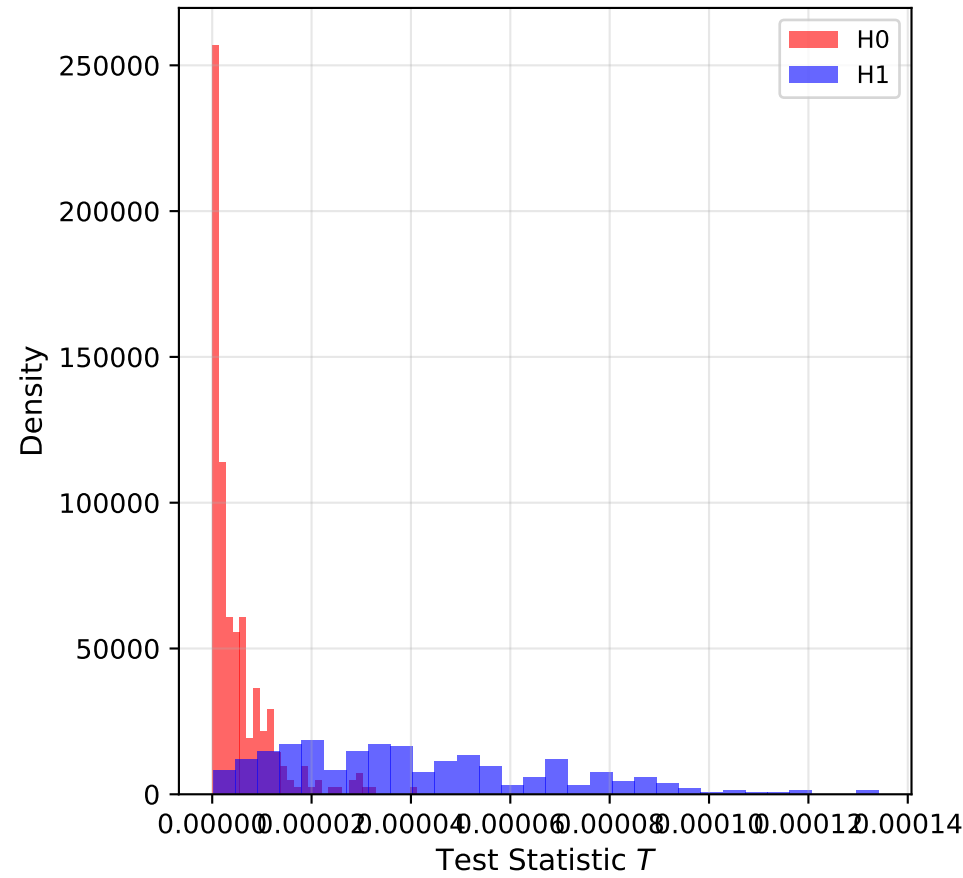


(a) Log-Envelope  $z(t) = \ln|r(t)|$ (b) DCT Before  $P_{\perp}$ (c) DCT After  $P_{\perp}$ 

(d) After Projection



(e) Detection (AUC=0.940, SNR=50dB)



(f) Design Summary

**SURVIVAL SPACE DESIGN (FINAL)**

**Physical Parameters:**

- Fresnel radius:  $r_F = 4.47$  m
- Crossing time:  $T_{\text{cross}} = 0.60$  ms
- Signal bandwidth:  $f_{\text{max}} = 1677$  Hz

**Projection Operator  $P_{\perp}$ :**

- Nulls DCT coefficients for  $f < f_{\text{cut}}$
- Frequency mapping:  $f_k = k \cdot f_s / (2N)$
- Preserved subspace:  $[f_{\text{cut}}, f_s/2]$

**Design Choice:  $f_{\text{cut}} = 300$  Hz**

- Condition:  $f_{\text{knee}} < f_{\text{cut}} \ll f_{\text{max}}$
- $f_{\text{cut}}/f_{\text{knee}} = 1.5$  (noise margin)
- $f_{\text{cut}}/f_{\text{max}} = 0.18$  (signal margin)

**Key Metrics ( $f_{\text{cut}} = 300$  Hz):**

- Signal retention:  $\eta_z > 99\%$
- Noise removed:  $\rho = 99.1\%$
- Detection AUC = 0.940 (SNR=50dB)

**Working Range:**

$f_{\text{knee}} < f_{\text{max}}/3 = 559$  Hz