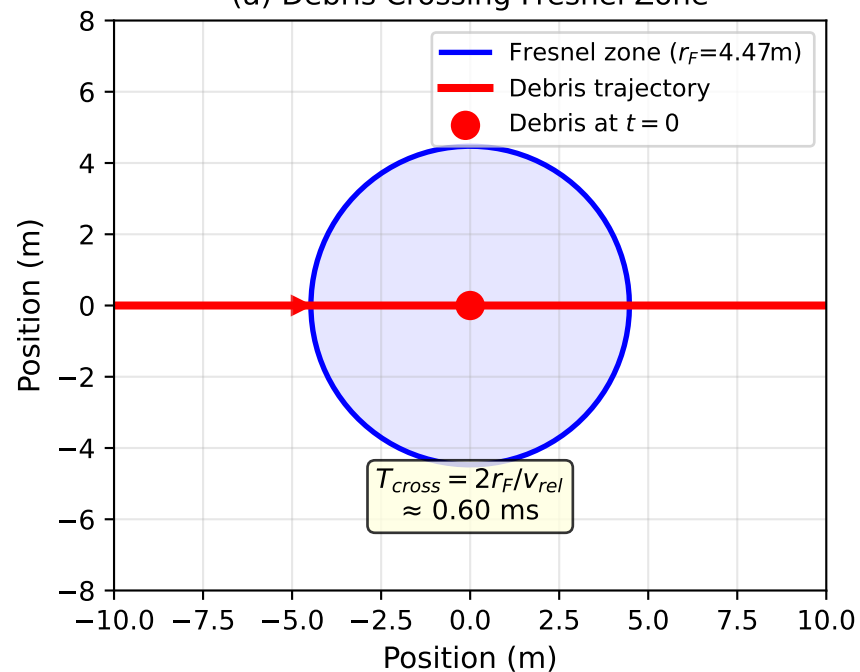
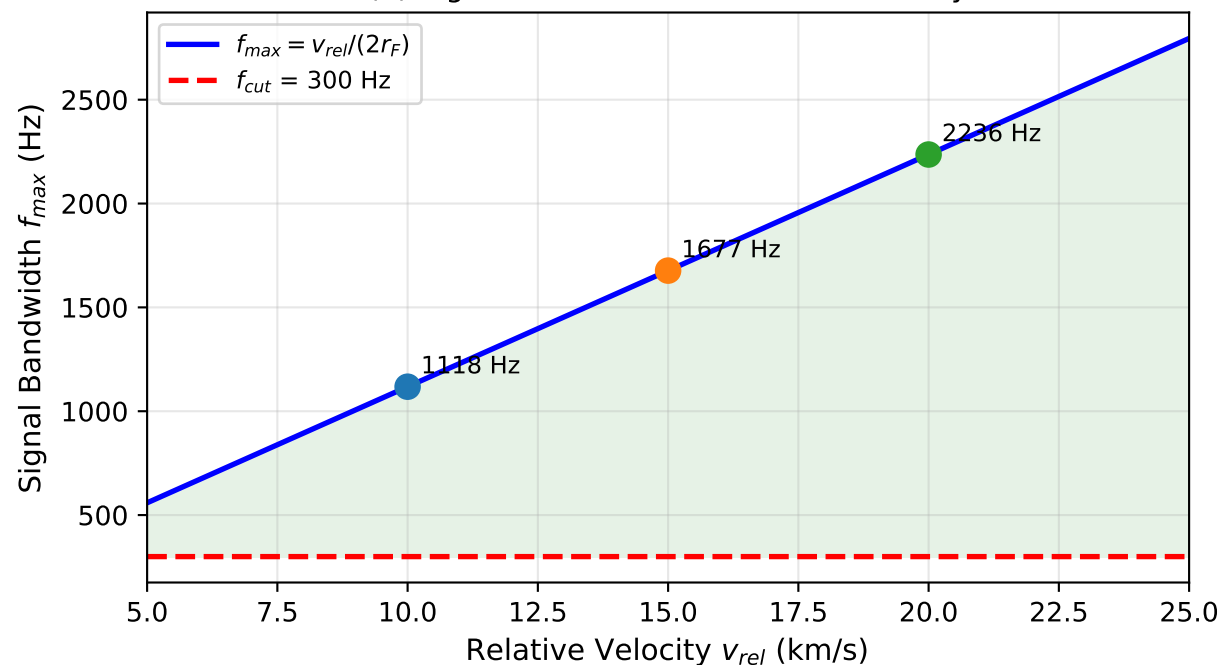


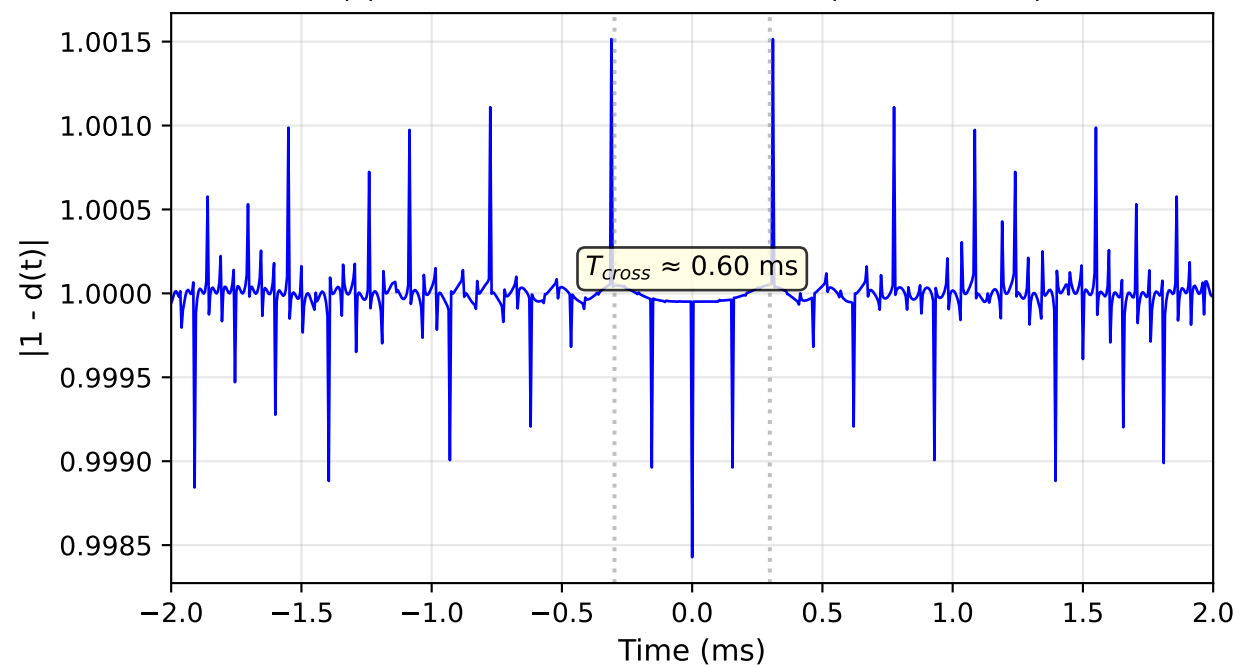
(a) Debris Crossing Fresnel Zone



(b) Signal Bandwidth vs Relative Velocity



(c) Debris Diffraction Modulation (Time Domain)



(d) Theoretical Derivation Summary

SIGNAL BANDWIDTH DERIVATION

{ '-'*40 }

1. Fresnel Zone Radius

$$r_F = \sqrt{\lambda \cdot L_{eff}}$$

For $\lambda = 1\text{ mm}$, $L_{eff} = 20\text{ km}$:

$$r_F = \sqrt{(10^{-3} \times 2 \times 10^4)} = 4.47\text{ m}$$

2. Fresnel Crossing Time

$$T_{cross} = \frac{2r_F}{v_{rel}}$$

For $v_{rel} = 15\text{ km/s}$:

$$T_{cross} = 8.94 / 15000 \approx 0.60\text{ ms}$$

3. Signal Bandwidth Upper Bound

$$f_{max} \approx \frac{1}{T_{cross}} = \frac{v_{rel}}{2r_F}$$

For $v_{rel} = 15\text{ km/s}$:

$$f_{max} \approx 1677\text{ Hz} \quad (\text{NOT } 5\text{ kHz!})$$

4. Survival Space Bounds

$$f_{cut} < f < f_s/2$$

With $f_{cut} = 300\text{ Hz}$:

$$300\text{ Hz} < f < 100\text{ kHz}$$

KEY CORRECTION:

□ Old claim: "300 Hz - 5 kHz"

✓ Correct: "300 Hz - ~1.7 kHz" (for $v=15\text{ km/s}$)