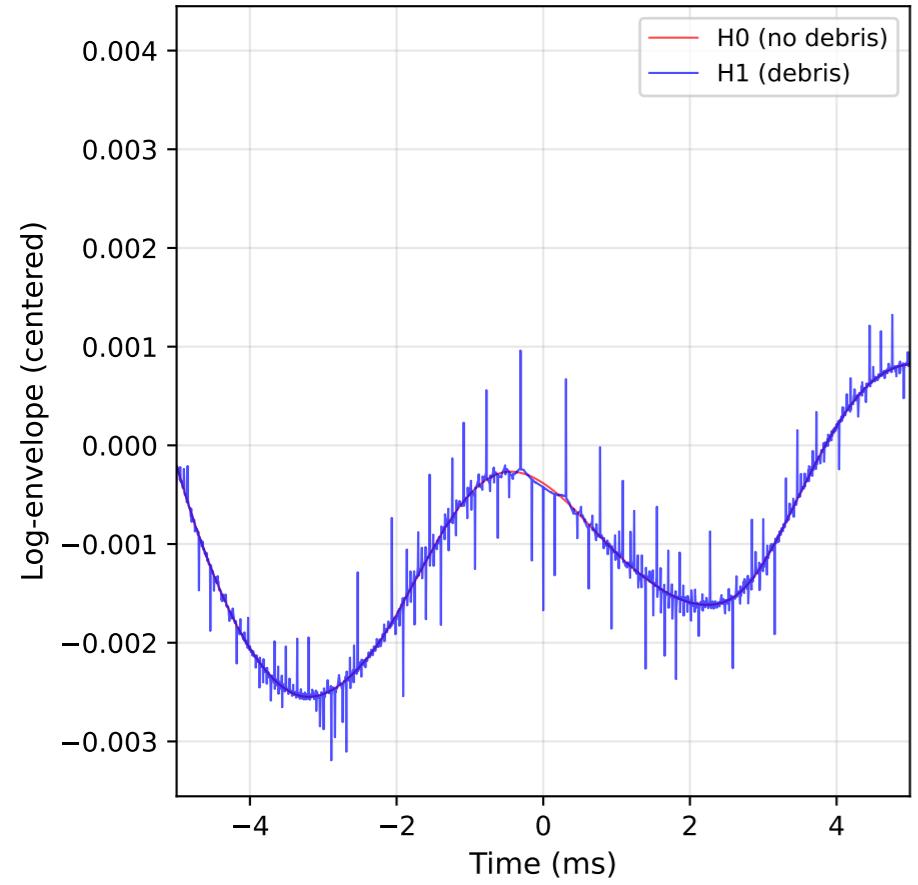
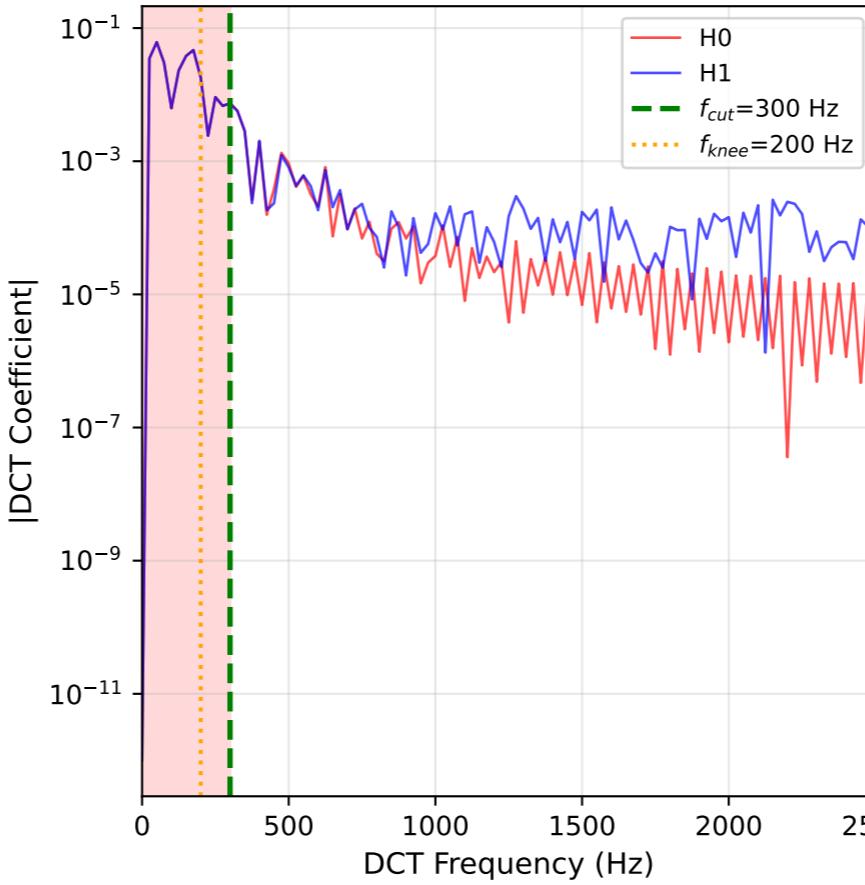
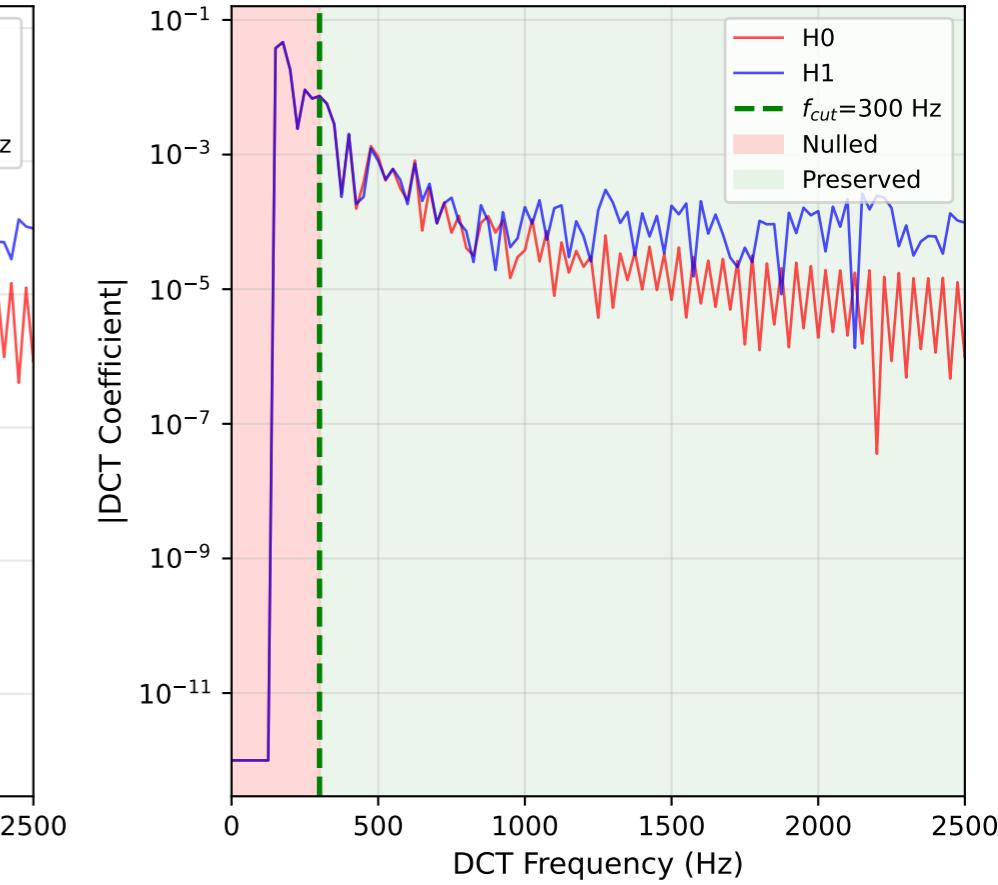
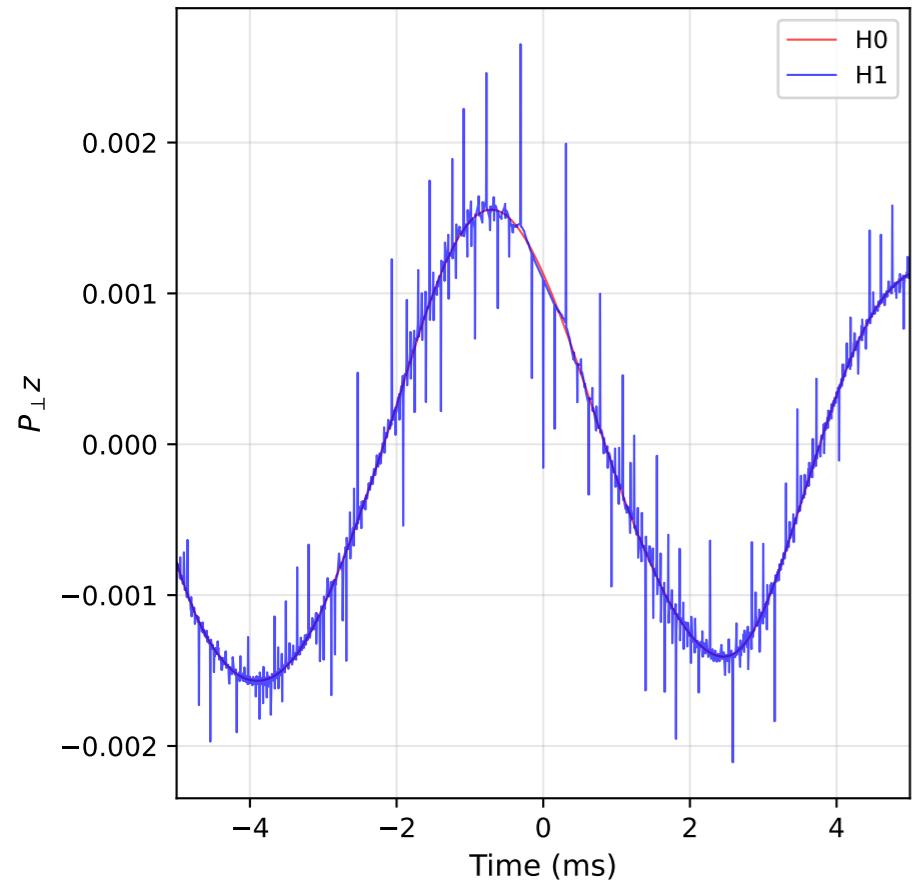
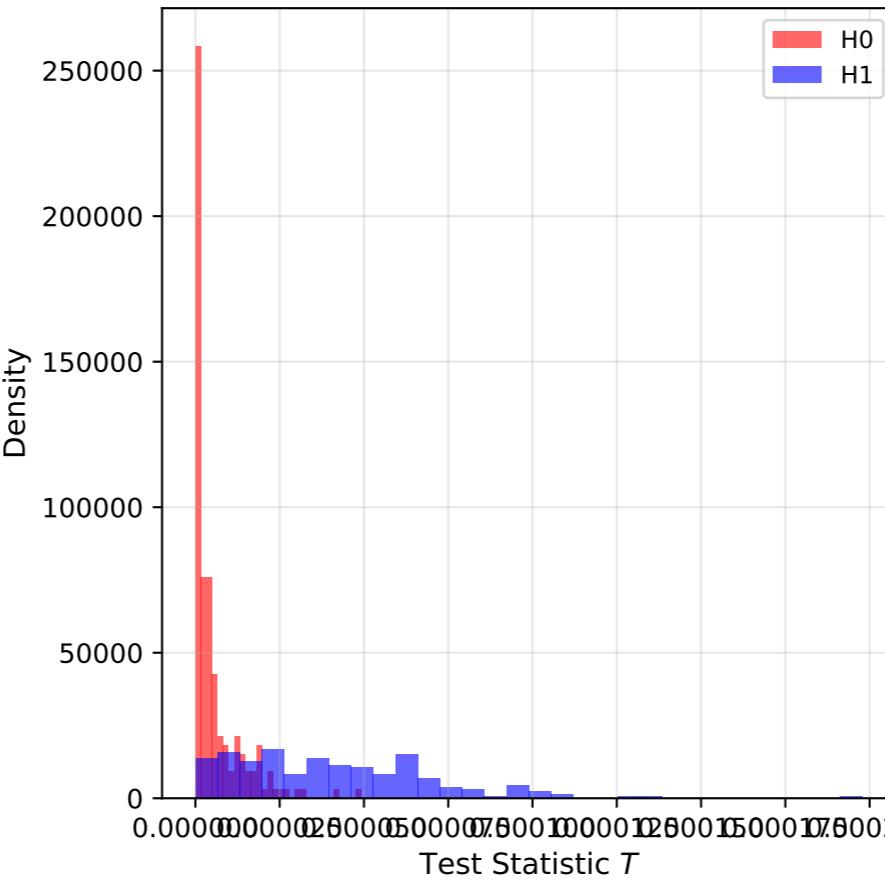


(a) Log-Envelope Signal $z(t) = \ln|r(t)|$ (b) DCT Spectrum Before P_{\perp} (c) DCT Spectrum After P_{\perp} 

(d) After Projection



(e) Detection (AUC=0.916)



(f) Design Summary

SURVIVAL SPACE DESIGN (CORRECTED)

Physical Parameters:

- Fresnel radius: $r_F = 4.47$ m
- Crossing time: $T_{cross} = 0.60$ ms
- Signal bandwidth: $f_{max} = 1677$ Hz

Projection Operator P_{\perp} :

- Nulls DCT coefficients for $f < f_{cut}$
- Preserved subspace: $[f_{cut}, f_{s/2}]$
- Signal energy concentrates in $[0, f_{max}]$

Design Choice: $f_{cut} = 300$ Hz

- Condition: $f_{knee} < f_{cut} \ll f_{max}$
- $f_{cut}/f_{knee} = 1.5$ (noise margin)
- $f_{cut}/f_{max} = 0.18$ (signal margin)

Key Metrics (at $f_{cut} = 300$ Hz):

- Signal energy retention: $\eta_z > 99\%$
- Noise energy removed: ~75-85%

Working Range:

- Requires $f_{knee} < f_{max}/3 \sim 560$ Hz