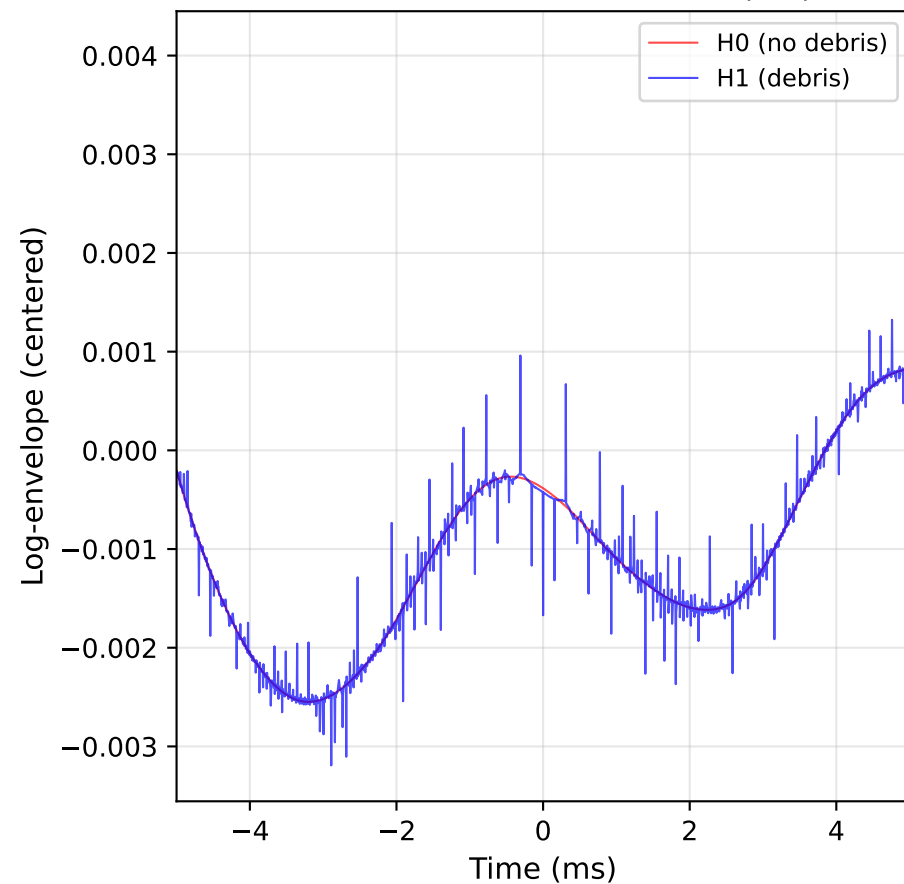
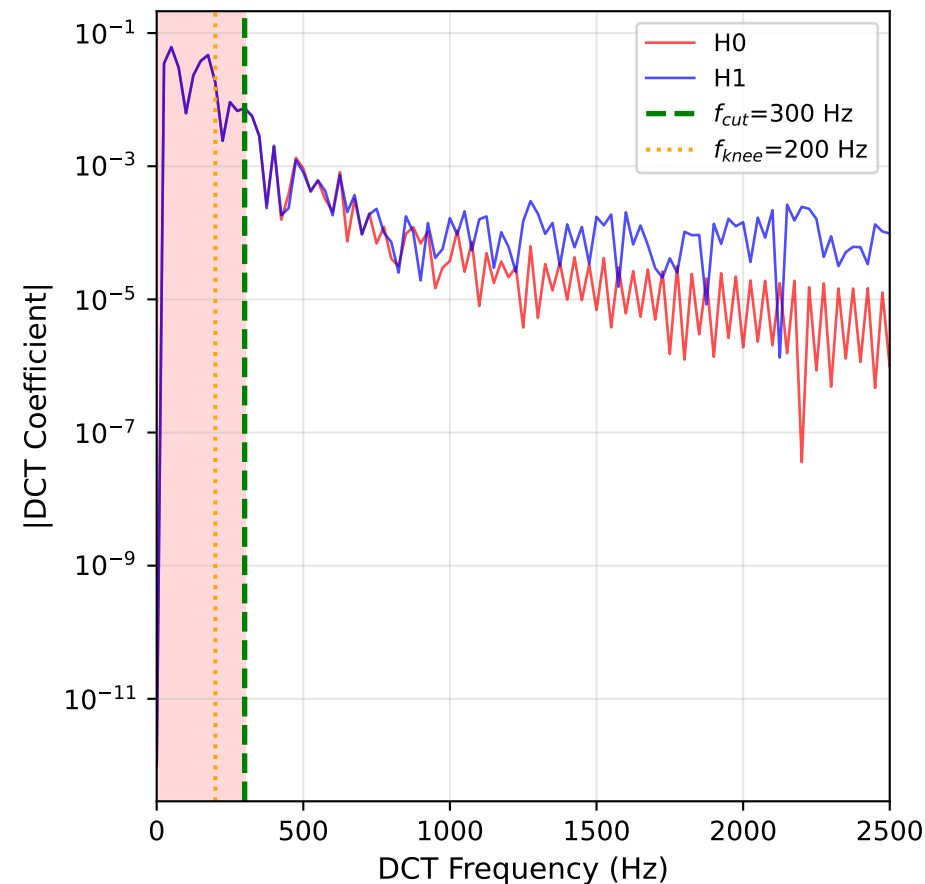
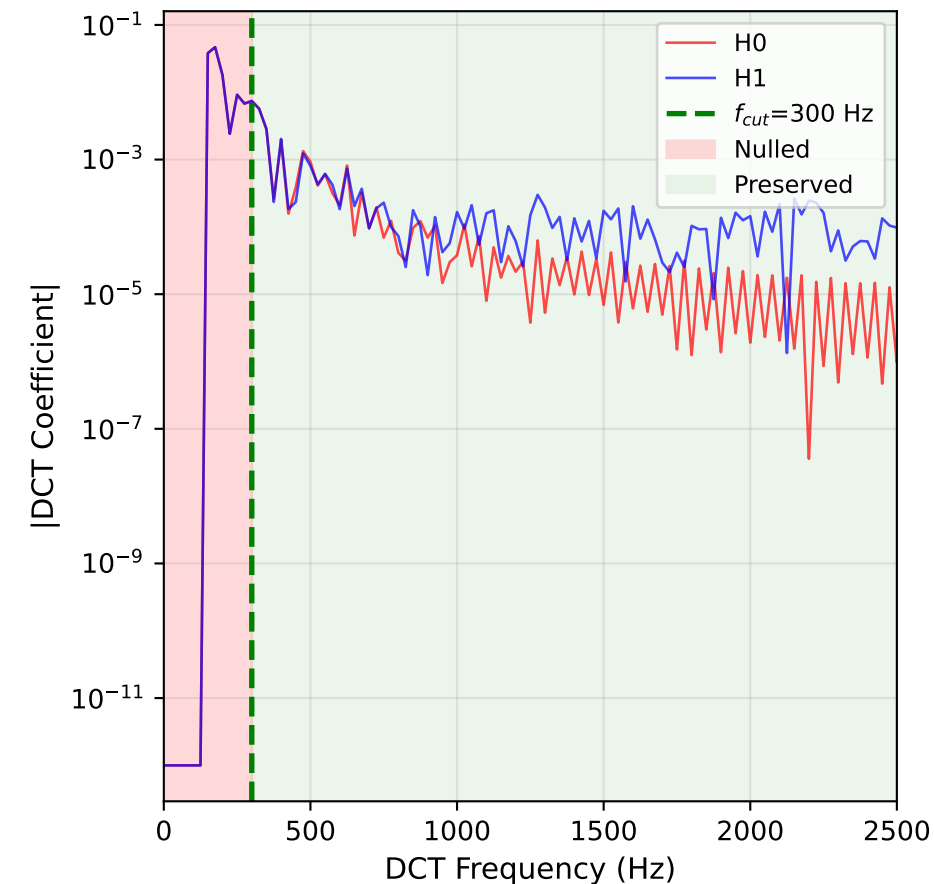
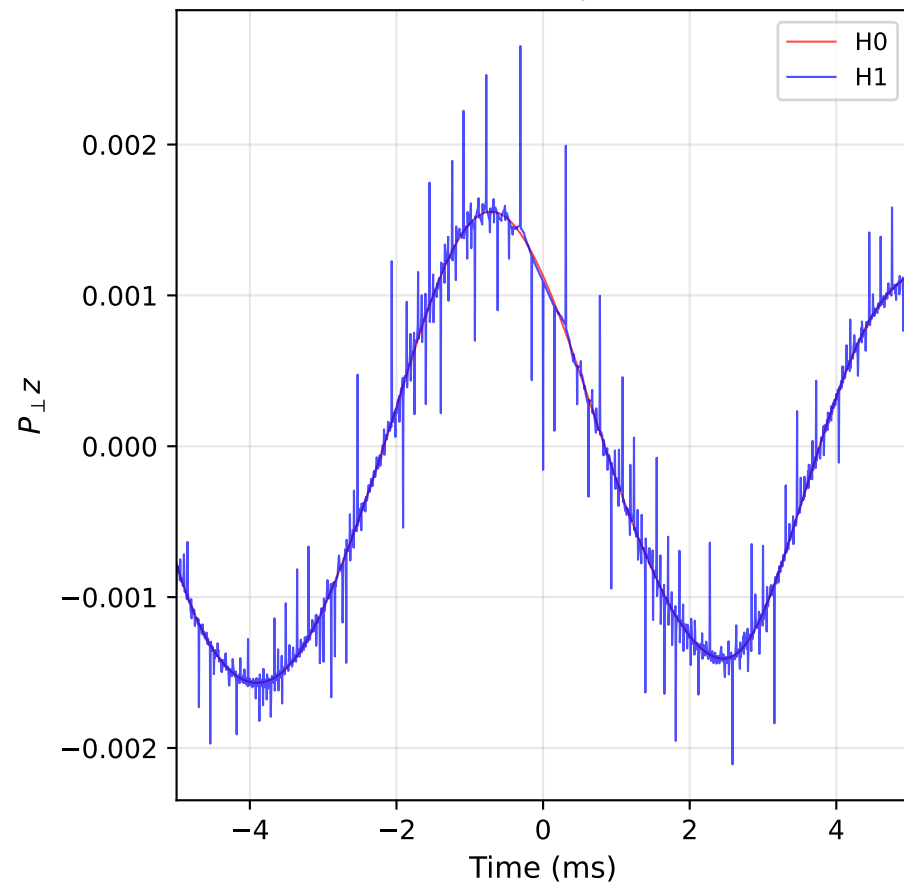
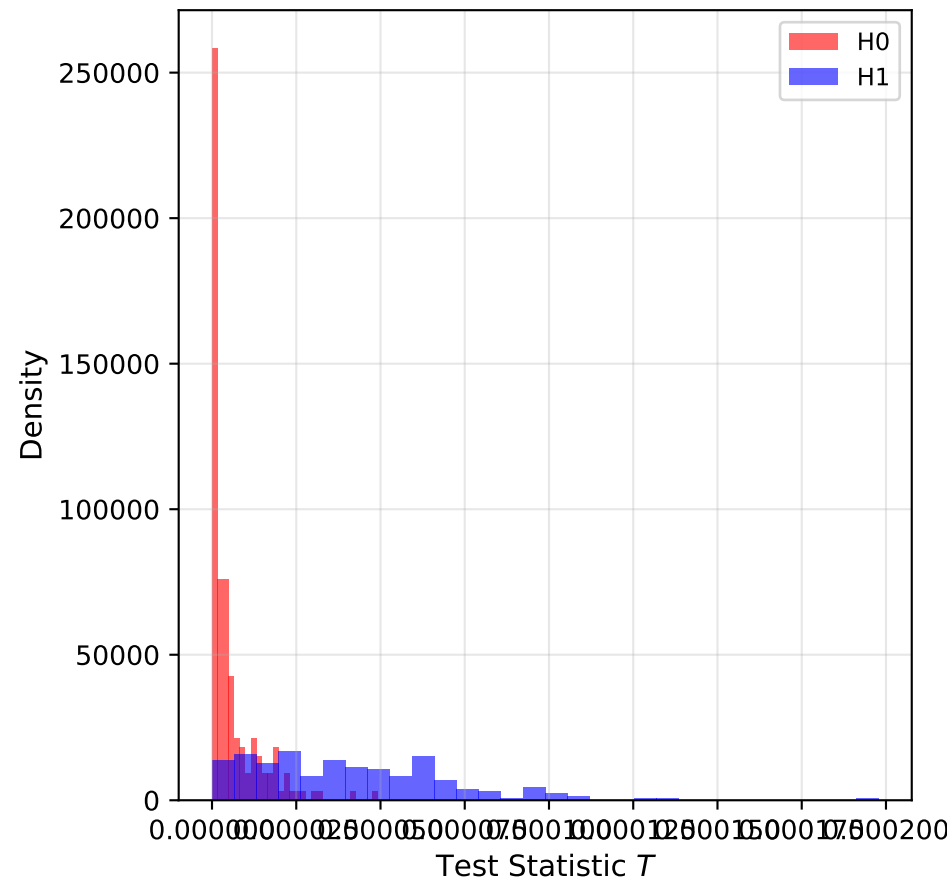


(a) Log-Envelope Signal $z(t) = \ln|r(t)|$ (b) DCT Spectrum Before P_{\perp} (c) DCT Spectrum After P_{\perp} 

(d) After Projection



(e) Detection (AUC=0.916)



(f) Design Summary

SURVIVAL SPACE DESIGN (CORRECTED)

Physical Parameters:

- Fresnel radius: $r_F = 4.47$ m
- Crossing time: $T_{\text{cross}} = 0.60$ ms
- Signal bandwidth: $f_{\text{max}} = 1677$ Hz

Projection Operator P_{perp} :

- Nulls DCT coefficients for $f < f_{\text{cut}}$
- Preserved subspace: $[f_{\text{cut}}, f_s/2]$
- Signal energy concentrates in $[0, f_{\text{max}}]$

Design Choice: $f_{\text{cut}} = 300$ Hz

- Condition: $f_{\text{knee}} < f_{\text{cut}} \ll f_{\text{max}}$
- $f_{\text{cut}}/f_{\text{knee}} = 1.5$ (noise margin)
- $f_{\text{cut}}/f_{\text{max}} = 0.18$ (signal margin)

Key Metrics (at $f_{\text{cut}} = 300$ Hz):

- Signal energy retention: $\eta_z > 99\%$
- Noise energy removed: $\sim 75\text{-}85\%$

Working Range:

- Requires $f_{\text{knee}} < f_{\text{max}}/3 \sim 560$ Hz