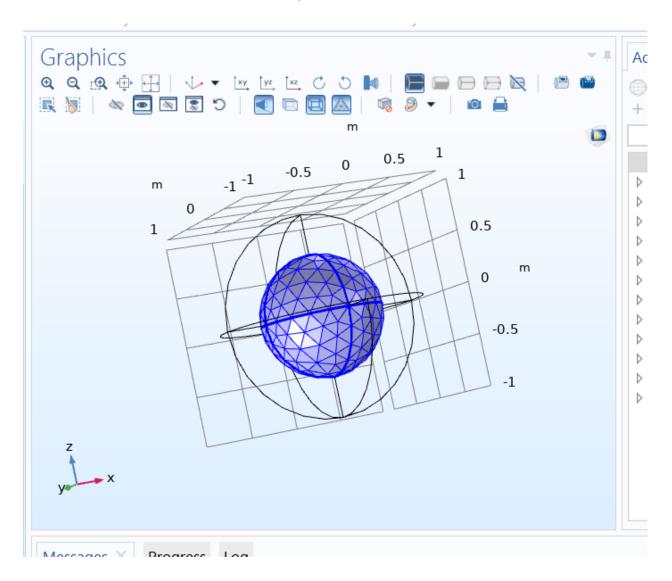
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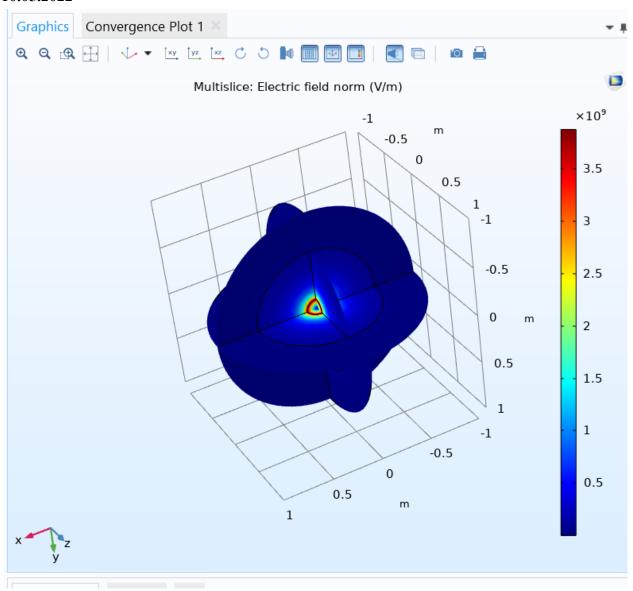
The outputs in PNG format and the corresponding COMSOL file can also be found on my GitHub repository: <a href="https://github.com/DRA-chaos/COMSOL-Multiphysics">https://github.com/DRA-chaos/COMSOL-Multiphysics</a>

A few screenshots from the COMSOL designed simulation are as follows:



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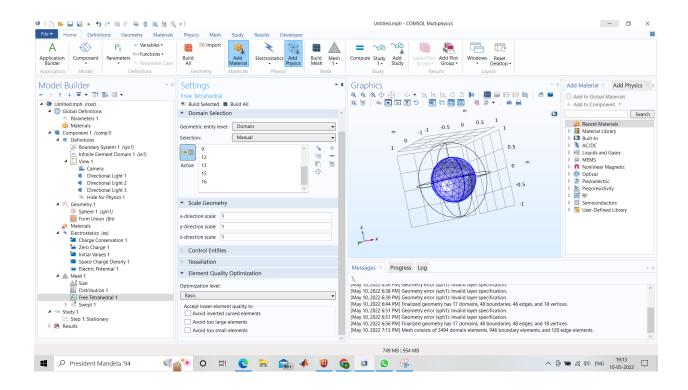


The time taken for solving the equations in 3-D space takes into account the degrees of freedom, the local GPU/ processor feedbacks and the runtime. The details of the run are enlisted below:

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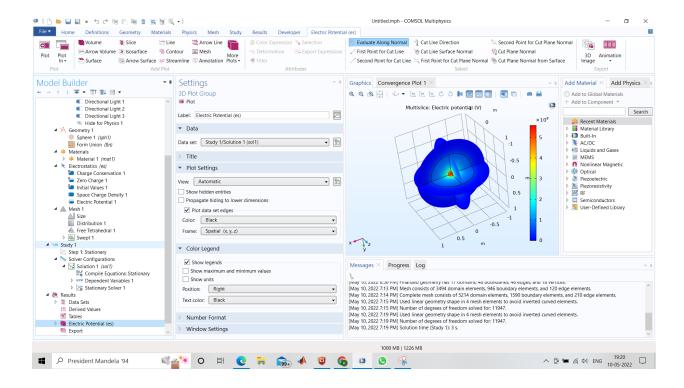
#### 10.05.2022

```
Keep warnings in stored log
<---- Stationary Solver 1 in Study 1/Solution
Started at May 10, 2022 7:19:41 PM.
Linear solver
Number of degrees of freedom solved for: 11947
Symmetric matrices found.
Scales for dependent variables:
Electric potential (comp1.V): 1
Orthonormal null-space function used.
          SolEst
                     Damping Stepsize #Res :
Iter
            0.89
                   1.0000000
                                  0.89
  1
                                            1
Solution time: 1 s.
Physical memory: 1.05 GB
Virtual memory: 1.35 GB
Ended at May 10, 2022 7:19:42 PM.
---- Stationary Solver 1 in Study 1/Solution
```



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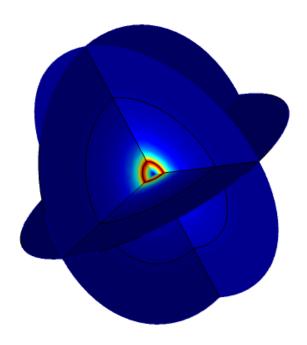
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Conjugate gradients of the Electric Field obtained in 3D

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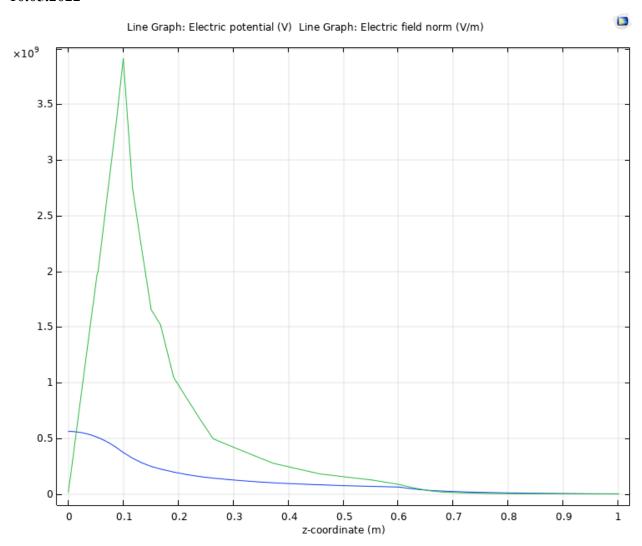
10.05.2022



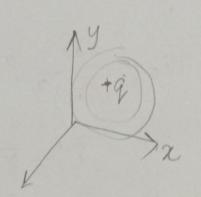
Graphics output of the Electric Field in 3D

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## 10.05.2022



If we have a point charge +9 situated at 11,4,3, we want to figure out the



electric field and potential at a point say (p,q,r) both theoretically and conjutationally Cusing comson)

The error in these two realms is drawn from the fact that we may use different spherical shells with different radli

Ideally 
$$E = kq = \frac{kq}{(x-p)^2 + (y-q)^2 + (z-r)^2}$$
  
and  $V = -kq$ 

agiven a stationary charge distribution PCP),

tre can calculate the electric field,

Chehere 28 = 71 - 8

to evaluate, une can first evaluate V(8)

$$V(\overline{r}) = \frac{1}{4\pi\epsilon_0} \int \frac{1}{\Delta r} P(\overline{r}') d\overline{r}' \quad \text{as } \overline{E} = -\overline{r} V.$$

this can be generalized to 3 Dimensions as.

$$\overline{E} = \left(\frac{\partial}{\partial n} \nabla_x + \frac{\partial}{\partial y} \nabla_y + \frac{\partial}{\partial z} \nabla_y\right)$$

The Poisson's equation to offer a belter affroach to dellume V

With affropriate boundary condulors,  $5^2V=0$  when J=0

We have,
$$\frac{\partial^2 V}{\partial n^2} + \frac{\partial^2 V}{\partial y^2} + \frac{\partial^2 V}{\partial z^2} = 0.$$

We can use the properties of solutions of the 1) Laglace equation to the valid here as well



$$d^2 = \gamma^2 + R^2 - 2\gamma R \cos \theta$$
.

$$\frac{1}{47120} \frac{9}{\sqrt{8^2+R^2-28R\cos\theta}}$$

we can obtain the average potential ky inlegting up a coss the sayace of the space.

We have somulated the scenario using comsol.

The electroslatic polyular V has no local, maxima or minima as can be seen from the grayhs. All the extremes occur at the boundance.

We can simulate similar results using different materials, and it would indeed be interesting to see the outputs obtained.