

## **DSE 310 : Assignment 1**

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We have a relational database schema titled 'Aircraft Information' that consists of three relational schemas Engine, Manufacturer and Airliner which are listed below with their schema and respective SQL data types.

- **Engine( Integer : S.NO, Varchar: Engine\_name, Varchar: Engine\_ID)**

This schema stores information on the type of jet engine used in the aircraft.

- **Manufacturer (Varchar: Engine\_ID, Varchar: Manufacturer\_name, Varchar: Manufacturer\_ID, Varchar: Headquarter)**

This schema contains information of the companies that manufacture the jet engines for the aircrafts.

- **Airliner (Varchar: Airline\_Brand, Varchar: Air\_ID, Varchar: Engine\_ID , Float: Top\_Speed)**

This schema contains the information on the Airliners, their associated engines used and the maximum speed that they can fly in.

Engine

I have designed the relational schemas below with some research done on the sample types.

Engine

| S.NO | Engine_name | Engine_ID |
|------|-------------|-----------|
| 1    | Turbojet    | 11j       |
| 2    | Turboprop   | 12p       |
| 3    | Turbofan    | 13f       |

Manufacturer

| Engine_ID | Manufacturer_name      | Manufacturer_ID | Headquarter |
|-----------|------------------------|-----------------|-------------|
| 11j       | Rolls Royce            | RR1             | London      |
| 11j       | Pratt & Whitney        | PW2             | Connecticut |
| 11j       | Williams International | WI3             | Michigan    |

|     |                     |     |                |
|-----|---------------------|-----|----------------|
| 12p | Rolls Royce         | RR1 | London         |
| 12p | GE Aviation         | GA4 | Ohio           |
| 12p | Honeywell Aerospace | HA5 | Arizona        |
| 13f | Rolls Royce         | RR1 | London         |
| 13f | Klimov              | KK6 | St. Petersburg |
| 13f | EuroJet             | EJ7 | Berlin         |

### Airliner

| Airline_Brand  | Air_ID | Engine_ID | Top_Speed (in km/h) |
|----------------|--------|-----------|---------------------|
| Etihad         | E1     | 13f       | 1020.32             |
| Lufthansa      | L1     | 12p       | 840                 |
| Concorde       | C1     | 11j       | 2179                |
| Indigo         | I1     | 13f       | 154                 |
| Cathay Pacific | PC1    | 12p       | 1931.213            |

The following questions have been framed involving the above three tables.

$\sigma$  refers to the select operator that selects rows with conditions

$\pi$  is the projection operator

$\bowtie$  is the natural join operator

U and - are set operators denoting union and subtraction respectively

Other predicate calculus related terminologies

1) Find all the airliner's details whose top\_speed is greater than 2000km/h

The Relational Algebra expression for this problem is :

$\sigma_{\text{Top\_Speed} > 2000}(\text{Airliner})$

The Tuple Relational Calculus expression for the problem can be written as:

$\{ t \mid t \in \text{Airliner} \wedge t[\text{Top\_speed}] > 2000 \}$

Where t is the resulting tuple and the rest is the predicate wherein t[Top\_speed] is the tuple variable on which we are placing conditions

The Domain Relational Calculus expression for this problem is :

$\{ \langle a, i, e, t \rangle \mid \langle a, i, e, t \rangle \in \text{Airliner} \wedge (t > 2000) \}$

Where a, i, e and t are domain variables corresponding to all the columns of the Airliner table in sequence

The following are some extra questions solved using **Relational Algebra**

- 2) Obtain the location of headquarters for the Turbofan engine manufactured by Klimov

In this question, we need to first obtain the Engine ID for Turbofan from the Engine table and then join the Manufacturer table with the Engine Table using the common attribute 'Engine\_ID'. Then the record from the Manufacturer table where Klimov is the company is outsourced. Then we project the resultant Headquarter from the obtained output.

$\pi_{\text{Headquarter}}(\sigma_{\text{Engine\_name} = \text{"Turbofan"}}(\text{Engine}) \bowtie \sigma_{\text{Manufacturer\_name} = \text{"Klimov"}}(\text{Manufacturer}))$

- 3) Find the engine manufacturer and Engine type of the airline whose top\_speed is greater than 2000km/h

This question involved the use of select operator on three tables to be joined through the common attribute 'Engine\_ID'. The record from the joint operation where Top\_speed > 2000 is obtained. A projection operator is then used to retrieve the Manufacturer\_name and the Engine\_name from the resultant output.

$\pi_{\text{Manufacturer\_name, Engine\_name}}(\sigma_{\text{Top\_speed} > 2000}(\text{Engine} \bowtie \text{Manufacturer} \bowtie \text{Airliner}))$

- 4) Give all the manufacturer details of the Engines manufactured by EuroJet or Pratt & Whitney

We use a union operation here to combine the individual results of the select operator applied onto the Manufacturer table for the two companies.

$(\sigma_{\text{Manufacturer\_name} = \text{"EuroJet"}}(\text{Manufacturer})) \cup (\sigma_{\text{Manufacturer\_name} = \text{"Pratt \& Whitney"}}(\text{Manufacturer}))$

- 5) List all the places or headquarters which do not have an airliner with the Air\_ID of C1

The projection of Engine ID from the Airliner table for the record of Air\_ID = C1 is subtracted from the Engine ID projected from the Manufacturer table. The output is joined with the Manufacturer table using the common key of Engine ID to project the Headquarter location.

$$\pi_{\text{Headquarter}}(\text{Manufacturer} \bowtie (\pi_{\text{Engine\_ID}}(\text{Manufacturer}) - \pi_{\text{Engine\_ID}}(\sigma_{\text{Air\_ID} = \text{"C1"}}(\text{Airliner})))$$

- 6) State the manufacturer names of all those airliners whose maximum speed of cruising lies between 1000 and 2000 km/h (excluding 1000 and 2000).

We find the projection of the company name from the result obtained by applying the select operation condition on the join of Manufacturer and Airliner schemas

$$\pi_{\text{Manufacturer\_name}}(\sigma_{\text{Top\_speed} > 1000 \wedge \text{Top\_speed} < 2000}(\text{Manufacturer} \bowtie \text{Airliner}))$$

Now we explore the use of **Relational Calculus** which encompasses both **Tuple Relational Calculus** as well as **Domain Relational Calculus**.

**Tuple Relational Calculus :**

- 7) Name the airliner(s) that run by exhausting the Turbojet Engine.

The Tuple Relational Calculus expression for the problem can be written as:

$$\{ t \mid \exists s \in \text{Airliner} ( t[\text{Airline\_brand}] = s[\text{Airline\_brand}] \wedge \exists u \in \text{Engine} ( u[\text{Engine\_name}] = \text{"Turbojet"} \wedge u[\text{Engine\_ID}] = s[\text{Engine\_ID}] ) ) \}$$

**Domain Relational Calculus**

- 8) Find the company name, manufacturing ID and the location of its headquarters for which Manufacturer ID is HA5.

The Domain Relational Calculus expression for the problem can be written as:

$$\{ \langle m, i, h \rangle \mid \langle m, i, h \rangle \in \text{Manufacturer} \wedge (i = \text{"HA5"}) \}$$

Where m, i and h represent the resulting domain variables corresponding to Manufacturer\_name, Manufacturer\_ID and Headquarter respectively.

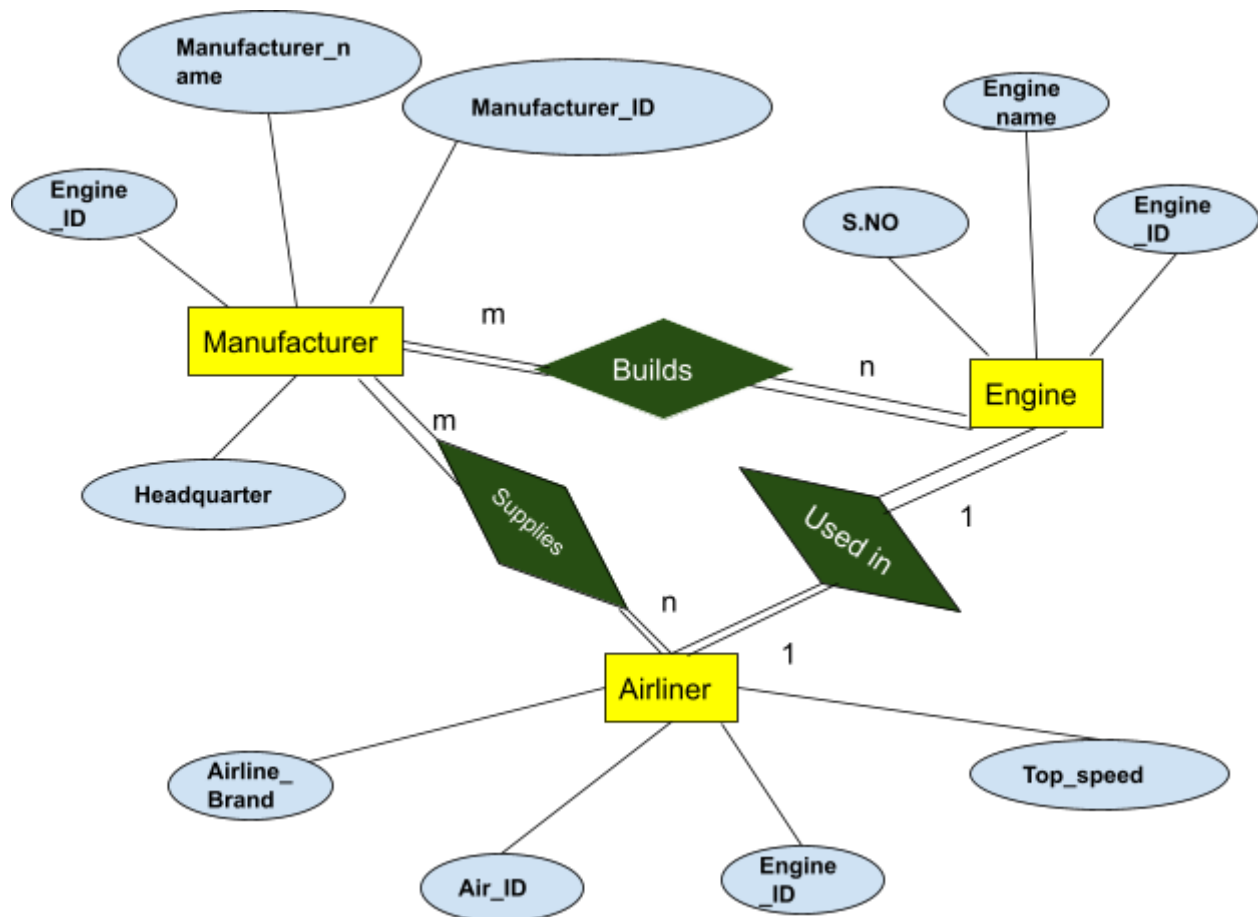
9) What are the names of the Airliner and its maximum speed corresponding to the Air\_ID of 'I1'

The Domain Relational Calculus expression for the problem can be written as:

$\{ \langle a, t \rangle \mid \langle a, d, t \rangle \in \text{Airliner} \wedge d = \text{"I1"} \}$

Where a, d and t represent the domain variables corresponding to Airline\_Brand, Air\_ID and top\_speed respectively.

The following is the Entity Relationship Diagram for our Entity Relationship model 'Aircraft Information'



The double lines represent total participation

**Practical applications of Relational Algebra and Relational Calculus applied to the above scenario :**

This has many practical applications: For example in determining the areas over which permit of flight is required. Places like Dubai have a top speed limit  $< 1000$  km/h owing to tall building structures, hence aircrafts like Concorde cannot operate on such terrains in the same high speed, they can only operate at a lower speed.

Another application could be for quickly finding the headquarter and subsequently office location, mail and other details from one value like Manufacturer\_ID or an aircraft detail making contacting easier.

I have tried to highlight these practical applications through the questions designed above.