

Spintronics and Nanomagnetism

ECS 521/641

Instructor: Dr. Kuntal Roy

Electrical Engineering and Computer Science (EECS) Dept.

Indian Institute of Science Education and Research (IISER) Bhopal

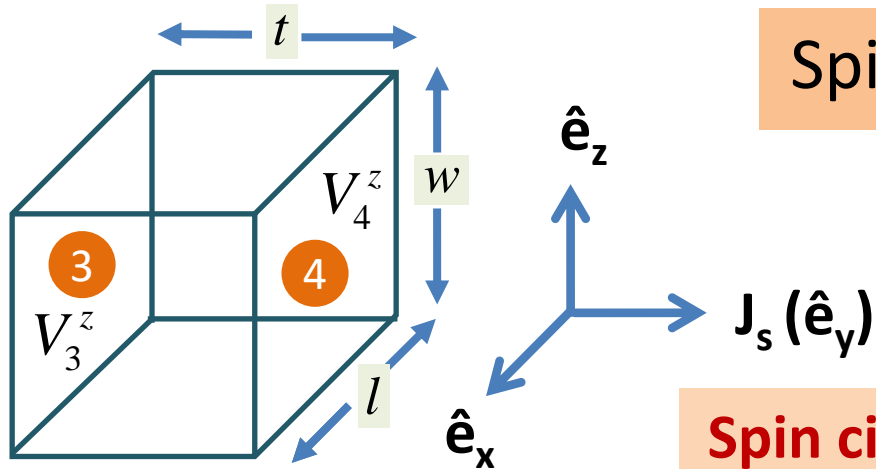
Email: kuntal@iiserb.ac.in

Spin relaxation
Magnetoresistance
Spin waves
Magnetic Force Microscopy

Spin relaxation

Spin relaxation

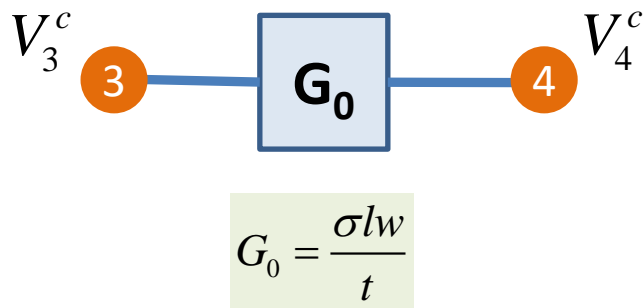
Spin relaxes due to spin diffusion



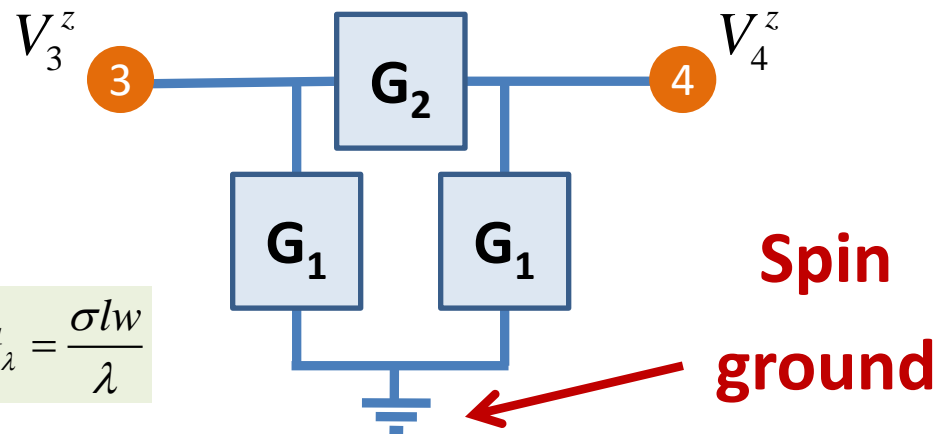
$$\frac{d^2 V^z(y)}{dy^2} = \frac{V^z(y)}{\lambda^2} \quad \lambda: \text{Spin diffusion length}$$

Spin circuit

Charge circuit



No shunt elements



$$G_1 = G_\lambda \tanh\left(\frac{t}{2\lambda}\right)$$

$$G_2 = G_\lambda \operatorname{csch}\left(\frac{t}{\lambda}\right)$$

Dispersion relation: $B = 0, v = 0$

$$E_{\pm} = \frac{\hbar^2(k_x^2 + k_z^2)}{2m^*} \pm \sqrt{\left(\frac{g\mu_B B_z}{2} + \eta k_x - vk_z\right)^2 + \left(\frac{g\mu_B B_x}{2} - \eta k_z + vk_x\right)^2}$$

$$E_{\pm} = \frac{\hbar^2 k^2}{2m^*} \pm \eta k$$

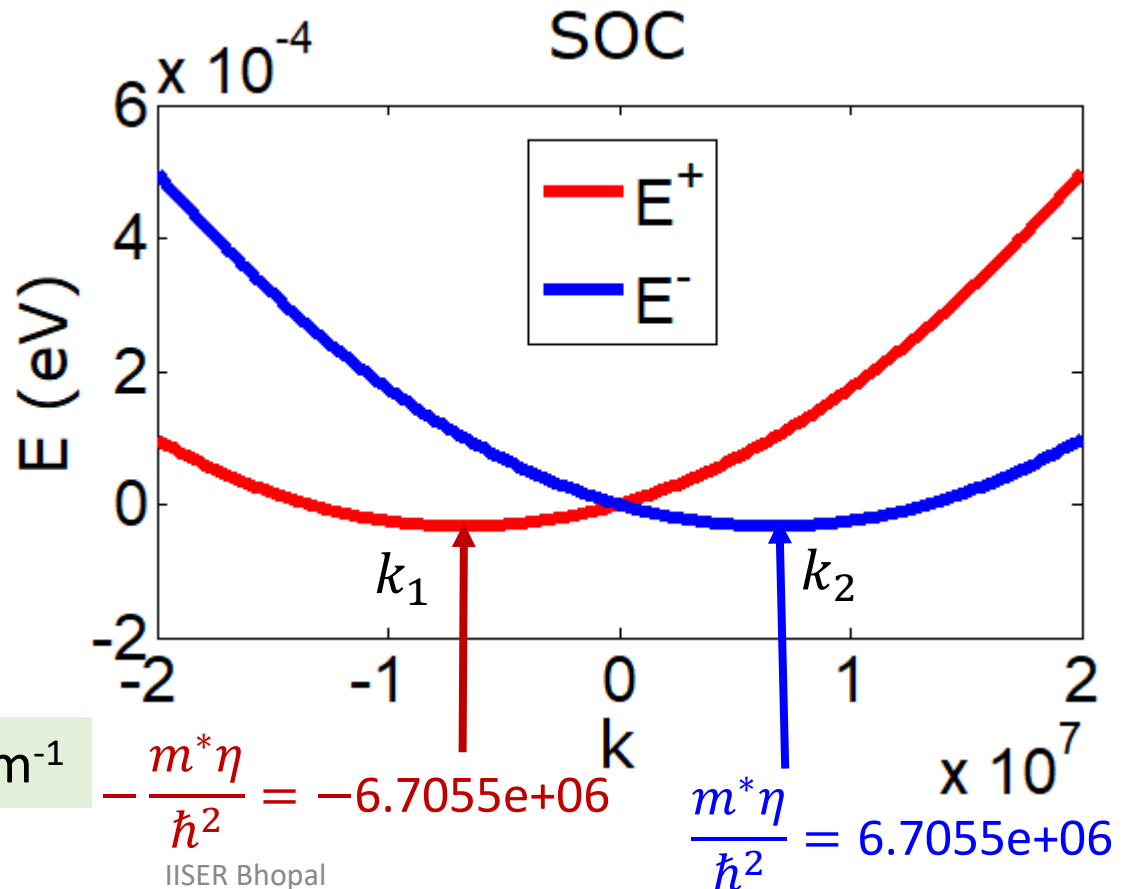
$$k_2 - k_1 = \frac{2m^*\eta}{\hbar^2}$$

$$m^* = 0.05m_0$$

$$\eta = 10^{-11} \text{ eV} - m$$

$$\frac{\hbar^2}{2m^*} = 7.4566 \times 10^{-19} \text{ eV} - m^2$$

$$\text{SOC splitting} = 1.3411 \times 10^7 \text{ m}^{-1}$$



Spin-orbit magnetic field

$$E_{\pm} = \frac{\hbar^2 k^2}{2m^*} \pm \eta k$$

$$k_2 - k_1 = \frac{2m^* \eta}{\hbar^2}$$

Similarly for
Dresselhaus SOC
 $\nu \rightarrow \eta$

$$v_1(E) = \frac{1}{\hbar} \frac{\partial E_+}{\partial k} = \frac{\hbar k_1(E)}{m^*} + \frac{\eta}{\hbar}$$

$$v_2(E) = \frac{1}{\hbar} \frac{\partial E_-}{\partial k} = \frac{\hbar k_2(E)}{m^*} - \frac{\eta}{\hbar}$$

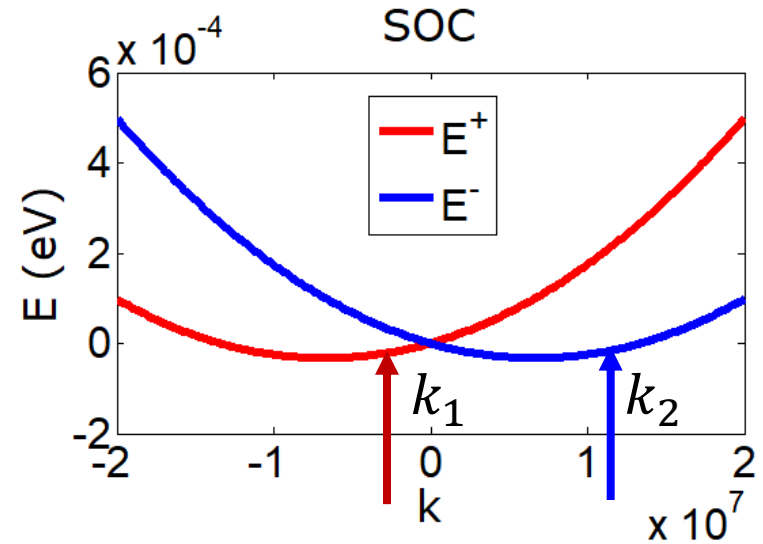
$$v_1(E) = v_2(E) = v(E)$$

Velocity is spin-independent

$$v(E) = \frac{v_1(E) + v_2(E)}{2} = \frac{\hbar}{m^*} \frac{k_1(E) + k_2(E)}{2} = \frac{\hbar k_{av}(E)}{m^*}$$

$$\mathbf{B}_{Rashba} = \frac{2a_R}{g\mu_B} (\mathbf{E} \times \mathbf{k})$$

$$|\mathbf{B}_{Rashba}| = \frac{2\eta}{g\mu_B} k_{av} = \frac{2\eta m^*}{g\mu_B \hbar} v = \frac{2^{3/2} \eta m^{*1/2}}{g\mu_B \hbar} \sqrt{E}$$

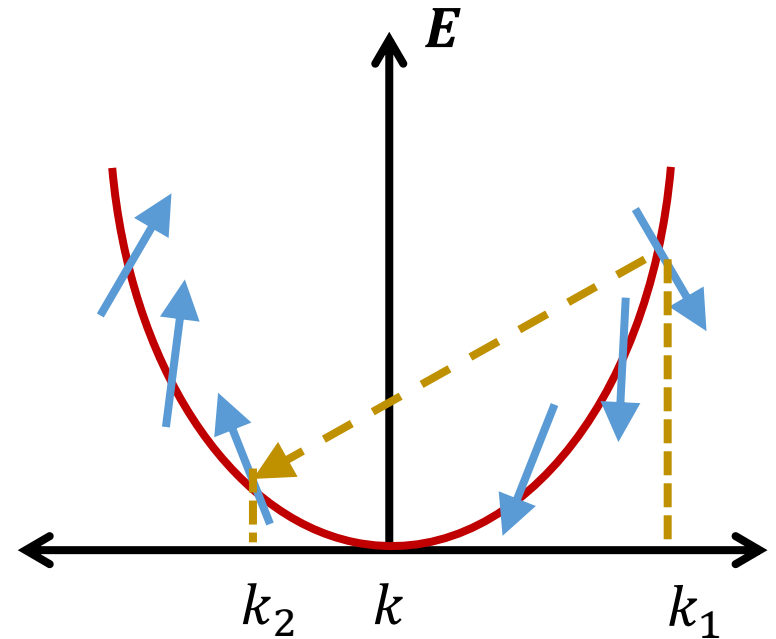


Elliott-Yafet spin relaxation

In a crystal, the Bloch states may not be spin eigenstates

The actual polarization depends on the wavevectors

Each wavevector state still has two possible spin orientations that are mutually anti-parallel



A momentum changing collision event e.g., phonon scattering changes the wavevector k_1 to k_2

$$\tau_{EY} \propto \tau_m$$

- R. J. Elliott, Phys. Rev. 96, 266 (1954)
- Y. Yafet, Phys. Lett. A 98, 287 (1983)

D'yakonov Perel' spin relaxation

$$|\mathbf{B}_{Rashba}| = \frac{2\eta}{g\mu_B} \mathbf{k} = \frac{2\eta m^*}{g\mu_B \hbar} \mathbf{v}$$

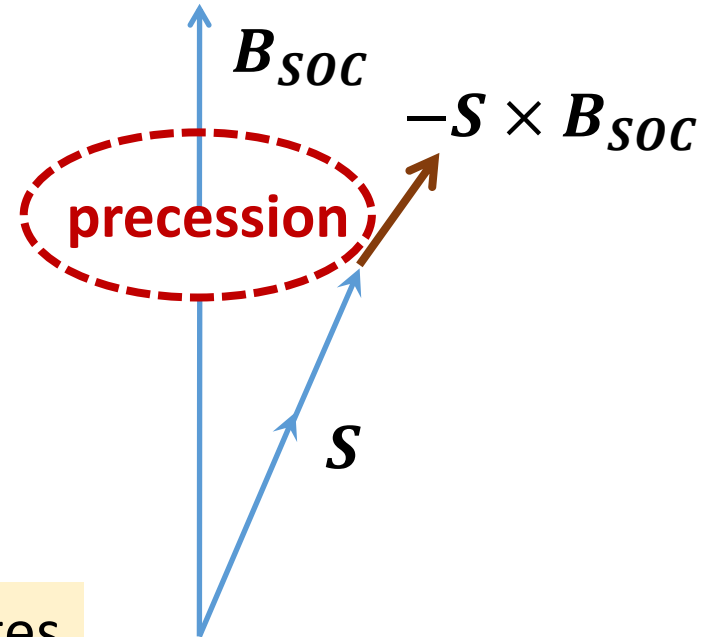
$$|\mathbf{B}_{Dresselhaus}| = \frac{2v}{g\mu_B} \mathbf{k} = \frac{2vm^*}{g\mu_B \hbar} \mathbf{v}$$

If the velocity/wavevector changes
randomly owing to scattering

The axis about which spin precesses changes

Frequency of precession changes

**Frequent momentum relaxing collisions
tend to slow down electrons and
suppress DP spin relaxations**



$$\frac{d\mathbf{S}}{dt} = -|\gamma| \mathbf{S} \times \mathbf{B}_{soc}$$

$$\tau_{DP} \propto \frac{1}{\tau_m}$$

➤ M. I. Dyakonov and V. I. Perel, Sov. Phys. Solid State 13, 3023 (1972)

Spin diffusion length

Drude model

$$\sigma = ne^2\tau_m/m^*$$

$$\lambda_{sf} = \sqrt{D \tau_{sf}}$$

D : Diffusions coefficient
 D_{OS} : Density of states

$$D = \sigma / e^2 D_{OS}$$

$$\tau_{sf} = \left(\frac{\lambda_{sf}^2 m^* D_{OS}}{n} \right) \frac{1}{\tau_m}$$

EY spin relaxation

$$\tau_{EY} \propto \tau_m$$

$$\lambda_{sf} \propto \sigma$$

DP spin relaxation

$$\tau_{DP} \propto \frac{1}{\tau_m}$$

$$\lambda_{sf} = \text{constant}$$

Other spin relaxation mechanisms

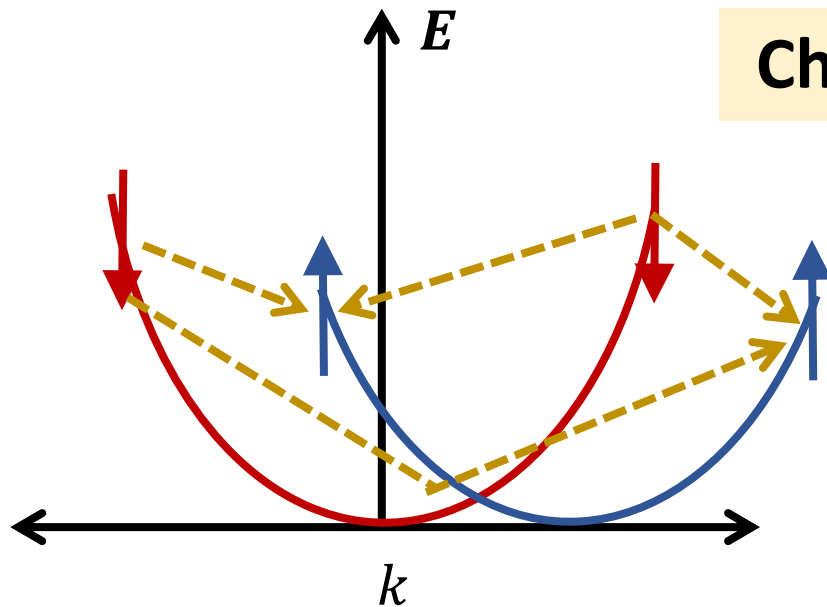
Bir-Arnov-Pikus spin relaxation

Spin relaxation in semiconductors when there is a significant concentration of both electrons and holes

Hyperfine interactions with nuclear spins

Nuclear spins generate a magnetic field which interacts with the electron spins via hyperfine interactions and can cause spin relaxation

Spin-galvanic effect



Charge current without a battery!

Spin-down band has higher energy

An electron from a filled state in the down-spin band to scatter to an empty state in the up-spin band

Asymmetric k -dependent scattering makes velocity asymmetric \rightarrow current flow

No violation of energy conservation

Spin-polarized carrier population using circularly polarized light

➤ Ganichev et al, Spin-galvanic effect, Nature **417**, 153 (2002)

Magnetoresistance

Nobel Prize in Physics (2007)



The Nobel Prize in Physics 2007
Albert Fert, Peter Grünberg

Giant Magneto-Resistance (GMR)

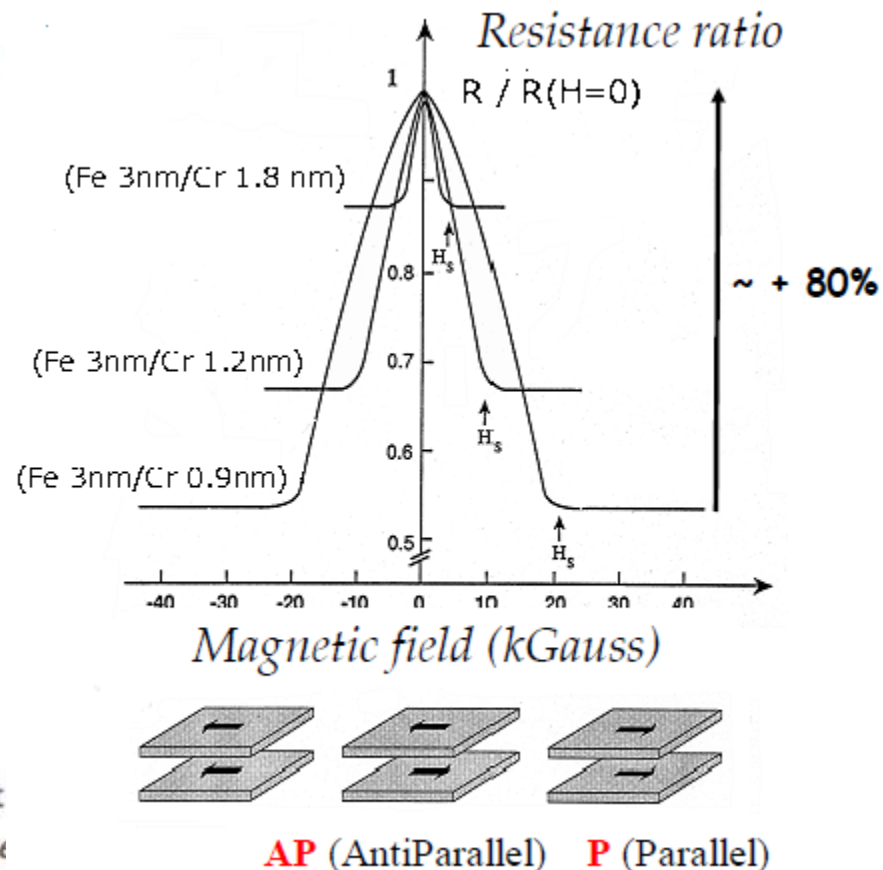
The Nobel Prize in Physics 2007



Photo: U. Montan
Albert Fert
Prize share: 1/2



Photo: U. Montan
Peter Grünberg
Prize share: 1/2



The Nobel Prize in Physics 2007 was awarded jointly to Albert Fert and Peter Grünberg "for the discovery of Giant Magnetoresistance"

- **A. Fert**, M.N. Baibich et al., Phys. Rev. Lett. **61**, 2472 (1988)
- **P. Grünberg**, G. Binash et al., Phys. Rev. B **39**, 4828 (1989)

1988

Magneto-Resistance (MR)



\mathbf{J}

\mathbf{H}

$$\frac{\Delta\rho}{\rho} = a \left(\frac{H}{\rho} \right)^2$$

MR can be positive
or negative

Resistance, R

$$MR = \frac{\Delta R}{R} [\%] = \frac{R(H) - R(0)}{R(0)} \times 100$$

Magnetic Field, H

Anisotropic Magneto-Resistance (AMR)

Anisotropic mixing of spin-up and spin-down conduction bands due to **spin-orbit coupling**

Ferromagnet

2-5% AMR

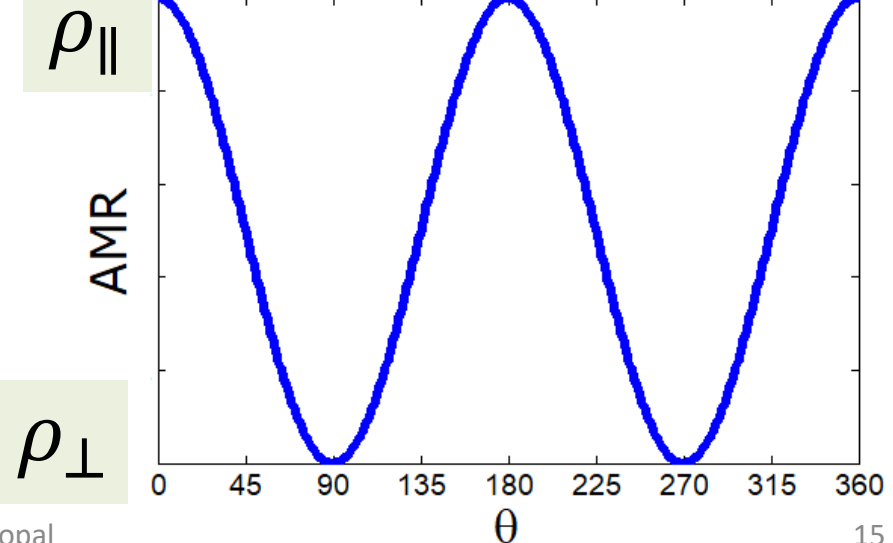
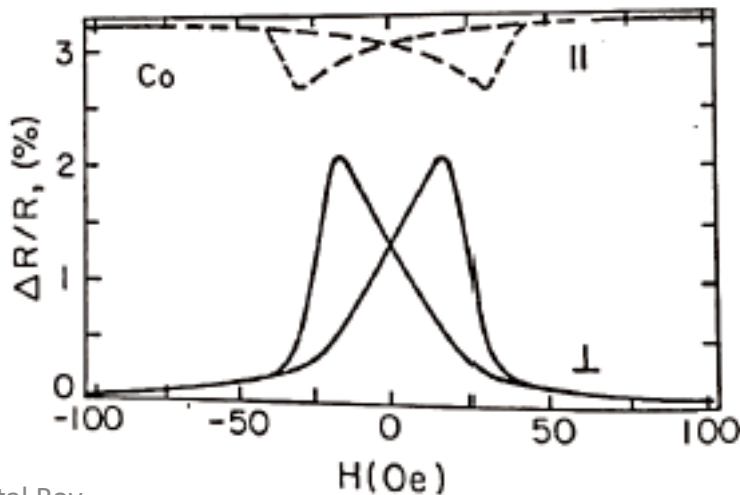
$$\frac{\Delta\rho}{\rho} \propto a \left(\frac{H}{\rho} \right)^2 + b \left(\frac{M}{\rho} \right)^2$$

Ordinary
Magnetoresistance

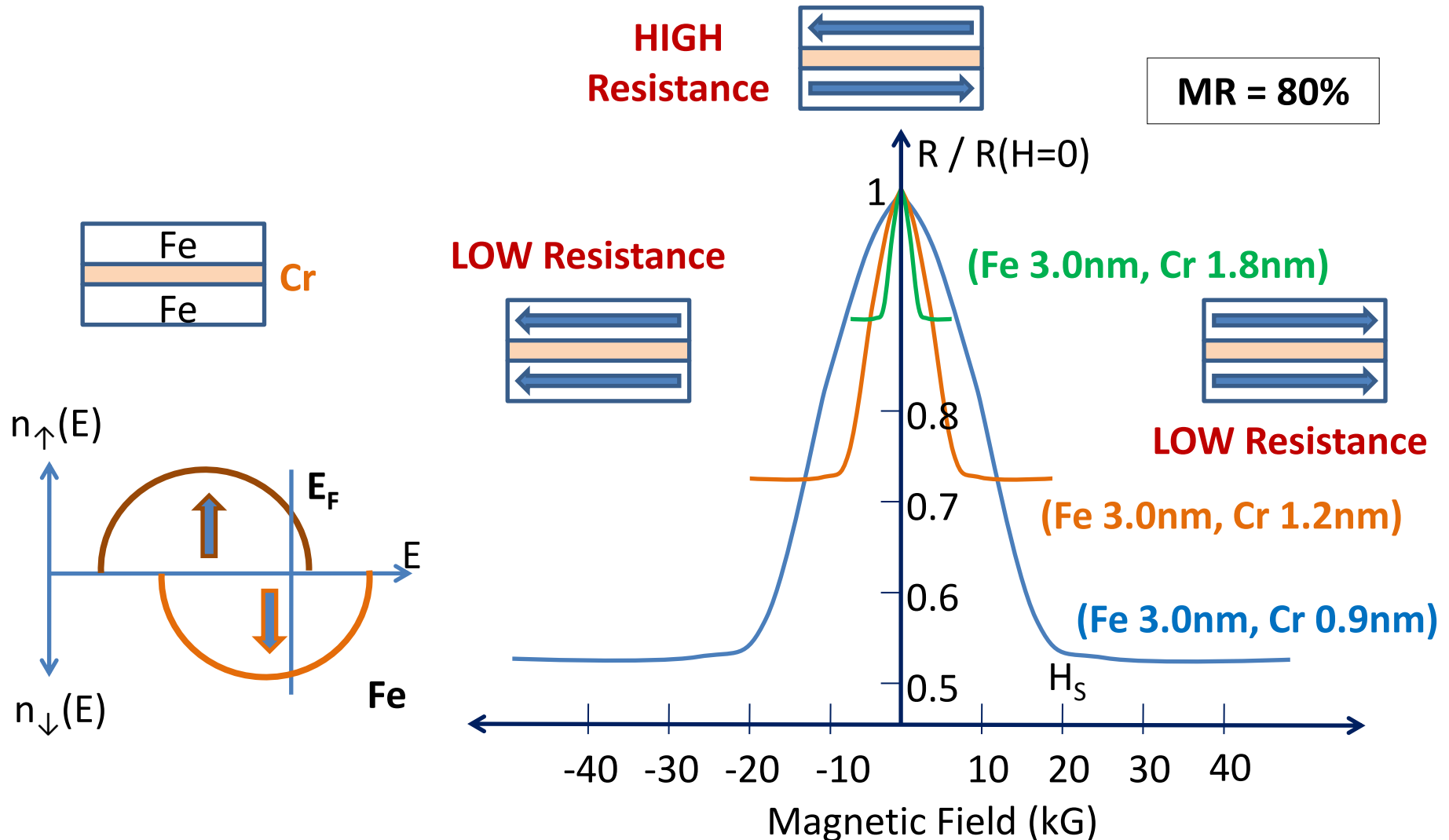
**Anisotropic
Magnetoresistance**

$$\rho(\theta) = \rho_{\perp} + (\rho_{\parallel} - \rho_{\perp}) \cos^2(\theta)$$

θ : angle (J, M)



Giant Magneto-Resistance (GMR)

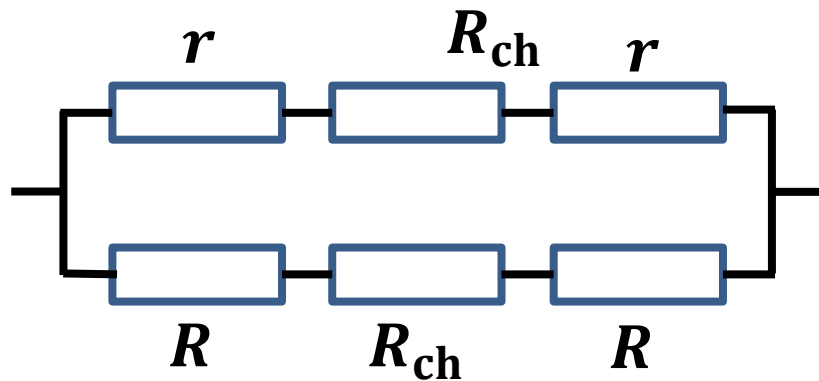
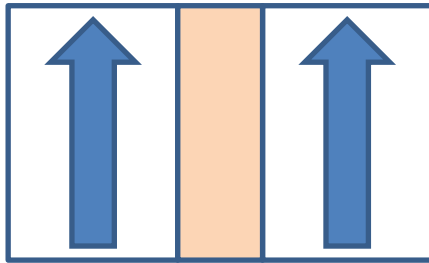


A. Fert, M.N. Baibich et al., Phys. Rev. Lett. **61**, 2472 (1988)

GMR: 2-current model

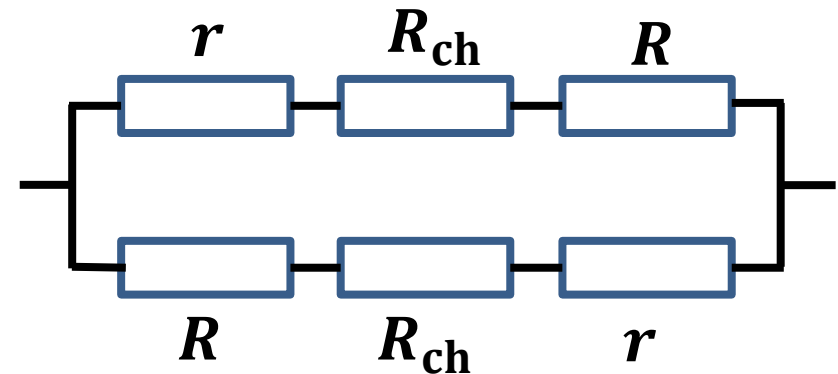
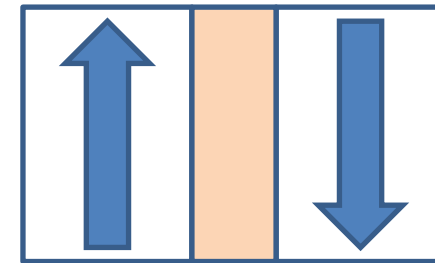
Parallel (P)

**LOW
Resistance**



Antiparallel (AP)

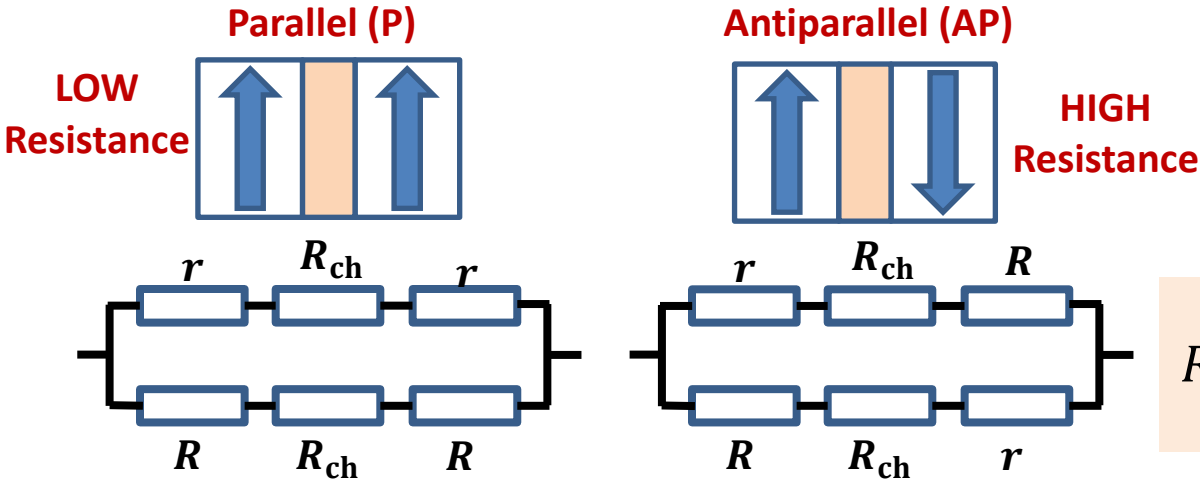
**HIGH
Resistance**



$$R_P = \left(\frac{1}{2r + R_{ch}} + \frac{1}{2R + R_{ch}} \right)^{-1}$$

$$R_{AP} = \frac{r + R + R_{ch}}{2}$$

GMR: 2-current model



$$R_{AP} = \frac{r + R + R_{ch}}{2}$$

$$R_P = \left(\frac{1}{2r + R_{ch}} + \frac{1}{2R + R_{ch}} \right)^{-1}$$

$$MR = \frac{R_{AP} - R_P}{R_P} = \frac{(R - r)^2}{4rR}$$

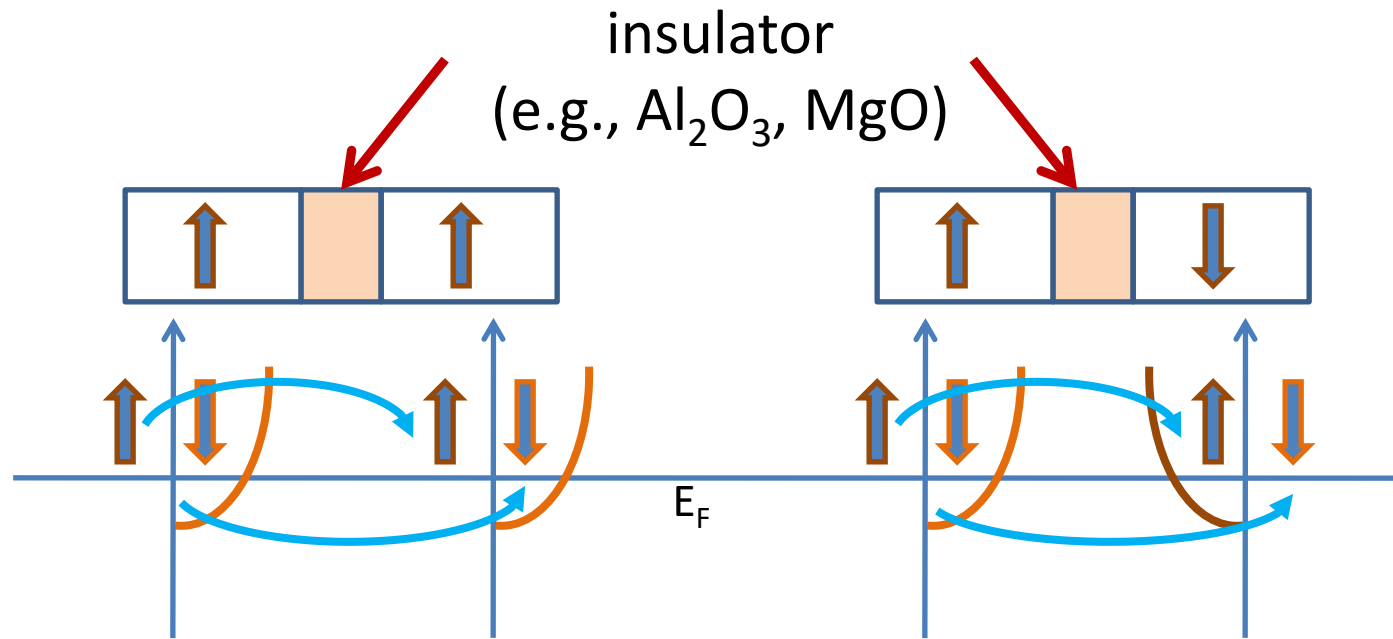
$$R_{ch} \simeq 0$$

Polarization

$$p = \frac{R - r}{R + r}$$

$$MR = \frac{p^2}{1 - p^2}$$

Tunneling Magneto-Resistance (TMR)



- Reported (1975) prior to GMR
- TMR >500% using MgO spacer

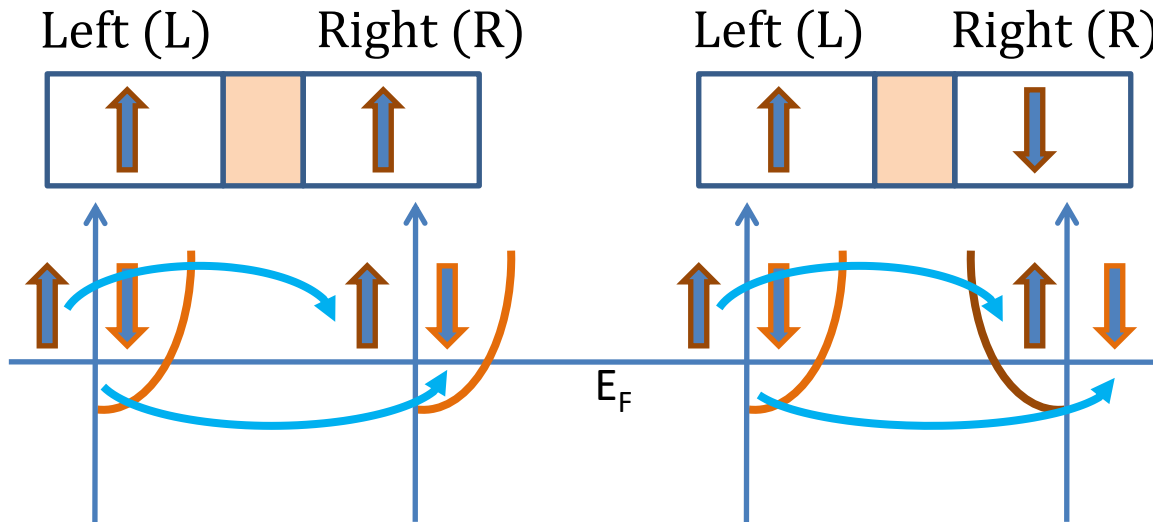
Julliere, M. Tunneling between ferromagnetic films. *Phys. Lett. A* **54**, 225–226 (1975)

Moodera, J. S. et al., *Phys. Rev. Lett.* **74**, 3273 (1995)

Mathon, J. et al., *Phys. Rev. B* **63**, 220403 (2001), Butler, W. et al., *Phys. Rev. B* **63**, 054416 (2001)

Yuasa, S. et al., *Nature Mater.* **3**, 868 (2004), Parkin, S. et al., *Nature Mater.* **3**, 862–867 (2004)

Tunneling Magneto-Resistance (TMR)



Conductance is proportional to the **density of states**

$$N_L^\uparrow, N_R^\uparrow, N_L^\downarrow, N_R^\downarrow$$

$$G^{\uparrow\uparrow} \propto N_L^\uparrow N_R^\uparrow$$

$$G^{\downarrow\downarrow} \propto N_L^\downarrow N_R^\downarrow$$

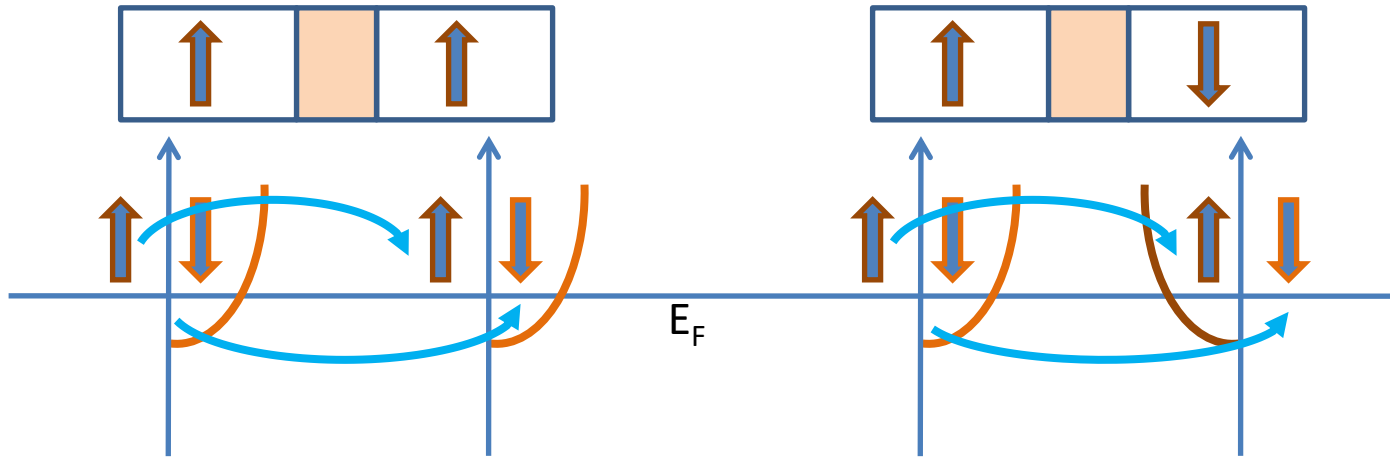
$$G^{\uparrow\downarrow} \propto N_L^\uparrow N_R^\downarrow$$

$$G^{\downarrow\uparrow} \propto N_L^\downarrow N_R^\uparrow$$

$$TMR = \frac{G_P - G_{AP}}{G_{AP}} = \frac{N_L^\uparrow N_R^\uparrow + N_L^\downarrow N_R^\downarrow - N_L^\uparrow N_R^\downarrow - N_L^\downarrow N_R^\uparrow}{N_L^\uparrow N_R^\downarrow + N_L^\downarrow N_R^\uparrow}$$

$$= \frac{(N_L^\uparrow - N_L^\downarrow)(N_R^\uparrow - N_R^\downarrow)}{\frac{1}{2} [(N_L^\uparrow - N_L^\downarrow)(N_R^\uparrow - N_R^\downarrow) - (N_L^\uparrow - N_L^\downarrow)(N_R^\uparrow - N_R^\downarrow)]}$$

Tunneling Magneto-Resistance (TMR)



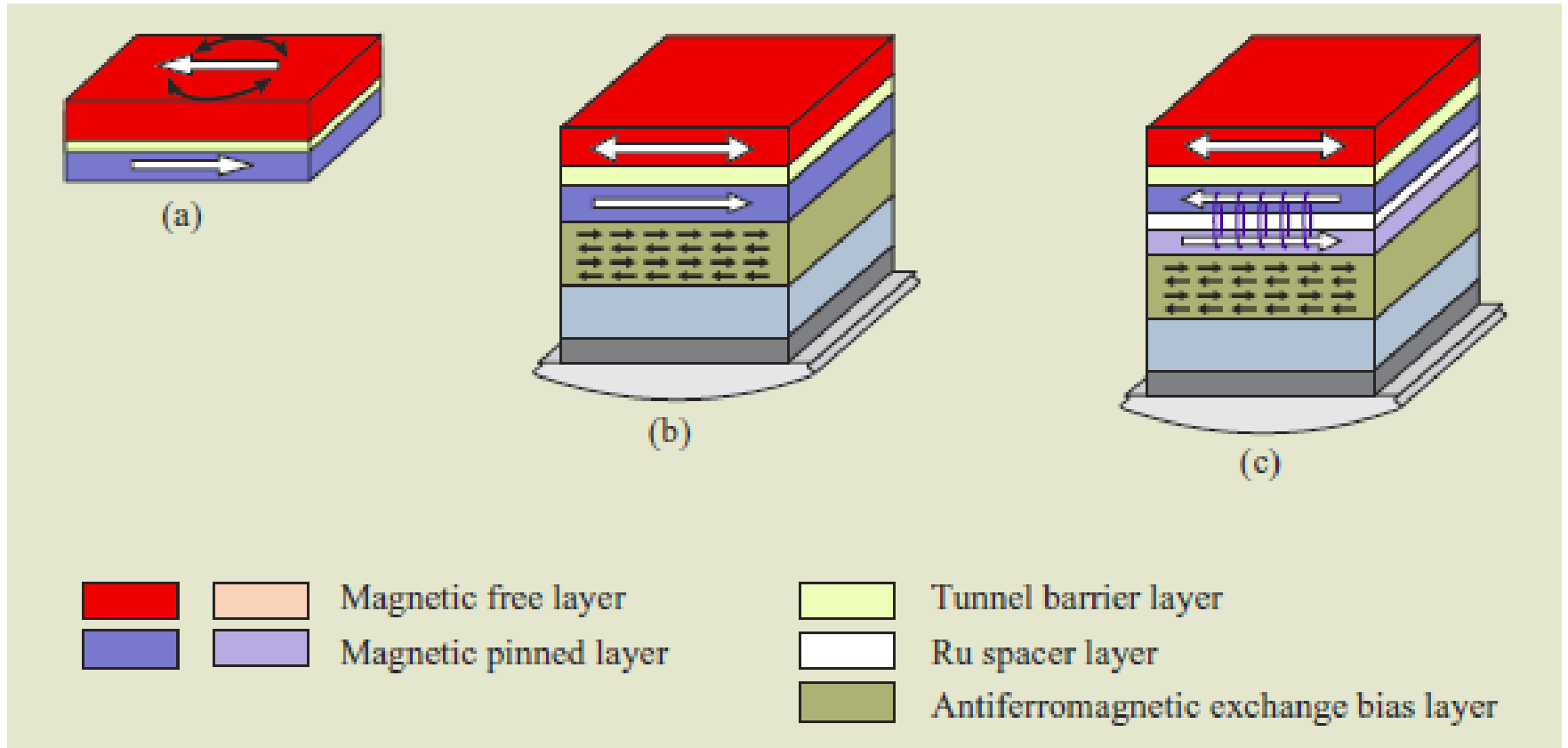
Conductance is proportional to the density of states

$$TMR = \frac{(N_L^{\uparrow} - N_L^{\downarrow})(N_R^{\uparrow} - N_R^{\downarrow})}{\frac{1}{2} [(N_L^{\uparrow} - N_L^{\downarrow})(N_R^{\uparrow} - N_R^{\downarrow}) - (N_L^{\uparrow} - N_L^{\downarrow})(N_R^{\uparrow} - N_R^{\downarrow})]}$$

$$p_{L,R} = \frac{N_{L,R}^{\uparrow} - N_{L,R}^{\downarrow}}{N_{L,R}^{\uparrow} + N_{L,R}^{\downarrow}}$$

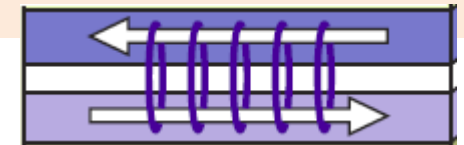
$$TMR = \frac{2p_L p_R}{1 - p_L p_R}$$

Magnetic Tunnel Junction (MTJ)



The magnetic offset caused by fields emanating from the pinned layer can be avoided by replacing a simple pinned layer with a **synthetic antiferromagnetic layer (SAF)**, a pair of ferromagnetic layers antiferromagnetically coupled through a **ruthenium (Ru) spacer layer**.

Gallagher, W. J. & Parkin, S. S. P., *IBM J. Res. Dev.* **50**, 5–23 (2006)



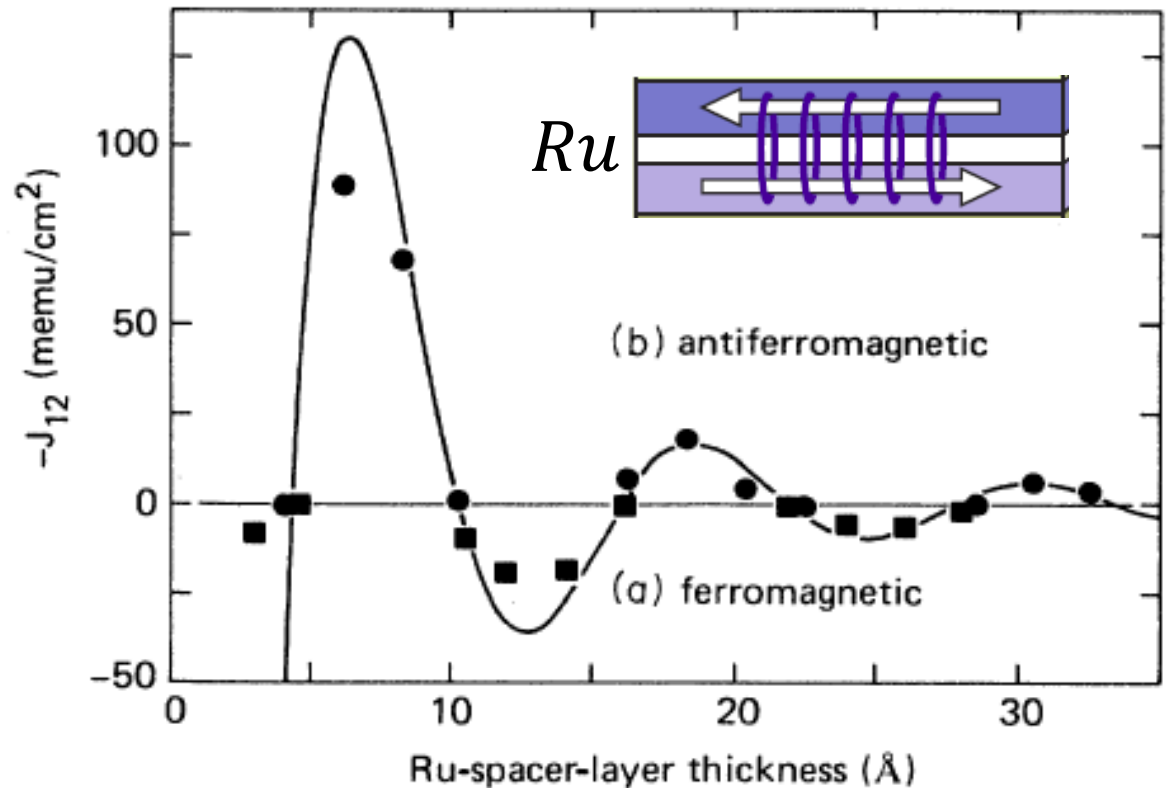
SAF: Interlayer exchange coupling

Ruderman–Kittel–Kasuya–Yosida

RKKY
interaction

Indirect
Exchange

Second-order
perturbation
theory



$$t_{Ru} = 0.8 \text{ nm}$$

$$J_{12} \propto \frac{\sin\left(\phi + \frac{2\pi t_{Ru}}{\lambda_F}\right)}{t_{Ru}^p}$$

$$\lambda_F = 11.5 \text{ \AA}$$

$$p = 1.8$$

Parkin, S. S. P. et al, Phys. Rev. B (Rapid Comm.) **44**, 7131 (1991)

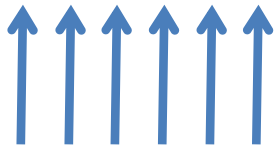
Spin waves and Magnons

Spin wave

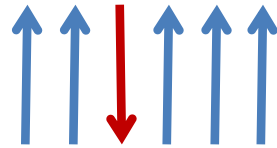
Ferromagnetic resonance

$$\frac{d\mathbf{M}}{dt} = -|\gamma|\mathbf{M} \times \mathbf{H}_{eff}$$

Neglecting damping



Ground state, U_0



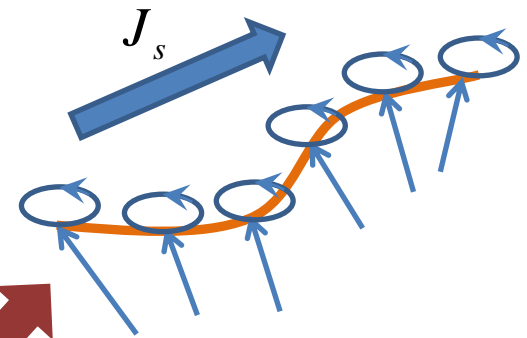
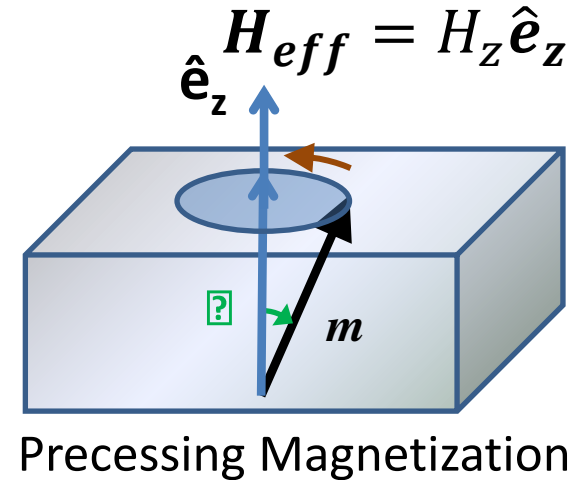
An excited state, U_1

$$U = -2J \sum_{p=1}^N \mathbf{S}_p \cdot \mathbf{S}_{p+1} \quad \mathbf{S}_p \cdot \mathbf{S}_{p+1} = S^2$$

$$U_0 = -2JNS^2$$

$$U_1 = U_0 + 8JS^2$$

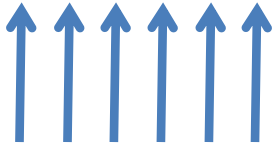
Excitation of much lower energy if all spins share the reversal



Spin-wave
spin current

**Interconnect
between devices**

Spin wave dispersion relation



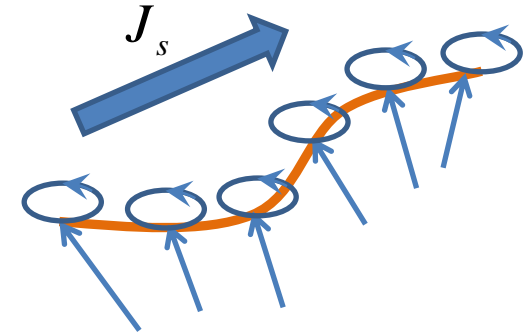
Ground state, U_0

$$U_0 = -2JNS^2$$

$$U = -2J \sum_{p=1}^N \mathbf{S}_p \cdot \mathbf{S}_{p+1}$$

Magnetic moment at site p

$$\boldsymbol{\mu}_p = -g\mu_B \mathbf{S}_p$$



**Nearest neighbor
exchange interaction**

$$-2J \mathbf{S}_p \cdot (\mathbf{S}_{p-1} + \mathbf{S}_{p+1}) = -\boldsymbol{\mu}_p \cdot \mathbf{B}_p$$

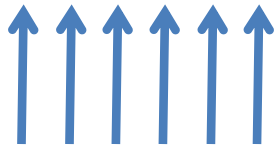
$$\Rightarrow \mathbf{B}_p = (-2J/g\mu_B) \cdot (\mathbf{S}_{p-1} + \mathbf{S}_{p+1})$$

$$\frac{d\mathbf{S}_p}{dt} = -|\gamma| \mathbf{S}_p \times \mathbf{B}_p = \frac{2J}{\hbar} (\mathbf{S}_p \times \mathbf{S}_{p-1} + \mathbf{S}_p \times \mathbf{S}_{p+1})$$

$$S_p^z = S$$

$$S_p^x, S_p^y \ll S$$

Spin wave dispersion relation



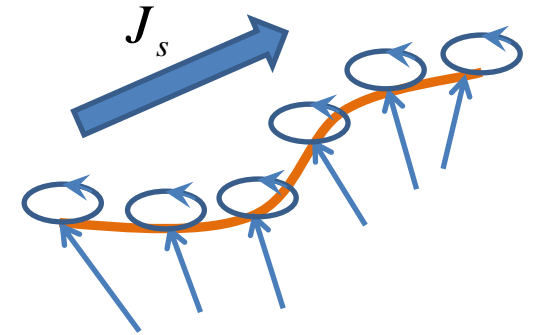
Ground state, U_0

$$U_0 = -2JNS^2$$

$$U = -2J \sum_{p=1}^N \mathbf{S}_p \cdot \mathbf{S}_{p+1}$$

$$S_p^z = S$$

$$S_p^x, S_p^y \ll S$$



$$\frac{d\mathbf{S}_p}{dt} = -|\gamma|\mathbf{S}_p \times \mathbf{B}_p = \frac{2J}{\hbar} (\mathbf{S}_p \times \mathbf{S}_{p-1} + \mathbf{S}_p \times \mathbf{S}_{p+1})$$

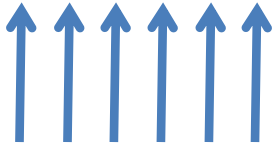
$$\frac{dS_p^x}{dt} = \frac{2J}{\hbar} \left[S_p^y (S_{p-1}^z + S_{p+1}^z) + S_p^z (S_{p-1}^y + S_{p+1}^y) \right]$$

$$\frac{dS_p^x}{dt} = \frac{2JS}{\hbar} \left[2S_p^y - S_{p-1}^y - S_{p+1}^y \right]$$

$$\frac{dS_p^z}{dt} = 0$$

$$\frac{dS_p^y}{dt} = -\frac{2JS}{\hbar} \left[2S_p^x - S_{p-1}^x - S_{p+1}^x \right]$$

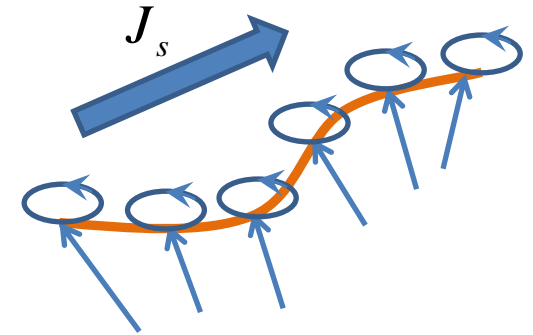
Spin wave dispersion relation



Ground state, U_0

$$U_0 = -2JNS^2$$

$$U = -2J \sum_{p=1}^N \mathbf{S}_p \cdot \mathbf{S}_{p+1}$$



a : lattice constant

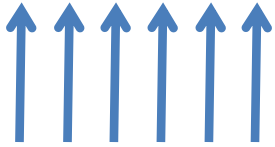
$$S_p^x = u e^{i(pka - \omega t)}$$

$$S_p^y = v e^{i(pka - \omega t)}$$

$$\frac{dS_p^x}{dt} = -\frac{2JS}{\hbar} [2S_p^x - S_{p-1}^x - S_{p+1}^x]$$

$$\begin{aligned} & u e^{i(pka - \omega t)} (-i\omega) \\ &= \frac{2JS}{\hbar} \left[2v e^{i(pka - \omega t)} - v e^{i((p-1)ka - \omega t)} - v e^{i((p+1)ka - \omega t)} \right] \\ & -i\omega u = \frac{2JS}{\hbar} [2 - e^{-ika} - e^{ika}] v = \frac{4JS}{\hbar} [1 - \cos ka] v \end{aligned}$$

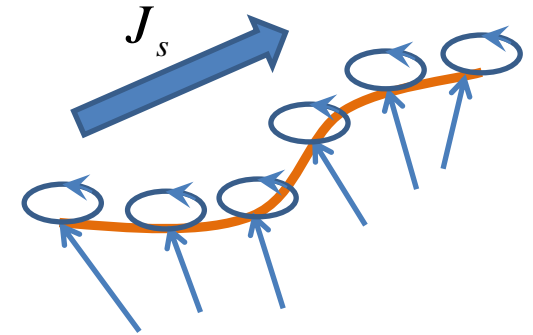
Spin wave dispersion relation



Ground state, U_0

$$U_0 = -2JNS^2$$

$$U = -2J \sum_{p=1}^N \mathbf{S}_p \cdot \mathbf{S}_{p+1}$$



a : lattice constant

$$S_p^x = u e^{i(pka - \omega t)}$$

$$S_p^y = v e^{i(pka - \omega t)}$$

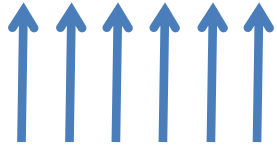
$$\frac{dS_p^x}{dt} = \frac{2JS}{\hbar} [2S_p^y - S_{p-1}^y - S_{p+1}^y]$$

$$\frac{dS_p^y}{dt} = -\frac{2JS}{\hbar} [2S_p^x - S_{p-1}^x - S_{p+1}^x]$$

$$-i\omega u = \frac{2JS}{\hbar} [2 - e^{-ika} - e^{ika}]v = \frac{4JS}{\hbar} (1 - \cos ka)v$$

$$-i\omega v = -\frac{2JS}{\hbar} [2 - e^{-ika} - e^{ika}]u = -\frac{4JS}{\hbar} (1 - \cos ka)u$$

Spin wave dispersion relation



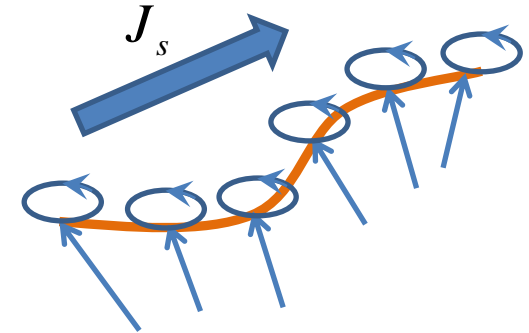
Ground state, U_0

$$U_0 = -2JNS^2$$

a : lattice constant

$$S_p^x = u e^{i(pka - \omega t)}$$

$$S_p^y = v e^{i(pka - \omega t)}$$



$$-i\omega u = \frac{2JS}{\hbar} [2 - e^{-ika} - e^{ika}] v = \frac{4JS}{\hbar} (1 - \cos ka) v$$

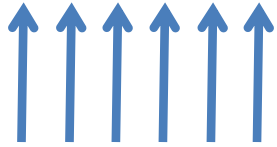
$$-i\omega v = -\frac{2JS}{\hbar} [2 - e^{-ika} - e^{ika}] u = -\frac{4JS}{\hbar} (1 - \cos ka) u$$

$$\begin{vmatrix} i\omega & \frac{4JS}{\hbar} (1 - \cos ka) \\ -\frac{4JS}{\hbar} (1 - \cos ka) & i\omega \end{vmatrix} = 0$$

$$\omega = \frac{4JS}{\hbar} (1 - \cos ka)$$

$$v = -iu$$

Spin wave dispersion relation



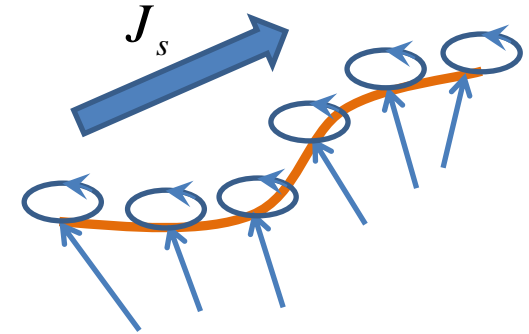
Ground state, U_0

$$U_0 = -2JNS^2$$

a : lattice constant

$$S_p^x = u e^{i(pka - \omega t)}$$

$$S_p^y = v e^{i(pka - \omega t)}$$



$$\omega = \frac{4JS}{\hbar} (1 - \cos ka)$$

$$v = -iu$$

Taking real parts

$$S_p^x = u \cos(pka - \omega t)$$

$$S_p^y = u \sin(pka - \omega t)$$

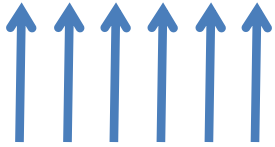
Circular
precession
about z-axis

$$ka \ll 1$$

$$\omega = \frac{4JSa^2}{\hbar} k^2 = Dk^2$$

D can be determined from
spin-wave resonance

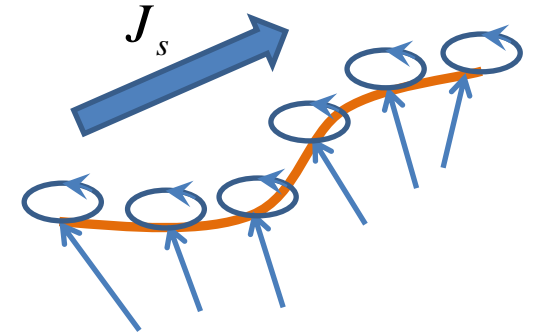
Magnon



Ground state, U_0
 $U_0 = -2JNS^2$

a : lattice constant

$$\omega = \frac{4JS}{\hbar} (1 - \cos ka)$$



Circular
precession
about z-axis

$ka \ll 1$

$$S_p^x = u \cos(pka - \omega t)$$

$$S_p^y = u \sin(pka - \omega t)$$

$$\omega = \frac{4JSa^2}{\hbar} k^2 = Dk^2$$

D can be determined from
spin-wave resonance

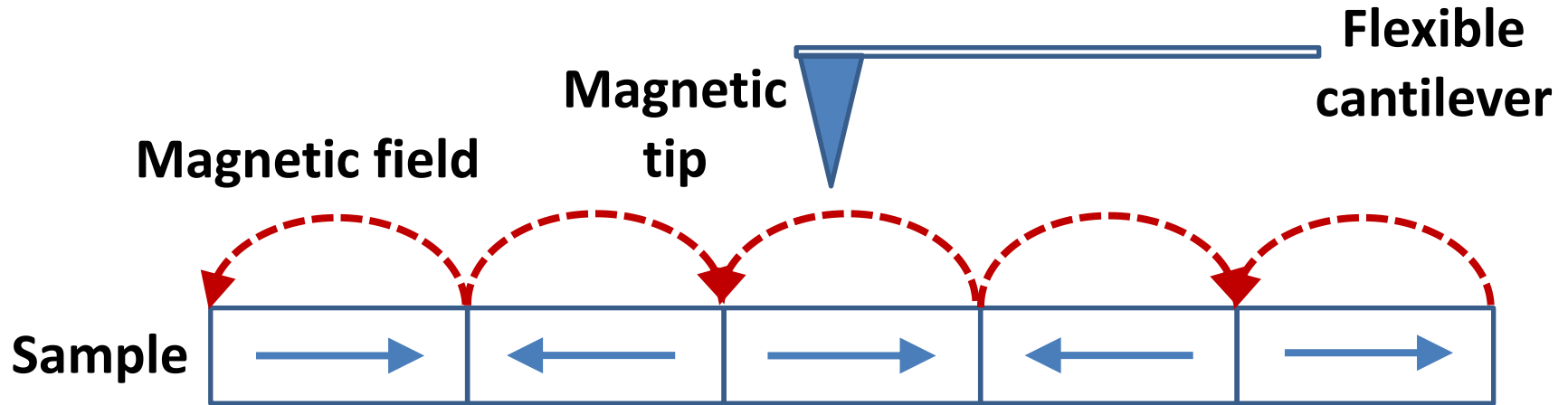
Magnon: Quantized spin waves

The energy of a mode of
frequency ω_k with n_k magnons

$$\epsilon_k = \left(n_k + \frac{1}{2} \right) \hbar \omega_k$$

Magnetic Force Microscopy

Magnetic Force Microscopy (MFM)



Forces from the magnetic sample act on the tip and cause a deflection

An image is formed by scanning sample relative to the tip

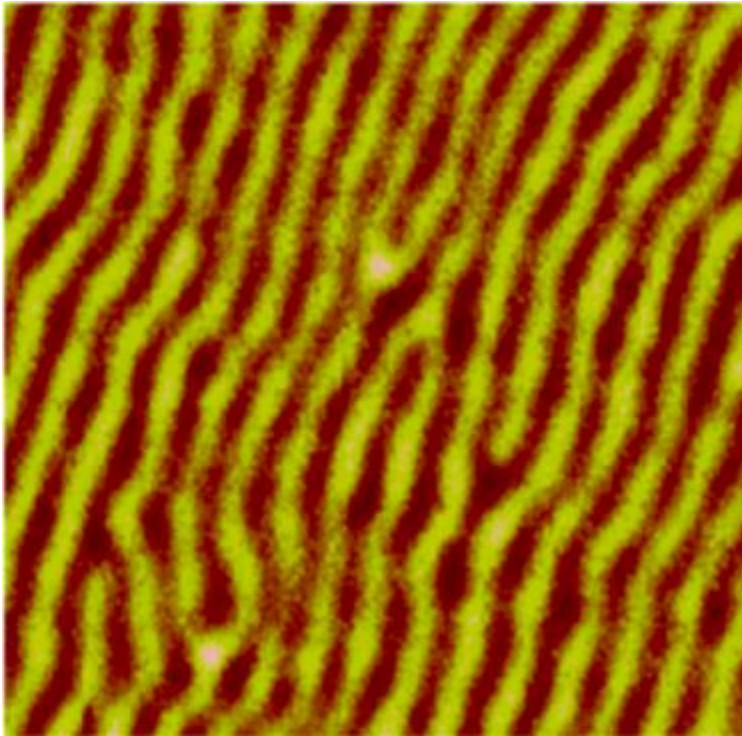
High resolution: $\sim 10\text{-}100\text{ nm}$

Contact mode: Tip is very near to sample ($\sim 0.1\text{ nm}$)

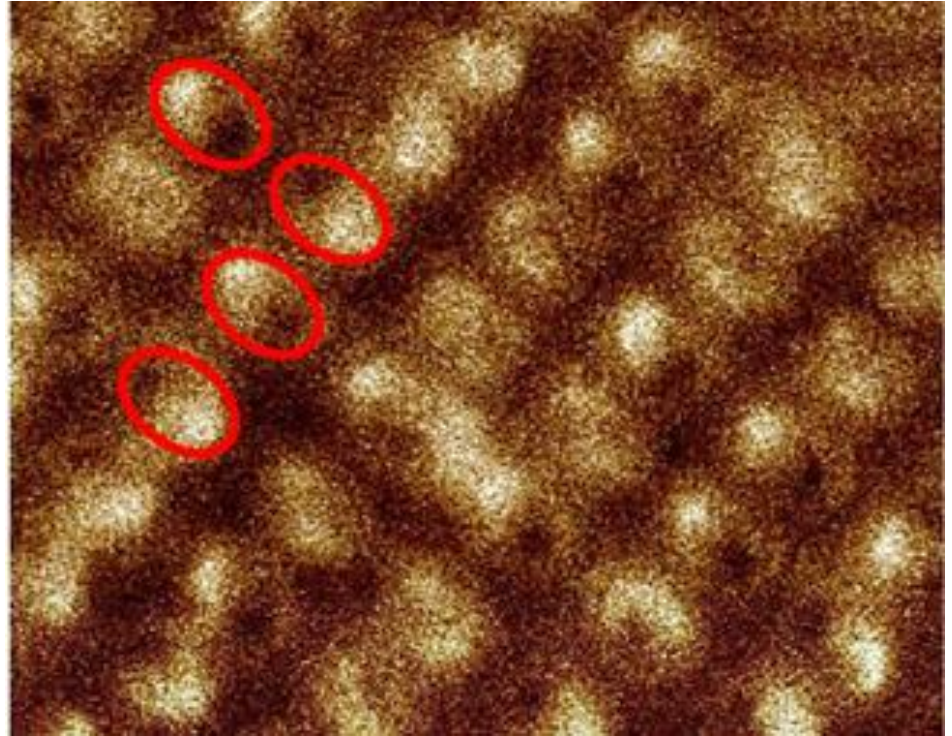
Tapping mode (AC): Probe comes near the sample momentarily to avoid damaging the sample and breaking of the tip that may happen in contact mode

Single-domain and Multi-domain

Multi-domain



Single-domain



Magnetic force microscopy (MFM) images