# paramagpy Documentation

Release 0.43

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# **CONTENTS**

1	Introduction	2
2	Features	3
3	Documentation	4
4	Citing paramagpy	5
5	Contents	6
	5.1 Installation Guide	6
	5.2 Examples	6
	5.3 Graphic User Interface (GUI)	33
	5.4 NMR Software Macros	34
	5.5 Reference Guide	36
Рy	ython Module Index	82

Release 0.43

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CONTENTS 1

# **INTRODUCTION**

paramagpy is a python module for calculating paramagnetic effects in NMR spectra of proteins. This currently includes fitting of paramagnetic susceptibility tensors to experimental data associated with pseudocontact shifts (PCS) residual dipolar couplings (RDC), paramagnetic relaxation enhancements (PRE) and cross-correlated relaxation (CCR). A GUI allows easy viewing of data and seamless transition between PCS/RDC/PR/CCR calculations.



Fig. 1: Please, not the eyes! - Canberra cyclist

#### **CHAPTER**

# **TWO**

# **FEATURES**

- Support for PDB protein structures with models
- Combined SVD gridsearch and gradient descent algorithms for solving PCS tensors
- Optional fitting of reference offset parameter for PCS datasets
- Support for Residual Anisotropic Chemical Shielding (RACS) and Residual Anisotropic Dipolar Shielding (RADS) corrections to PCS
- Lanthanide parameter templates available
- Plotting of correlation between experiment/calculated values
- Plotting of tensor isosurfaces compatible with PyMol
- Q-factor calculations
- Error analysis of tensor fit quality Monte-Carlo or Bootstrap methods
- Optimisation of multiple PCS/PRE/CCR datasets to a common position
- Unique tensor representation compatible with Numbat (program)
- Fitting of RDC tensor by SVD algorithm
- PRE calculations by Solomon and Curie spin mechanisms
- CSA cross-correlation correction to PRE calculations
- Dipole-dipole/Curie spin cross-correlated relaxation calculations
- Fitting of tensor parameters to PRE/CCR data
- Macro scripts for integration with CCPNMR and Sparky

# **CHAPTER**

# **THREE**

# **DOCUMENTATION**

• https://henryorton.github.io/paramagpy/

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ΕΩI	

# **CITING PARAMAGPY**

Hopefully paramagpy will be published soon the journal of biomolecular NMR

**CHAPTER** 

**FIVE** 

# **CONTENTS**

# 5.1 Installation Guide

# 5.1.1 Requirements

Paramagpy is written for python 3. It requires packages:

- NumPy
- SciPy
- matplotlib
- BioPython

# 5.1.2 Unix/OSX Installation

Install directly using pip:

```
$ pip install paramagpy
```

Or, download the source code and run:

```
$ python setup.py install
```

within the source directory.

# 5.1.3 Windows Installation

Paramagpy has never been tested on windows, but theoretically it should work. Good luck!

# 5.1.4 Running the GUI

Once you have installed paramagpy, see Graphic User Interface (GUI) for how to run the GUI.

# 5.2 Examples

# 5.2.1 PCS data

#### Fit Tensor to PCS Data

This example shows how to fit a  $\Delta\chi$ -tensor to experimental PCS data for the protein calbindin D9k. These data contain amide 1H and 15N chemical shifts between diamagnetic and paramagnetic states with the lanthanide Er3+ bound.

#### **Downloads**

- Download the data files 4icbH\_mut.pdb and calbindin\_Er\_HN\_PCS.npc from here:
- Download the script pcs fit.py

#### **Script + Explanation**

Firstly, the necessary modules are imported from paramagpy.

```
from paramagpy import protein, fit, dataparse, metal
```

The protein is then loaded from a PDB file using <code>paramagpy.protein.load\_pdb()</code> into the variable <code>prot</code>. This returns a <code>CustomStructure</code> object which is closely based on the <code>Structure</code> object from BioPython and contains the atomic coordinates. The object, and how to access atomic coordinates is discussed at this link.

```
# Load the PDB file
prot = protein.load_pdb('../data_files/4icbH_mut.pdb')
```

The PCS data is then loaded from a .npc file using the function <code>paramagpy.dataparse.read\_pcs()</code> into the variable <code>rawData</code>. This is a dictionary of (PCS, Error) tuples which may be accessed by <code>rawData[(seq, atom)]</code> where <code>seq</code> is an integer specifying the sequence and <code>atom</code> is the atom name e.g (3, 'HA'). Note that these should match the corresponding sequence and atom in the PDB file.

```
# Load the PCS data
rawData = dataparse.read_pcs('../data_files/calbindin_Er_HN_PCS.npc')
```

To associate the experimental PCS value with atoms of the PDB structure, the method paramagpy.protein. CustomStructure.parse() is called on rawData. The new list parsedData contains elements [atom, PCS, Error], where atom is now an atom object from the PDB.

```
# Associate PCS data with atoms of the PDB parsedData = prot.parse(rawData)
```

An initial  $\Delta \chi$ -tensor is defined by initialising a paramagpy.metal.Metal object. The initial position is known to be near the binding site, which is set to the CA atom of residue 56. Note that the position attribute is always in Angstrom units.

```
# Define an initial tensor
mStart = metal.Metal()

# Set the starting position to an atom close to the metal
mStart.position = prot[0]['A'][56]['CA'].position
```

A quick gridsearch is conducted in a sphere of 10 Angstrom with 10 points per radius using the function <code>paramagpy.fit.svd\_gridsearch\_fit\_metal\_from\_pcs()</code>. This requires two lists containing the starting metals mStart and parsed experimental data parsedData. This function return lists containing a new fitted metal object, the calculated PCS values from the fitted model, and the Q-factor.

This is then refined using a non-linear regression gradient descent with the function paramagpy.fit.  $nlr_fit_metal_from_pcs().$ 

```
# Refine the tensor using non-linear regression
mFit, calc, qfac = fit.nlr_fit_metal_from_pcs(mGuess, [parsedData])
```

The fitted tensor parameters are saved by calling the method paramagpy.metal.Metal.save(). Alterntaively they may be displayed using print (mFit[0].info())

```
# Save the fitted tensor to file
mFit[0].save('calbindin_Er_HN_PCS_tensor.txt')
```

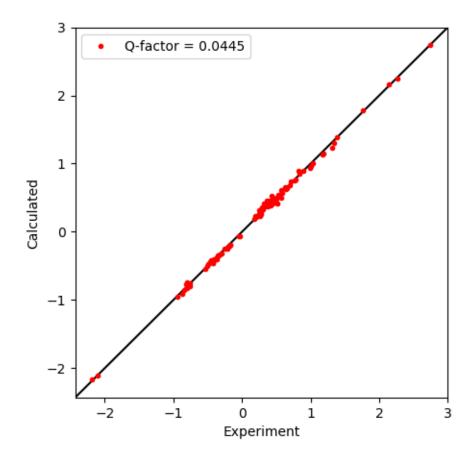
Output: [calbindin\_Er\_HN\_PCS\_tensor.txt]

```
| 1E-32 m^3 : -8.688
     | 1E-32 m^3 :
                   -4.192
rh
       1E-10 m :
                  25.517
Х
     1E-10 m :
                   8.652
У
     1E-10 \ m :
                   6.358
Z
     deg: 116.011
а
     deg: 138.058
     43.492
g
     deg :
mueff |
           Bm :
                   0.000
shift |
          ppm :
                   0.000
В0
     T :
                  18.790
                 298.150
temp |
            K :
                   0.000
t1e
     ps :
                    0.000
taur |
           ns :
```

These experimental/calculated PCS values are then plotted in a correlation plot to assess the fit. This is achieved using standard functions of the plotting module matplotlib.

```
#### Plot the correlation ####
from matplotlib import pyplot as plt
fig, ax = plt.subplots(figsize=(5,5))
# Unpack the experimental values
atoms, experiment, errors = zip(*parsedData)
# Plot the data
ax.plot(experiment, calc[0], marker='o', lw=0, ms=3, c='r',
        label="Q-factor = \{:5.4f\}".format(qfac[0]))
# Plot a diagonal
1, h = ax.get_xlim()
ax.plot([1,h],[1,h],'-k',zorder=0)
ax.set xlim(l,h)
ax.set_ylim(l,h)
# Make axis labels and save figure
ax.set_xlabel("Experiment")
ax.set_ylabel("Calculated")
ax.legend()
fig.savefig("pcs_fit.png")
```

Output: [pcs\_fit.png]



#### Plot PCS isosurface (PyMol view)

This example shows how to plot the PCS isosurface of a fitted  $\Delta \chi$ -tensor for data from the example *Fit Tensor to PCS Data*. The isosurface can be viewed in PyMol.

#### **Downloads**

- Download the data files 4icbH\_mut.pdb and calbindin\_Er\_HN\_PCS\_tensor.txt from here:
- Download the script pcs\_plot\_isosurface.py

# **Explanation**

The protein and tensor are loaded as described previously in.

The isosurface files are generated using the function <code>paramagpy.metal.Metal.isomap()</code>. The contour level can be chosen by setting the <code>isoval</code> argument. A larger <code>density</code> value will result in a smoother surface. This function writes two files <code>isomap.pml</code> and <code>isomap.pml.ccp4</code> which are the PyMol script and PCS grid files respectively.

The isosurface can be displayed by executing pymol isomap.pml from a terminal, or by selecting File>Run and navigating to the script isomap.pml.

#### **Script**

[pcs\_plot\_isosurface.py]

```
from paramagpy import protein, fit, dataparse, metal

# Load the PDB file
prot = protein.load_pdb('../data_files/4icbH_mut.pdb')

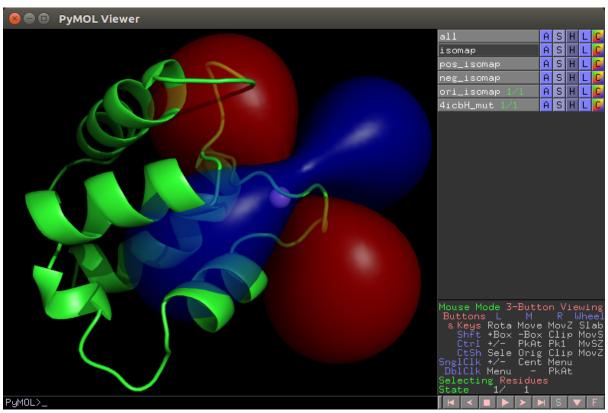
# Load the fitted tensor
met = metal.load_tensor('../data_files/calbindin_Er_HN_PCS_tensor.txt')

# Plot the isosurface to be opened in PyMol
met.isomap(prot.id, density=1, isoval=1.0)
```

#### **Output**

#### PyMol view of isosurface

[pcs\_plot\_isosurface.png]



# Fit multiple PCS datasets to common position

This example shows how to fit multiple  $\Delta \chi$ -tensors to their respective datasets with a common position, but varied magnitude and orientation. This may arise if several lanthanides were investigated at the same binding site, and the data may be used simultaneously to fit a common position. Data from several PCS datasets for calbindin D9k were used here, and is a generalisation of the previous example: Fit Tensor to PCS Data.

#### **Downloads**

- Download the data files 4icbH\_mut.pdb, calbindin\_Tb\_HN\_PCS.npc, calbindin\_Er\_HN\_PCS.npc and calbindin\_Yb\_HN\_PCS\_tensor.txt from here:
- Download the script pcs\_fit\_multiple.py

#### **Explanation**

The protein and PCS datasets are loaded and parsed. These are placed into a list parsedData, for which each element is a PCS dataset of a given lanthanide.

The two fitting functions:

- paramagpy.fit.svd\_gridsearch\_fit\_metal\_from\_pcs()
- paramagpy.fit.nlr\_fit\_metal\_from\_pcs()

can accept a list of metal objects and a list of datasets with arbitrary size. If this list contains more than one element, fitting will be performed to a common position. The starting position is taken only from the first metal of the list.

After fitting, a list of fitted metals is returned. The fitted tensor are then written to files and a correlation plot is made.

#### **Script**

[pcs\_fit\_multiple.py]

```
from paramagpy import protein, fit, dataparse, metal
# Load the PDB file
prot = protein.load_pdb('../data_files/4icbH_mut.pdb')
# Load the PCS data
rawData1 = dataparse.read_pcs('../data_files/calbindin_Tb_HN_PCS.npc')
rawData2 = dataparse.read_pcs('../data_files/calbindin_Er_HN_PCS.npc')
rawData3 = dataparse.read_pcs('../data_files/calbindin_Yb_HN_PCS.npc')
# Associate PCS data with atoms of the PDB
parsedData = []
for rd in [rawData1, rawData2, rawData3]:
       parsedData.append(prot.parse(rd))
# Make a list of starting tensors
mStart = [metal.Metal(), metal.Metal(), metal.Metal()]
# Set the starting position to an atom close to the metal
mStart[0].position = prot[0]['A'][56]['CA'].position
# Calculate initial tensors from an SVD gridsearch
mGuess = fit.svd_gridsearch_fit_metal_from_pcs(
       mStart, parsedData, radius=10, points=10)
# Refine the tensors using non-linear regression
fitParameters = ['x','y','z','ax','rh','a','b','g']
mFit = fit.nlr_fit_metal_from_pcs(mGuess, parsedData, fitParameters)
# Save the fitted tensors to files
for name, metal in zip(['Tb','Er','Yb'], mFit):
       metal.save("tensor_{}.txt".format(name))
```

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```
# Make experimental and calculated PCS lists
exp = []
cal = []
for metal, data in zip(mFit, parsedData):
       ex = []
        ca = []
        for atom, exp_pcs, error in data:
                ex.append(exp_pcs)
                ca.append(metal.atom_pcs(atom))
        exp.append(ex)
        cal.append(ca)
#### Plot the correlation ####
from matplotlib import pyplot as plt
fig, ax = plt.subplots(figsize=(5,5))
# Plot the data
for e, c, name, colour in zip(exp, cal, ['Tb','Er','Yb'],['r','g','b']):
       qfactor = fit.qfactor(e,c)
        ax.plot(e, c, marker='o', lw=0, ms=1, c=colour,
                label="\{0:\} - \{1:5.3f\}".format(name, qfactor))
# Plot a diagonal
l, h = ax.get_xlim()
ax.plot([1,h],[1,h],'-k',zorder=0)
ax.set_xlim(l,h)
ax.set_ylim(l,h)
# Axis labels
ax.set_xlabel("Experiment")
ax.set_ylabel("Calculated")
ax.legend()
fig.savefig("pcs_fit_multiple.png")
```

# **Outputs**

#### Tb fitted tensor

[tensor\_Tb.txt]

```
| 1E-32 m^3 : 31.096
    | 1E-32 m^3 : 12.328
    | 1E-10 m : 25.937
       1E-10 m : 9.481
У
       1E-10 \ m :
                  6.597
        deg : 151.053
а
          deg: 152.849
b
          deg: 69.821
g
                  0.000
           Bm :
mueff |
shift |
          ppm :
                   0.000
          T :
K :
                  18.790
                298.150
temp
    ps :
                  0.000
```

#### Er fitted tensor

```
[tensor_Er.txt]
```

```
| 1E-32 m^3 :
                      -8.421
rh
      | 1E-32 \text{ m}^3 :
                      -4.886
                     25.937
         1E-10 \ m :
Х
                     9.481
6.597
         1E-10 \ m :
У
         1E-10 \ m:
                    126.015
             deg :
а
                     142.899
b
             deg :
             deg :
                     41.040
mueff |
             Bm :
                      0.000
shift |
                      0.000
             ppm :
В0
              T :
                      18.790
temp |
              K :
                    298.150
t1e
             ps :
                       0.000
```

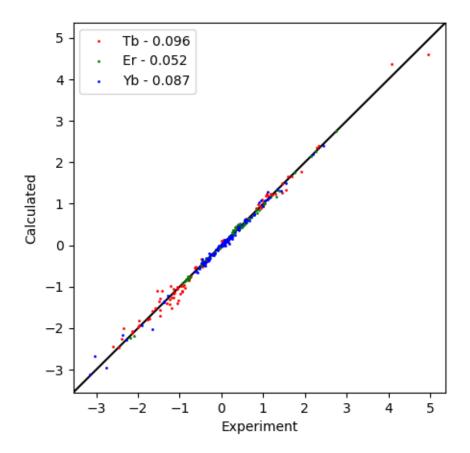
# Yb fitted tensor

# [tensor\_Yb.txt]

```
| 1E-32 m^3 :
                    -5.392
ax
     | 1E-32 m^3 :
                    -2.490
rh
     | 1E-10 m :
                   25.937
Х
       1E-10 \ m :
                    9.481
У
       1E-10 \ m :
                    6.597
           deg: 129.650
            deg: 137.708
b
           deg: 88.796
                    0.000
            Bm :
mueff |
shift |
                     0.000
            ppm :
В0
            T :
                    18.790
             K :
                   298.150
temp
t1e
                     0.000
             ps :
```

#### Correlation Plot

[pcs\_fit\_multiple.png]



#### Fit Tensor to PDB with Models

This example shows how to fit a  $\Delta\chi$ -tensor to experimental PCS data using an NMR structure that contains many models. The tensor can be fit to ensemble averaged PCS values, or to individual models. An ensemble averaged PCS is the mean calculated PCS of all models. No structural averages are ever taken.

Data for calbindin D9k are used as in the previous example Fit Tensor to PCS Data.

### **Downloads**

- Download the data files 2bcb.pdb and calbindin\_Er\_HN\_PCS.npc from here:
- Download the script pcs\_fit\_models.py

# Script + Explanation

Firstly, the standard preamble and loading of data.

```
from paramagpy import protein, fit, dataparse, metal

# Load data
prot = protein.load_pdb('.../data_files/2bcb.pdb')
rawData = dataparse.read_pcs('.../data_files/calbindin_Er_HN_PCS.npc')
mStart = metal.Metal()
mStart.position = prot[0]['A'][56]['CA'].position
```

The default method of fitting is to minimise the difference to the experimental values of the ensemble average of the calculated values. The default behaviour is to average atoms with the same serial number in the PDB file. To manipulate ensemble averaging, you can specify the <code>sumIndices</code> argument of any fitting function such as <code>paramagpy.fit.nlr\_fit\_metal\_from\_pcs()</code>. This array contains common integers for corresponding atoms to be averaged. To remove ensemble averaging completely, just specify a list of unique integers with length equal to the data such as <code>sumIndices=list(range(len(parsedData)))</code>.

If desired, you can also fit a separate tensor to each model of the PDB and the compare them. In this case, we loop over each model, fit a tensor, then keep the one with the smallest Q-factor. Selected models can be parsed by specifying the models argument of paramagpy.protein.CustomStructure.parse().

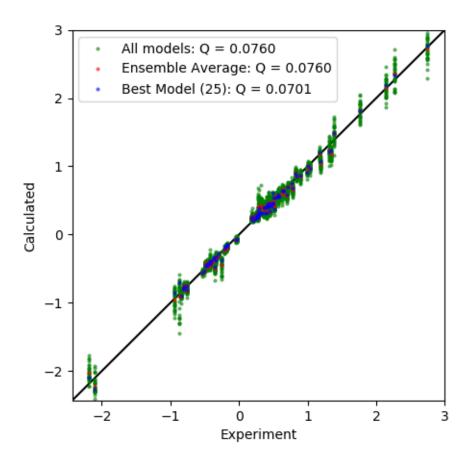
Finally we plot three sets of data:

- The ensemble average fit calculated for each model (green)
- The ensemble average of the calculated values of the ensemble fit (red)
- The best fitting single model (blue)

Note that to calculate the ensemble average of the calculated values we use the function <code>paramagpy.fit.ensemble\_average()</code>. This can take any number of arguments, and will average values based on common serial numbers of the list of atoms in the first argument.

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Output: [pcs\_fit\_models.png]



### **Constrained Fitting**

This example shows how to fit a  $\Delta\chi$ -tensor with constraints applied. The two cases here constrain position to fit a tensor to a known metal ion position form an X-ray structure, and fit an axially symmetric tensor with only 6 of the usual 8 parameters.

#### **Downloads**

• Download the data files 4icbH\_mut.pdb and calbindin\_Er\_HN\_PCS.npc from here:

• Download the script pcs\_fit\_constrained.py

### Script + Explanation

The necessary modules are imported and data is loaded

```
from paramagpy import protein, fit, dataparse, metal

# Load data
prot = protein.load_pdb('../data_files/4icbH_mut.pdb')
rawData = dataparse.read_pcs('../data_files/calbindin_Er_HN_PCS.npc')
parsedData = prot.parse(rawData)
mStart = metal.Metal()
```

The calcium ion from the X-ray structure is contained in a heteroatom of the PDB file. We set the starting position of the tensor to this position.

```
# Set the starting position to Calcium ion heteroatom in PDB mStart.position = prot[0]['A'][('H_ CA', 77, ' ')]['CA'].position
```

To fit the anisotropy and orientation without position, the linear PCS equation can be solved analytically by the SVD gridsearch method but using only one point with a radius of zero. This tensor is then saved.

Output: [pcs\_fit\_constrained.png]

```
| 1E-32 m^3 :
                      -8.152
      | 1E-32 \text{ m}^3 :
rh
                      -4.911
                     25.786
Х
         1E-10 m :
         1E-10 \ m:
                       9.515
У
         1E-10 \ m :
                       6.558
Z
                    125.841
             deg :
а
                    142.287
h
             deg :
                     41.758
             deg :
q
mueff |
                      0.000
             Bm :
                      0.000
shift |
             ppm :
В0
             T :
                     18.790
              K: 298.150
temp
     t1e
              ps :
                       0.000
```

To fit an axially symmetric tensor, we can used the Non-linear regression method and specify exactly which parameters we want to fit. This will be the axiality ax, two Euler angles b and g and the position coordinates. Note that in the output, the rhombic rh and alpha a parameters are redundant.

Output: [pcs\_fit\_constrained.png]

```
ax | 1E-32 m<sup>3</sup>: 9.510

rh | 1E-32 m<sup>3</sup>: 0.000

x | 1E-10 m: 24.948
```

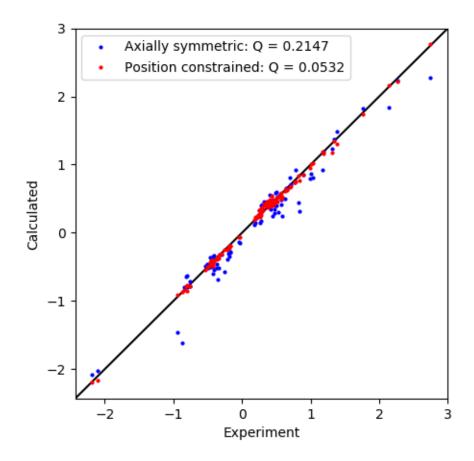
(continues on next page)

```
1E-10 m : 8.992
                  3.205
        1E-10 \ m:
          deg :
                  0.000
b
          deg: 134.697
          deg: 180.000
                  0.000
mueff |
           Bm :
shift |
                  0.000
          ppm :
В0
                  18.790
            T :
temp
            K :
                298.150
    t1e
           ps :
                  0.000
```

#### Finally we plot the data.

```
#### Plot the correlation ####
from matplotlib import pyplot as plt
fig, ax = plt.subplots(figsize=(5,5))
# Unpack the experimental values
atoms, experiment, errors = zip(*parsedData)
# Plot the data
ax.plot(experiment, calc[0], marker='o', lw=0, ms=2, c='r',
       label="Position constrained: Q = {:5.4f}".format(qfac[0]))
ax.plot(experiment, calcAx[0], marker='o', lw=0, ms=2, c='b',
       label="Axially symmetric: Q = \{:5.4f\}".format(qfacAx[0]))
# Plot a diagonal
l, h = ax.get_xlim()
ax.plot([1,h],[1,h],'-k',zorder=0)
ax.set_xlim(l,h)
ax.set_ylim(l,h)
# Make axis labels and save figure
ax.set_xlabel("Experiment")
ax.set_ylabel("Calculated")
ax.legend()
fig.savefig("pcs_fit_constrained.png")
```

Output: [pcs\_fit\_constrained.png]



#### Fit a tensor to PCS data with uncertainties

This example shows how to conduct a weighted fit of a  $\Delta \chi$ -tensor to experimental PCS data with experimental errors.

#### **Downloads**

- Download the data files 4icbH\_mut.pdb and calbindin\_Er\_HN\_PCS\_errors.npc from here:
- Download the script pcs\_fit\_error.py

#### Script + Explanation

This script follows very closely the script *Fit Tensor to PCS Data*. The only difference being that errors are included in the fourth column of the .npc file and errorbars are included in the plotting routine.

```
from paramagpy import protein, fit, dataparse, metal

# Load the PDB file
prot = protein.load_pdb('../data_files/4icbH_mut.pdb')

# Load the PCS data
rawData = dataparse.read_pcs('../data_files/calbindin_Er_HN_PCS_errors.npc')

# Associate PCS data with atoms of the PDB
```

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```
parsedData = prot.parse(rawData)
# Define an initial tensor
mStart = metal.Metal()
# Set the starting position to an atom close to the metal
mStart.position = prot[0]['A'][56]['CA'].position
# Calculate an initial tensor from an SVD gridsearch
mGuess, calc, qfac = fit.svd_gridsearch_fit_metal_from_pcs(
        [mStart],[parsedData], radius=10, points=10)
# Refine the tensor using non-linear regression
mFit, calc, qfac = fit.nlr_fit_metal_from_pcs(mGuess, [parsedData])
# Save the fitted tensor to file
mFit[0].save('calbindin_Er_HN_PCS_tensor_errors.txt')
#### Plot the correlation ####
from matplotlib import pyplot as plt
fig, ax = plt.subplots(figsize=(5,5))
# Unpack the experimental values
atoms, experiment, errors = zip(*parsedData)
# Plot the data
ax.errorbar(experiment, calc[0], xerr=errors, fmt='o', c='r', ms=2,
        ecolor='k', capsize=3, label="Q-factor = {:5.4f}".format(qfac[0]))
# Plot a diagonal
l, h = ax.get_xlim()
ax.plot([1,h],[1,h],'grey',zorder=0)
ax.set_xlim(l,h)
ax.set_ylim(l,h)
# Make axis labels and save figure
ax.set_xlabel("Experiment")
ax.set_ylabel("Calculated")
ax.legend()
fig.savefig("pcs_fit_error.png")
```

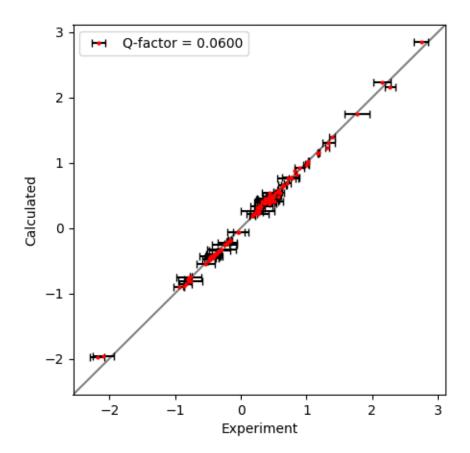
#### The fitted tensor:

Output: [calbindin\_Er\_HN\_PCS\_tensor\_errors.txt]

```
| 1E-32 m^3 : -8.012
aх
     | 1E-32 m^3 :
                   -4.125
rh
       1E-10 \ m :
                  24.892
X
        1E-10 m :
                   8.456
У
       1E-10 \ m :
                   6.287
Z
а
           deg: 112.440
b
           deg: 135.924
          deg: 46.210
g
mueff |
           Bm :
                   0.000
shift |
          ppm :
                   0.000
            T :
                  18.790
В0
            K: 298.150
temp |
           ps : 0.000
t.1e
           ns :
                    0.000
taur
```

#### And correlation plot:

Output: [pcs\_fit\_error.png]



Fit to PCS data with offset, RACS and RADS corrections

# 5.2.2 RDC data

#### Fit Tensor to RDC Data

This example shows how to fit a  $\Delta\chi$ -tensor or equivalently, and alignment tensor to experimental RDC data. These data are taken from a Tb3+ tagged ubiquitin mutant:

Benjamin J. G. Pearce, Shereen Jabar, Choy-Theng Loh, Monika Szabo, Bim Graham, Gottfried Otting (2017) Structure restraints from heteronuclear pseudocontact shifts generated by lanthanide tags at two different sites *J. Biomol. NMR* 68:19-32

#### **Downloads**

- Download the data files 2kox.pdb, ubiquitin\_a28c\_c1\_Tb\_HN.rdc and ubiquitin\_s57c\_c1\_Tb\_HN.rdc from here:
- Download the script rdc\_fit.py

# Script + Explanation

Firstly, the necessary modules are imported from paramagpy. And the two RDC datasets are loaded. Because this PDB contains over 600 models, loading may take a few seconds

```
from paramagpy import protein, fit, dataparse, metal

# Load the PDB file
prot = protein.load_pdb('../data_files/2kox.pdb')

# Load the RDC data
rawData1 = dataparse.read_rdc('../data_files/ubiquitin_a28c_c1_Tb_HN.rdc')
rawData2 = dataparse.read_rdc('../data_files/ubiquitin_s57c_c1_Tb_HN.rdc')

# Associate RDC data with atoms of the PDB
parsedData1 = prot.parse(rawData1)
parsedData2 = prot.parse(rawData2)
```

Two starting metals are initialised. It is important here to set the magnetic field strength and temperature.

```
# Define an initial tensor
mStart1 = metal.Metal(B0=18.8, temperature=308.0)
mStart2 = metal.Metal(B0=18.8, temperature=308.0)
```

The alignment tensor is solved using the function <code>paramagpy.fit.svd\_fit\_metal\_from\_rdc()</code> which return a tuple of (metal, calculated, qfactor), where metal is the fitted metal, calculated is the calculated RDC values. These tensor are then saved.

```
# Calculate the tensor using SVD
sol1 = fit.svd_fit_metal_from_rdc(mStart1, parsedData1)
sol2 = fit.svd_fit_metal_from_rdc(mStart2, parsedData2)

# Save the fitted tensor to file
sol1[0].save('ubiquitin_a28c_c1_Tb_tensor.txt')
sol2[0].save('ubiquitin_s57c_c1_Tb_tensor.txt')
```

Output: [ubiquitin\_a28c\_c1\_Tb\_tensor.txt]

```
| 1E-32 m^3 : -4.776
      | 1E-32 \text{ m}^3 :
                     -1.397
rh
         1E-10 \ m :
                      0.000
Х
         1E-10 m :
                     0.000
У
        1E-10 \ m :
                      0.000
7.
                    16.022
            deg :
а
b
            deq:
                     52.299
g
            deg :
                    83.616
mueff |
            Bm :
                     0.000
shift |
            ppm :
                      0.000
B0
             T :
                    18.800
temp |
              K: 308.000
                     0.000
t.1e
             ps :
                      0.000
taur
            ns :
```

Output: [ubiquitin\_s57c\_c1\_Tb\_tensor.txt]

```
| 1E-32 \text{ m}^3 :
aх
                        -5.930
      | 1E-32 \text{ m}^3 :
rh
                        -1.899
          1E-10 \ m :
                        0.000
Х
          1E-10 m :
                        0.000
У
          1E-10 \ m :
                        0.000
                        9.976
а
              deg :
                       99.463
b
              deg :
                       37.410
              deq:
mueff |
                        0.000
              Bm :
shift |
                        0.000
              ppm:
BΩ
               T :
                       18.800
temp
                K :
                       308.000
```

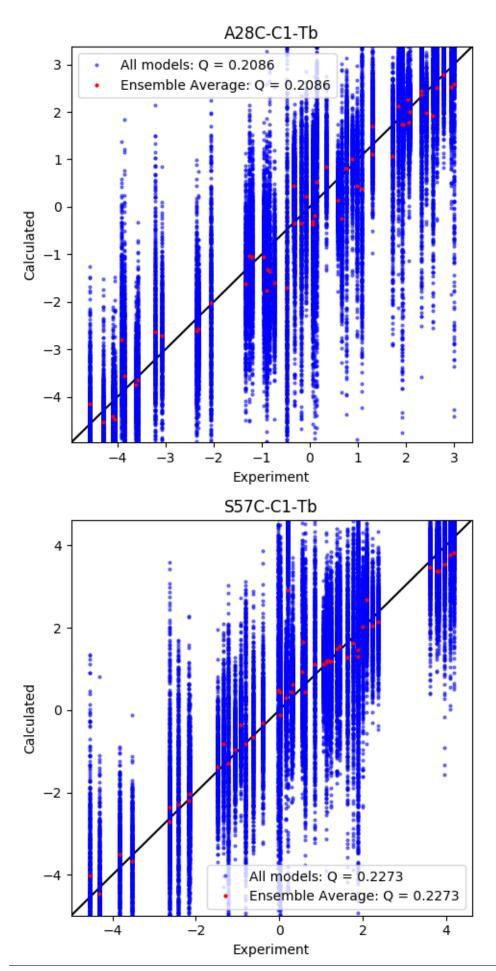
(continues on next page)

```
tle | ps: 0.000
taur | ns: 0.000
```

The experimental/calculated correlations are then plotted. The tensor is by default fitted to the ensemble averaged calculated values. Backcalculation of all models is shown here, as well as the ensemble average.

```
#### Plot the correlation ####
from matplotlib import pyplot as plt
fig = plt.figure(figsize=(5,10))
ax1 = fig.add_subplot(211)
ax2 = fig.add_subplot(212)
ax1.set_title('A28C-C1-Tb')
ax2.set_title('S57C-C1-Tb')
for sol, ax, pdata in zip([sol1,sol2], [ax1,ax2],
        [parsedData1,parsedData2]):
        # Unpack the experimental values
        atoms1, atoms2, exp, err = zip(*pdata)
        atoms = list(zip(atoms1, atoms2))
        metal, calc, qfac = sol
        expEnsemble, calcEnsemble = fit.ensemble_average(atoms, exp, calc)
        # Plot all models
        ax.plot(exp, calc, marker='o', lw=0, ms=2, c='b',
                alpha=0.5, label="All models: Q = \{:5.4f\}".format(gfac))
        # Plot the ensemble average
        ax.plot(expEnsemble, calcEnsemble, marker='o', lw=0, ms=2, c='r',
                label="Ensemble Average: Q = {:5.4f}".format(qfac))
        # Plot a diagonal
        l, h = ax.get_xlim()
        ax.plot([1,h],[1,h],'-k',zorder=0)
        ax.set_xlim(1,h)
        ax.set_ylim(l,h)
        # Make axis labels and save figure
        ax.set_xlabel("Experiment")
        ax.set_ylabel("Calculated")
        ax.legend()
fig.tight_layout()
fig.savefig("rdc_fit.png")
```

Output: [rdc\_fit.png]



#### Calculate RDC from a known Tensor

This example shows how to calculate theoretical RDC values from a known  $\Delta \chi$ -tensor which has been fitted from PCS data. Paramagpy allows seamless calculation of one PCS/PRE/RDC/CCR effect from a tensor fitted from another effect.

#### **Downloads**

- Download the data files 4icbH\_mut.pdb and calbindin\_Er\_HN\_PCS\_tensor.txt from here:
- Download the script rdc\_calculate.py

# Script + Explanation

First the relevant modules are loaded, the protein is loaded and the metal is loaded from file. The magnetic field strength and temperature are also set.

```
from paramagpy import protein, metal

# Load the PDB file
prot = protein.load_pdb('../data_files/4icbH_mut.pdb')

# Load the fitted tensor
met = metal.load_tensor('../data_files/calbindin_Er_HN_PCS_tensor.txt')
met.B0 = 18.8
```

A loop is made over the atoms of the protein. The amide H and N atoms are selected and then the RDC value is calculated. Finally the formated data is appended to list forFile.

The formatted data is written to file:

Output: [calbindin\_Er\_RDC\_calc.rdc]

```
Ν
           -1.724 0.0
1
  Н
      1
        N
           -6.196 0.0
          -4.993 0.0
2
  Н
     2
        N
     4 N -0.922 0.0
4
  Н
     5 N
           1.783 0.0
5
 Н
     6 N
          0.280 0.0
6 H
7
     7 N -1.906 0.0
  Η
8 H
     8 N
           1.056 0.0
9 H 9 N 0.713 0.0
```

(continues on next page)

```
10 H 10 N
            0.213 0.0
11 H 11 N -0.881 0.0
12 H 12 N 2.712 0.0
13 H 13 N 0.614 0.0
14 \quad H \quad 14 \quad N \quad -2.346 \quad 0.0
15 H 15 N 1.659 0.0
16 H 16 N
            0.648 0.0
17 H 17 N
            0.383 0.0
18 H 18 N
             0.420 0.0
19
   Н
      19
         N
            -7.863 0.0
21
   Н
      21
         Ν
             0.973 0.0
22
   Н
      22
         Ν
             1.026 0.0
            -0.613 0.0
23
   Н
      23
         Ν
24
         N -5.847 0.0
   H 24
            1.761 0.0
25
   Н
      25
         Ν
26 H 26 N
            6.470 0.0
27
            5.541 0.0
   Н 27
         Ν
28 H 28 N -0.334 0.0
29 H 29 N
            3.624 0.0
30 H 30 N
            6.673 0.0
            3.952 0.0
31 H 31 N
32 H 32 N
           1.658 0.0
33 H 33 N 5.449 0.0
34 H 34 N 7.370 0.0
35 H 35 N 1.033 0.0
36 H 36 N 1.136 0.0
38 H 38 N -7.378 0.0
39 \quad H \quad 39 \quad N \quad -6.979 \quad 0.0
40 H 40 N -4.810 0.0
41 H 41 N -3.187 0.0
             2.415 0.0
42
  H 42 N
43
   Н
      43
         Ν
             1.710 0.0
            -5.977 0.0
44
   Н
      44
         N
45 H
     45
         N
            -5.467 0.0
46 H 46
            3.243 0.0
         N
47 H 47
            3.937 0.0
         N
48 H 48 N
            7.047 0.0
49 H 49 N 4.577 0.0
50 H 50 N 3.718 0.0
51 H 51 N 4.519 0.0
52 H 52 N 6.077 0.0
53 H 53 N 2.940 0.0
54 H 54 N 2.541 0.0
55 H 55 N -7.493 0.0
56 H 56 N -7.159 0.0
57 H 57 N 4.948 0.0
58 H 58 N -1.078 0.0
59 H 59 N -0.759 0.0
60 H 60 N 0.161 0.0
61 H 61 N
            -1.132 0.0
62 H 62 N -5.719 0.0
             4.025 0.0
63 H 63
         N
   Н
      64
         Ν
             5.929 0.0
65 H
      65
         Ν
             2.363 0.0
66
   Н
      66
         Ν
             2.477 0.0
            8.265 0.0
67
   Н 67
         Ν
            5.078 0.0
68 H 68
         N
69 H 69
            3.724 0.0
         N
70 H 70 N
            7.743 0.0
71 H 71 N
            2.188 0.0
72 H 72 N
            4.911 0.0
```

(continues on next page)

```
73 H 73 N 7.514 0.0
74 H 74 N -0.001 0.0
75 H 75 N 1.119 0.0
```

#### 5.2.3 PRE data

#### Fit Tensor to PRE Data

This example demonstrates fitting of the rotational correlation time  $\tau_r$  to 1H PRE data of calbindin D9k. You can fit any parameters of the  $\chi$ -tensor you desire, such as position or magnitude as well.

#### **Downloads**

- Download the data files 4icbH\_mut.pdb, calbindin\_Er\_H\_R2\_600.npc and calbindin\_Tb\_H\_R2\_800.npc from here:
- Download the script pre\_fit\_proton.py

#### **Script + Explanation**

Firstly, the necessary modules are imported from paramagpy.

```
from paramagpy import protein, fit, dataparse, metal
```

The protein is then loaded from a PDB file.

```
# Load the PDB file
prot = protein.load_pdb('../data_files/4icbH_mut.pdb')
```

The PRE data is loaded. Note that the Er data was recorded at 600 MHz and the Tb data was recorded at 800 MHz.

```
rawData_er = dataparse.read_pre('../data_files/calbindin_Er_H_R2_600.pre')
rawData_tb = dataparse.read_pre('../data_files/calbindin_Tb_H_R2_800.pre')
```

The  $\Delta \chi$ -tensors that were fitted from PCS data are loaded from file and the relevant  $B_0$  magnetic field strengths are set.

```
mStart_er = metal.load_tensor('../data_files/calbindin_Er_HN_PCS_tensor.txt')
mStart_tb = metal.load_tensor('../data_files/calbindin_Tb_HN_PCS_tensor.txt')
mStart_er.B0 = 14.1
mStart_tb.B0 = 18.8
```

Fitting of the rotational correlation time is done with the function paramagpy.fit.  $nlr_fit_metal_from_pre()$ . To fit position or  $\chi$ -tensor magnitude, you can change the params argument.

The fitted tensors are saved to file. Note that the Er dataset gives a reasonable  $\tau_r$  of around 4 ns which is close to the literature value of 4.25 ns. However, the Tb dataset gives an unreasonably large value of 18 ns. This is due to magnetisation attenuation due to 1H-1H RDCs present during the relaxation evolution time as discussed in literature giving rise to artificially large measured PREs for lanthanides with highly anisotropic  $\Delta\chi$ -tensors. This is also reflected in the correlation plot below.

```
m_er.save('calbindin_Er_H_R2_600_tensor.txt')
m_tb.save('calbindin_Tb_H_R2_800_tensor.txt')
```

#### Output: [calbindin\_Er\_H\_R2\_600\_tensor.txt]

```
| 1E-32 m^3 :
                 -8.152
    | 1E-32 m^3 :
                  -4.911
rh
       1E-10 m :
                  25.786
X
    9.515
6.558
       1E-10 m :
    1E-10 m :
7.
    deg: 125.841
а
     b
          deg: 142.287
     deq: 41.758
     mueff |
           Bm :
                   9.581
shift |
          ppm :
                   0.000
B0
            T :
                  14.100
            K: 298.150
temp |
                  0.189
t1e
    ps :
                   3.923
taur |
           ns :
```

#### Output: [calbindin\_Tb\_H\_R2\_800\_tensor.txt]

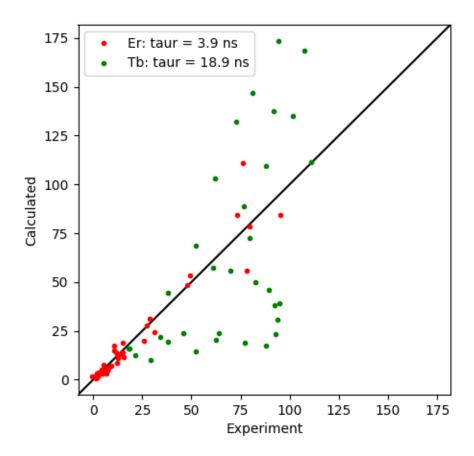
```
| 1E-32 \text{ m}^3 :
                     30.375
     | 1E-32 m^3 :
                     12.339
Х
         1E-10 \ m :
                    25.786
     1E-10 m :
                      9.515
У
        1E-10 \ m :
     6.558
     deg :
                    150.957
                    152.671
h
     deg :
           deg :
                    70.311
g
     mueff |
                     9.721
            Bm :
shift |
                     0.000
            ppm :
             T :
                    18.800
     K :
                  298.150
temp |
                     0.251
t.1e
     ps :
taur |
            ns: 18.917
```

#### And the results are plotted.

```
from matplotlib import pyplot as plt
fig, ax = plt.subplots(figsize=(5,5))
# Unpack the experimental values
atm_er, exp_er, err_er = zip(*data_er)
atm_tb, exp_tb, err_tb = zip(*data_tb)
# Plot the data
ax.plot(exp_er, cal_er, marker='o', lw=0, ms=3, c='r',
        label="Er: taur = {:3.1f} ns".format(1E9*m_er.taur))
ax.plot(exp_tb, cal_tb, marker='o', lw=0, ms=3, c='g',
        label="Tb: taur = {:3.1f} ns".format(1E9*m_tb.taur))
# Plot a diagonal
l, h = ax.get_ylim()
ax.plot([1,h],[1,h],'-k',zorder=0)
ax.set_xlim(l,h)
ax.set_ylim(l,h)
# Make axis labels and save figure
ax.set_xlabel("Experiment")
ax.set_ylabel("Calculated")
ax.legend()
```

(continues on next page)

fig.savefig("pre\_fit\_proton.png")



#### Calculate 15N PREs with cross-correlation effects

This example shows how to conduct a weighted fit of a  $\Delta \chi$ -tensor to experimental PCS data with experimental errors.

# Downloads

- Download the data files 4icbH\_mut.pdb, calbindin\_Tb\_N\_R1\_600.pre and calbindin\_Tb\_HN\_PCS\_tensor.txt from here:
- Download the script pre\_calc\_nitrogen.py

# Script + Explanation

First the relevant modules are loaded, the protein and data are read and the data is parsed by the protein.

```
from paramagpy import protein, metal, dataparse

# Load the PDB file
prot = protein.load_pdb('../data_files/4icbH_mut.pdb')
```

(continues on next page)

```
# Load PRE data
rawData = dataparse.read_pre('../data_files/calbindin_Tb_N_R1_600.pre')
# Parse PRE data
data = prot.parse(rawData)
```

The Tb tensor fitted from PCS data is loaded and the relevant parameters, in this case the magnetic field strength, temperature and rotational correlation time are set.

```
met = metal.load_tensor('../data_files/calbindin_Tb_HN_PCS_tensor.txt')
met.B0 = 14.1
met.T = 298.0
met.taur = 4.25E-9
```

A loop is conducted over the nitrogen atoms that are present in the experimental data. The PRE is calculated using the function  $paramagpy.metal.atom\_pre()$ . Calculations without CSA are appended to the list cal and calculations including CSA cross-correlation with the Curie-spin relaxation are appended to the list cal\_csa.

Finally the data are plotted. Clearly CSA cross-correlation is a big effect for backbone nitrogen atoms and should always be taken into account for Curie-spin calculations. Also note the existence and correct prediction of negative PREs!

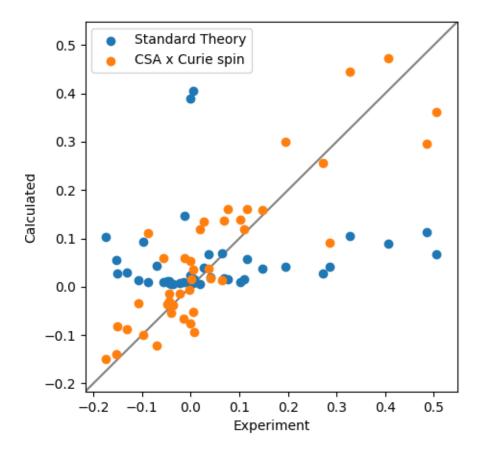
```
from matplotlib import pyplot as plt
fig, ax = plt.subplots(figsize=(5,5))

# Plot the data
ax.scatter(exp, cal, label="Standard Theory")
ax.scatter(exp, cal_csa, label="CSA x Curie spin")

# Plot a diagonal
1, h = ax.get_xlim()
ax.plot([l,h],[l,h],'grey',zorder=0)
ax.set_xlim(l,h)
ax.set_ylim(l,h)

# Make axis labels and save figure
ax.set_xlabel("Experiment")
ax.set_ylabel("Calculated")
ax.legend()
fig.savefig("pre_calc_nitrogen.png")
```

Output: [pre\_calc\_nitrogen.png]



# 5.2.4 CCR data

#### **Calculate Cross-correlated Relaxation**

This example shows how to calculate dipole-dipole/Curie-spin cross-correlated relaxation as measured for data in the literature by Pintacuda et. al.

#### **Downloads**

- Download the data files 1bzrH.pdb, myoglobin\_cn.ccr and myoglobin\_f.ccr from here:
- Download the script ccr\_calculate.py

### **Script + Explanation**

First the relevant modules are loaded, and the iron atom (paramagnetic centre) is identified as the variable ironAtom.

```
from paramagpy import protein, fit, dataparse, metal
import numpy as np

# Load the PDB file and get iron centre
prot = protein.load_pdb('../data_files/lbzrH.pdb')
ironAtom = prot[0]['A'][("H_HEM",154," ")]['FE']
```

Two paramagnetic centres are defined for the high and low spin iron atom. The positions are set to that of the iron centre along with other relevant parameters. The measured isotropic  $\chi$ -tensor magnitudes are also set.

The experimental data are loaded and parsed by the protein.

```
data_cn = prot.parse(dataparse.read_ccr("../data_files/myoglobin_cn.ccr"))
data_f = prot.parse(dataparse.read_ccr("../data_files/myoglobin_f.ccr"))
```

A loop is conducted over the atoms contained in the experimental data and the CCR rate is calculated using the function <code>paramagpy.metal.Metal.atom\_ccr()</code>. These are appended to lists <code>compare\_cn</code> and <code>compare\_f</code>.

Note that the two H and N atoms are provided. The first atom is the nuclear spin undergoing active relaxation. The second atom is the coupling partner. Thus by swapping the H and N atoms to give  $atom\_ccr(N, H)$ , the differential line broadening can be calculated in the indirect dimension.

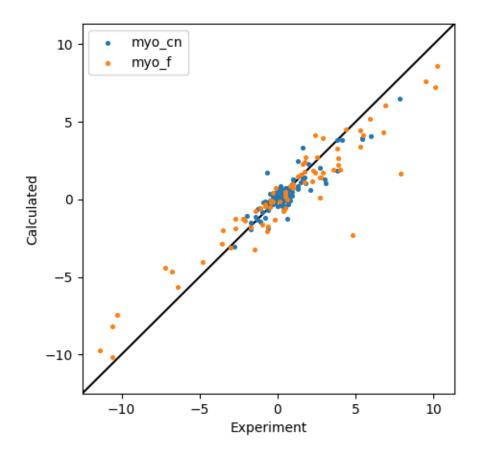
```
# Calculate the cross-correlated realxation
compare_cn = []
for H, N, value, error in data_cn:
    delta = met_cn.atom_ccr(H, N)
        compare_cn.append((value, delta*0.5))

compare_f = []
for H, N, value, error in data_f:
        delta = met_f.atom_ccr(H, N)
        compare_f.append((value, delta*0.5))
```

Finally a correlation plot is made.

```
#### Plot the correlation ####
from matplotlib import pyplot as plt
fig, ax = plt.subplots(figsize=(5,5))
# Plot the data correlations
ax.scatter(*zip(*compare_cn), s=7, label="myo_cn")
ax.scatter(*zip(*compare_f), s=7, label="myo_f")
# Plot a diagonal
l, h = ax.get_xlim()
ax.plot([1,h],[1,h],'-k',zorder=0)
ax.set_xlim(l,h)
ax.set_ylim(l,h)
# Make axis labels and save figure
ax.set_xlabel("Experiment")
ax.set_ylabel("Calculated")
ax.legend()
fig.savefig("ccr_calculate.png")
```

Output: [ccr\_calculate.png]



# 5.3 Graphic User Interface (GUI)

Paramagpy is equipped with a GUI which is cross-platform and contains most of the functionality of the scripted module. This gives a rapid way for new users to fit and compare PCS, RDC and PRE effects.

#### 5.3.1 YouTube Tutorial

Check out the tutorial on YouTube

# 5.3.2 Running the GUI

To run the GUI, first open the python inperpreter in the terminal

```
user@computer:~$ python3
Python 3.5.2 (default, Nov 23 2017, 16:37:01)
[GCC 5.4.0 20160609] on linux
Type "help", "copyright", "credits" or "license" for more information.
>>>
```

Then import paramagpy and start the gui with paramagpy.gui.run().

```
user@computer:~$ python3
Python 3.5.2 (default, Nov 23 2017, 16:37:01)
[GCC 5.4.0 20160609] on linux
```

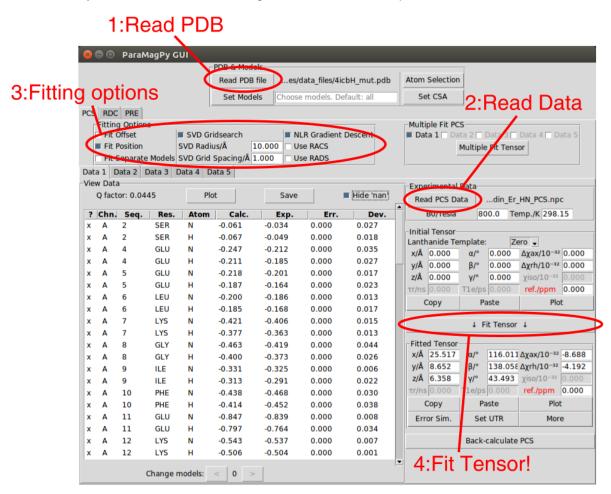
(continues on next page)

```
Type "help", "copyright", "credits" or "license" for more information.
>>> import paramagpy
>>> paramagpy.gui.run()
```

Alternatively you can simply execute the following from the command line

```
user@computer:~$ echo "import paramagpy; paramagpy.gui.run()" | python3
```

If all this fails, you can contact the author for a prebuilt executable at henry.orton@anu.edu.au



# 5.4 NMR Software Macros

Paramagpy includes scripts for reading/writing PCS values directly from popular NMR software. This drastically improves the iterative process of tensor fitting.

# 5.4.1 CCPNMR Analysis 2.4

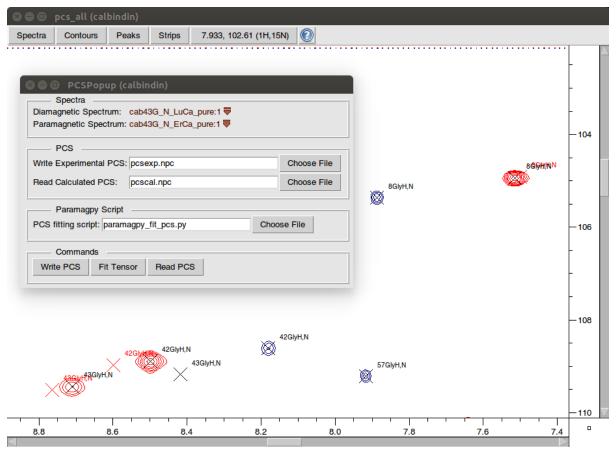
Download the two scripts:

- paramagpy\_ccpnmr\_macro.py
- paramagpy\_fit\_pcs.py

In the first line of the script *paramagpy\_fit\_pcs.py*, replace the shebang with the path to the python version on your machine that contains the paramagpy installation. On my computer this is set to.

#### #!/usr/bin/python3

Open CCPNMR analysis and navigate to Menu->Macro->Organise Macros. At the lower right click *Add Macro* and open the script *paramagpy\_ccpnmr\_macro.py*, then select *paramagpyMACRO* and click *Load Macro*. You can then select if from the list and click *Run* to reveal the screen below.



The popup window allows you to select a diamagnetic and paramagnetic spectrum and has 3 available buttons:

- Write PCS: This will calculate the difference between assigned peaks in the paramagnetic and diamagnetic spectra and write them to a .npc file (as specified in the relevant field).
- Fit Tensor: This will call the paramagpy script *paramagpy\_fit\_pcs.py* to fit the tensor the written PCS values.
- Read PCS: This will read back-calculated PCS values from file (as specified in the relevant field) and plot the expected peaks on the paramagnetic spectrum in red.

Note, to alter the parameters for fitting of the PCS tensor, you can change the values within the script *paramagpy\_fit\_pcs.py*.

# 5.4.2 Sparky

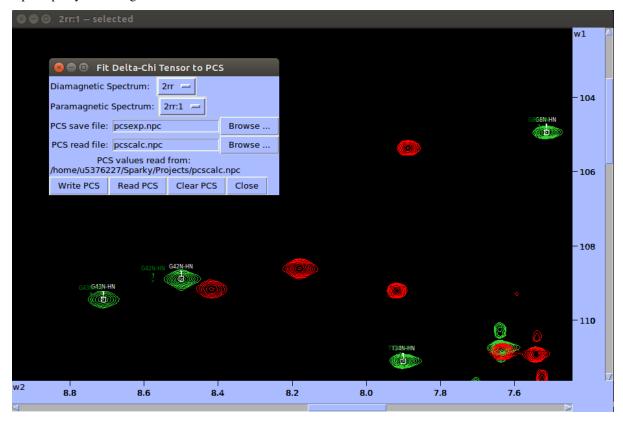
Download the 3 scripts:

- paramagpy\_sparky\_macro.py
- sparky\_init.py
- paramagpy\_fit\_pcs.py

Place the first two scripts *paramagpy\_sparky\_macro.py* and *sparky\_init.py* in the Sparky directory ~/Sparky/Python. Note that the Sparky directory usually contains the *Projects*, *Lists* and *Save* folders. You may need to create the *Python* directory here in which to place the two scripts.

Place the third script *paramagpy\_fit\_pcs.py* in your home directory.

Open Sparky and navigate to Extensions->Read and write PCS files.



The popup window allows you to select a diamagnetic and paramagnetic spectrum and has 3 available buttons:

- Write PCS: This will calculate the difference between assigned peaks in the paramagnetic and diamagnetic spectra and write them to a .npc file (as specified in the relevant field).
- Read PCS: This will read back-calculated PCS values from file (as specified in the relevant field) and plot the expected peaks on the paramagnetic spectrum in green.
- Clear PCS: This will remove all calculated PCS peaks from the spectrum.

Note, to perform the tensor fitting, you will need to execute the paramagpy script in a separate terminal including an argument with the experimental PCS file such as:

```
user@computer:~$ ./paramagpy_fit_pcs.py pcsexp.npc
```

To alter the parameters for fitting of the PCS tensor, you can change the values within the script paramagpy\_fit\_pcs.py.

# 5.5 Reference Guide

# 5.5.1 Paramagnetic module

This module handles the paramagnetic centre by defining the magnetic susceptibility tensor and methods for PCS, RDC and PRE calculations.

### paramagpy.metal

#### **Functions**

euler_to_matrix(eulers)	Calculate a rotation matrix from euler angles using
	ZYZ convention
matrix_to_euler(M)	Calculate Euler angles from a rotation matrix using
	ZYZ convention
unique_eulers(eulers)	Calculate Euler angles in unique tensor representa-
	tion.
<pre>make_tensor(x, y, z, axial, rhombic, alpha,)</pre>	Make a ChiTensor isntance from given parameters.

### paramagpy.metal.euler\_to\_matrix

```
paramagpy.metal.euler_to_matrix(eulers)
```

Calculate a rotation matrix from euler angles using ZYZ convention

**Parameters eulers** (array of floats) – the euler angles [alpha,beta,gamma] in radians by ZYZ convention.

**Returns** matrix – the rotation matrix

Return type 3x3 numpy ndarray

# **Examples**

```
>>> eulers = np.array([0.5,1.2,0.8])
>>> euler_to_matrix(eulers)
array([[-0.1223669 , -0.5621374 , 0.81794125],
        [ 0.75057357 , 0.486796 , 0.44684334],
        [-0.64935788 , 0.66860392 , 0.36235775]])
```

# paramagpy.metal.matrix\_to\_euler

```
paramagpy.metal.matrix_to_euler(M)
```

Calculate Euler angles from a rotation matrix using ZYZ convention

Parameters M (3x3 numpy ndarray) – a rotation matrix

Returns eulers – the euler angles [alpha,beta,gamma] in radians by ZYZ convention

**Return type** array of floats

#### **Examples**

# paramagpy.metal.unique\_eulers

```
paramagpy.metal.unique_eulers(eulers)
```

Calculate Euler angles in unique tensor representation.

Given general Euler angles by ZYZ convention, this function accounts for the symmetry of a second rank symmetric tensor to map all angles within the range [0, pi].

Parameters eulers (array of float) – the three Euler angles in radians

**Returns eulers\_utr** – the euler angles [alpha,beta,gamma] in radians by ZYZ convention

Return type array of floats

### **Examples**

```
>>> eulers = np.array([-5.2,10.3,0.1])
>>> unique_eulers(eulers)
np.array([1.08318531 0.87522204 3.04159265])
```

# paramagpy.metal.make\_tensor

```
paramagpy.metal.make_tensor(x, y, z, axial, rhombic, alpha, beta, gamma, lanthanide=None, temperature=298.15)
```

Make a ChiTensor isntance from given parameters. This is designed to use pdb coordinates (x, y, z) and euler angles from an output like Numbat.

#### **Parameters**

- y,  $\mathbf{z}(x_t)$  tensor position in pdb coordinate in Angstroms
- **rhombic** (axial,) the tensor anisotropies in units 10^-32
- beta, gamma (alpha,) the euler angles in degrees that maps the tensor to the pdb (I think?)

**Returns** ChiTensor – a tensor object for calulating paramagnetic effects on nuclear spins in the pdb coordinate

Return type object paramagpy.metal.Metal

#### **Classes**

<pre>Metal([position, eulers, axrh, mueff,])</pre>	An object for paramagnetic chi tensors and delta-chi
	tensors.

# paramagpy.metal.Metal

```
class paramagpy.metal.Metal (position=(0, 0, 0), eulers=(0, 0, 0), axrh=(0, 0), mueff=0.0, shift=0.0, temperature=298.15, t1e=0.0, B0=18.79, taur=0.0)
```

An object for paramagnetic chi tensors and delta-chi tensors. This class has basic attributes that specify position, axiality/rhombicity, isotropy and euler angles. It also has methods for calculating PCS, RDC, PRE and CCR values.

```
__init__ (position=(0, 0, 0), eulers=(0, 0, 0), axrh=(0, 0), mueff=0.0, shift=0.0, tempera-
ture=298.15, t1e=0.0, B0=18.79, taur=0.0)
Instantiate ChiTensor object
```

#### **Parameters**

- **position** (array of floats, optional) the (x,y,z) position in meters. Default is (0,0,0) stored as a np.matrix object.
- eulers (array of floats, optional) the euler angles [alpha,beta,gamma] in radians by ZYZ convention. Defualt is (0,0,0)
- axrh (array of floats, optional) the axial and rhombic values defining the magnetic susceptibility anisotropy

- mueff(float) the effective magnetic moment in units of  $A.m^2$
- **shift** (float) a bulk shift value applied to all PCS calculations. This is a correction parameter that may arise due to an offset between diamagnetic and paramagnetic PCS datasets.
- temperature (float) the temperature in Kelvin
- **tle** (float) the longitudinal electronic relaxation time
- **BO** (float) the magnetic field in Telsa
- taur (float) the rotational correlation time in seconds

# Methods

atom_ccr(atom, atomPartner)	Calculate R2 cross-corelated relaxation due to DDxDSA
atom_pcs(atom[, racs, rads])	Calculate the psuedo-contact shift at the given
ason_pos(atomp, raos, raos)	atom
atom_pre(atom[, rtype, dsa, sbm, csa])	Calculate the PRE for an atom
atom_rdc(atom1, atom2)	Calculate the residual dipolar coupling between
atom_rac(atomr, atom2)	two atoms
atom_set_position(atom)	Set the position of the Metal object to that of an
	atom
ccr(position, gamma, dipole_shift_tensor)	Calculate R2 cross-corelated relaxation due to
	DDxDSA
copy()	Copy the current Metal object to a new instance
dipole_shift_tensor(position)	Calculate the chemical shift tensor at the given
dipole_onile_censor(position)	postition
dsa_r1(position, gamma[, csa])	Calculate R1 relaxation due to Curie Spin
dsa_r2(position, gamma[, csa])	Calculate R2 relaxation due to Curie Spin
fast_ccr(posarray, gammaarray, dstarray)	Vectorised version of paramagpy.metal.
	Metal.ccr()
<pre>fast_dipole_shift_tensor(posarray)</pre>	A vectorised version of paramagpy.metal.
	<pre>Metal.dipole_shift_tensor()</pre>
fast_dsa_r1(posarray, gammaarray[, csaar-	Vectorised version of paramagpy.metal.
ray])	Metal.dsa_r1()
fast_dsa_r2(posarray, gammaarray[, csaar-	Vectorised version of paramagpy.metal.
ray])	Metal.dsa_r2()
fast_first_invariant_squared(t)	Vectorised version of paramagpy.metal.
	<pre>Metal.first_invariant_squared()</pre>
fast_pcs(posarray)	A vectorised version of paramagpy.metal.
	Metal.pcs()
fast_pre(posarray, gammaarray, rtype[, dsa,	Calculate the PRE for a set of spins using Curie
])	and or SBM theory
fast_racs(csaarray)	A vectorised version of paramagpy.metal.
( <i>)</i> /	Metal.racs()
fast_rads(posarray)	A vectorised version of paramagpy.metal.
	Metal.rads()
fast_rdc(vecarray, gammaProdArray)	A vectorised version of paramagpy.metal.
rass_ras(vectary, gammarrow may)	Metal.rdc() method.
fast_sbm_r1(posarray, gammaarray)	Vectorised version of paramagpy.metal.
= 4 7.5	Metal.sbm_r1()
fast_sbm_r2(posarray, gammaarray)	Vectorised version of paramagpy.metal.
	Metal.sbm_r2()
	Continued on next page

Continued on next page

Table 3 – continued from previous page

	rom previous page
<pre>fast_second_invariant_squared(t)</pre>	Vectorised version of
	paramagpy.metal.Metal.
	second_invariant_squared()
first_invariant_squared(t)	Calculate the antisymmetric contribution to re-
	laxation via the first invariant of a tensor.
get_params(params)	Get tensor parameters that have been scaled ap-
	propriately
info([comment])	Get basic information about the Metal object
isomap([protein, isoval])	
make_mesh([density, size])	Construct a 3D grid of points to map an isosur-
	face
pcs(position)	Calculate the psuedo-contact shift at the given
-	postition
pcs_mesh(mesh)	Calculate a PCS value at each location of cubic
	grid of points
pre(position, gamma, rtype[, dsa, sbm, csa])	Calculate the PRE for a set of spins using Curie
	and or SBM theory
pre_mesh(mesh[, gamma, rtype, dsa, sbm])	Calculate a PRE value at each location of cubic
	grid of points
racs(csa)	Calculate the residual anisotropic chemical shift
( )	at the given postition.
rads(position)	Calculate the residual anisotropic dipolar shift
4	at the given postition.
rdc(vector, gammaProd)	Calculate Residual Dipolar Coupling (RDC)
save([fileName])	1 1 5 7
sbm_r1(position, gamma)	Calculate R1 relaxation due to Solomon-
_ 4	Bloembergen-Morgan theory
sbm_r2(position, gamma)	Calculate R2 relaxation due to Solomon-
	Bloembergen-Morgan theory
second_invariant_squared(t)	Calculate the second invariant squared of a ten-
,	sor.
$set\_Jg(J,g)$	Set the magnetic susceptibility absolute magni-
5 ( · <b>C</b> )	tude from J/g.
set_lanthanide(lanthanide[, set_dchi])	Set the anisotropy, isotropy and T1e parameters
	from literature values
set_params(paramValues)	Set tensor parameters that have been scaled ap-
	propriately
set_utr()	Modify current tensor parameters to unique ten-
_	sor representation (UTR)
spec_dens(tau, omega)	A spectral density function with Lorentzian
-1 (,0)	shape:
write_isomap(mesh, bounds[, fileName])	Write a PyMol script to file which allows load-
<u></u>	ing of the isosurface file
write_pymol_script([isoval, surface-	Write a PyMol script to file which allows load-
Name,])	ing of the isosurface file

# paramagpy.metal.Metal.atom\_ccr

Metal.atom\_ccr(atom, atomPartner)

Calculate R2 cross-corelated relaxation due to DDxDSA

#### **Parameters**

- atom (paramagpy.protein.CustomAtom) the active nuclear spin for which relaxation will be calculated must have attributes 'position' and 'gamma'
- atomPartner (paramagpy.protein.CustomAtom) the coupling parnter nuclear spin must have method 'dipole\_shift\_tensor'

Returns value – the CCR differential line broadening in Hz

### Return type float

### paramagpy.metal.Metal.atom\_pcs

Metal.atom\_pcs (atom, racs=False, rads=False)

Calculate the psuedo-contact shift at the given atom

#### **Parameters**

- atom (biopython atom object) must have 'position' attribute
- racs (bool (optional)) when True, RACS (residual anisotropic chemical shielding) correction is included. Default is False
- rads (bool (optional)) when True, RADS (residual anisotropic dipolar shielding) correction is included. Defualt is False

**Returns** pcs – the pseudo-contact shift in parts-per-million (ppm)

Return type float

# paramagpy.metal.Metal.atom\_pre

Metal.atom\_pre(atom, rtype='r2', dsa=True, sbm=True, csa=0.0)

Calculate the PRE for an atom

#### **Parameters**

- atom (paramagpy.protein.CustomAtom) the active nuclear spin for which relaxation will be calculated must have attributes 'position' and 'gamma'
- **rtype** (*str*) either 'r1' or 'r2', the relaxation type
- **dsa** (bool (optional)) when True (defualt), DSA or Curie spin relaxation is included
- **sbm** (bool (optional)) when True (defualt), SBM spin relaxation is included
- **csa** (array with shape (3,3) (optional)) **CSA** tensor of the spin. This defualts to 0.0, meaning CSAxDSA crosscorrelation is not accounted for.

**Returns** rate – The PRE rate in /s

Return type float

#### paramagpy.metal.Metal.atom\_rdc

Metal.atom\_rdc(atom1, atom2)

Calculate the residual dipolar coupling between two atoms

# **Parameters**

- atom1 (biopython atom object) must have 'position' and 'gamma' attribute
- atom1 must have 'position' and 'gamma' attribute

Returns rdc – the RDC values in Hz

Return type float

# paramagpy.metal.Metal.atom\_set\_position

```
Metal.atom_set_position(atom)
```

Set the position of the Metal object to that of an atom

Parameters atom (biopython atom object) - must have 'position' attribute

#### paramagpy.metal.Metal.ccr

Metal.ccr (position, gamma, dipole\_shift\_tensor)

Calculate R2 cross-corelated relaxation due to DDxDSA

If the metal has an anisotropic magnetic susceptibility, this is taken into account.

#### **Parameters**

- **position** (array of floats) three coordinates (x,y,z) this is the position of the nuclear spin
- gamma (float) the gyromagnetic ratio of the relaxing spin
- **dipole\_shift\_tensor** (3x3 array of floats) this is the dipole shift tensor arising from the nuclear spin of the coupling partner

**Returns value** – The R2 differential line broadening rate in /s **Return type** float

### paramagpy.metal.Metal.copy

```
Metal.copy()
```

Copy the current Metal object to a new instance

**Returns** new\_tensor – a new Metal instance with the same parameters **Return type** Metal object

# paramagpy.metal.Metal.dipole\_shift\_tensor

```
Metal.dipole_shift_tensor(position)
```

Calculate the chemical shift tensor at the given postition

This arises due to the paramagnetic dipole tensor field

Parameters position (array floats) - the position (x, y, z) in meters

**Returns dipole\_shift\_tensor** – the tensor describing chemical shift at the nuclear position

**Return type** 3x3 array

### paramagpy.metal.Metal.dsa\_r1

```
Metal.dsa_r1 (position, gamma, csa=0.0)
```

Calculate R1 relaxation due to Curie Spin

If the metal has an anisotropic magnetic susceptibility, this is taken into account, resulting in orientation dependent PRE as predicted by Vega and Fiat. CSA cross-correlated relaxation may be included by providing an appropriate CSA tensor.

#### **Parameters**

- position (array of floats) three coordinates (x,y,z) in meters
- gamma (float) the gyromagnetic ratio of the spin
- **csa** (3x3 matrix (optional)) the CSA tensor of the given spin. This defualts to 0.0, meaning CSAxDSA crosscorrelation is not accounted for.

**Returns value** – The R1 relaxation rate in /s

Return type float

# paramagpy.metal.Metal.dsa\_r2

```
Metal.dsa_r2 (position, gamma, csa=0.0)
```

Calculate R2 relaxation due to Curie Spin

If the metal has an anisotropic magnetic susceptibility, this is taken into account, resulting in orientation dependent PRE as predicted by Vega and Fiat. CSA cross-correlated relaxation may be included by providing an appropriate CSA tensor.

#### **Parameters**

- position (array of floats) three coordinates (x,y,z)
- gamma (float) the gyromagnetic ratio of the spin

• **csa** (3x3 matrix (optional)) – the CSA tensor of the given spin. This defualts to 0.0, meaning CSAxDSA crosscorrelation is not accounted for.

**Returns value** – The R2 relaxation rate in /s **Return type** float

# paramagpy.metal.Metal.fast\_ccr

```
Metal.fast_ccr(posarray, gammaarray, dstarray)
```

Vectorised version of paramagpy.metal.Metal.ccr()

This is generally used for speed in fitting DDxDSA data

If the metal has an anisotropic magnetic susceptibility, this is taken into account.

#### **Parameters**

- posarray (array with shape (n, 3)) array of positions in meters
- gammaarray (array with shape (n, 3)) array of gyromagnetic ratios of the spins
- **dstarray** (array with shape (n, 3, 3)) array of nuclear dipole shift tensors arising from the coupling partners

**Returns** rates – The R2 differential line broadening rates in /s **Return type** array with shape (n,1)

### paramagpy.metal.Metal.fast\_dipole\_shift\_tensor

### Metal.fast\_dipole\_shift\_tensor(posarray)

A vectorised version of paramagpy.metal.Metal.dipole shift tensor()

This is generally used for fast calculations.

**Parameters** posarray (array) – an array of positions with shape (n,3)

**Returns dipole\_shift\_tensor\_array** – and array of dipole shift tensors at corresponding positions. This has shape (n,3,3)

Return type array

# paramagpy.metal.Metal.fast\_dsa\_r1

```
Metal.fast_dsa_r1 (posarray, gammaarray, csaarray=0.0)

Vectorised version of paramagpy.metal.Metal.dsa_r1()
```

This is generally used for speed in fitting PRE data

#### **Parameters**

- posarray (array with shape (n, 3)) array of positions in meters
- gammaarray (array with shape (n, 3)) array of gyromagnetic ratios of the spins
- **csaarray** (array with shape (m, 3, 3) (optional)) array of CSA tensors of the spins. This defualts to 0.0, meaning CSAxDSA crosscorrelation is not accounted for.

**Returns rates** – The R1 relaxation rates in /s

**Return type** array with shape (n,1)

#### paramagpy.metal.Metal.fast dsa r2

```
Metal.fast_dsa_r2 (posarray, gammaarray, csaarray=0.0)
Vectorised version of paramagpy.metal.Metal.dsa_r2()
```

This is generally used for speed in fitting PRE data.

#### **Parameters**

• posarray (array with shape (n, 3)) – array of positions in meters

- gammaarray (array with shape (n, 3)) array of gyromagnetic ratios of the spins
- **csaarray** (array with shape (m, 3, 3) (optional)) array of CSA tensors of the spins. This defualts to 0.0, meaning CSAxDSA crosscorrelation is not accounted for

**Returns** rates – The R2 relaxation rates in /s

**Return type** array with shape (n,1)

# paramagpy.metal.Metal.fast\_first\_invariant\_squared

```
static Metal.fast_first_invariant_squared(t)
```

Vectorised version of paramagpy.metal.Metal.first\_invariant\_squared()

This is generally used for speed in fitting PRE data

Parameters tensorarray (array with shape (n, 3, 3)) - array of shielding tensors

**Returns** firstInvariantSquared – the first invariants squared of the tensors Return type array with shape (n,1)

### paramagpy.metal.Metal.fast\_pcs

```
Metal.fast pcs(posarray)
```

A vectorised version of paramagpy.metal.Metal.pcs()

This efficient algorithm calculates the PCSs for an array of positions and is best used where speed is required for fitting.

**Parameters posarray** (array with shape (n, 3)) – array of 'n' positions (x, y, z) in meters

**Returns** pcs – the peudo-contact shift in parts-per-million (ppm)

**Return type** array of floats with shape (n,1)

# paramagpy.metal.Metal.fast\_pre

Metal.**fast\_pre** (*posarray*, *gammaarray*, *rtype*, *dsa=True*, *sbm=True*, *csaarray=0.0*)

Calculate the PRE for a set of spins using Curie and or SBM theory

#### **Parameters**

- posarray (array with shape (n, 3)) array of positions in meters
- gammaarray (array with shape (n, 3)) array of gyromagnetic ratios of the spins
- **rtype** (*str*) either 'r1' or 'r2', the relaxation type
- dsa (bool (optional)) when True (defualt), DSA or Curie spin relaxation is included
- **sbm** (bool (optional)) when True (defualt), SBM spin relaxation is included
- **csaarray** (array with shape (m, 3, 3) (optional)) array of CSA tensors of the spins. This defualts to 0.0, meaning CSAxDSA crosscorrelation is not accounted for.

**Returns rates** – The PRE rates in /s **Return type** array with shape (n,1)

# paramagpy.metal.Metal.fast\_racs

```
Metal.fast_racs(csaarray)
```

A vectorised version of paramagpy.metal.Metal.racs()

This is generally used when speed is required for fitting

```
Parameters csaarray (array with shape (n, 3, 3)) – array of chemical shift anisotropy tensors
```

**Returns**  $racs_array$  – the residual anisotropic chemical shift in parts-per-million (ppm) **Return type** array of floats with shape (n,1)

# paramagpy.metal.Metal.fast\_rads

```
Metal.fast_rads (posarray)
```

A vectorised version of paramagpy.metal.Metal.rads()

This is generally used when speed is required for fitting

**Parameters posarray** (array with shape (n, 3)) – an array of 'n' positions (x, y, z) in meters

**Returns rads\_array** – the residual anisotropic dipole shift in parts-per-million (ppm) **Return type** array of floats with shape (n,1)

# paramagpy.metal.Metal.fast\_rdc

```
Metal.fast_rdc(vecarray, gammaProdArray)
```

A vectorised version of paramagpy.metal.Metal.rdc() method.

This is generally used for speed in fitting RDC data

#### **Parameters**

- **vecarray** (array with shape (n, 3)) array of internuclear vectors in meters
- gammaProdArray (array with shape (n, 1))—the products of gyromagnetic ratios of spins A and B where each has units of rad/s/T

**Returns** rdc\_array – the RDC values in Hz

**Return type** array with shape (n,1)

#### paramagpy.metal.Metal.fast sbm r1

```
Metal.fast_sbm_r1 (posarray, gammaarray)
```

Vectorised version of paramagpy.metal.Metal.sbm\_r1()

This is generally used for speed in fitting PRE data

### **Parameters**

- posarray (array with shape (n, 3)) array of positions in meters
- gammaarray (array with shape (n, 3)) array of gyromagnetic ratios of the spins

**Returns** rates – The R1 relaxation rates in /s

**Return type** array with shape (n,1)

#### paramagpy.metal.Metal.fast sbm r2

```
Metal.fast_sbm_r2 (posarray, gammaarray)
```

Vectorised version of paramagpy.metal.Metal.sbm\_r2()

This is generally used for speed in fitting PRE data

#### **Parameters**

- posarray (array with shape (n, 3)) array of positions in meters
- gammaarray (array with shape (n, 3)) array of gyromagnetic ratios of the spins

Returns rates – The R2 relaxation rates in /s

**Return type** array with shape (n,1)

#### paramagpy.metal.Metal.fast second invariant squared

```
static Metal.fast_second_invariant_squared(t)
```

Vectorised version of paramagpy.metal.Metal.second\_invariant\_squared()

This is generally used for speed in fitting PRE data

Parameters tensorarray(array with shape (n, 3, 3)) - array of shielding tensors

**Returns secondInvariantSquared** – the second invariants squared of the tensors **Return type** array with shape (n,1)

### paramagpy.metal.Metal.first invariant squared

```
static Metal.first_invariant_squared(t)
```

Calculate the antisymmetric contribution to relaxation via the first invariant of a tensor.

This is required for PRE calculations using the shilding tensor

**Parameters** tensor (3x3 matrix) – a second rank tensor

**Returns** firstInvariantSquared – the first invariant squared of the shift tensor **Return type** float

### paramagpy.metal.Metal.get\_params

```
Metal.get_params (params)
```

Get tensor parameters that have been scaled appropriately

This is often used to get parameter values during fitting where floating point errors would otherwise occur on the small values encountered.

**Parameters params** (list of str) – each element of the list is a string that corresponds to an attribute of the Metal to be retrieved.

**Returns scaled\_params** – a list with respective scaled parameter values from the input. **Return type** list

# **Examples**

```
>>> metal = Metal(axrh=[20E-32, 3E-32],position=[0.0,10E-10,-5E-10])
>>> metal.get_params(['ax','rh','x','y','z'])
[20.0, 3.0, 0.0, 10.0, -5.0]
```

# paramagpy.metal.Metal.info

```
Metal.info(comment=True)
```

Get basic information about the Metal object

This is returned as a string in human readable units This is also the file format for saving the tensor

Parameters comment (bool (optional)) - if True, each line has a '#' placed at the front

**Returns information** – a string containing basic information about the Metal **Return type** str

# **Examples**

```
>>> metal = Metal()
>>> metal.set_lanthanide('Er')
>>> metal.info()
# ax | 1E-32 m^3 : -11.600
# rh | 1E-32 m^3 : -8.600
# x | 1E-10 m : 0.000
      | 1E-10 m :
# X
                       0.000
      | 1E-10 m :
# y
      | 1E-10 m : 0.000
| deg : 0.000
# z
# a
                       0.000
# b
      dea :
     -
                       0.000
# a
             dea :
# mueff |
                       9.581
              Bm :
             ppm :
# shift |
                       0.000
                      18.790
# B0 |
               T :
               K: 298.150
# temp |
                       0.189
# t1e |
              ps :
                        0.000
# taur |
              ns :
```

### paramagpy.metal.Metal.isomap

Metal.isomap (protein=None, isoval=1.0, \*\*kwargs)

# paramagpy.metal.Metal.make\_mesh

```
Metal.make_mesh (density=2, size=40.0)
```

Construct a 3D grid of points to map an isosurface

This is contained in a cube

### **Parameters**

- density (int (optional)) the points per Angstrom in the grid
- **size** (float (optional)) the length of one edge of the cube

#### Returns

- **mesh** (*cubic grid array*) This has shape (n,n,n,3) where n is the number of points along one edge of the grid. Units are meters
- **bounds** (*tuple* (*origin*, *low*, *high*, *points*)) This tuple has information about the bounding box

origin: array of floats, the (x,y,z) location of mesh vertex **low** [array of ints, the integer location of the first] point in each dimension **high** [array of ints, the integer location of the last] point in each dimension points: array of ints, the number of points along each dimension

# paramagpy.metal.Metal.pcs

```
Metal.pcs (position)
```

Calculate the psuedo-contact shift at the given postition

**Parameters** position (array floats) – the position (x, y, z) in meters

**Returns** pcs – the pseudo-contact shift in parts-per-million (ppm)

Return type float

# **Examples**

```
>>> metal = Metal()
>>> metal.set_lanthanide('Er')
>>> metal.pcs([0.,0.,10E-10])
-6.153991132886608
```

# paramagpy.metal.Metal.pcs\_mesh

Metal.pcs\_mesh(mesh)

Calculate a PCS value at each location of cubic grid of points

**Parameters mesh** (array with shape (n, n, n, 3)) – a cubic grid as generated by the method <make\_mesh>

**Returns** pcs\_mesh – The same grid shape, with PCS values at the respective locations **Return type** array with shape (n,n,n,1)

### paramagpy.metal.Metal.pre

Metal.**pre** (*position*, *gamma*, *rtype*, *dsa=True*, *sbm=True*, *csa=0.0*)

Calculate the PRE for a set of spins using Curie and or SBM theory

#### **Parameters**

- position (array of floats) position in meters
- gamma (float) gyromagnetic ratio of the spin
- rtype (str) either 'r1' or 'r2', the relaxation type
- dsa (bool (optional)) when True (defualt), DSA or Curie spin relaxation is included
- **sbm** (bool (optional)) when True (defualt), SBM spin relaxation is included
- **csa** (array with shape (3,3) (optional)) **CSA** tensor of the spin. This defualts to 0.0, meaning CSAxDSA crosscorrelation is not accounted for.

**Returns** rate – The PRE rate in /s

Return type float

# paramagpy.metal.Metal.pre\_mesh

Metal.pre\_mesh (mesh, gamma=267512897.63847807, rtype='r2', dsa=True, sbm=True) Calculate a PRE value at each location of cubic grid of points

### **Parameters**

- **mesh** (array with shape (n, n, n, 3)) a cubic grid as generated by the method <make\_mesh>
- gamma (float) the gyromagnetic ratio of the spin
- **rtype** (str) either 'r1' or 'r2', the relaxation type
- **dsa** (bool (optional)) when True (defualt), DSA or Curie spin relaxation is included
- **sbm** (bool (optional)) when True (defualt), SBM spin relaxation is included

**Returns pre\_mesh** – The same grid shape, with PRE values at the respective locations **Return type** array with shape (n,n,n,1)

# paramagpy.metal.Metal.racs

```
Metal.racs(csa)
```

Calculate the residual anisotropic chemical shift at the given postition.

The partial alignment induced by an anisotropic magnetic susceptibility causes the chemical shift tensor at a nuclear position to average to a value different to the isotropic value.

**Parameters** csa (3 x 3 array) – the chemical shift anisotropy tensor

**Returns** racs – the residual anisotropic chemical shift in parts-per-million (ppm)

Return type float

# paramagpy.metal.Metal.rads

```
Metal.rads (position)
```

Calculate the residual anisotropic dipolar shift at the given postition.

The partial alignment induced by an anisotropic magnetic susceptibility causes the dipole shift tensor at a nuclear position to average to a value different to the PCS.

**Parameters** position (array floats) – the position (x, y, z) in meters

**Returns** rads – the residual anisotropic dipole shift in parts-per-million (ppm)

Return type float

### paramagpy.metal.Metal.rdc

```
Metal.rdc(vector, gammaProd)
```

Calculate Residual Dipolar Coupling (RDC)

#### **Parameters**

- **vector** (array of floats) internuclear vector (x,y,z) in meters
- gammaProd (float) the product of gyromagnetic ratios of spin A and B where each has units of rad/s/T

Returns rdc - the RDC in Hz

Return type float

#### paramagpy.metal.Metal.save

```
Metal.save (fileName='tensor.txt')
```

# paramagpy.metal.Metal.sbm\_r1

```
Metal.sbm_r1 (position, gamma)
```

Calculate R1 relaxation due to Solomon-Bloembergen-Morgan theory

#### **Parameters**

- position (array of floats) three coordinates (x,y,z)
- gamma (float) the gyromagnetic ratio of the spin

**Returns value** – The R1 relaxation rate in /s

Return type float

# paramagpy.metal.Metal.sbm\_r2

Metal.sbm\_r2 (position, gamma)

Calculate R2 relaxation due to Solomon-Bloembergen-Morgan theory

#### **Parameters**

- **position** (array of floats) three coordinates (x,y,z)
- gamma (float) the gyromagnetic ratio of the spin

**Returns value** – The R2 relaxation rate in /s

Return type float

# paramagpy.metal.Metal.second\_invariant\_squared

# ${\tt static} \ {\tt Metal.second\_invariant\_squared} \ (t)$

Calculate the second invariant squared of a tensor.

This is required for PRE calculations using the shilding tensor

Parameters tensor (3x3 matrix) - a second rank tensor

Returns secondInvariantSquared - the second invariant squared of the shift tensor

Return type float

# paramagpy.metal.Metal.set\_Jg

$$Metal.set_Jg(J, g)$$

Set the magnetic susceptibility absolute magnitude from J/g.

This is achieved using the following formula:

$$\mu_{eff} = g\mu_B \sqrt{J(J+1)}$$

#### **Parameters**

- **J** (str) the total spin angular momentum quantum number
- **g**(bool, optional) the Lande g-factor

#### paramagpy.metal.Metal.set lanthanide

Metal.set\_lanthanide (lanthanide, set\_dchi=True)

Set the anisotropy, isotropy and T1e parameters from literature values

# **Parameters**

- lanthanide (str) –
   one of ['Ce','Pr','Nd','Pm','Sm','Eu','Gd', 'Tb','Dy','Ho','Er','Tm','Yb']
- **set\_dichi** (bool (optional)) if True (default), the tensor anisotropy is set. Otherwise only the isotropy and T1e values are set

# paramagpy.metal.Metal.set\_params

Metal.set\_params (paramValues)

Set tensor parameters that have been scaled appropriately

This is the inverse of the method <get\_params>

**Parameters** paramValues (list of tuple) – each element is a tuple (variable, value) where 'variable' is the string indentifying the attribute to be set, and 'value' is the corresponding value

### **Examples**

```
>>> metal = Metal()
>>> metal.set_params([('ax',20.0),('rh',3.0)])
>>> metal.axrh
[2.e-31 3.e-32]
```

### paramagpy.metal.Metal.set utr

Metal.set\_utr()

Modify current tensor parameters to unique tensor representation (UTR)

Note that multiple axial/rhombic and euler angles can give congruent tensors. This method ensures that identical tensors may always be compared by using Numbat style representation.

# paramagpy.metal.Metal.spec\_dens

static Metal.spec dens(tau, omega)

A spectral density function with Lorentzian shape:

$$\mathbb{J}(\tau,\omega) = \frac{\tau}{1 + (\omega\tau)^2}$$

#### **Parameters**

- tau (float) correaltion time
- omega (float) frequency

**Returns value** – the value of the spectral denstiy

Return type float

### paramagpy.metal.Metal.write\_isomap

 ${\tt Metal.write\_isomap}~(\textit{mesh}, \textit{bounds}, \textit{fileName} = \textit{'isomap.pml.ccp4'})$ 

Write a PyMol script to file which allows loading of the isosurface file

### **Parameters**

- mesh (3D scalar np.ndarray of floats) the scalar field of PCS or PRE values in a cubic grid
- bounds (tuple (origin, low, high, points)) as generated by paramagpy.metal.Metal.make\_mesh()
- **fileName** (str (optional)) the filename of the isosurface file

# paramagpy.metal.Metal.write\_pymol\_script

 $\label{eq:metal.write_pymol_script} Metal. write_pymol_script (isoval=1.0, surfaceName='isomap', script-Name='isomap.pml', meshName='./isomap.pml.ccp4', pdbFile=None)$ 

Write a PyMol script to file which allows loading of the isosurface file

# **Parameters**

- isoval (float (optional)) the contour level of the isosurface
- **surfaceName** (*str* (*optional*)) the name of the isosurface file within PyMol
- scriptName (str (optional)) the name of the PyMol script to load the tensor isosurface
- meshName (str (optional)) the name of the binary isosurface file
- **pdbFile** (str (optional)) if not <None>, the file name of the PDB file to be loaded with the isosurface.

# **Attributes**

BO_MHz	1H NMR frequency for the given field in MHz
GAMMA	1 ,
HBAR	
K	
MU0	
MUB	
а	alpha euler anglue
alignment_factor	Factor for conversion between magnetic suscep-
	tibility and alignment tensors
ax	axiality
b	beta euler anglue
eigenvalues	The eigenvalues defining the magnitude of the
	principle axes
fit_scaling	
g	gamma euler anglue
iso	isotropy
isotropy	The magnidue of the isotropic component of the
	tensor
lanth_axrh	
lanth_lib	
lower_coords	
rh	rhombicity
rotationMatrix	The rotation matrix as defined by the euler an-
	gles
saupe_factor	Factor for conversion between magnetic suscep-
	tibility and saupe tensors
tauc	The effective rotational correlation time.
tensor	The magnetic susceptibility tensor matrix repre-
	sentation
tensor_alignment	The alignment tensor matrix representation
tensor_saupe	The saupe tensor matrix representation
tensor_traceless	The traceless magnetic susceptibility tensor ma-
	trix representation
upper_coords	Continued on next page

Continued on next page

Table 4 – continued from previous page

upper_triang	Fetch 5 unique matrix element defining the
	magnetic susceptibility tensor
upper_triang_alignment	Fetch 5 unique matrix element defining the
	alignment tensor
upper_triang_saupe	Fetch 5 unique matrix element defining the
	magnetic susceptibility tensor
X	x coordinate
Y	y coordinate
Z	z coordinate

# paramagpy.metal.Metal.B0\_MHz

Metal.B0\_MHz

1H NMR frequency for the given field in MHz

# paramagpy.metal.Metal.GAMMA

Metal.GAMMA = 176085964400.0

# paramagpy.metal.Metal.HBAR

Metal.HBAR = 1.0546e-34

# paramagpy.metal.Metal.K

Metal.K = 1.381e-23

# paramagpy.metal.Metal.MU0

Metal.MU0 = 1.2566370614359173e-06

# paramagpy.metal.Metal.MUB

Metal.MUB = 9.274e-24

# paramagpy.metal.Metal.a

Metal.a

alpha euler anglue

# paramagpy.metal.Metal.alignment\_factor

#### Metal.alignment\_factor

Factor for conversion between magnetic susceptibility and alignment tensors

# paramagpy.metal.Metal.ax

Metal.ax axiality

# paramagpy.metal.Metal.b

```
Metal.b beta euler anglue
```

# paramagpy.metal.Metal.eigenvalues

# Metal.eigenvalues

The eigenvalues defining the magnitude of the principle axes

# paramagpy.metal.Metal.fit\_scaling

```
Metal.fit_scaling = {'a': 57.29577951308232, 'ax': 1e+32, 'b': 57.29577951308
```

# paramagpy.metal.Metal.g

```
Metal.g gamma euler anglue
```

### paramagpy.metal.Metal.iso

```
Metal.iso isotropy
```

# paramagpy.metal.Metal.isotropy

```
Metal.isotropy
```

The magnidue of the isotropic component of the tensor

# paramagpy.metal.Metal.lanth\_axrh

```
Metal.lanth_axrh = {'Ce': (2.1, 0.7), 'Dy': (34.7, 20.3), 'Er': (-11.6, -8.6)
```

# paramagpy.metal.Metal.lanth\_lib

```
Metal.lanth_lib = {'Ce': (2.5, 0.8571428571428571, 1.33e-13), 'Dy': (7.5, 1.33e-13)
```

# paramagpy.metal.Metal.lower\_coords

```
Metal.lower\_coords = ((0, 1, 1, 2, 2), (0, 1, 0, 0, 1))
```

# paramagpy.metal.Metal.rh

```
Metal.rh rhombicity
```

#### paramagpy.metal.Metal.rotationMatrix

#### Metal.rotationMatrix

The rotation matrix as defined by the euler angles

# paramagpy.metal.Metal.saupe\_factor

#### Metal.saupe\_factor

Factor for conversion between magnetic susceptibility and saupe tensors

# paramagpy.metal.Metal.tauc

#### Metal.tauc

The effective rotational correlation time.

This is calculated by combining the rotational correlation time and the electronic relaxation time:

$$\tau_c = \frac{1}{\frac{1}{\tau_r} + \frac{1}{T_{1e}}}$$

#### paramagpy.metal.Metal.tensor

#### Metal.tensor

The magnetic susceptibility tensor matrix representation

# paramagpy.metal.Metal.tensor\_alignment

# Metal.tensor\_alignment

The alignment tensor matrix representation

### paramagpy.metal.Metal.tensor\_saupe

# Metal.tensor\_saupe

The saupe tensor matrix representation

# paramagpy.metal.Metal.tensor\_traceless

# Metal.tensor\_traceless

The traceless magnetic susceptibility tensor matrix representation

# paramagpy.metal.Metal.upper\_coords

Metal.upper\_coords = ((0, 1, 0, 0, 1), (0, 1, 1, 2, 2))

# paramagpy.metal.Metal.upper\_triang

# Metal.upper\_triang

Fetch 5 unique matrix element defining the magnetic susceptibility tensor

# paramagpy.metal.Metal.upper\_triang\_alignment

# Metal.upper\_triang\_alignment

Fetch 5 unique matrix element defining the alignment tensor

# paramagpy.metal.Metal.upper\_triang\_saupe

#### Metal.upper\_triang\_saupe

Fetch 5 unique matrix element defining the magnetic susceptibility tensor

# paramagpy.metal.Metal.x

```
Metal.x
```

x coordinate

# paramagpy.metal.Metal.y

```
Metal.y y coordinate
```

# paramagpy.metal.Metal.z

Metal.z

z coordinate

#### 5.5.2 Protein module

This module handles the protein structure coordinates and includes methods for loading a PDB file and calculating atomic properites such as CSA or gyromagnetic ratio

# paramagpy.protein

### **Functions**

load_pdb(fileName[, ident])	Read PDB from file into biopython structure object
rotation_matrix(axis, theta)	Return the rotation matrix associated with counter-
	clockwise rotation about the given axis by theta ra-
	dians.

# paramagpy.protein.load\_pdb

paramagpy.protein.load\_pdb (fileName, ident=None)

Read PDB from file into biopython structure object

### **Parameters**

- **fileName** (str) the path to the file
- ident (str (optional)) the desired identity of the structure object

Returns values – a structure object containing the atomic coordinates

Return type paramagpy.protein.CustomStructure

# paramagpy.protein.rotation\_matrix

paramagpy.protein.rotation\_matrix(axis, theta)

Return the rotation matrix associated with counterclockwise rotation about the given axis by theta radians.

**Parameters axis**  $(array \ of \ floats)$  – the [x,y,z] axis for rotation.

**Returns** matrix – the rotation matrix

Return type numpy 3x3 matrix object

#### **Classes**

CustomAtom(*arg, **kwargs)	
CustomStructure(*arg, **kwargs)	This is an overload hack of the BioPython Structure
	object
CustomStructureBuilder(*arg, **kwargs)	This is an overload hack of BioPython's Custom-
	StructureBuilder

### paramagpy.protein.CustomAtom

class paramagpy.protein.CustomAtom(\*arg, \*\*kwargs)

\_\_init\_\_ (\*arg, \*\*kwargs)
Create Atom object.

The Atom object stores atom name (both with and without spaces), coordinates, B factor, occupancy, alternative location specifier and (optionally) anisotropic B factor and standard deviations of B factor and positions.

### **Parameters**

- name (string) atom name (eg. "CA"). Note that spaces are normally stripped.
- coord (Numeric array (Float0, size 3)) atomic coordinates (x,y,z)
- bfactor (number) isotropic B factor
- occupancy (number) occupancy (0.0-1.0)
- altloc (string) alternative location specifier for disordered atoms
- **fullname** (*string*) full atom name, including spaces, e.g. "CA ". Normally these spaces are stripped from the atom name.
- **element** (uppercase string (or None if unknown)) atom element, e.g. "C" for Carbon, "HG" for mercury,

### **Methods**

copy()	Create a copy of the Atom.
detach_parent()	Remove reference to parent.
dipole_shift_tensor(position)	Calculate the magnetic field shielding tensor at
	the given postition due to the nuclear dipole
flag_disorder()	Set the disordered flag to 1.
get_altloc()	Return alternative location specifier.
·	•

Continued on next page

Table 7 – continued from previous page

	oontinaca nom previous page
get_anisou()	Return anisotropic B factor.
get_bfactor()	Return B factor.
get_coord()	Return atomic coordinates.
get_full_id()	Return the full id of the atom.
get_fullname()	Return the atom name, including leading and
	trailing spaces.
get_id()	Return the id of the atom (which is its atom
	name).
get_level()	
get_name()	Return atom name.
get_occupancy()	Return occupancy.
get_parent()	Return parent residue.
<pre>get_serial_number()</pre>	
get_sigatm()	Return standard deviation of atomic parame-
	ters.
get_siguij()	Return standard deviations of anisotropic tem-
	perature factors.
get_vector()	Return coordinates as Vector.
is_disordered()	Return the disordered flag (1 if disordered, 0
	otherwise).
set_altloc(altloc)	
set_anisou(anisou_array)	Set anisotropic B factor.
set_bfactor(bfactor)	
set_coord(coord)	
<pre>set_occupancy(occupancy)</pre>	
set_parent(parent)	Set the parent residue.
set_serial_number(n)	
<pre>set_sigatm(sigatm_array)</pre>	Set standard deviation of atomic parameters.
set_siguij(siguij_array)	Set standard deviations of anisotropic tempera-
	ture factors.
top()	
transform(rot, tran)	Apply rotation and translation to the atomic co-
	ordinates.

# paramagpy.protein.CustomAtom.copy

CustomAtom.copy()

Create a copy of the Atom.

Parent information is lost.

# $paramagpy.protein. Custom Atom. detach\_parent$

CustomAtom.detach\_parent()

Remove reference to parent.

# paramagpy.protein.CustomAtom.dipole\_shift\_tensor

CustomAtom.dipole\_shift\_tensor(position)

Calculate the magnetic field shielding tensor at the given postition due to the nuclear dipole

Assumes nuclear spin 1/2

**Parameters** position (array floats) – the position (x, y, z) in meters

```
Returns dipole_shielding_tensor – the tensor describing magnetic shielding at the given position
```

```
Return type 3x3 array
```

# paramagpy.protein.CustomAtom.flag\_disorder

```
CustomAtom.flag_disorder()
Set the disordered flag to 1.
```

The disordered flag indicates whether the atom is disordered or not.

### paramagpy.protein.CustomAtom.get\_altloc

```
CustomAtom.get_altloc()
```

Return alternative location specifier.

# paramagpy.protein.CustomAtom.get\_anisou

```
CustomAtom.get_anisou()
```

Return anisotropic B factor.

# paramagpy.protein.CustomAtom.get\_bfactor

```
CustomAtom.get_bfactor()
```

Return B factor.

### paramagpy.protein.CustomAtom.get coord

```
CustomAtom.get_coord()
```

Return atomic coordinates.

# paramagpy.protein.CustomAtom.get\_full\_id

```
CustomAtom.get_full_id()
```

Return the full id of the atom.

The full id of an atom is the tuple (structure id, model id, chain id, residue id, atom name, altloc).

# paramagpy.protein.CustomAtom.get\_fullname

```
CustomAtom.get_fullname()
```

Return the atom name, including leading and trailing spaces.

### paramagpy.protein.CustomAtom.get\_id

```
CustomAtom.get_id()
```

Return the id of the atom (which is its atom name).

```
paramagpy.protein.CustomAtom.get_level
CustomAtom.get_level()
paramagpy.protein.CustomAtom.get_name
CustomAtom.get_name()
    Return atom name.
paramagpy.protein.CustomAtom.get_occupancy
CustomAtom.get_occupancy()
    Return occupancy.
paramagpy.protein. Custom Atom.get\_parent
CustomAtom.get_parent()
    Return parent residue.
paramagpy.protein.CustomAtom.get_serial_number
CustomAtom.get_serial_number()
paramagpy.protein.CustomAtom.get_sigatm
CustomAtom.get_sigatm()
    Return standard deviation of atomic parameters.
paramagpy.protein.CustomAtom.get_siguij
CustomAtom.get_siguij()
    Return standard deviations of anisotropic temperature factors.
paramagpy.protein.CustomAtom.get_vector
CustomAtom.get_vector()
    Return coordinates as Vector.
        Returns coordinates as 3D vector
        Return type Bio.PDB. Vector class
paramagpy.protein.CustomAtom.is_disordered
CustomAtom.is_disordered()
    Return the disordered flag (1 if disordered, 0 otherwise).
paramagpy.protein.CustomAtom.set_altloc
CustomAtom.set_altloc(altloc)
```

```
paramagpy.protein.CustomAtom.set anisou
CustomAtom.set_anisou(anisou_array)
    Set anisotropic B factor.
        Parameters anisou_array (Numeric array (length 6)) - anisotropic B
paramagpy.protein.CustomAtom.set_bfactor
CustomAtom.set_bfactor(bfactor)
paramagpy.protein.CustomAtom.set_coord
CustomAtom.set_coord(coord)
paramagpy.protein.CustomAtom.set_occupancy
CustomAtom.set_occupancy(occupancy)
paramagpy.protein.CustomAtom.set_parent
CustomAtom.set_parent (parent)
    Set the parent residue.
        Parameters parent - Residue object (-)-
paramagpy.protein.CustomAtom.set serial number
CustomAtom.set_serial_number(n)
paramagpy.protein.CustomAtom.set_sigatm
CustomAtom.set_sigatm(sigatm_array)
    Set standard deviation of atomic parameters.
    The standard deviation of atomic parameters consists of 3 positional, 1 B factor and 1 occupancy
    standard deviation.
        Parameters sigatm_array (Numeric array (length 5)) - standard de-
           viations of atomic parameters.
paramagpy.protein.CustomAtom.set_siguij
CustomAtom.set_siguij (siguij_array)
    Set standard deviations of anisotropic temperature factors.
        Parameters siguij_array (Numeric array (length 6)) - standard de-
           viations of anisotropic temperature factors.
paramagpy.protein.CustomAtom.top
CustomAtom.top()
```

# paramagpy.protein.CustomAtom.transform

```
CustomAtom.transform(rot, tran)
```

Apply rotation and translation to the atomic coordinates.

#### **Parameters**

- rot (3x3 Numeric array) A right multiplying rotation matrix
- tran (size 3 Numeric array) the translation vector

### **Examples**

```
>>> rotation=rotmat(pi, Vector(1, 0, 0))
>>> translation=array((0, 0, 1), 'f')
>>> atom.transform(rotation, translation)
```

#### **Attributes**

IID 3 D	
HBAR	
MU0	
csa	Get the CSA tensor at the nuclear position This
	uses the geometry of neighbouring atoms and a
	standard library from Bax J.
csa_lib	docstring for CustomAtom
gyro_lib	
position	

# paramagpy.protein.CustomAtom.HBAR

CustomAtom.HBAR = 1.0546e-34

# paramagpy.protein.CustomAtom.MU0

CustomAtom.MU0 = 1.2566370614359173e-06

# paramagpy.protein.CustomAtom.csa

CustomAtom.csa

Get the CSA tensor at the nuclear position This uses the geometry of neighbouring atoms and a standard library from Bax J. Am. Chem. Soc. 2000

**Returns matrix** – the CSA tensor in the PDB frame if appropriate nuclear positions are not available <None> is returned.

**Return type** 3x3 array

# paramagpy.protein.CustomAtom.csa\_lib

```
CustomAtom.csa_lib = {'C': (array([-8.65e-05, 1.18e-05, 7.47e-05]), 0.663225115
    docstring for CustomAtom
```

# paramagpy.protein.CustomAtom.gyro\_lib

CustomAtom.gyro\_lib = {'C': 67261498.71335746, 'H': 267512897.63847807, 'N': -2

# paramagpy.protein.CustomAtom.position

 ${\tt CustomAtom.position}$ 

# paramagpy.protein.CustomStructure

```
class paramagpy.protein.CustomStructure(*arg, **kwargs)
    This is an overload hack of the BioPython Structure object
    __init__(*arg, **kwargs)
    Initialize the class.
```

#### **Methods**

add(entity)	Add a child to the Entity.
copy()	
detach_child(id)	Remove a child.
detach_parent()	Detach the parent.
<pre>get_atoms()</pre>	
get_chains()	
get_full_id()	Return the full id.
get_id()	Return the id.
<pre>get_iterator()</pre>	Return iterator over children.
get_level()	Return level in hierarchy.
get_list()	Return a copy of the list of children.
<pre>get_models()</pre>	
<pre>get_parent()</pre>	Return the parent Entity object.
get_residues()	
has_id(id)	Check if a child with given id exists.
insert(pos, entity)	Add a child to the Entity at a specified position.
parse(dataValues[, models])	
set_parent(entity)	Set the parent Entity object.
transform(rot, tran)	Apply rotation and translation to the atomic co-
	ordinates.

# paramagpy.protein.CustomStructure.add

```
CustomStructure.add(entity)
Add a child to the Entity.
```

# paramagpy.protein.CustomStructure.copy

CustomStructure.copy()

# paramagpy.protein.CustomStructure.detach\_child

CustomStructure.detach\_child(id)
Remove a child.

# paramagpy.protein.CustomStructure.detach\_parent

```
CustomStructure.detach_parent()

Detach the parent.
```

# paramagpy.protein.CustomStructure.get\_atoms

```
CustomStructure.get_atoms()
```

#### paramagpy.protein.CustomStructure.get chains

```
CustomStructure.get_chains()
```

### paramagpy.protein.CustomStructure.get full id

```
CustomStructure.get_full_id()
```

Return the full id.

The full id is a tuple containing all id's starting from the top object (Structure) down to the current object. A full id for a Residue object e.g. is something like:

```
("1abc", 0, "A", (" ", 10, "A"))
```

This corresponds to:

Structure with id "labc" Model with id 0 Chain with id "A" Residue with id (", 10, "A")

The Residue id indicates that the residue is not a hetero-residue (or a water) because it has a blank hetero field, that its sequence identifier is 10 and its insertion code "A".

# paramagpy.protein.CustomStructure.get\_id

```
CustomStructure.get_id()
Return the id.
```

# paramagpy.protein.CustomStructure.get\_iterator

```
CustomStructure.get_iterator()
Return iterator over children.
```

# paramagpy.protein.CustomStructure.get\_level

```
\label{eq:customStructure.get_level()} Return \ level \ in \ hierarchy. A - atom \ R - residue \ C - chain \ M - model \ S - structure
```

paramagpy.protein.CustomStructure.get\_list

```
CustomStructure.get_list()

Return a copy of the list of children.
```

# paramagpy.protein.CustomStructure.get\_models

```
CustomStructure.get_models()
```

# paramagpy.protein.CustomStructure.get\_parent

```
CustomStructure.get_parent()
Return the parent Entity object.
```

# paramagpy.protein.CustomStructure.get\_residues

```
CustomStructure.get_residues()
```

### paramagpy.protein.CustomStructure.has id

```
CustomStructure.has_id (id)

Check if a child with given id exists.
```

### paramagpy.protein.CustomStructure.insert

```
CustomStructure.insert (pos, entity)

Add a child to the Entity at a specified position.
```

# paramagpy.protein.CustomStructure.parse

CustomStructure.parse(dataValues, models=None)

#### paramagpy.protein.CustomStructure.set\_parent

```
CustomStructure.set_parent (entity)
Set the parent Entity object.
```

# paramagpy.protein.CustomStructure.transform

```
CustomStructure.transform(rot, tran)
```

Apply rotation and translation to the atomic coordinates.

#### **Parameters**

- rot (3x3 Numeric array) A right multiplying rotation matrix
- tran (size 3 Numeric array) the translation vector

# **Examples**

```
>>> rotation = rotmat(pi, Vector(1, 0, 0))
>>> translation = array((0, 0, 1), 'f')
>>> entity.transform(rotation, translation)
```

### **Attributes**

id

# paramagpy.protein.CustomStructure.id

CustomStructure.id

#### paramagpy.protein.CustomStructureBuilder

### **Methods**

	D : 1 : 1
get_structure()	Return the structure.
<pre>init_atom(name, coord, b_factor, occu-</pre>	Create a new Atom object.
pancy,)	
init_chain(chain_id)	Create a new Chain object with given id.
<pre>init_model(model_id[, serial_num])</pre>	Create a new Model object with given id.
init_residue(resname, field, resseq,	Create a new Residue object.
icode)	
init_seg(segid)	Flag a change in segid.
<pre>init_structure(structure_id)</pre>	Initialize a new Structure object with given id.
set_anisou(anisou_array)	Set anisotropic B factor of current Atom.
set_header(header)	
set_line_counter(line_counter)	Tracks line in the PDB file that is being parsed.
set_sigatm(sigatm_array)	Set standard deviation of atom position of cur-
	rent Atom.
set_siguij(siguij_array)	Set standard deviation of anisotropic B factor of
	current Atom.
<pre>set_symmetry(spacegroup, cell)</pre>	

### paramagpy.protein.CustomStructureBuilder.get\_structure

```
CustomStructureBuilder.get_structure()
    Return the structure.
```

# paramagpy.protein.CustomStructureBuilder.init atom

```
CustomStructureBuilder.init_atom(name, coord, b_factor, occupancy, alt-
loc, fullname, serial_number=None, ele-
ment=None)
```

Create a new Atom object. :param - name - string, atom name, e.g. CA, spaces should be stripped: :param - coord - Numeric array: :type - coord - Numeric array: Float0, size 3 :param - b\_factor - float, B factor: :param - occupancy - float: :param - altloc - string, alternative location specifier: :param - fullname - string, atom name including spaces, e.g. "CA ": :param - element - string, upper case, e.g. "HG" for mercury:

# paramagpy.protein.CustomStructureBuilder.init\_chain

```
CustomStructureBuilder.init_chain (chain_id)
Create a new Chain object with given id.
```

```
Parameters chain_id - string(-)-
```

# paramagpy.protein.CustomStructureBuilder.init\_model

CustomStructureBuilder.init\_model (model\_id, serial\_num=None)
Create a new Model object with given id.

#### **Parameters**

- id int (-)-
- serial\_num int(-)-

### paramagpy.protein.CustomStructureBuilder.init\_residue

CustomStructureBuilder.init\_residue (resname, field, resseq, icode)
Create a new Residue object.

#### **Parameters**

- resname string, e.g. "ASN" (-) -
- field hetero flag, "W" for waters, "H" for (-) hetero residues, otherwise blank.
- resseq int, sequence identifier (-) -
- icode string, insertion code (-) -

#### paramagpy.protein.CustomStructureBuilder.init seg

```
CustomStructureBuilder.init_seg(segid) Flag a change in segid.
```

```
Parameters segid - string(-)-
```

# paramagpy.protein.CustomStructureBuilder.init\_structure

```
CustomStructureBuilder.init_structure(structure_id)
Initialize a new Structure object with given id.
```

```
Parameters id - string(-)-
```

# paramagpy.protein.CustomStructureBuilder.set\_anisou

```
CustomStructureBuilder.set_anisou(anisou_array)
Set anisotropic B factor of current Atom.
```

### paramagpy.protein.CustomStructureBuilder.set header

```
CustomStructureBuilder.set_header(header)
```

### paramagpy.protein.CustomStructureBuilder.set line counter

```
CustomStructureBuilder.set_line_counter(line_counter)
Tracks line in the PDB file that is being parsed.
```

```
Parameters line_counter - int(-)-
```

# paramagpy.protein.CustomStructureBuilder.set\_sigatm

```
CustomStructureBuilder.set_sigatm(sigatm_array)
Set standard deviation of atom position of current Atom.
```

# paramagpy.protein.CustomStructureBuilder.set\_siguij

```
CustomStructureBuilder.set_siguij (siguij_array)
Set standard deviation of anisotropic B factor of current Atom.
```

# paramagpy.protein.CustomStructureBuilder.set\_symmetry

CustomStructureBuilder.set\_symmetry(spacegroup, cell)

# 5.5.3 Data I/O module

This module handles the reading and writing of experimental data.

# paramagpy.dataparse

# **Functions**

read_pcs(fileName)	Read pseudo contact shift values from file.
read_rdc(fileName)	Read residual dipolar coupling values from file.
read_pre(fileName)	Read paramagnetic relaxation enhancement values
	from file.
read_ccr(fileName)	Read cross-correlated relaxation values from file.

# paramagpy.dataparse.read\_pcs

```
paramagpy.dataparse.read_pcs(fileName)
```

Read pseudo contact shift values from file. The returned object is a dicationary. They keys are tuples of (sequence, atomName) The values are tuples of (value, error)

```
Parameters fileName (str) – the path to the file
```

Returns values – a dictionary containing the parsed data

Return type paramagpy.dataparse.DataContainer

# **Examples**

```
>>> values = paramagpy.dataparse.read_pcs("calbindin_Er_HN_PCS_errors.npc")
>>> for v in values.items():
... print(v)
```

(continues on next page)

(continued from previous page)

```
((2, 'H'), (-0.04855485, 0.0016))

((2, 'N'), (-0.03402764, 0.0009))

((4, 'H'), (-0.18470315, 0.0004))

...

((75, 'H'), (0.19553661, 0.0005))

((75, 'N'), (0.17840666, 0.0004))
```

### paramagpy.dataparse.read rdc

```
paramagpy.dataparse.read_rdc(fileName)
```

Read residual dipolar coupling values from file. The returned object is a dicationary. They keys are frozensets of tuples of the form: frozenset({(sequence1, atomName1), (sequence2, atomName2)}) The frozenset only allows unordered unique atom identification pairs The values are tuples of (value, error)

**Parameters fileName** (str) – the path to the file

Returns values – a dictionary containing the parsed data

Return type paramagpy.dataparse.DataContainer

# **Examples**

```
>>> values = paramagpy.dataparse.read_rdc("ubiquitin_a28c_c1_Tb_HN.rdc")
>>> for v in values.items():
... print(v)
...
(frozenset({(2, 'N'), (2, 'H')}), (-2.35, 0.32))
(frozenset({(3, 'N'), (3, 'H')}), (-4.05, 0.38))
(frozenset({(4, 'H'), (4, 'N')}), (-3.58, 0.42))
...
(frozenset({(73, 'N'), (73, 'H')}), (-0.47, 0.75))
(frozenset({(76, 'H'), (76, 'N')}), (0.14, 0.3))
```

# paramagpy.dataparse.read\_pre

```
paramagpy.dataparse.read_pre (fileName)
```

Read paramagnetic relaxation enhancement values from file. The returned object is a dicationary. They keys are tuples of (sequence, atomName) The values are tuples of (value, error)

**Parameters fileName** (str) – the path to the file

**Returns values** – a dictionary containing the parsed data

Return type paramagpy.dataparse.DataContainer

# **Examples**

see paramagpy.dataparse.read\_pcs() which has the same file structure

### paramagpy.dataparse.read\_ccr

```
paramagpy.dataparse.read_ccr(fileName)
```

Read cross-correlated relaxation values from file. These are typically Curie-spin cross Dipole-dipole relaxation rates The returned object is a dicationary. They keys are tuples of the form: ((sequence1, atomName1),

(sequence2, atomName2)) Note that the first column is for the active nucleus undergoing relaxation and the second column is for the partner spin. The values are tuples of (value, error)

**Parameters fileName** (str) – the path to the file

Returns values – a dictionary containing the parsed data

Return type paramagpy.dataparse.DataContainer

# **Examples**

see paramagpy.dataparse.read\_rdc() which has the similar file structure

#### **Classes**

DataContainer(*args, **kwargs)	A dictionary-like container for storing PCS, RDC,
	PRE and CCR data Has an additional attribute 'dtype'
	to define datatype

# paramagpy.dataparse.DataContainer

class paramagpy.dataparse.DataContainer(\*args, \*\*kwargs)

A dictionary-like container for storing PCS, RDC, PRE and CCR data Has an additional attribute 'dtype' to define datatype

\_\_\_init\_\_\_(\*args, \*\*kwargs)

Initialize self. See help(type(self)) for accurate signature.

# **Methods**

clear()	
copy()	
fromkeys(S[, v])	If not specified, the value defaults to None.
get(k[,d])	
items()	
keys()	
move_to_end	Move an existing element to the end (or begin-
	ning if last==False).
pop(k[,d])	value.
popitem()	Pairs are returned in LIFO order if last is true or
	FIFO order if false.
setdefault(k[,d])	
update([E, ]**F)	If E is present and has a .keys() method, then
	does: for k in E: $D[k] = E[k]$ If E is present and
	lacks a .keys() method, then does: for k, v in E:
	D[k] = v In either case, this is followed by: for
	k  in  F: D[k] = F[k]
values()	

# paramagpy.dataparse.DataContainer.clear

 ${\tt DataContainer.clear()} \to None. \ Remove \ all \ items \ from \ od.$ 

## paramagpy.dataparse.DataContainer.copy

DataContainer.copy()  $\rightarrow$  a shallow copy of od

## paramagpy.dataparse.DataContainer.fromkeys

DataContainer.fromkeys  $(S[, v]) \rightarrow \text{New ordered dictionary with keys from S.}$  If not specified, the value defaults to None.

## paramagpy.dataparse.DataContainer.get

DataContainer.get  $(k[,d]) \rightarrow D[k]$  if k in D, else d. d defaults to None.

## paramagpy.dataparse.DataContainer.items

DataContainer.items ()  $\rightarrow$  a set-like object providing a view on D's items

## paramagpy.dataparse.DataContainer.keys

DataContainer.keys()  $\rightarrow$  a set-like object providing a view on D's keys

## paramagpy.dataparse.DataContainer.move\_to\_end

```
DataContainer.move_to_end()
```

Move an existing element to the end (or beginning if last==False).

Raises KeyError if the element does not exist. When last=True, acts like a fast version of self[key]=self.pop(key).

#### paramagpy.dataparse.DataContainer.pop

DataContainer.pop  $(k[,d]) \rightarrow v$ , remove specified key and return the corresponding value. If key is not found, d is returned if given, otherwise KeyError is raised.

#### paramagpy.dataparse.DataContainer.popitem

DataContainer.popitem()  $\rightarrow$  (k, v), return and remove a (key, value) pair. Pairs are returned in LIFO order if last is true or FIFO order if false.

## paramagpy.dataparse.DataContainer.setdefault

DataContainer.setdefault  $(k \mid d) \rightarrow \text{od.get}(k,d)$ , also set od[k]=d if k not in od

## paramagpy.dataparse.DataContainer.update

DataContainer.update ([E], \*\*F)  $\rightarrow$  None. Update D from dict/iterable E and F. If E is present and has a .keys() method, then does: for k in E: D[k] = E[k] If E is present and lacks a .keys() method, then does: for k, v in E: D[k] = v In either case, this is followed by: for k in F: D[k] = F[k]

## paramagpy.dataparse.DataContainer.values

<code>DataContainer.values()</code>  $\rightarrow$  an object providing a view on D's values

## 5.5.4 Fitting module

This module handles the fitting of paramagnetic objects to experimental data.

paramagpy.fit

## paramagpy.fit

## **Functions**

cantor_pairing(a, b)	Map two integers to a single integer.
clean_indices(indices)	Uniquely map a list of integers to their smallest size.
ensemble_average(atoms, *values)	
extract_ccr(data)	Extract values required for CCR calculations
extract_csa(data)	Extract CSA tensors from atoms
extract_pcs(data)	Extract values required for PCS calculations
extract_pre(data)	Extract values required for PRE calculations
extract_rdc(data)	Extract values required for RDC calculations
nlr_fit_metal_from_ccr(initMetals, ccrs[,	Fit deltaChi tensor to CCR values using non-linear re-
])	gression.
nlr_fit_metal_from_pcs(initMetals, pcss[,	Fit deltaChi tensor to PCS values using non-linear re-
])	gression.
<pre>nlr_fit_metal_from_pre(initMetals, pres[,</pre>	Fit deltaChi tensor to PRE values using non-linear re-
])	gression.
nlr_fit_metal_from_rdc(metal, rdc[,	Fit deltaChi tensor to RDC values using non-linear
params,])	regression.
pcs_fit_error_bootstrap(initMetals, pcss,	Analyse uncertainty of PCS fit by Bootstrap methods.
)	
<pre>pcs_fit_error_monte_carlo(initMetals,</pre>	Analyse uncertainty of PCS fit by Monte-Carlo simu-
pcss,)	lation This repeatedly adds noise to experimental PCS
	data and fits the tensor.
<pre>qfactor(experiment, calculated[, sumIndices])</pre>	Calculate the Q-factor to judge tensor fit quality
sphere_grid(origin, radius, points)	Make a grid of cartesian points within a sphere
<pre>svd_calc_metal_from_pcs(pos, pcs, idx, er-</pre>	Solve PCS equation by single value decomposition.
rors)	
<pre>svd_calc_metal_from_pcs_offset(pos,</pre>	Solve PCS equation by single value decomposition
pcs,)	with offset.
<pre>svd_calc_metal_from_rdc(vec,)</pre>	Solve RDC equation by single value decomposition.
<pre>svd_fit_metal_from_rdc(metal, rdc[, su-</pre>	Fit deltaChi tensor to RDC values using SVD algo-
mIndices])	rithm.
svd_gridsearch_fit_metal_from_pcs(metalsFit deltaChi tensor to PCS values using Single Value	
pcss)	Decomposition over a grid of points in a sphere.
unique_pairing(a, b)	Bijectively map two integers to a single integer.

## paramagpy.fit.cantor\_pairing

paramagpy.fit.cantor\_pairing(a, b)

Map two integers to a single integer. The mapped space is minimum size. Ordering matters in this case. see Bijective mapping f:ZxZ->N.

#### **Parameters**

- a (int) -
- **b**(int)-

**Returns** c – bijective mapping (a, b) -> c

Return type int

#### paramagpy.fit.clean indices

```
paramagpy.fit.clean_indices(indices)
```

Uniquely map a list of integers to their smallest size. For example: [7,4,7,9,9,10,1] -> [4 2 4 0 0 1 3]

Parameters indices (array-like integers) - a list of integers

**Returns** new\_indices – the mapped integers with smallest size

Return type array-like integers

## paramagpy.fit.ensemble\_average

```
paramagpy.fit.ensemble_average(atoms, *values)
```

#### paramagpy.fit.extract ccr

```
paramagpy.fit.extract_ccr(data)
```

Extract values required for CCR calculations

**Parameters data** (list of lists) – A list with elements [Atom1, Atom2, value, error], where Atom is an Atom object, value is the CCR value, and error is the uncertainty

Returns tuple – all information required for CCR calculations

Return type dict

## paramagpy.fit.extract\_csa

```
paramagpy.fit.extract_csa(data)
```

Extract CSA tensors from atoms

**Parameters data** (list of lists) – A list with elements [Atom, value, error], where Atom is an Atom object, value is the PCS/RDC/PRE value, and error is the uncertainty

Returns csas – an array of each CSA tensor

**Return type** array of 3x3 arrays

## paramagpy.fit.extract pcs

```
paramagpy.fit.extract_pcs(data)
```

Extract values required for PCS calculations

**Parameters data** (list of lists) – A list with elements [Atom, value, error], where Atom is an Atom object, value is the PCS value, and error is the uncertainty

**Returns** tuple – all information required for PCS calculations

Return type (atom coordinates, PCS values, PCS errors, atom indices)

#### paramagpy.fit.extract pre

```
paramagpy.fit.extract_pre(data)
```

Extract values required for PRE calculations

**Parameters data** (list of lists) – A list with elements [Atom, value, error], where Atom is an Atom object, value is the PRE value, and error is the uncertainty

**Returns** tuple – all information required for PRE calculations

Return type (atom coordinates, PRE values, PRE errors, atom indices)

#### paramagpy.fit.extract rdc

```
paramagpy.fit.extract_rdc(data)
```

Extract values required for RDC calculations

**Parameters data** (*list of lists*) – A list with elements [Atom1, Atom2, value, error], where Atom is an Atom object, value is the RDC value, and error is the uncertainty

**Returns tuple** – RDC errors, atom indices) all information required for RDC calculations and fitting

Return type (inter-atomic vector, gamma values, RDC values,

## paramagpy.fit.nlr\_fit\_metal\_from\_ccr

```
paramagpy.fit.nlr_fit_metal_from_ccr(initMetals, ccrs, params=('x', 'y', 'z'), su-
mIndices=None, progress=None)
```

Fit deltaChi tensor to CCR values using non-linear regression.

#### **Parameters**

- initMetals (list of Metal objects) a list of metals used as starting points for fitting. a list must always be provided, but may also contain only one element. If multiple metals are provided, each metal is fitted to their respective CCR dataset by index, but all are fitted to a common position.
- ccrs (list of CCR datasets) each CCR dataset must correspond to an associated metal for fitting. each CCR dataset has structure [Atom, value, error], where Atom is an Atom object, value is the PCS/RDC/PRE/CCR value and error is the uncertainty
- params (list of str) the parameters to be fit. For example ['x','y','z','ax','rh','a','b','g','shift'] This defaults to ['x','y','z']
- sumIndices (list of arrays of ints, optional) each index list must correspond to an associated ccr dataset. each index list contains an index assigned to each atom. Common indices determine summation between models for ensemble averaging. If None, defaults to atom serial number to determine summation between models.
- **progress** (*object*, *optional*) to keep track of the calculation, progress.set(x) is called each iteration and varies from 0.0 -> 1.0 when the calculation is complete.

#### Returns

- metals (list of metals) the metals fitted by NLR to the CCR data provided
- calc\_ccrs (list of lists of floats) the calculated CCR values
- qfactors (list)

## paramagpy.fit.nlr\_fit\_metal\_from\_pcs

```
paramagpy.fit.nlr_fit_metal_from_pcs (initMetals, pcss, params=('x', 'y', 'z', 'ax', 'rh', 'a', 'b', 'g'), sumIndices=None, userads=False, useracs=False, progress=None)
```

Fit deltaChi tensor to PCS values using non-linear regression.

#### **Parameters**

- initMetals (list of Metal objects) a list of metals used as starting points for fitting. a list must always be provided, but may also contain only one element. If multiple metals are provided, each metal is fitted to their respective PCS dataset by index, but all are fitted to a common position.
- **pcss** (*list of PCS datasets*) each PCS dataset must correspond to an associated metal for fitting. each PCS dataset has structure [Atom, value, error], where Atom is an Atom object, value is the PCS/RDC/PRE value and error is the uncertainty
- params (list of str) the parameters to be fit. For example ['x','y','z','ax','rh','a','b','g','shift']
- **sumIndices** (list of arrays of ints, optional) each index list must correspond to an associated pcs dataset. each index list contains an index assigned to each atom. Common indices determine summation between models for ensemble averaging. If None, defaults to atom serial number to determine summation between models.
- userads (bool, optional) include residual anisotropic dipolar shielding (RADS) during fitting
- useracs (bool, optional) include residual anisotropic chemical shielding (RACS) during fitting. CSA tensors are taken using the <csa> method of atoms.
- **progress** (object, optional) to keep track of the calculation, progress.set(x) is called each iteration and varies from 0.0 -> 1.0 when the calculation is complete.

#### Returns

- metals (list of metals) the metals fitted by NLR to the PCS data provided
- calc\_pcss (list of lists of floats) the calculated PCS values

#### paramagpy.fit.nlr\_fit\_metal\_from\_pre

```
paramagpy.fit.nlr_fit_metal_from_pre (initMetals, pres, params=('x', 'y', 'z'), su-mIndices=None, rtypes=None, usesbm=True, usedsa=True, usecsa=False, progress=None) Fit deltaChi tensor to PRE values using non-linear regression.
```

## Parameters

- initMetals (list of Metal objects) a list of metals used as starting points for fitting. a list must always be provided, but may also contain only one element. If multiple metals are provided, each metal is fitted to their respective PRE dataset by index, but all are fitted to a common position.
- **pres** (*list of PRE datasets*) each PRE dataset must correspond to an associated metal for fitting. each PRE dataset has structure [Atom, value, error], where Atom is an Atom object, value is the PCS/RDC/PRE value and error is the uncertainty
- params (list of str) the parameters to be fit. For example ['x','y','z','ax','rh','a','b','g','iso','taur','tle']

- **sumIndices** (list of arrays of ints, optional) each index list must correspond to an associated pcs dataset. each index list contains an index assigned to each atom. Common indices determine summation between models for ensemble averaging. If None, defaults to atom serial number to determine summation between models.
- **rtypes** (list of str, optional) the relaxtion type, either 'r1' or 'r2'. A list must be provided with each element corresponding to an associated dataset. Defaults to 'r2' for all datasets of None is specified.
- usesbm (bool, optional) include Solomon-Bloemenbergen-Morgan (Dipole-dipole) relaxation theory. default is True
- usedsa (bool, optional) include Dipolar-Shielding-Anisotropy (Curie Spin) relaxation theory. default is True
- usecsa (bool, optional) include Chemical-Shift-Anisotropy cross-correlated realization theory. default is False
- **progress** (*object*, *optional*) to keep track of the calculation, progress.set(x) is called each iteration and varies from 0.0 -> 1.0 when the calculation is complete.

Returns metals – the metals fitted by NLR to the PRE data provided

**Return type** list of metals

## paramagpy.fit.nlr fit metal from rdc

paramagpy.fit.nlr\_fit\_metal\_from\_rdc(metal, rdc, params=('ax', 'rh', 'a', 'b', 'g'), sumIndices=None, progress=None)

Fit deltaChi tensor to RDC values using non-linear regression.

#### **Parameters**

- metal (Metal object) the starting metal for fitting
- rdc (the RDC dataset) each RDC dataset has structure [Atom, value, error], where Atom is an Atom object, value is the PCS/RDC/PRE value and error is the uncertainty
- params (list of str, optional) the parameters to be fit. this defaults to ['ax','rh','a','b','g']
- **sumIndices** (array of ints, optional) the list contains an index assigned to each atom. Common indices determine summation between models for ensemble averaging. If None, defaults to atom serial number to determine summation between models.
- **progress** (object, optional) to keep track of the calculation, progress.set(x) is called each iteration and varies from 0.0 -> 1.0 when the calculation is complete.

#### Returns

- fitMetal (Metal object) the fitted metal by NLR to the RDC data provided
- calculated (array of floats) the calculated RDC values
- qfac (float) the qfactor judging the fit quality

#### paramagpy.fit.pcs\_fit\_error\_bootstrap

```
paramagpy.fit.pcs_fit_error_bootstrap(initMetals, pcss, iterations, fraction, params=('x', 'y', 'z', 'ax', 'rh', 'a', 'b', 'g'), sumIndices=None, userads=False, useracs=False, progress=None)
```

Analyse uncertainty of PCS fit by Bootstrap methods. This repeats the tensor fitting, but each time samples a fraction of the data randomly. The standard deviation in fitted parameters over each iteration is then reported.

#### **Parameters**

- initMetals (list of Metal objects) a list of metals used as starting points for fitting. a list must always be provided, but may also contain only one element. If multiple metals are provided, each metal is fitted to their respective PCS dataset by index, but all are fitted to a common position.
- **pcss** (*list of PCS datasets*) each PCS dataset must correspond to an associated metal for fitting. each PCS dataset has structure [Atom, value, error], where Atom is an Atom object, value is the PCS/RDC/PRE value and error is the uncertainty
- iterations (int) the number of Monte Carlo iterations to perform
- **fraction** (float) must be between 0 and 1 the proportion of data to be sample for fitting with each iteration of the bootstrap method.
- params (list of str) the parameters to be fit. For example ['x','y','z','ax','rh','a','b','g','shift']
- sumIndices (list of arrays of ints, optional) each index list must correspond to an associated pcs dataset. each index list contains an index assigned to each atom. Common indices determine summation between models for ensemble averaging. If None, defaults to atom serial number to determine summation between models.
- userads (bool, optional) include residual anisotropic dipolar shielding (RADS) during fitting
- useracs (bool, optional) include residual anisotropic chemical shielding (RACS) during fitting. CSA tensors are taken using the <csa> method of atoms.
- **progress** (object, optional) to keep track of the calculation, progress.set(x) is called each iteration and varies from 0.0 -> 1.0 when the calculation is complete.

#### Returns

- **sample\_metals** (*list of list of metals*) the metals fitted by NLR to the PCS data with noise at each iteration
- **std\_metals** (*list of metals*) the standard deviation in fitted parameters over all iterations of the Monte Carlo simulation. These are stored within the metal object. All unfitted parameters are zero.

## paramagpy.fit.pcs\_fit\_error\_monte\_carlo

```
paramagpy.fit.pcs_fit_error_monte_carlo(initMetals, pcss, iterations, params=('x', 'y', 'z', 'ax', 'rh', 'a', 'b', 'g'), su-mIndices=None, userads=False, useracs=False, progress=None)
```

Analyse uncertainty of PCS fit by Monte-Carlo simulation This repeatedly adds noise to experimental PCS data and fits the tensor. The standard deviation of the fitted parameters across each iteration is then reported.

#### **Parameters**

- initMetals (list of Metal objects) a list of metals used as starting points for fitting. a list must always be provided, but may also contain only one element. If multiple metals are provided, each metal is fitted to their respective PCS dataset by index, but all are fitted to a common position.
- pcss (list of PCS datasets) each PCS dataset must correspond to an associated metal for fitting. each PCS dataset has structure [Atom, value, error], where Atom is an Atom object, value is the PCS/RDC/PRE value and error is the uncertainty
- iterations (int) the number of Monte Carlo iterations to perform
- params (list of str) the parameters to be fit. For example ['x','y','z','ax','rh','a','b','g','shift']
- **sumIndices** (list of arrays of ints, optional) each index list must correspond to an associated pcs dataset. each index list contains an index assigned to each atom. Common indices determine summation between models for ensemble averaging. If None, defaults to atom serial number to determine summation between models.
- userads (bool, optional) include residual anisotropic dipolar shielding (RADS) during fitting
- useracs (bool, optional) include residual anisotropic chemical shielding (RACS) during fitting. CSA tensors are taken using the <csa> method of atoms.
- **progress** (*object*, *optional*) to keep track of the calculation, progress.set(x) is called each iteration and varies from 0.0 -> 1.0 when the calculation is complete.

#### Returns

- **sample\_metals** (*list of list of metals*) the metals fitted by NLR to the PCS data with noise at each iteration
- **std\_metals** (*list of metals*) the standard deviation in fitted parameters over all iterations of the Monte Carlo simulation. These are stored within the metal object. All unfitted parameters are zero.

## paramagpy.fit.qfactor

paramagpy.fit.**qfactor** (experiment, calculated, sumIndices=None)

Calculate the Q-factor to judge tensor fit quality

A lower value indicates a better fit. The Q-factor is calculated using the following equation:

$$Q = \sqrt{\frac{\sum_{i} \left[ \left( \sum_{m} \left[ PCS_{m,i}^{exp} - PCS_{m,i}^{calc} \right] \right)^{2} \right]}{\sum_{i} \left[ \left( \sum_{m} \left[ PCS_{m,i}^{exp} \right] \right)^{2} \right]}}$$

where m and i are usually indexed over models and atoms respectively.

## **Parameters**

- experiment (list of floats) the experimental values
- calculated (list of floats) the corresponding caluclated values from the fitted model
- **sumIndices** (list ints, optional) Common indices determine summation between models for ensemble averaging. If None, no ensemble averaging is conducted

Returns qfactor - the Q-factor

#### Return type float

## paramagpy.fit.sphere\_grid

```
paramagpy.fit.sphere_grid(origin, radius, points)
```

Make a grid of cartesian points within a sphere

#### **Parameters**

- origin (float) the centre of the sphere
- radius (float) the radius of the sphere
- points (int) the number of points per radius

**Returns** array – the points within the sphere

**Return type** array of [x,y,z] coordinates

## paramagpy.fit.svd\_calc\_metal\_from\_pcs

```
paramagpy.fit.svd_calc_metal_from_pcs (pos, pcs, idx, errors)
```

Solve PCS equation by single value decomposition. This function is generally called by higher methods like <svd\_gridsearch\_fit\_metal\_from\_pcs>

#### **Parameters**

- $pos(array \ of [x,y,z] \ floats)$  the atomic positions in meters
- pcs (array of floats) the PCS values in ppm
- idx (array of ints) an index assigned to each atom. Common indices determine summation between models for ensemble averaging.
- **errors** (array of floats) the standard deviation representing experimental uncertainty in the measured value

**Returns tuple** – calc are the calculated PCS values from the fitted tensor sol is the solution to the linearised PCS equation and consists of the tensor matrix elements

Return type (calc, sol)

## paramagpy.fit.svd\_calc\_metal\_from\_pcs\_offset

```
paramagpy.fit.svd_calc_metal_from_pcs_offset (pos, pcs, idx, errors)
```

Solve PCS equation by single value decomposition with offset. An offset arising from referencing errors between diamagnetic and paramagnetic datasets can be accounted for using this method. This function is generally called by higher methods like <svd\_gridsearch\_fit\_metal\_from\_pcs>

NOTE: the factor of 1E26 is required for floating point error mitigation

## **Parameters**

- pos(array of [x,y,z] floats) the atomic positions in meters
- pcs (array of floats) the PCS values in ppm
- idx (array of ints) an index assigned to each atom. Common indices determine summation between models for ensemble averaging.
- **errors** (array of floats) the standard deviation representing experimental uncertainty in the measured value

**Returns tuple** – calc are the calculated PCS values from the fitted tensor sol is the solution to the linearised PCS equation and consists of the tensor matrix elements and offset

## Return type (calc, sol)

## paramagpy.fit.svd\_calc\_metal\_from\_rdc

paramagpy.fit.svd\_calc\_metal\_from\_rdc(vec, rdc\_parameterised, idx, errors)

Solve RDC equation by single value decomposition. This function is generally called by higher methods like <svd fit metal from rdc>

#### **Parameters**

- **vec**  $(array \ of \ [x,y,z] \ floats)$  the internuclear vectors in meters
- rdc\_parameterised (array of floats) the experimental RDC values, normalised by a prefactor
- idx (array of ints) an index assigned to each atom. Common indices determine summation between models for ensemble averaging.
- **errors** (array of floats) the standard deviation representing experimental uncertainty in the measured value

#### Returns

- calc (array of floats) the calculated RDC values from the fitted tensor
- sol (array of floats) sol is the solution to the linearised PCS equation and consists of the tensor matrix elements

## paramagpy.fit.svd\_fit\_metal\_from\_rdc

```
paramagpy.fit.svd_fit_metal_from_rdc (metal, rdc, sumIndices=None)
```

Fit deltaChi tensor to RDC values using SVD algorithm. Note this is a weighted SVD calculation which takes into account experimental errors. Ensemble averaging defaults to atom numbers.

#### **Parameters**

- metal (Metal object) the starting metal for fitting
- rdc (the RDC dataset) each RDC dataset has structure [(Atom1, Atom2), value, error], where Atom is an Atom object, value is the RDC value and error is the uncertainty
- **sumIndices** (array of ints, optional) the list contains an index assigned to each atom. Common indices determine summation between models for ensemble averaging. If None, defaults to atom serial number to determine summation between models.

#### Returns

- fitMetal (Metal object) the fitted metal by NLR to the RDC data provided
- calculated (array of floats) the calculated RDC values
- qfac (float) the qfactor judging the fit quality

## paramagpy.fit.svd\_gridsearch\_fit\_metal\_from\_pcs

```
paramagpy.fit.svd_gridsearch_fit_metal_from_pcs (metals, pcss, sumIndices=None, origin=None, radius=20.0, points=16, offsetShift=False, progress=None)

Fit deltaChi tensor to PCS values using Single Value Decomposition over a grid of points in a sphere. Note
```

this uses a weighted SVD fit which takes into account experimental errors Ensemble averaging is determined by atom number.

#### **Parameters**

- metals (list of Metal objects) a list of metals used as starting points for fitting. a list must always be provided, but may also contain only one element. If multiple metals are provided, each metal is fitted to their respective PCS dataset by index, but all are fitted to a common position.
- **pcss** (*list* of *PCS* datasets) each PCS dataset must correspond to an associated metal for fitting. each PCS dataset has structure [Atom, value, error], where Atom is an Atom object, value is the PCS/RDC/PRE value and error is the uncertainty
- sumIndices (list of arrays of ints, optional) each index list must correspond to an associated pcs dataset. each index list contains an index assigned to each atom. Common indices determine summation between models for ensemble averaging. If None, defaults to atom serial number to determine summation between models.
- **origin** (*float*, *optional*) the centre of the gridsearch of positions in Angstroms. If None, the position of the first metal is used
- radius (float, optional) the radius of the gridsearch in Angstroms.
- points (int, optional) the number of points per radius in the gridsearch
- offsetShift (bool, optional) if True, an offset value added to all PCS values is included in the SVD fitting. This may arise due to a referencing error between diamagnetic and paramagnetic PCS datasets and may be used when many data points are available. Default False, no offset is included in the fitting.
- **progress** (object, optional) to keep track of the calculation, progress.set(x) is called each iteration and varies from 0.0 -> 1.0 when the calculation is complete.

Returns minmetals – the metals fitted by SVD to the PCS data provided

**Return type** list of metals

#### paramagpy.fit.unique pairing

```
paramagpy.fit.unique_pairing(a, b)
```

Bijectively map two integers to a single integer. The mapped space is minimum size. The input is symmetric. see Bijective mapping f:ZxZ->N.

#### **Parameters**

- a (int) -
- **b**(int)-

**Returns** c – bijective symmetric mapping  $(a, b) \mid (b, a) \rightarrow c$ 

Return type int

# **PYTHON MODULE INDEX**

# p

paramagpy.dataparse,68 paramagpy.fit,72 paramagpy.metal,36 paramagpy.protein,56