

Permittivity of free space:  $\epsilon_0 = 8.854 \times 10^{-12}$   
 Elementary charge:  $e = 1.602 \cdot 10^{-19}$   
 Proton mass:  $1.673 \cdot 10^{-27}$   
 Electron mass:  $9.11 \cdot 10^{-31}$   
 Speed of light:  $c = 3 \cdot 10^8$   
 Permeability constant:  $\mu_0 = 1.26 \times 10^{-6}$

### Moving Conductor

$$I = \frac{\Delta V}{R} = \frac{\varepsilon}{R} = \frac{v l B}{R}$$

$$F_{\text{mag}} = F_{\text{pull}} = I l B = \frac{v l^2 B^2}{R}$$

$$P_{\text{input}} = P_{\text{dissipated}} = I^2 R = \frac{v^2 l^2 B^2}{R}$$

$$\Phi_m = \vec{A} \cdot \vec{B} = |A| |B| \cos \theta \quad (\text{uniform magnetic field})$$

- Increasing flux: The induced magnetic field points opposite the applied magnetic field.
- Decreasing flux: The induced magnetic field points in the same direction as the applied magnetic field.
- Steady flux: There is no induced magnetic field.

$$\varepsilon_{\text{induced}} = \frac{d\Phi_m}{dt} \quad I_{\text{induced}} = \frac{\varepsilon_{\text{induced}}}{R}$$

$$E_{\text{inside}} = \frac{r}{2} \left| \frac{dB}{dt} \right| \quad \text{Solenoid}$$

$$\frac{V_2}{V_1} = \frac{N_2}{N_1} \quad \text{Transformers}$$

### Inductors

$$L = \frac{\Phi_m}{I} \quad \text{henry (H)}$$

$$\Delta V_L = -L \frac{dI}{dt} \quad U_L = L \int_0^I I dI = \frac{1}{2} L I^2$$

### LC Circuits

$$I = -\frac{dQ}{dt} \quad Q(t) = Q_0 \cos \omega t$$

$$\omega = \frac{1}{\sqrt{LC}} \quad f = \omega / 2\pi$$

### LR Circuits

$$I = I_0 e^{-t/(L/R)}$$

$$\tau = \frac{L}{R} \quad \text{where current has decreased to } e^{-1}$$

### Right-hand rule (wire)

- Point thumb in the direction of current
- Point fingers in the direction of magnetic field
- Point palm in the face of force on wire

$$\vec{E}_B = \vec{E}_A + \vec{v}_{BA} \times \vec{B}_A$$

$$\vec{B}_B = \vec{B}_A - \frac{1}{c^2} \vec{v}_{BA} \times \vec{E}_A$$

$$a \times b = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ a_x & a_y & a_z \\ b_x & b_y & b_z \end{vmatrix}$$

$$I_{\text{disp}} = \epsilon_0 \frac{d\Phi_e}{dt} = \epsilon_0 \frac{dE \cdot A}{dt}$$

$$\oint \vec{E} \cdot d\vec{A} = \frac{Q_{\text{in}}}{\epsilon_0} \quad \text{Gauss's Law}$$

$$\oint \vec{B} \cdot d\vec{A} = 0 \quad \text{Gauss's Law for Magnetism}$$

$$\oint \vec{E} \cdot d\vec{s} = -\frac{d\Phi_m}{dt} \quad \text{Faraday's Law}$$

$$\oint \vec{B} \cdot d\vec{s} = \mu_0 I_{\text{through}} + \epsilon_0 \mu_0 \frac{d\Phi_e}{dt} \quad \text{Ampere-Maxwell Law}$$

$$\vec{F} = q(\vec{E} + \vec{v} \times \vec{B}) \quad \text{Lorentz Force Law}$$

$$E(x, t) = E_0 \cos(kx - \omega t + \phi)$$

- $k = \frac{2\pi}{\lambda}$  where  $k$  is wave number and  $\lambda$  is wavelength
- $T = \frac{2\pi}{\omega}$  where  $T$  is period and  $\omega$  is angular frequency
- $f = \frac{1}{T}$  where  $f$  is frequency
- $v = f\lambda$  where  $v$  is the propagation speed
- $v = \frac{E_0}{B_0}$  where  $E_0$  and  $B_0$  are the electric and magnetic field components

$$E = cB$$

$$I = \frac{P}{4\pi r^2} = \frac{c\epsilon_0 E_0^2}{2}$$

$$\langle S \rangle = \frac{1}{\mu_0} EB \sin \theta$$

### Right-hand rule (electromagnetic waves)

- Point index finger in the direction of electric field
- Point middle finger in the direction of magnetic field
- Point thumb in the direction of motion

$$I_{\text{transmitted}} = \frac{1}{2} I_0 \quad \text{unpolarized}$$

$$I_{\text{transmitted}} = I_0 \cos^2 \theta \quad \text{polarized}$$

$$X_C = \frac{1}{2\pi f C}$$

where  $X_C$  is the capacitive reactance in ohms,  $f$  is the frequency, and  $C$  is the capacitance.