Midterm Exam 1

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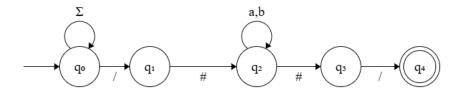
Problem 1

$$(a \cup d)^* c(b(dd)^* \cup c \cup d)^* b$$

Problem 2

Let M be a DFA that recognizes L. We can construct an NFA M' to recognize h(L) by replacing each transition $\delta(q,a)$ in M with a sequence of transitions in M' that process h(a) instead of a. Since NFAs and DFAs both define the class of regular languages, the resulting language h(L) is regular. Therefore, regular languages are closed under homomorphism.

Problem 3



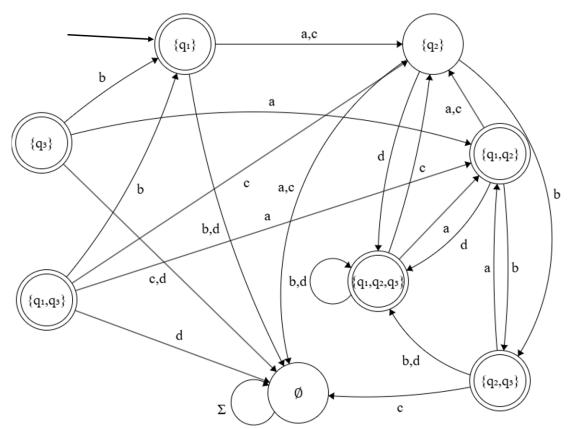
Problem 4

If $L = \{ccc\#cc\#c \text{ with } c \in \{a,b\}^*\}$ is a regular language, then it must satisfy the Pumping Lemma, where there exists a pumping length p such that any string s in L with $|s| \geq p$ can be split into s = xyz where:

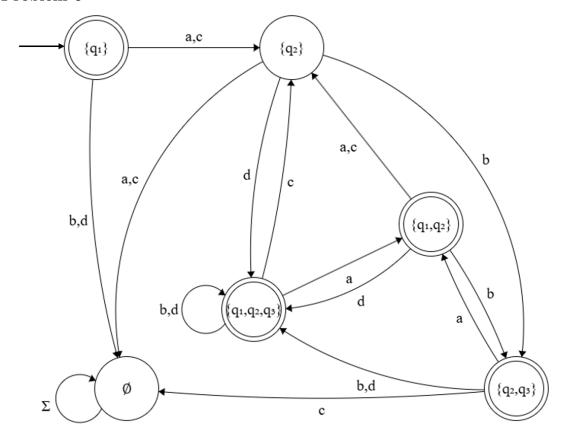
- 1. $xy^kz \in L$ for all $k \ge 0$
- 2. |y| > 0
- $3. |xy| \leq p$

Consider a string $s = a^p b^p a^p b^p a^p b^p \# a^p b^p \# a^p b^p \# a^p b^p \# a^p b^p$ in L where $c = a^p b^p$. Pumping y increases the number of a's only in the first c, while the other instances of c are unchanged. Since the resulting string no longer follows the pattern ccc# cc# c, it contradicts the Pumping Lemma and L is not a regular language.

Problem 5



Problem 6



Problem 7

