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Section - ML

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Subject - Design & Analysis of Algo.

TCS 505

### Tutorial

1

Minimum spanning tree is a spanning tree where the cost is minimum among all the spanning trees. There can be multiple minimum spanning trees also.

Minimum spanning tree has direct application in the design of networks. It is used in algorithms approximating the travelling salesman problem, multi-terminal minimum cut problem and minimum-cost weighted perfect matching.

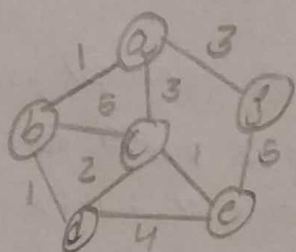
Its other practical applications are -

- ① Image segmentation
- ② Handwriting recognition
- ③ Cluster analysis

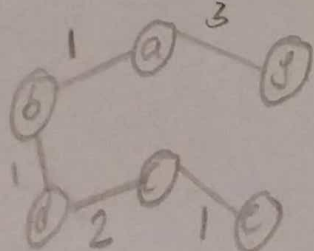
2

Algorithm	Time complexity	Space complexity
	$O(V^2)$	$O(V)$
Prim's Algo.	$O(E \log V)$	$O(V)$
Kruskal's Algo.	$O(E \log E) \equiv O(E \log V)$	$O(V)$
Dijkstra's Algo.	$O(E \log V)$	$O(V + E)$
Bellman Ford's Algo	$O(V \cdot E)$	$O(V)$

3.



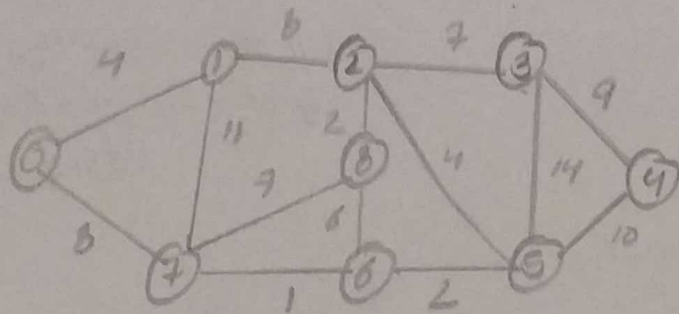
MST



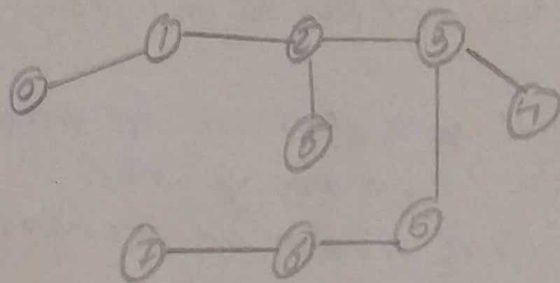
Min wt = 8

Using Kruskal's Algorithm

u	v	w	
a	b	1	✓
b	d	2	✓
c	d	1	✓
c	d	2	✓
a	c	3	
a	f	3	✓
d	e	4	
b	c	5	
c	f	6	



MST



Min wt = 37

	$\epsilon$	$w$
0,1	2	✓
0,7	8	
1,2	11	
1,3	8	✓
2,3	7	✓
2,8	2	✓
2,6	4	✓
3,7	7	
3,6	6	
5,6	2	✓
5,3	14	
6,4	10	
6,7	1	✓
3,4	9	✓

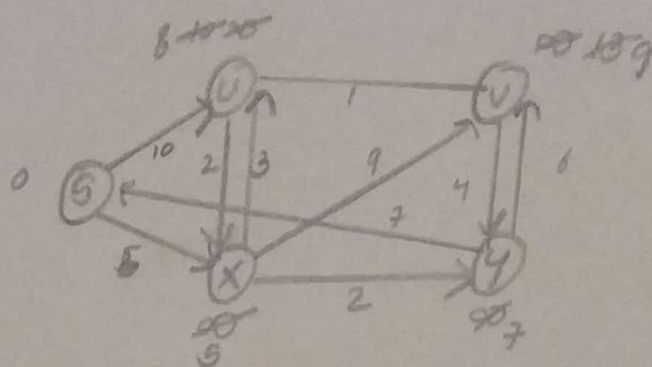
4

- The shortest path may change. The reason is, there may be a different no. of edges in different paths from  $1s'$  to  $1t'$  eg. let shortest path be of weight 15 and has 5 edges. let there be another path where 2 edges & total weight 25. The weight of the shortest path is increased by  $5 \times 10$  and become 15+50.

weight of other path is increased by  $2 \times 10$  & becomes  $25 + 20 = 45$ . So, the shortest path changes to the other path with weight as 45.

- If we multiply all edge weights by 10, shortest path doesn't change. The no. of edges on a path doesn't change. The no. of edges on a path doesn't matter.

5



Dijkstra Algorithm

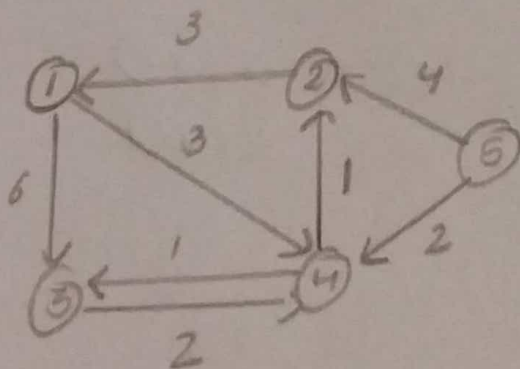
Node	Shortest dist. from source
U	8
V	9
X	5
Y	7

Bellman Ford's Algorithm

8	U	V	X	Y
0	<del>10</del>	<del>13</del>	<del>5</del>	<del>7</del>
	8	9	5	7

8	U	V	X	Y
0	8	9	5	7

6





$$D =$$

	1	2	3	4	5
1	0	$\infty$	6	3	$\infty$
2	3	0	$\infty$	$\infty$	$\infty$
3	$\infty$	$\infty$	0	2	$\infty$
4	$\infty$	1	1	0	$\infty$
5	$\infty$	4	$\infty$	2	0

$$D_1 =$$

	1	2	3	4	5
1	0	$\infty$	6	3	$\infty$
2	3	0	9	6	$\infty$
3	$\infty$	$\infty$	0	2	$\infty$
4	$\infty$	1	1	0	$\infty$
5	$\infty$	4	$\infty$	2	0

$$D_2 =$$

	1	2	3	4	5
1	0	$\infty$	6	3	$\infty$
2	3	0	9	6	$\infty$
3	$\infty$	$\infty$	0	2	$\infty$
4	4	1	1	0	$\infty$
5	7	4	13	2	0

$$D_3 =$$

	1	2	3	4	5
1	0	$\infty$	6	3	$\infty$
2	3	0	9	6	$\infty$
3	$\infty$	$\infty$	0	2	$\infty$
4	4	1	1	0	$\infty$
5	7	4	13	2	0

$$D_4 =$$

	1	2	3	4	5
1	0	4	4	3	$\infty$
2	3	0	7	6	$\infty$
3	6	3	0	2	$\infty$
4	4	1	1	0	$\infty$
5	6	3	3	2	0

$$D_5 =$$

	1	2	3	4	5
1	0	4	4	3	$\infty$
2	3	0	7	6	$\infty$
3	6	3	0	2	$\infty$
4	4	1	1	0	$\infty$
5	6	3	3	2	0

$$TC = 0 (v^3)$$

$$SC = 0 (v^2)$$