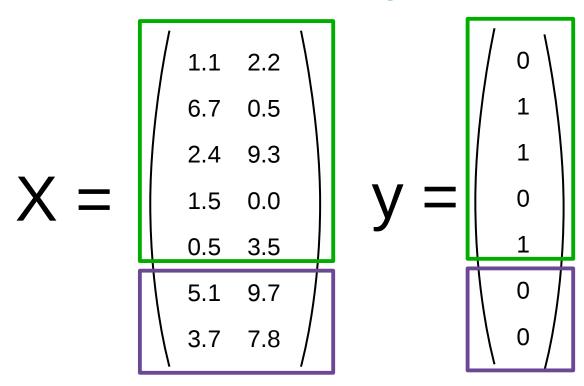
Model evaluation and metrics

Andreas Müller

training set



test set

Overfitting the test set

```
from sklearn.datasets import load_breast_cancer
from sklearn.preprocessing import scale

data = load_breast_cancer()
X, y = data.data, data.target
X = scale(X)

X_trainval, X_test, y_trainval, y_test = train_test_split(X, y)
X_train, X_val, y_train, y_val = train_test_split(X_trainval, y_trainval)

knn = KNeighborsClassifier(n_neighbors=5).fit(X_train, y_train)

print("Validation: {:.3f}".format(knn.score(X_val, y_val)))
print("Test: {:.3f}".format(knn.score(X_test, y_test)))
```

Validation: 0.963

Test: 0.972

Overfitting the test set

```
val = []
test = []

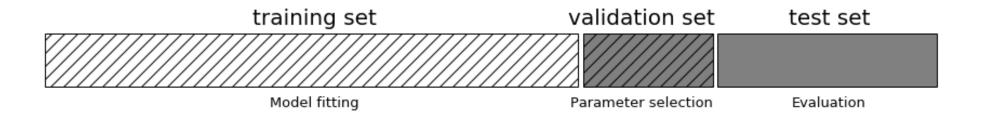
for i in range(1000):
    rng = np.random.RandomState(i)
    noise = rng.normal(scale=.1, size=X_train.shape)
    knn = KNeighborsClassifier(n_neighbors=5).fit(X_train + noise, y_train)
    val.append(knn.score(X_val, y_val))
    test.append(knn.score(X_test, y_test))

print("Validation: {:.3f}".format(np.max(val)))
print("Test: {:.3f}".format(test[np.argmax(val)]))
```

Validation: 0.991

Test: 0.958

Three-fold split



pro: fast, simple

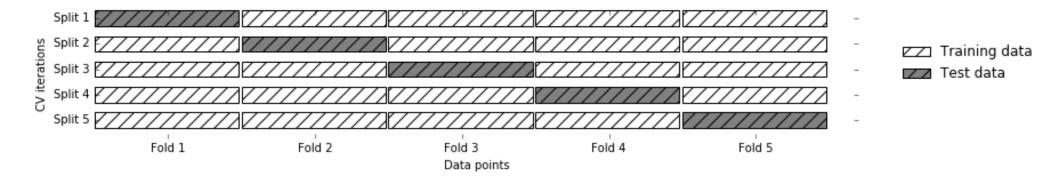
con: high variance, bad use of data.

```
val_scores = []
neighbors = np.arange(1, 15, 2)
for i in neighbors:
    knn = KNeighborsClassifier(n_neighbors=i)
    knn.fit(X_train, y_train)
    val_scores.append(knn.score(X_val, y_val))
print("best validation score: {:.3f}".format(np.max(val_scores)))
best_n_neighbors = neighbors[np.argmax(val_scores)]
print("best n_neighbors: {}".format(best_n_neighbors))
knn = KNeighborsClassifier(n_neighbors=best_n_neighbors)
knn.fit(X_trainval, y_trainval)
print("test-set score: {:.3f}".format(knn.score(X_test, y_test)))
best validation score: 0.972
```

best n_neighbors: 3

test-set score: 0.965

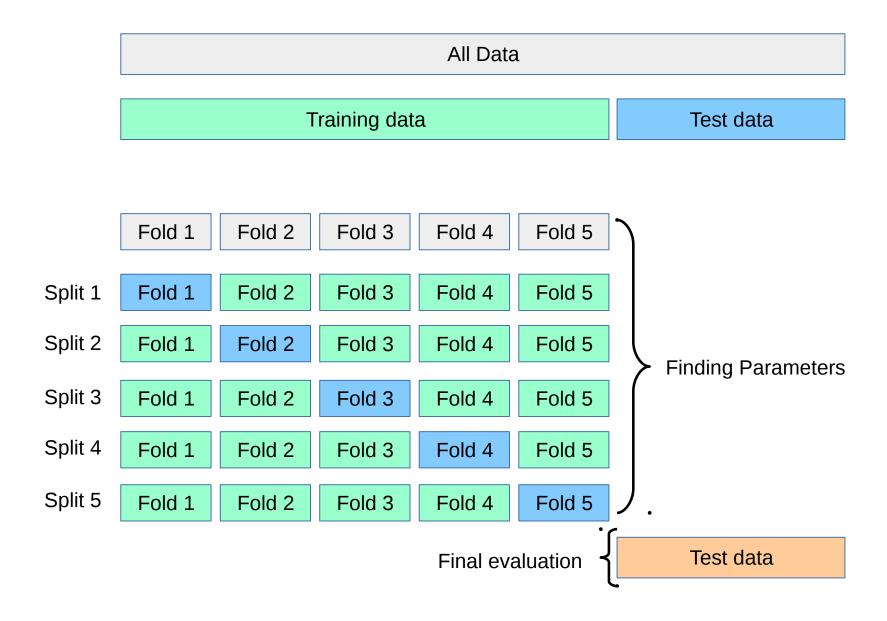
Cross-validation



Pro: more stable, more data

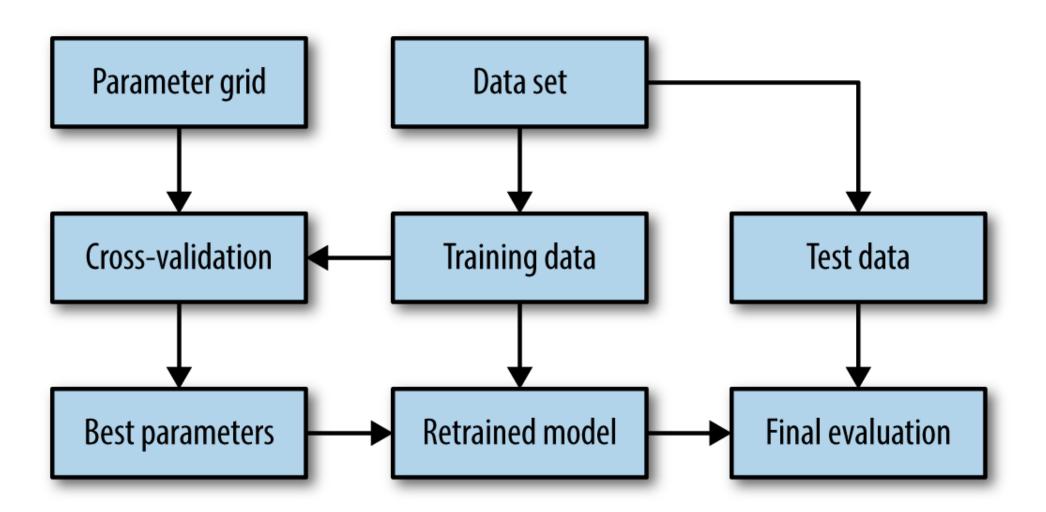
con: slower

Cross-validation + test-set



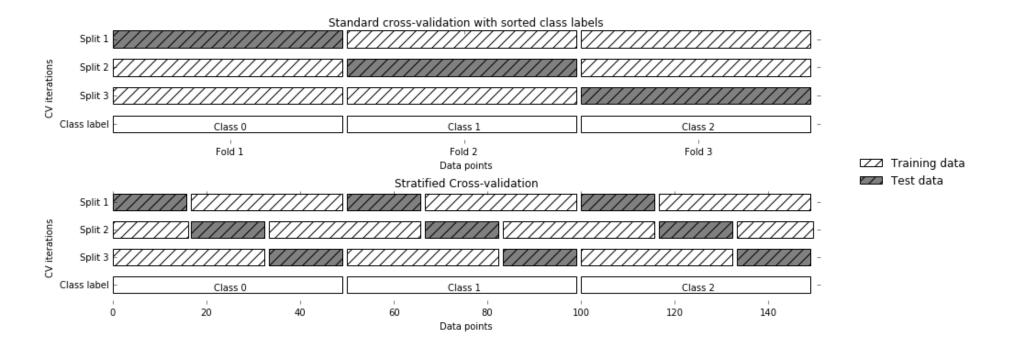
```
from sklearn.model_selection import cross val score
X train, X test, y train, y test = train test split(X, y)
cross val scores = []
for i in neighbors:
    knn = KNeighborsClassifier(n neighbors=i)
    scores = cross val score(knn, X trainval, y trainval, cv=10)
    cross val scores.append(np.mean(scores))
print("best cross-validation score: {:.3f}".format(np.max(cross val scores)))
best n neighbors = neighbors[np.argmax(cross val scores)]
print("best n neighbors: {}".format(best n neighbors))
knn = KNeighborsClassifier(n neighbors=best n neighbors)
knn.fit(X train, y train)
print("test-set score: {:.3f}".format(knn.score(X test, y test)))
best cross-validation score: 0.972
```

best cross-validation score: 0.972
best n_neighbors: 3
test-set score: 0.972



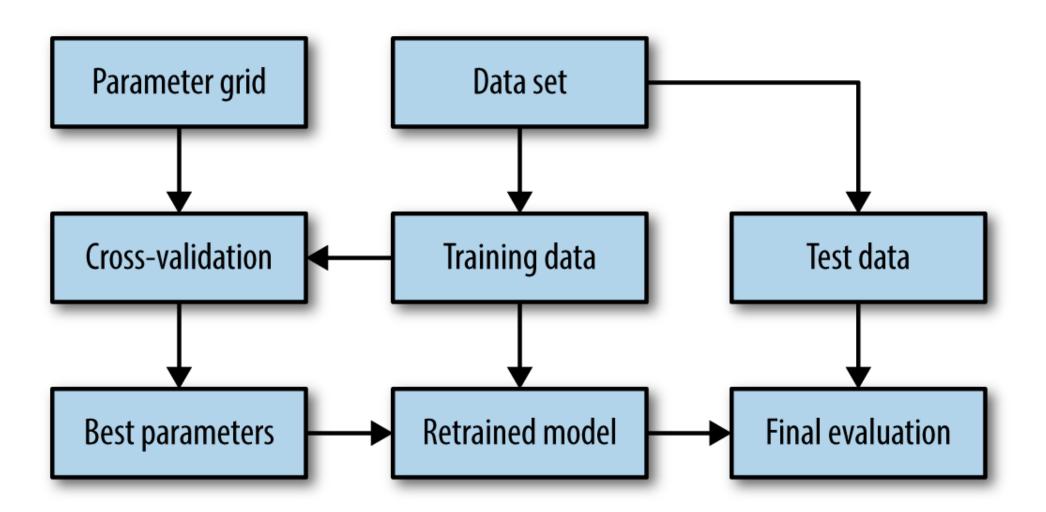
Metrics for Binary Classification

StratifiedKFold



Stratified:

Ensure relative class frequencies in each fold reflect relative class frequencies on the whole dataset.



Grid-Search

```
from sklearn.model_selection import GridSearchCV

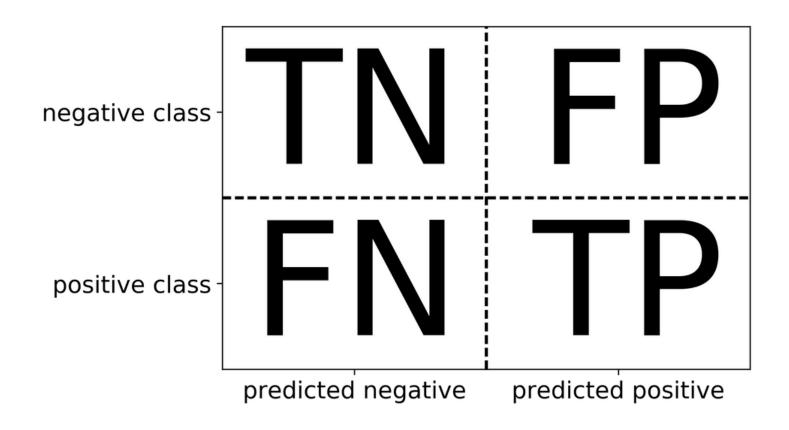
X_train, X_test, y_train, y_test = train_test_split(X, y, stratify=y)

param_grid = {'n_neighbors': np.arange(1, 15, 2)}
grid = GridSearchCV(KNeighborsClassifier(), param_grid=param_grid, cv=10)
grid.fit(X_train, y_train)
print("best mean cross-validation score: {:.3f}".format(grid.best_score_))
print("best parameters: {}".format(grid.best_params_))

print("test-set score: {:.3f}".format(grid.score(X_test, y_test)))
best mean cross-validation score: 0.967
```

best mean cross-validation score: 0.967
best parameters: {'n_neighbors': 7}
test-set score: 0.951

Review: confusion matrix



$$Accuracy = \frac{TP + TN}{TP + TN + FP + FN}$$

Diagonal divided by everything.

```
from sklearn.datasets import load_breast_cancer
from sklearn.linear_model import LogisticRegression
data = load_breast_cancer()

X_train, X_test, y_train, y_test = train_test_split(
    data.data, data.target, stratify=data.target, random_state=0)

lr = LogisticRegression().fit(X_train, y_train)
y_pred = lr.predict(X_test)

from sklearn.metrics import confusion_matrix
print(confusion_matrix(y_test, y_pred))
print(lr.score(X_test, y_test))
```

[[49 4] [5 85]] 0.937062937063

Problems with accuracy

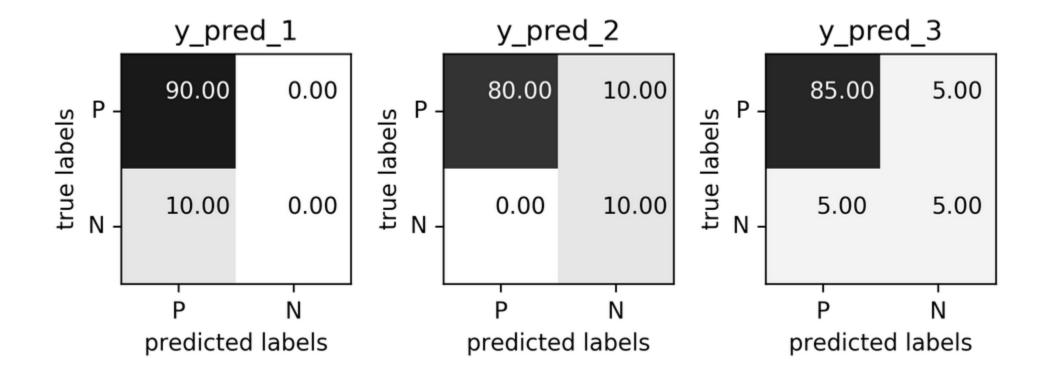
Imbalanced classes lead to hard-to-interpret accuracy:

```
from sklearn.metrics import accuracy_score
for y_pred in [y_pred_1, y_pred_2, y_pred_3]:
    print(accuracy_score(y_true, y_pred))
```

Data with 90% negatives

0.9 0.9

0.9



Precision, Recall, f-score

$$Precision = \frac{TP}{TP + FP}$$

Positive Predicted Value (PPV)

$$Recall = \frac{TP}{TP + FN}$$

Sensitivity, coverage, true positive rate.

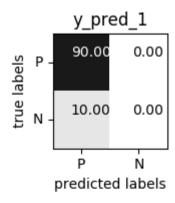
$$F = 2 \cdot \frac{\text{precision} \cdot \text{recall}}{\text{precision} + \text{recall}}$$

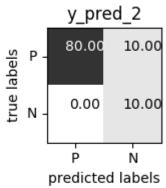
All depend on definition of positive and negative!

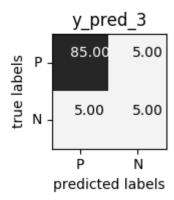
The zoo

			Predicted condition			
		Total population	Predicted Condition positive	Predicted Condition negative	Prevalence = $\frac{\Sigma \text{ Condition positive}}{\Sigma \text{ Total population}}$	
	True	condition positive	True positive	False Negative (Type II error)	True positive rate (TPR), Sensitivity, Recall, probability of detection = $\frac{\Sigma \text{ True positive}}{\Sigma \text{ Condition positive}}$	False negative rate (FNR), Miss rate $= \frac{\Sigma \text{ False negative}}{\Sigma \text{ Condition positive}}$
	condition	condition negative	False Positive (Type I error)	True negative	False positive rate (FPR), Fall-out, probability of false alarm = $\frac{\Sigma \text{ False positive}}{\Sigma \text{ Condition negative}}$	True negative rate (TNR), Specificity $(SPC) = \frac{\Sigma \text{ True negative}}{\Sigma \text{ Condition negative}}$
		Accuracy (ACC) =	Positive predictive value (PPV), Precision $= \frac{\Sigma \text{ True positive}}{\Sigma \text{ Test outcome positive}}$	False omission rate (FOR) $= \frac{\Sigma \text{ False negative}}{\Sigma \text{ Test outcome negative}}$	Positive likelihood ratio (LR+) = $\frac{\text{TPR}}{\text{FPR}}$	Diagnostic odds ratio (DOR) = $\frac{LR+}{IR-}$
		$\frac{\Sigma \text{ True positive} + \Sigma \text{ True negative}}{\Sigma \text{ Total population}}$	False discovery rate (FDR) $= \frac{\Sigma \text{ False positive}}{\Sigma \text{ False positive}}$	Negative predictive value (NPV) $= \frac{\sum \text{True negative}}{\sum \text{Test enterpression}}$	Negative likelihood ratio (LR-) = $\frac{FNR}{TNR}$	Diagnostic odds (ado (bok) = LR-

https://en.wikipedia.org/wiki/Precision_and_recal







support	1-score	recall f	recision	р
90	0.95	1.00	0.90	Θ
10	0.00	0.00	0.00	1
100	0.85	0.90	0.81	avg / total
SUPPOR	f1-score	rocall	precision	
suppor	11-30016	recatt	precision	
9(0.94	0.89	1.00	0
	0.67	1.00	0.50	1
10				

	precision	recall	f1-score	support
0 1	0.94 0.50	0.94 0.50	0.94 0.50	90 10
avg / total	0.90	0.90	0.90	100

Goal setting!

- What do I want? What do I care about?
 (precision, recall, something else)
- Can I assign costs to the confusion matrix?
 (i.e. a false positive costs me \$10, a false negative \$100)
- What guarantees do we want to give?

Changing Thresholds

```
# logistic regresson on breast cancer, but change threshold:
data = load_breast_cancer()

X_train, X_test, y_train, y_test = train_test_split(
    data.data, data.target, stratify=data.target, random_state=0)

lr = LogisticRegression().fit(X_train, y_train)
y_pred = lr.predict(X_test)

print(classification_report(y_test, y_pred))
```

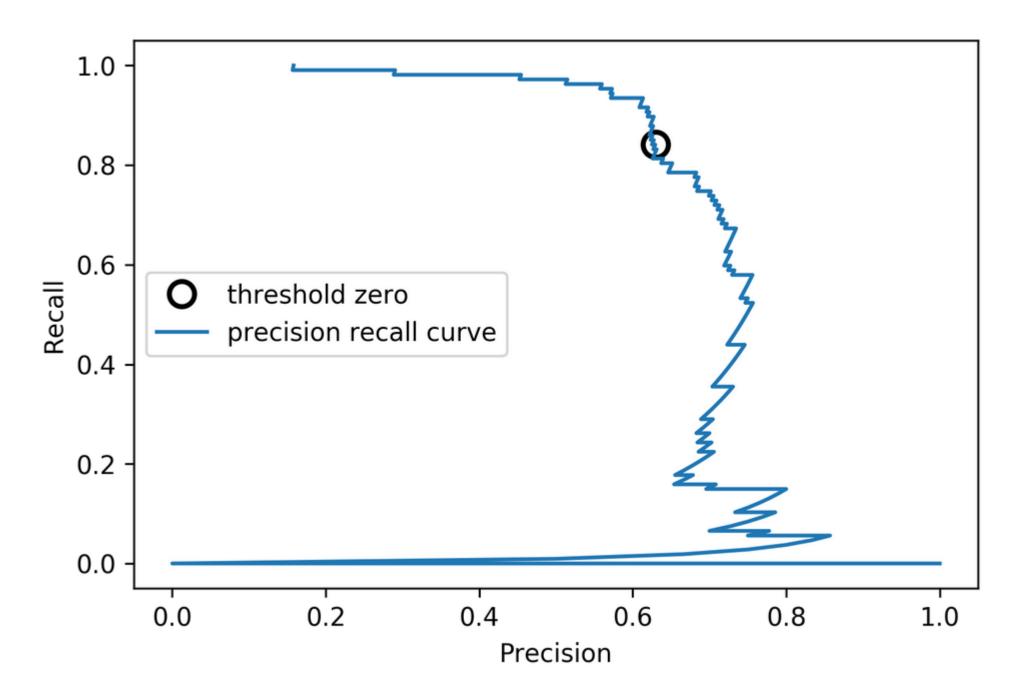
support	f1-score	recall	precision	
53 90	0.92 0.95	0.92 0.94	0.91 0.96	0 1
143	0.94	0.94	0.94	avg / total

```
y_pred = lr.predict_proba(X_test)[:, 1] > .85
print(classification_report(y_test, y_pred))
```

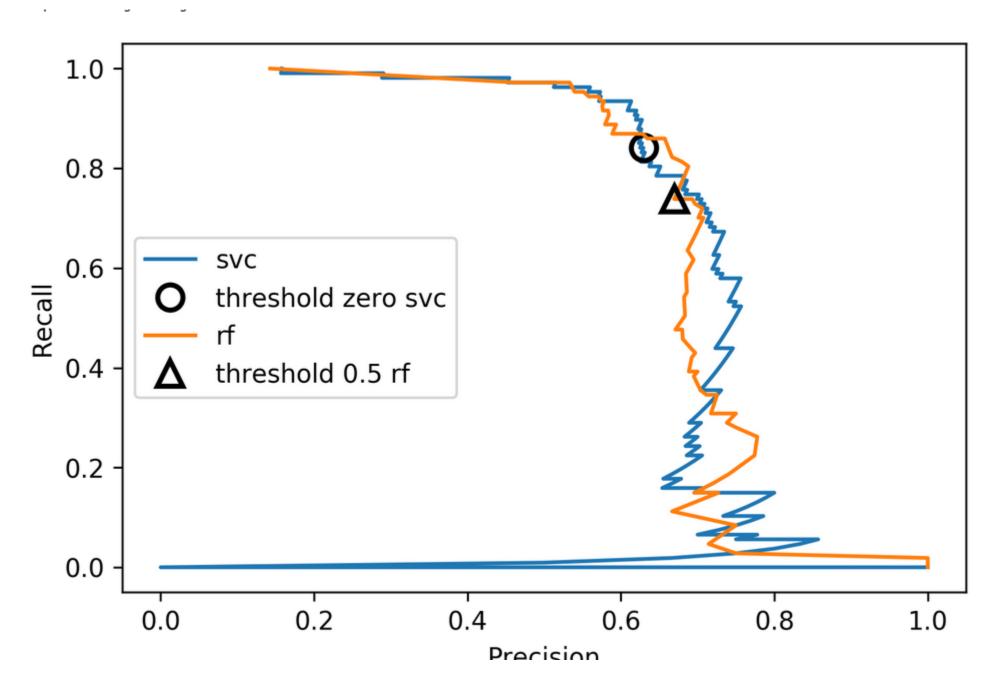
	precision	recall	f1-score	support
0 1	0.84 1.00	1.00 0.89	0.91 0.94	53 90
avg / total	0.94	0.93	0.93	143

Precision-Recall Curve

Precision-Recall Curve



Comparing RF and SVC



Average Precision

Precision at threshold k

$$\operatorname{AveP} = \sum_{k=1}^n P(k) \Delta r(k)$$
 Change in recall between k and k-1

Sum over data points, ranked by decision function

Same as area under the precision-recall curve (depending on how you treat edge-cases)

F1 vs average precision

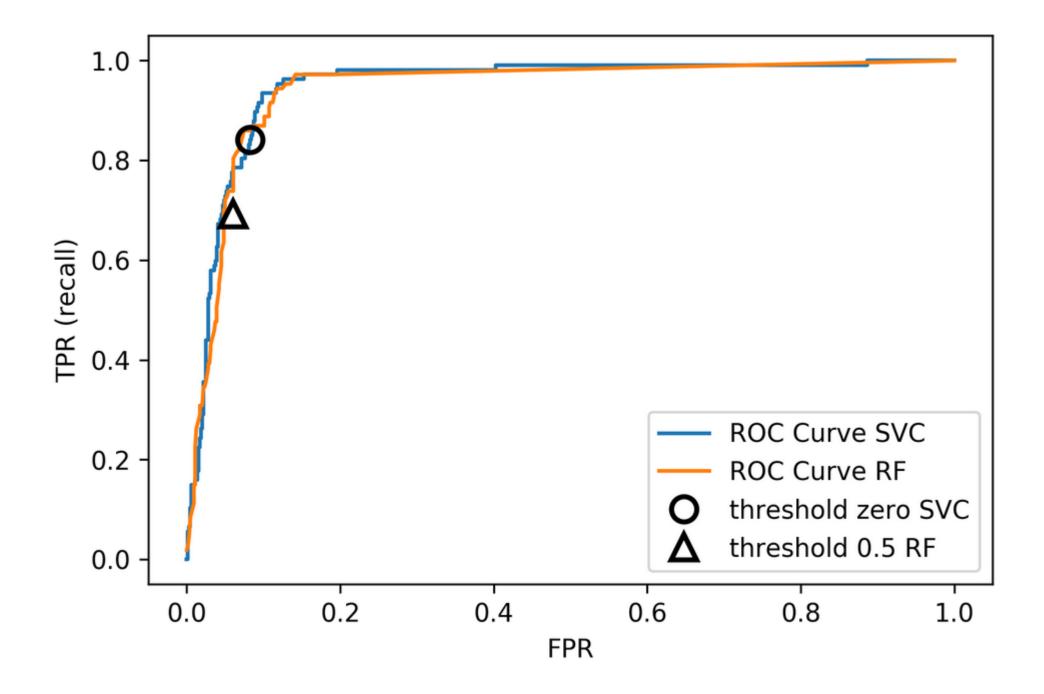
AP only considers ranking!

ROC Curve

		Predicted condition			
	Total population	Predicted Condition positive	Predicted Condition negative	$\frac{\Sigma \text{ Condition positive}}{\Sigma \text{ Total population}}$	
True	condition positive	True positive	False Negative (Type II error)	True positive rate (TPR), Sensitivity, Recall, probability of detection = $\frac{\Sigma \text{ True positive}}{\Sigma \text{ Condition positive}}$	False negative rate (FNR), Miss rate $= \frac{\Sigma \text{ False negative}}{\Sigma \text{ Condition positive}}$
condition	condition negative	False Positive (Type I error)	True negative	False positive rate (FPR), Fall-out, probability of false alarm = $\frac{\Sigma \text{ False positive}}{\Sigma \text{ Condition negative}}$	True negative rate (TNR), Specificity $(SPC) = \frac{\Sigma \text{ True negative}}{\Sigma \text{ Condition negative}}$
	Accuracy (ACC) = $\frac{\Sigma \text{ True positive} + \Sigma \text{ True negative}}{\Sigma \text{ Total population}}$	Positive predictive value (PPV), Precision $= \frac{\Sigma \text{ True positive}}{\Sigma \text{ Test outcome positive}}$	False omission rate (FOR) $= \frac{\Sigma \text{ False negative}}{\Sigma \text{ Test outcome negative}}$	Positive likelihood ratio (LR+) = $\frac{\text{TPR}}{\text{FPR}}$	Diagnostic odds ratio (DOR) = $\frac{LR+}{ID-}$
		False discovery rate (FDR) $= \frac{\Sigma \text{ False positive}}{\Sigma \text{ Test outcome positive}}$	Negative predictive value (NPV) $= \frac{\Sigma \text{ True negative}}{\Sigma \text{ Test outcome negative}}$	Negative likelihood ratio (LR-) = $\frac{FNR}{TNR}$	Diagnostic odds ratio (DOR) = $\frac{1}{LR}$

$$\mathrm{FPR} = \frac{\mathrm{FP}}{\mathrm{FP} + \mathrm{TN}}$$

$$TPR = \frac{TP}{TP + FN} = \text{recall}$$



ROC AUC

- Area under ROC Curve
- Always .5 for random / constant prediction

```
from sklearn.metrics import roc_auc_score
rf_auc = roc_auc_score(y_test, rf.predict_proba(X_test)[:, 1])
svc_auc = roc_auc_score(y_test, svc.decision_function(X_test))
print("AUC for Random Forest: {:.3f}".format(rf_auc))
print("AUC for SVC: {:.3f}".format(svc_auc))
AUC for Random Forest: 0.937
AUC for SVC: 0.916
```

The Relationship Between Precision-Recall and ROC Curves https://www.biostat.wisc.edu/~page/rocpr.pdf

Multi-class classification

Confusion Matrix

Normalizing confusion matrix (by rows) can be helpful

0 1 0 1 0 0 1 44]]

<pre>print(classification_report(y_test, pred))</pre>				
	precision	recall	f1-score	support
0	1.00	1.00	1.00	37
1	0.89	0.91	0.90	43
2	0.95	0.93	0.94	44
3	0.90	0.96	0.92	45
4	0.97	1.00	0.99	38
5	0.98	0.98	0.98	48
6	0.96	1.00	0.98	52
7	1.00	0.94	0.97	48
8	0.93	0.90	0.91	48
9	0.96	0.94	0.95	47
avg / total	0.95	0.95	0.95	450

Micro and Macro F1

- Macro-average f1: Average f1 scores over classes
- Micro-average f1: Average binary confusion matrices, then compute recall, precision once

```
print("Micro average f1 score: {:.3f}".format(f1_score(y_test, pred, average="micro")))
print("Macro average f1 score: {:.3f}".format(f1_score(y_test, pred, average="macro")))
Micro average f1 score: 0.953
Macro average f1 score: 0.954
```

Macro: "all classes are equally important"

Micro: "all samples are equally important" - same for other metric averages

Picking metrics?

- Accuracy rarely what you want
- Problems are rarely balanced
- Find the right criterion for the task
- OR pick one arbitrarily, but at least think about it
- Emphasis on recall or precision?
- Which classes are the important ones?

Using metrics in cross-validation

```
X = digits.data
y = digits.target == 9

# default scoring for classification is accuracy
scores_default = cross_val_score(SVC(), X, y)

# providing scoring="accuracy" doesn't change the results
explicit_accuracy = cross_val_score(SVC(), X, y, scoring="accuracy")

# using ROC AUC
roc_auc = cross_val_score(SVC(), X, digits.target == 9, scoring="roc_auc")

print("Default scoring: {}".format(scores_default))
print("Explicit accuracy scoring: {}".format(explicit_accuracy))
print("AUC scoring: {}".format(roc_auc))

Default scoring: [ 0.9  0.9  0.9]
Explicit accuracy scoring: [ 0.9  0.9  0.9]
AUC scoring: [ 0.994  0.99  0.996]
```

Same for GridSearchCV Will make GridSearchCV.score use your metric!

Built-in scoring

- "scoring" can be string or callable.
- Strings:

```
from sklearn.metrics.scorer import SCORERS
print("\n".join(sorted(SCORERS.keys())))
accuracy
adjusted mutual info score
adjusted rand score
average precision
completeness score
f1
f1 macro
fl micro
f1 samples
fl weighted
fowlkes mallows score
homogeneity score
log loss
mean absolute error
mean squared error
median absolute error
mutual info score
```

```
neg log loss
neg mean absolute error
neg mean squared error
neg mean squared log error
neg median absolute error
normalized mutual info score
precision
precision macro
precision micro
precision samples
precision weighted
r2
recall
recall macro
recall micro
recall samples
recall weighted
roc auc
v measure score
```

Metrics for regression models

Build-in standard metrics

- R^2 : easy to understand scale
- MSE: easy to relate to input
- Mean absolute error, median absolute error: more robust.

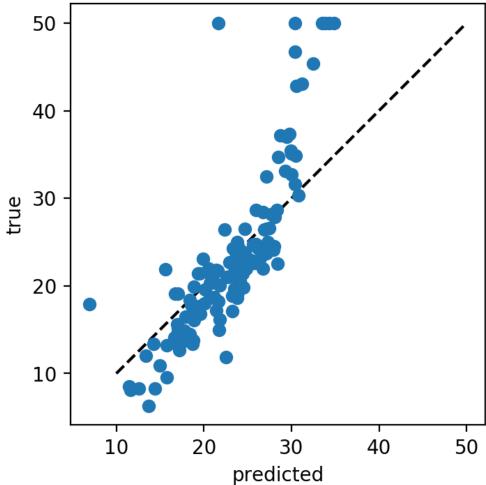
 When using "scoring" use "neg_mean_squared_error" etc

Prediction plots

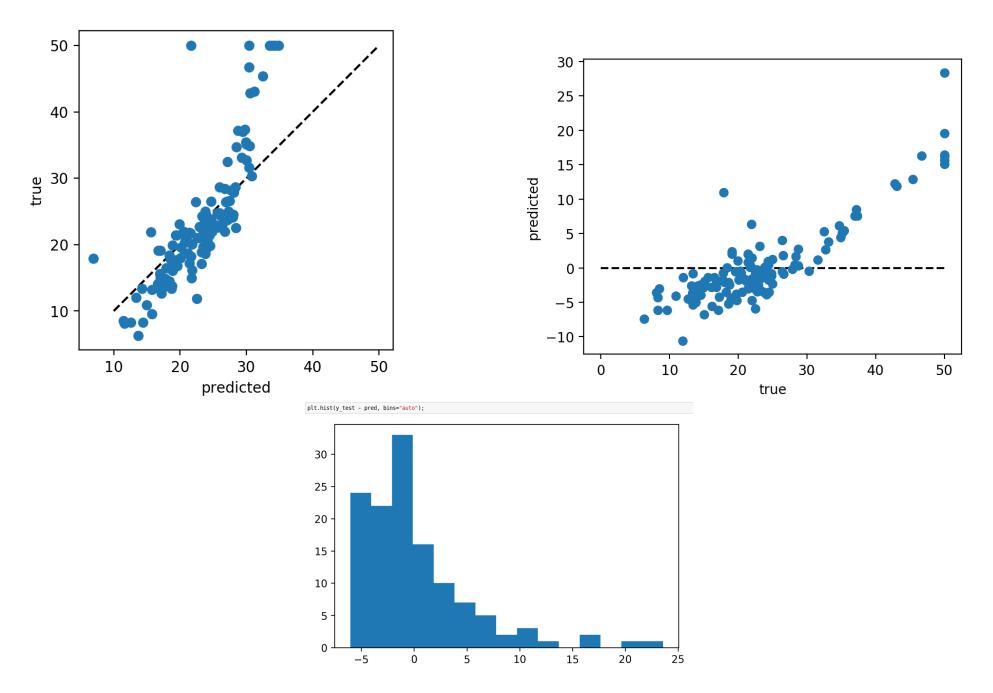
```
from sklearn.linear_model import Ridge
from sklearn.datasets import load_boston
boston = load_boston()

X_train, X_test, y_train, y_test = train_test_split(boston.data, boston.target)

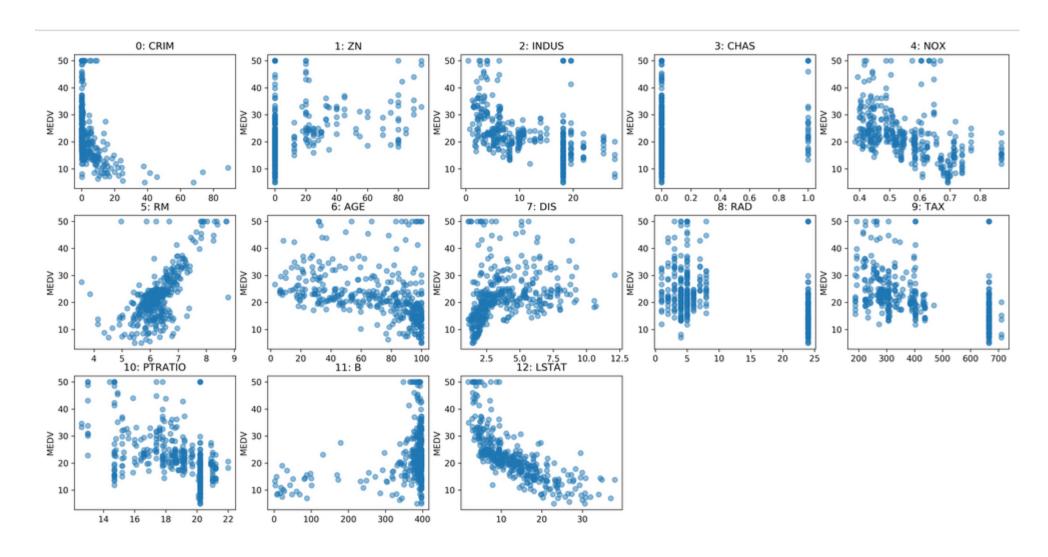
ridge = Ridge(normalize=True).fit(X_train, y_train)
pred = ridge.predict(X_test)
plt.plot(pred, y_test, 'o')
```



Residual Plots



Target vs Feature



Absolute vs relative: MAPE

$$MAPE = \frac{100}{n} \sum_{i=1}^{n} \left| \frac{y - \hat{y}}{y} \right|$$

Over vs under

- Overprediction and underprediction can have different cost.
- Try to create cost-matrix: how much does overprediction and underprediction cost?
- Is it linear?