### **Continuous Variables**

### **Continuous Variables**

We're looking for features such as:

- Asymmetry
- Outliers
- Multimodality
- Gaps
- Heaping / Rounding
- Impossibilities / Errors

- primary tool for continuous data
- count / relative frequency / density
- boundaries
- binwidth

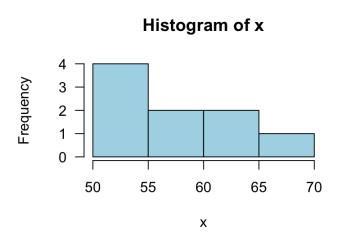
### How are histograms created?

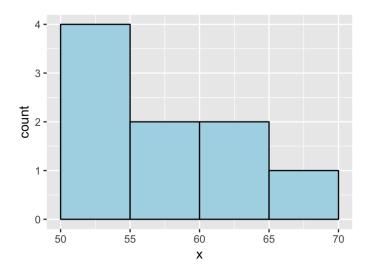
Draw a histogram on paper of the following data.

(use binwidth = 5)

50, 51, 53, 55, 56, 60, 65, 65, 68

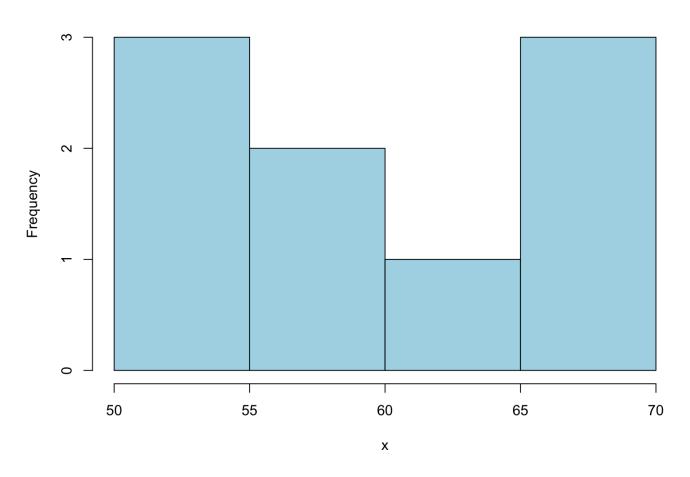
## How are histograms created?



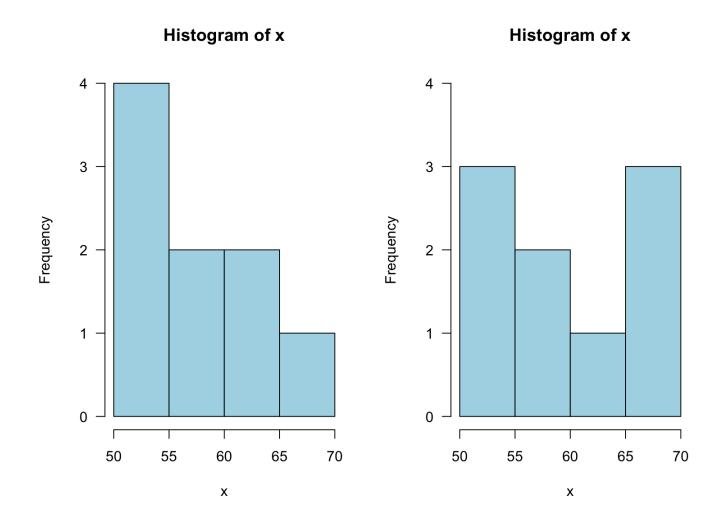


## How are histograms created?

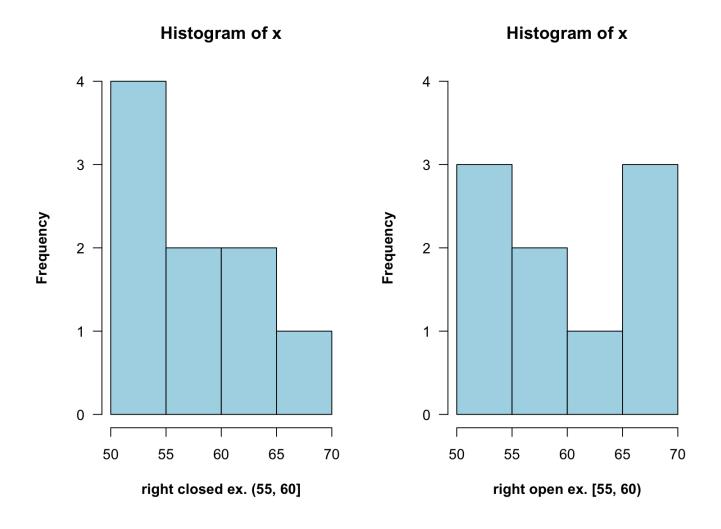




### What is causing the difference?

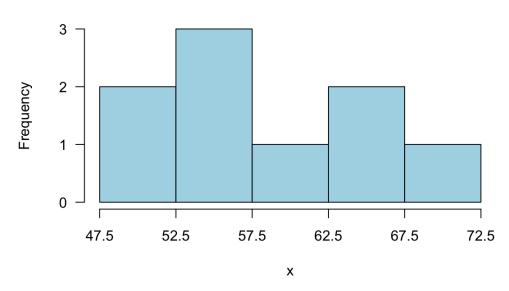


### **B**in boundaries

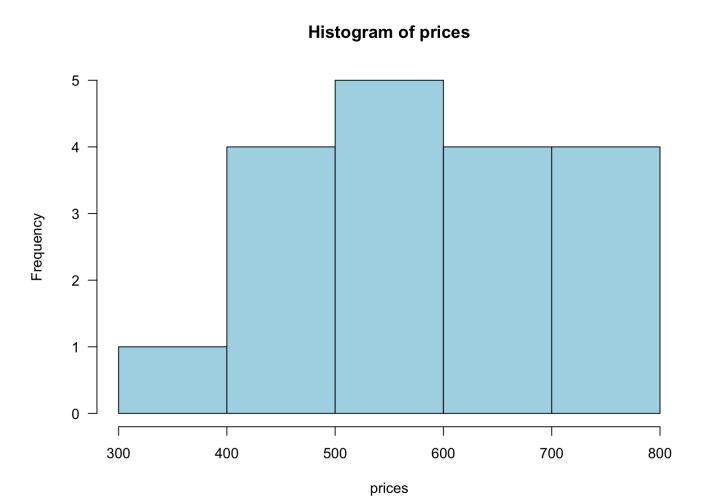


### **B**in boundaries





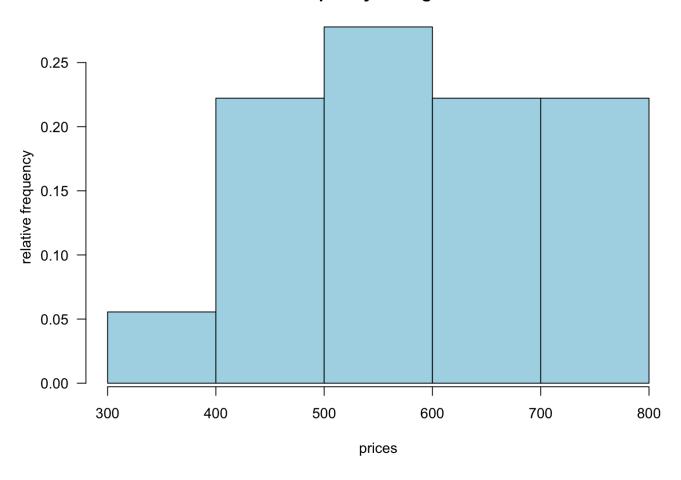
### Frequency (count) histogram



Prices of one-bedroom apartments in Morningside Heights (zip 10027) in \$1000k

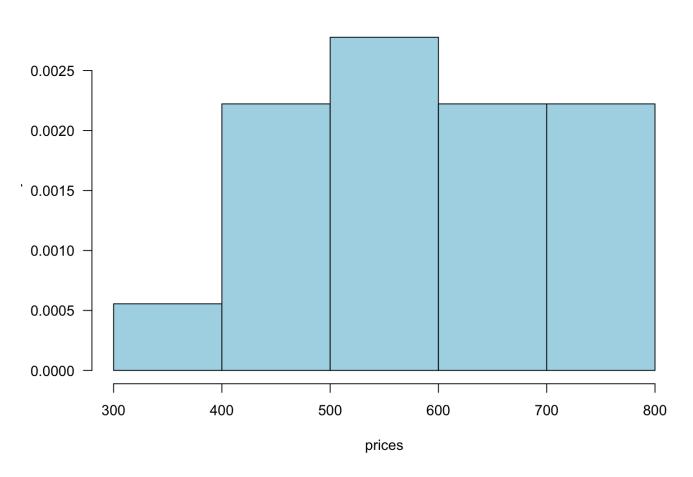
### Relative frequency histogram

#### **Relative Frequency Histogram of Prices**



## **Density Histogram**



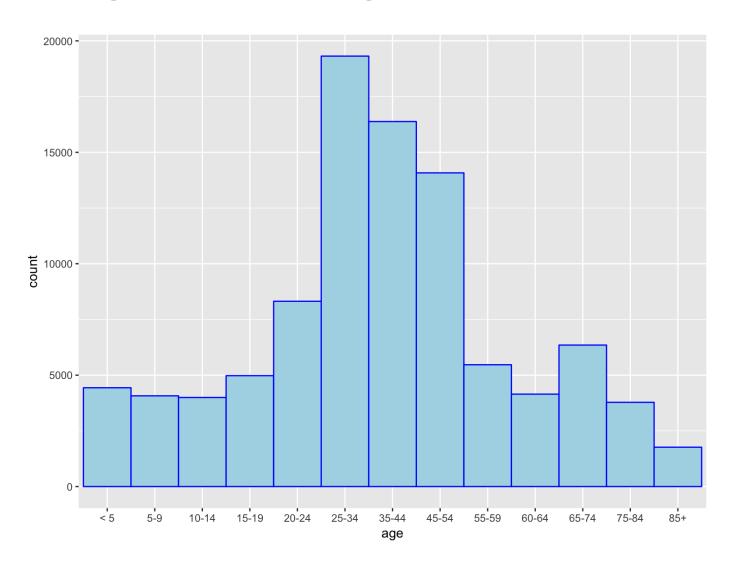


### **Count, Relative Frequency, Density**

Bin	Count	<b>Relative Frequency</b>	Density
300-400	I	.056	.00056
400-500	4	.22	.0022
500-600	5	.28	.0028
600-700	4	.22	.0022
700-800	4	.22	.0022

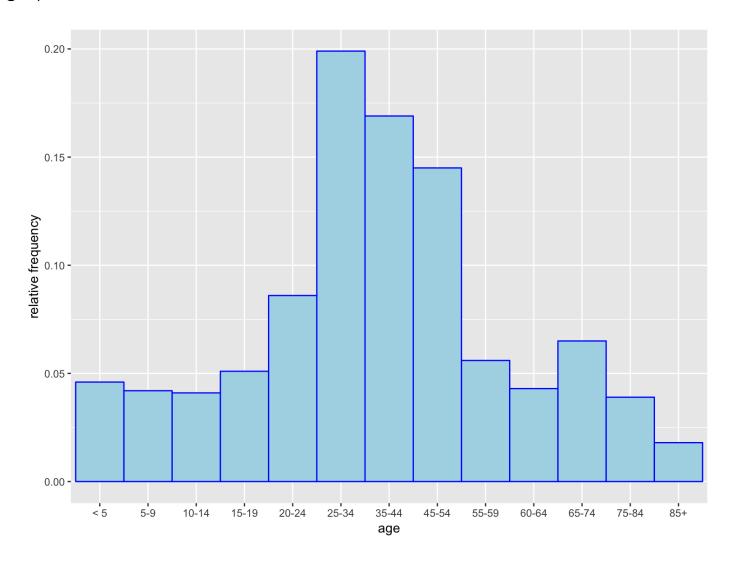
- How is relative frequency calculated?
- How is density calculated?

## What's wrong with this histogram?

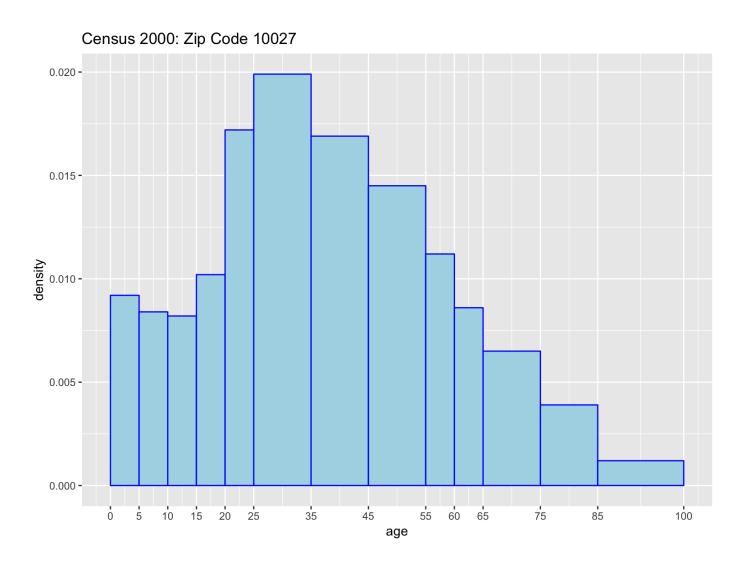


## Relative frequency histogram

(still wrong...)



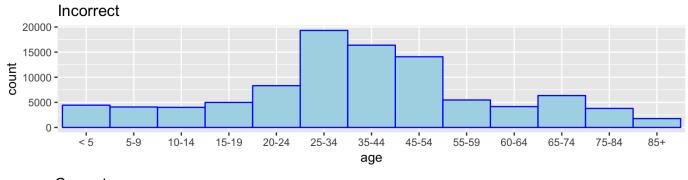
### Density histogram with unequal bin (or class) widths

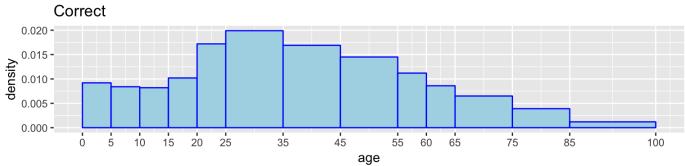


### **Density = RelFreq / Binwidth**

Class	<b>Frequency</b>	RelFreq	ClassWidth	Density
< 5	4435	0.046	5	0.009
5-9	4072	0.042	5	0.008
10-14	3999	0.041	5	0.008
15-19	4977	0.051	5	0.010
20-24	8316	0.086	5	0.017
25-34	19317	0.199	10	0.020
35-44	16380	0.169	10	0.017
45-54	14077	0.145	10	0.014
55-59	5467	0.056	5	0.011
60-64	4148	0.043	5	0.009
65-74	6350	0.065	10	0.007
75-84	3781	0.039	10	0.004
85+	1767	0.018	15	0.001

### Compare the histograms

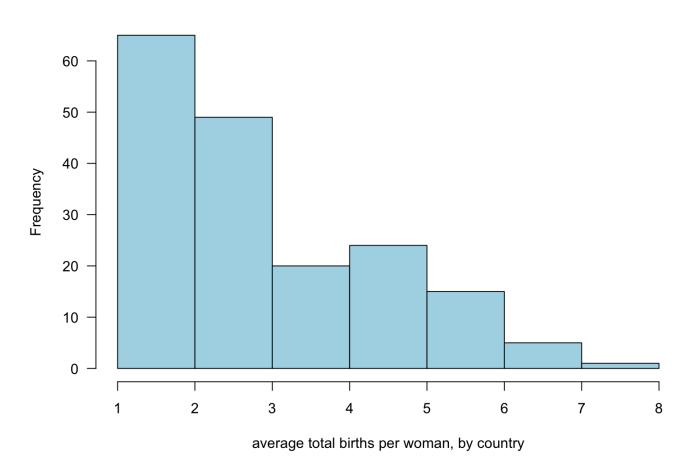


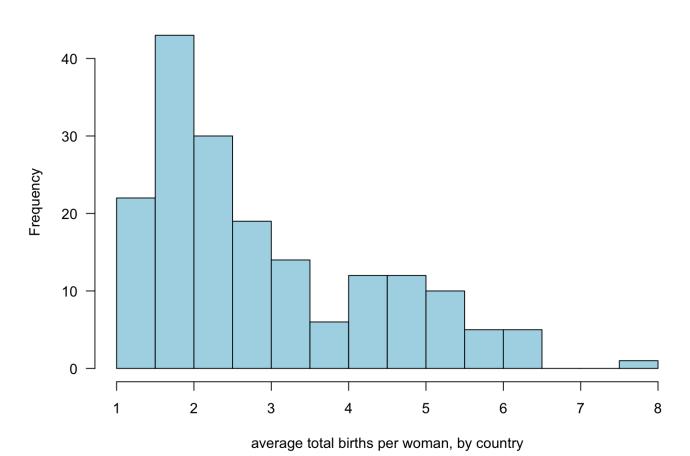


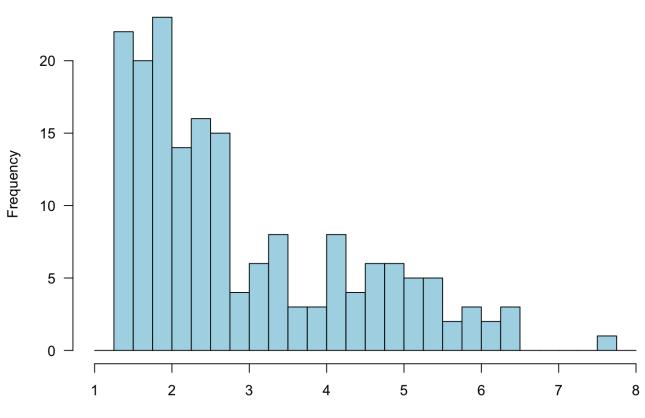
Source: https://factfinder.census.gov/

### **Binwidth**

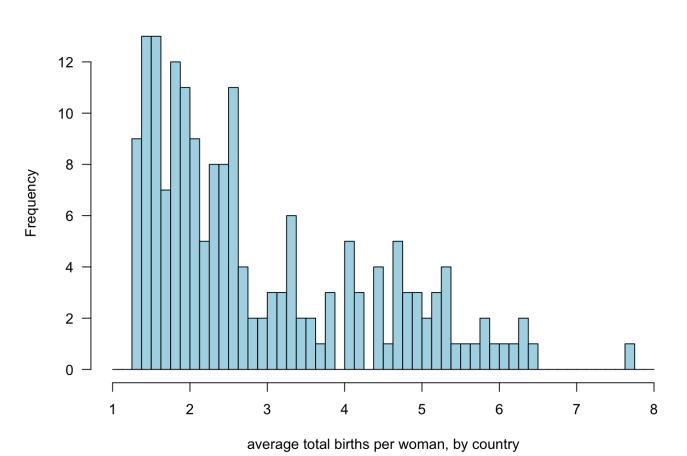
'stat\_bin()' using 'bins = 30'. Pick better
value with 'binwidth'.

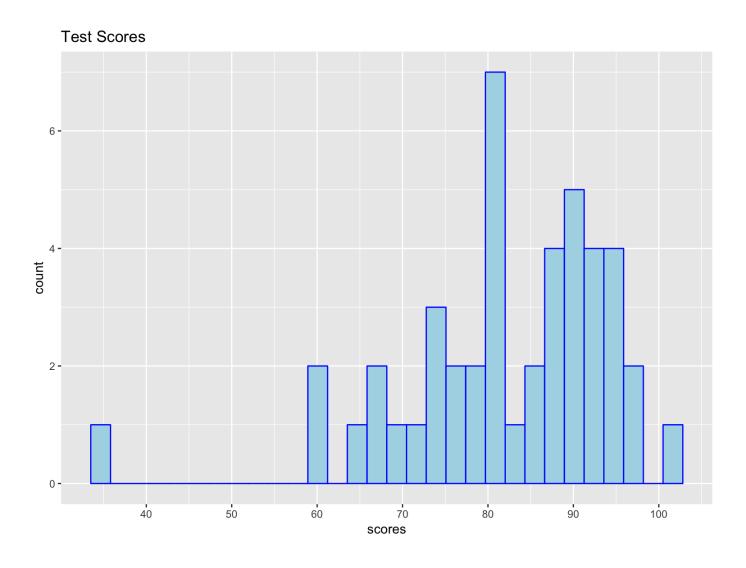




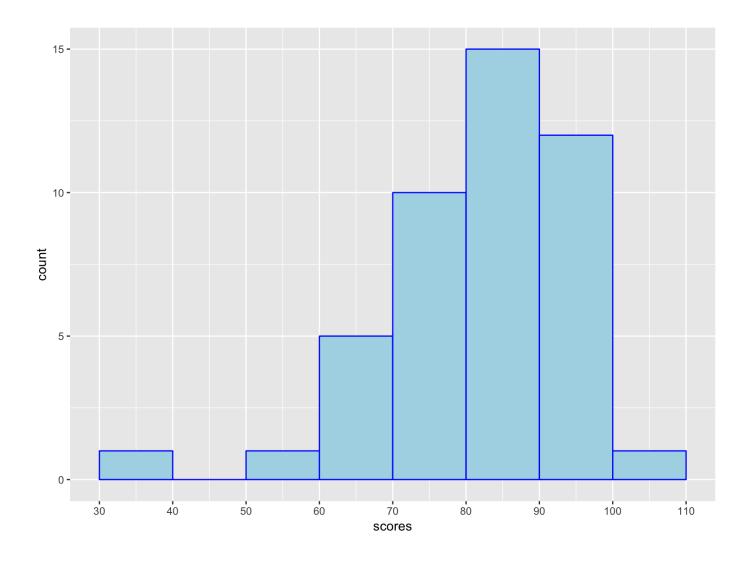


average total births per woman, by country





### **Fewer bins**



## **Weekly Savings**

Search:	

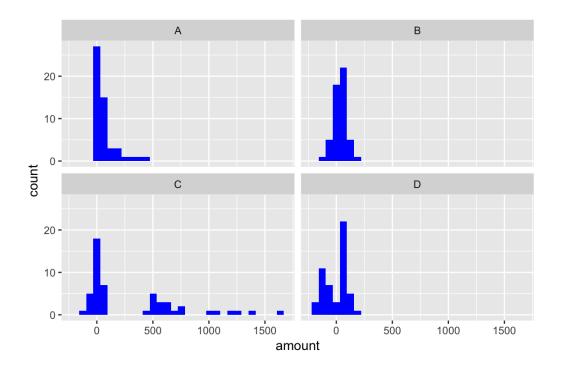
	A	В	c	D
I	\$0.91	-\$95.25	-\$95.25	-\$195.25
2	\$1.50	-\$75.12	-\$75.12	-\$175.12
3	\$2.02	-\$61.77	-\$61.77	-\$161.77
4	\$2.40	-\$46.18	-\$46.18	-\$146.18
5	\$3.27	-\$39.82	-\$39.82	-\$139.82
6	\$4.77	-\$37.62	-\$37.62	-\$137.62
7	\$5.58	-\$22.62	-\$22.62	-\$122.62
8	\$6.65	-\$16.22	-\$16.22	-\$116.22
9	\$7.93	-\$6.19	-\$6.19	-\$106.19
10	\$10.86	-\$4.29	-\$4.29	-\$104.29
11	\$12.04	-\$3.25	-\$3.25	-\$103.25
12	\$13.92	-\$2.04	-\$2.04	-\$102.04
13	\$14.07	-\$1.52	-\$1.52	-\$101.52
14	\$14.23	\$0.58	\$0.58	-\$99.42

	A	В	С	D
15	\$14.58	\$8.38	\$8.38	-\$91.62
16	\$16.23	\$10.08	\$10.08	-\$89.92
17	\$18.85	\$13.60	\$13.60	-\$86.40
18	\$19.98	\$16.91	\$16.91	-\$83.09
19	\$24.44	\$17.47	\$17.47	-\$82.53
20	\$25.11	\$18.65	\$18.65	-\$81.35
21	\$25.68	\$20.10	\$20.10	-\$79.90
22	\$25.87	\$24.33	\$24.33	\$24.33
23	\$26.00	\$28.20	\$28.20	\$28.20
24	\$28.54	\$31.10	\$31.10	\$31.10
25	\$29.54	\$31.81	\$31.81	\$31.81
26	\$30.48	\$32.74	\$32.74	\$32.74
27	\$30.65	\$35.03	\$35.03	\$35.03
28	\$39.09	\$37.77	\$37.77	\$37.77
29	\$40.21	\$40.5 I	\$40.51	\$40.5 I
30	\$47.27	\$40.71	\$40.71	\$40.71
31	\$51.40	\$41.00	\$41.00	\$41.00

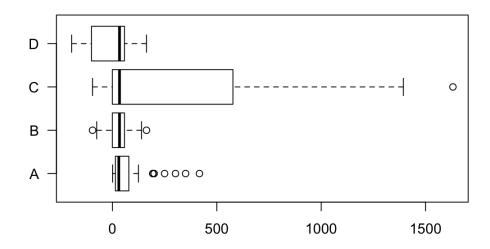
	A	В	С	D
32	\$52.3 I	\$45.79	\$457.93	\$45.79
33	\$57.08	\$48.48	\$484.75	\$48.48
34	\$58.27	\$49.30	\$493.00	\$49.30
35	\$65.17	\$49.78	\$497.84	\$49.78
36	\$65.55	\$52.18	\$521.84	\$52.18
37	\$73.49	\$52.62	\$526.19	\$52.62
38	\$73.73	\$54.15	\$541.53	\$54.15
39	\$74.93	\$55.68	\$556.83	\$55.68
40	\$82.54	\$59.80	\$597.98	\$59.80
41	\$85.92	\$62.60	\$626.02	\$62.60
42	\$92.27	\$65.14	\$651.41	\$65.14
43	\$95.69	\$65.37	\$653.71	\$65.37
44	\$104.58	\$70.36	\$703.56	\$70.36
45	\$124.60	\$76.70	\$766.99	\$76.70
46	\$192.96	\$78.21	\$782.15	\$78.21
47	\$194.34	\$103.50	\$1,035.00	\$103.50
48	\$199.99	\$109.22	\$1,092.22	\$109.22

	Α	В	С	D
49	\$249.96	\$119.50	\$1,194.99	\$119.50
50	\$302.12	\$128.15	\$1,281.47	\$128.15
51	\$350.54	\$139.37	\$1,393.66	\$139.37
52	\$416.85	\$163.11	\$1,631.09	\$163.11

Showing I to 52 of 52 entries

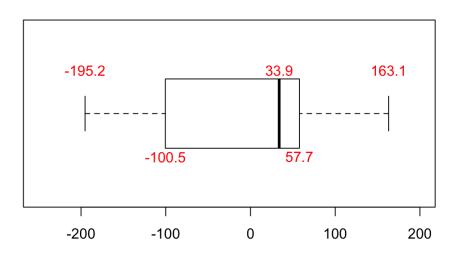


## **Boxplots**



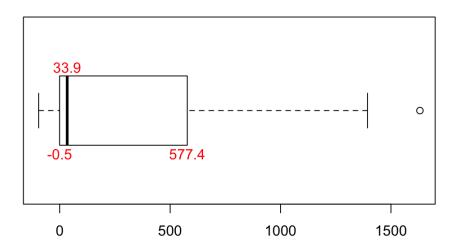
## **Boxplot (Person "D")**

```
## min lower-hinge median upper-hinge max
## -195.2 -100.5 33.9 57.7 163.1
```

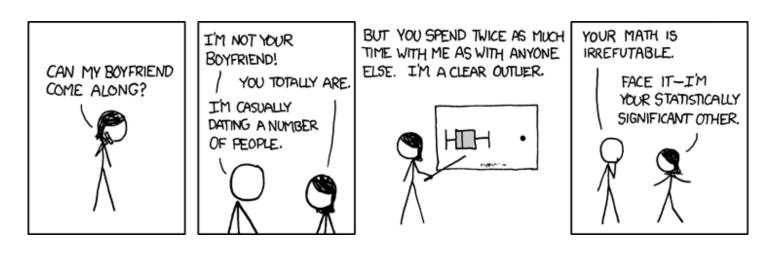


### **Boxplot with outliers (Person "C")**

## min lower-hinge median upper-hinge max ## -95.249 -0.473 33.889 577.408 1631.089



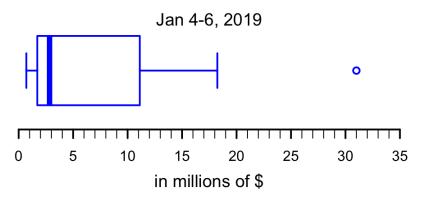
#### What does it take to be an outlier?



https://www.explainxkcd.com/wiki/index.php/539:\_Boyfriend

#### What does it take to be an outlier?

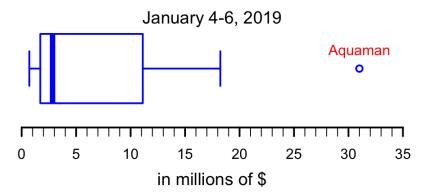
Weekend Box Office Gross, Top 20



Source: http://www.boxofficemojo.com/weekend/chart/

#### What does it take to be an outlier?

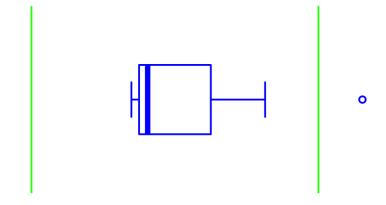
#### Weekend Box Office Gross, Top 20



#### fences:

- 1.5 x hinge spread above upper-hinge
- 1.5 x hinge spread below lower-hinge

### **Fences**

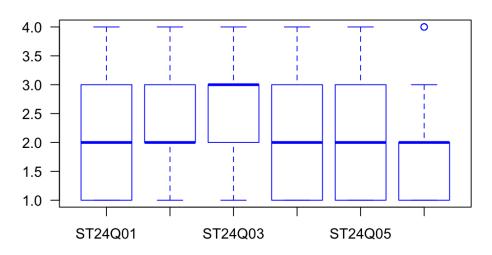


#### fences:

- $1.5 \times \text{hinge spread above upper-hinge}$
- $1.5 \times \text{hinge spread below lower-hinge}$

### Not for discrete data

PISA data (scale: 1 - 4)

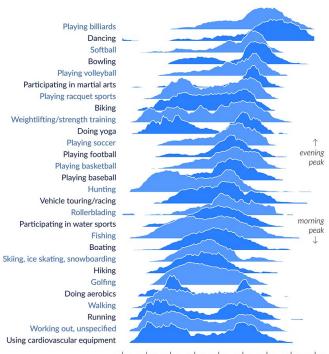


Source: R likert::pisaitems dataset

### Ridgeline plot

#### Peak time of day for sports and leisure

Number of participants throughout the day compared to peak popularity. Note the morning-and-evening everyday workouts, the midday hobbies, and the evenings/late nights out.



03:00 06:00 09:00 12:00 15:00 18:00 21:00 00:00 03:00

@hnrkIndbrg | Source: American Time Use Survey

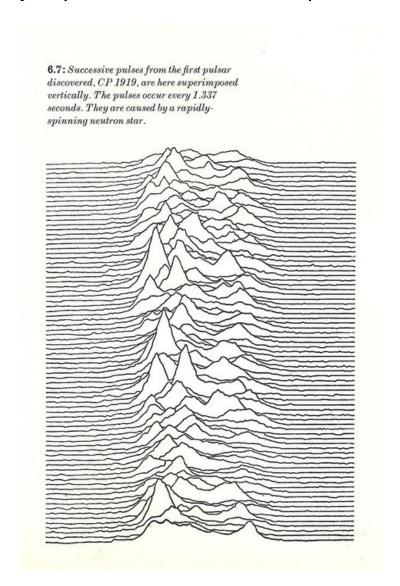
Source: https://eagereyes.org/blog/2017/joy-plots

Additional resources:

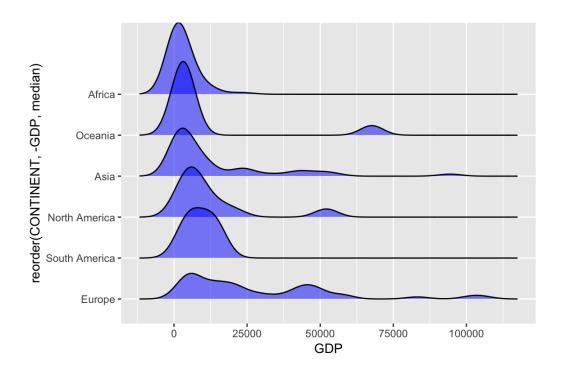
http://blog.revolutionanalytics.com/2017/07/joyplots.html

## Ridgeline plot inspiration

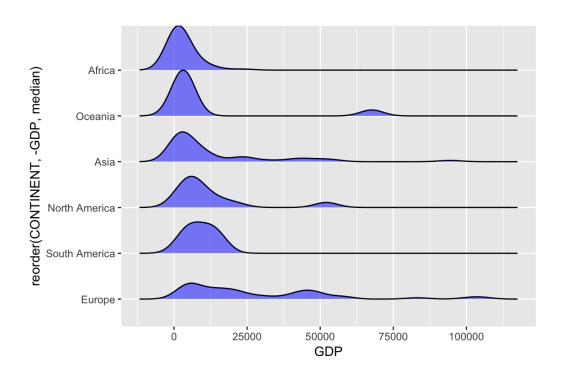
Jocelyn Bell discovers first radio pulsars, 1967



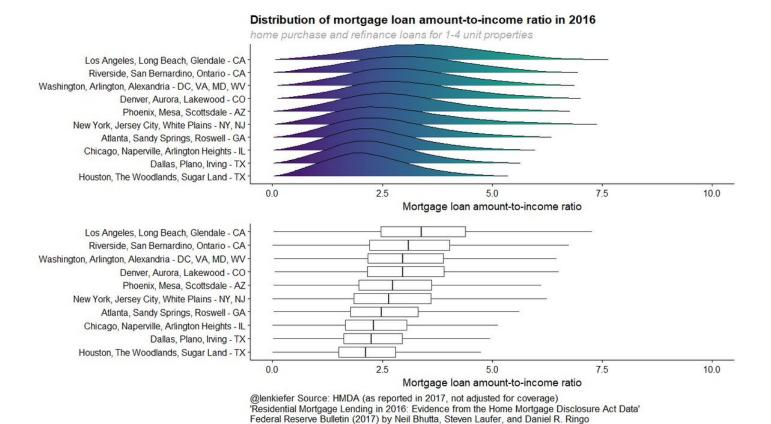
## Ridgeline plot



## Ridgeline plot, change scale



### Ridgeline vs. boxplot



Source: https://twitter.com/lenkiefer/status/916823350726610946

### ggridges package

**CRAN** https://CRAN.R-project.org/package=ggridges

**Github** https://github.com/clauswilke/ggridges

Package vignette(s) https://cran.r-project.org/web/packages/ggridges/vignettes/introduction.html

https://cran.r-project.org/web/packages/ggridges/vignettes/gallery.html

Package manual https://cran.r-project.org/web/packages/ggridges/ggridges.pdf