

Statistical learning

Ngô Minh Nhựt

2024

Course info

☐ Materials

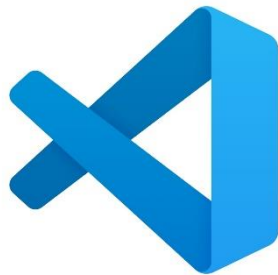
- Lecture notes
- Books:
 - G. James, An Introduction to Statistical Learning (2nd edition), Springer, 2021
 - C. Bishop, Pattern Recognition and Machine Learning, Springer, 2006 ([pdf](#))

☐ Lecturers

- Theory: Ngô Minh Nhật
- Labs: Lê Long Quốc

Course info

- ❑ Labs and coding environment
 - Through instruction session and Q&A on forum
 - Python (with Visual Code)
 - Google Colab (for training with powerful machines)



<https://code.visualstudio.com>



<https://colab.research.google.com>

Course info

□ Tests

- Quiz and report: 10%
- Lab assignment: 20%
- Mid-term test: 35%
- Final project: 35%

Course info

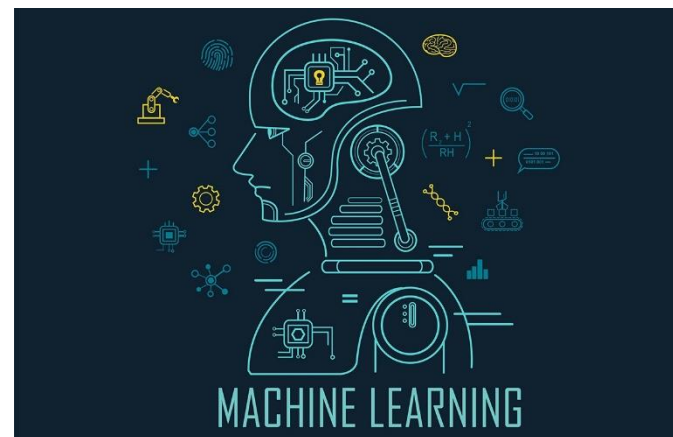
- This course provides
 - basic knowledge about machine learning and
 - underlying mechanism about machine learning as well as
 - some applications in practical problems

Course topic

Week	Topic	Week	Topic
1	Introduction	8	Support vector machine
2	Linear regression	9	K-mean
3	Logistic regression	10	Dimensionality reduction
4	Overfitting and model validation	11	Decision tree
5	Neural network		
6	Midterm test		
7	Convolutional neural network		

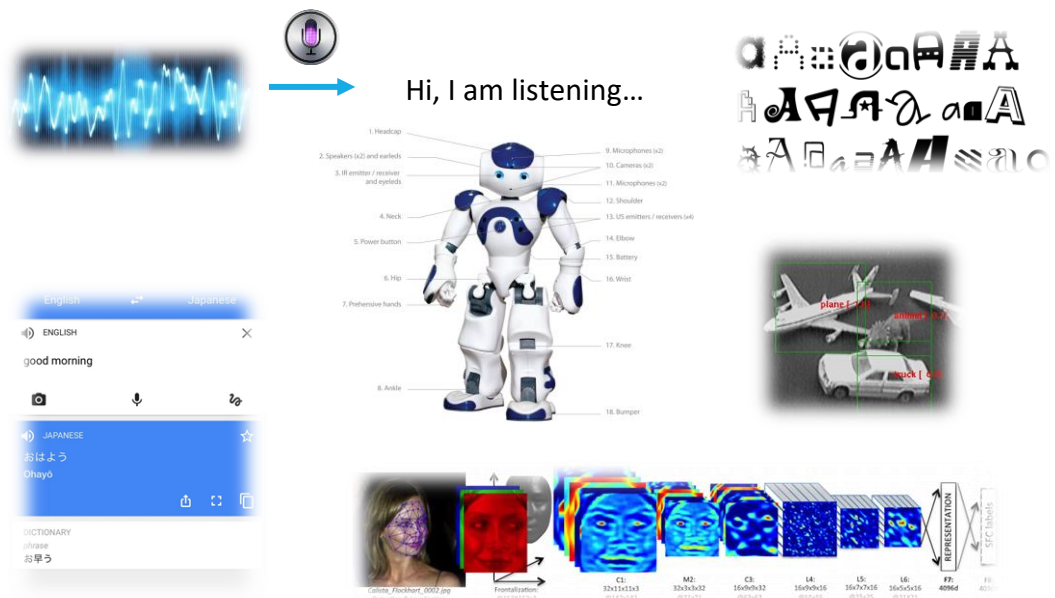
Machine learning

- A machine learning algorithm is an algorithm learning to accomplish a task by observing data.
- Used on complex tasks where it's hard to develop algorithms with handcrafted-rules
- Exploits patterns in observed data and extract rules automatically



Applications

- ❑ Computer vision
- ❑ Speech to text, text to speech
- ❑ Financial analysis
- ❑ Self-driving cars
- ❑ Ads-targeting
- ❑ Virtual assistance



Example: object detection



- ❑ Learn from annotated corpus of examples (a dataset) to classify unknown images among different object types
- ❑ Observe images to learn patterns
- ❑ Lot of data available (i.e: ImageNet dataset)
- ❑ Very good error rates ($< 5\%$ with deep-CNN)

Types of machine learning algorithms

□ Supervised

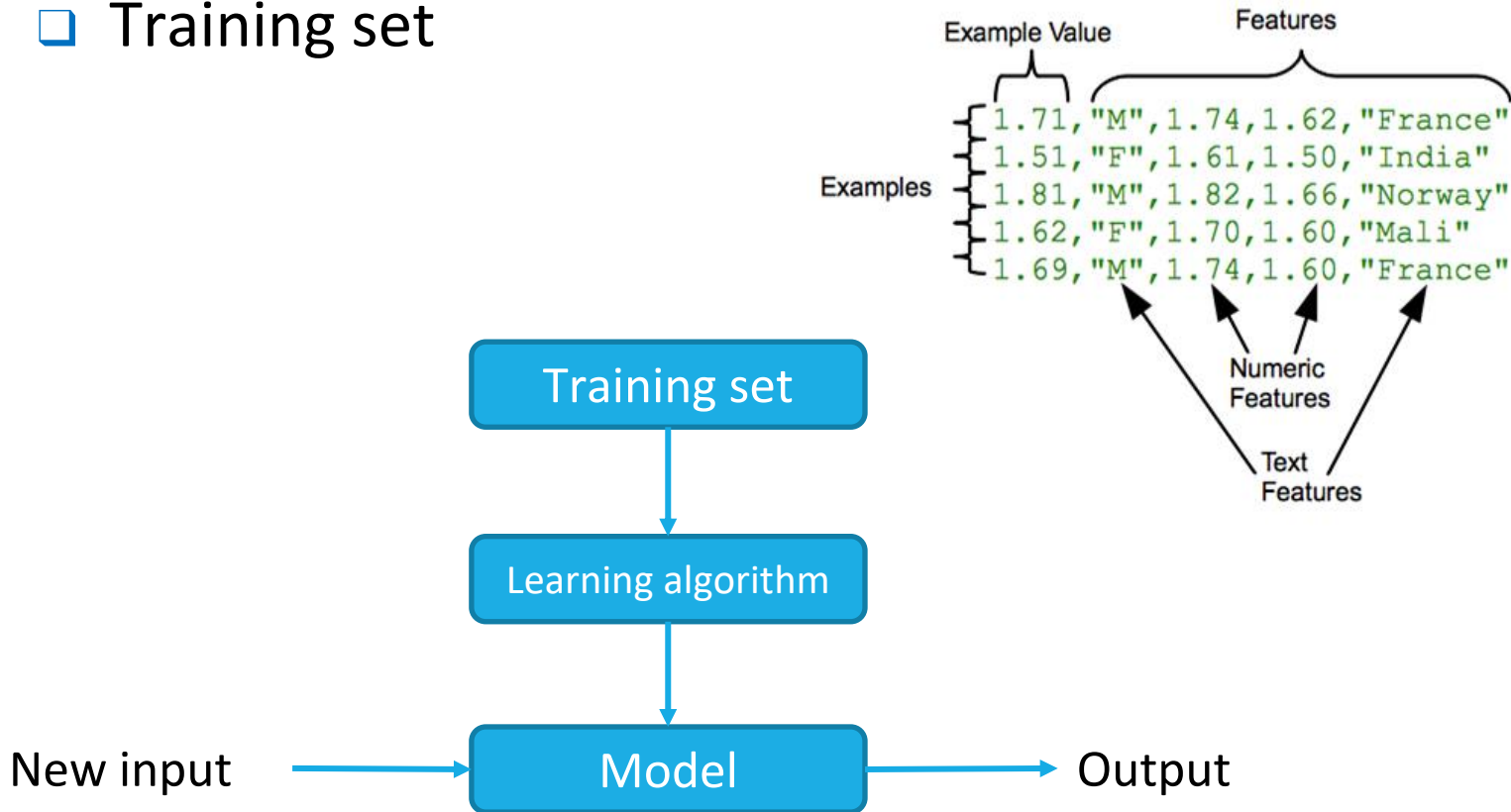
- Learn a function by observing labeled samples, containing input and expected output
- Classification
- Regression

□ Unsupervised

- Find underlying relations in data by observing unlabeled samples, containing only input
- Clustering
- Dimensionality reduction

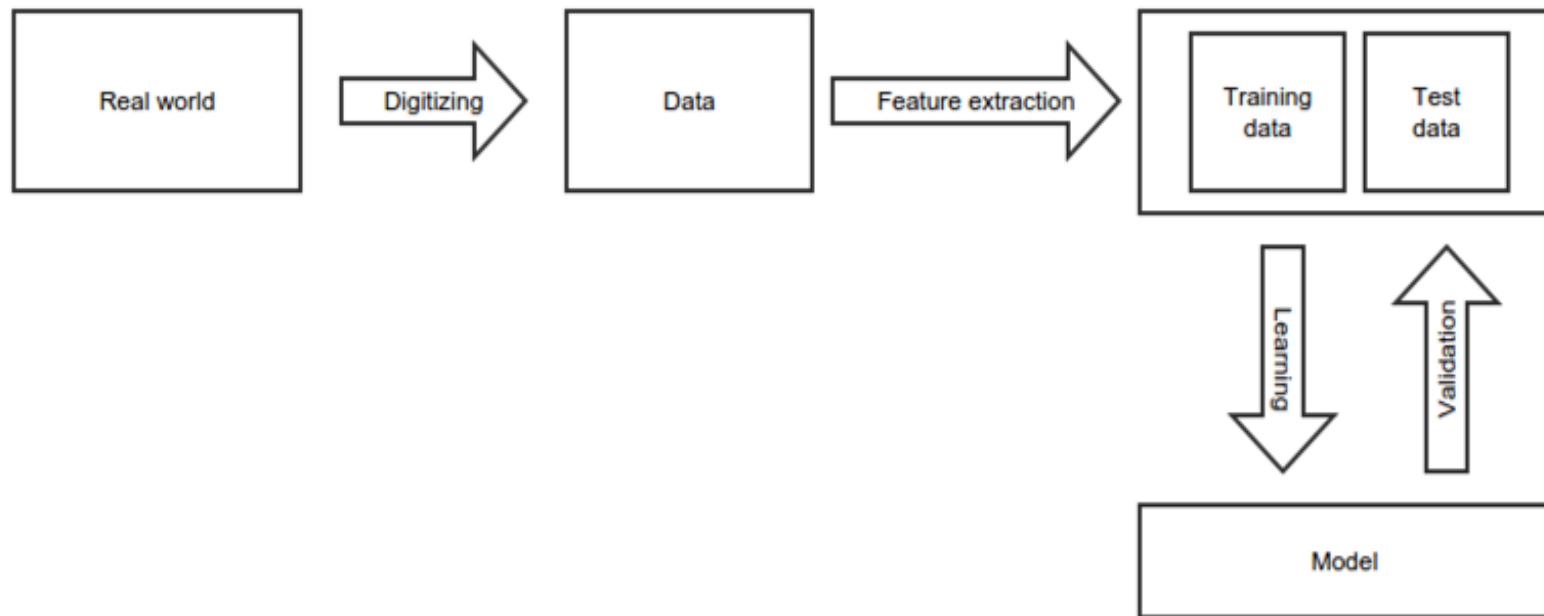
Machine learning

□ Training set



Machine learning

□ Learning process



Feature extraction

- ❑ Extract the information useful for the task (features) we want to learn

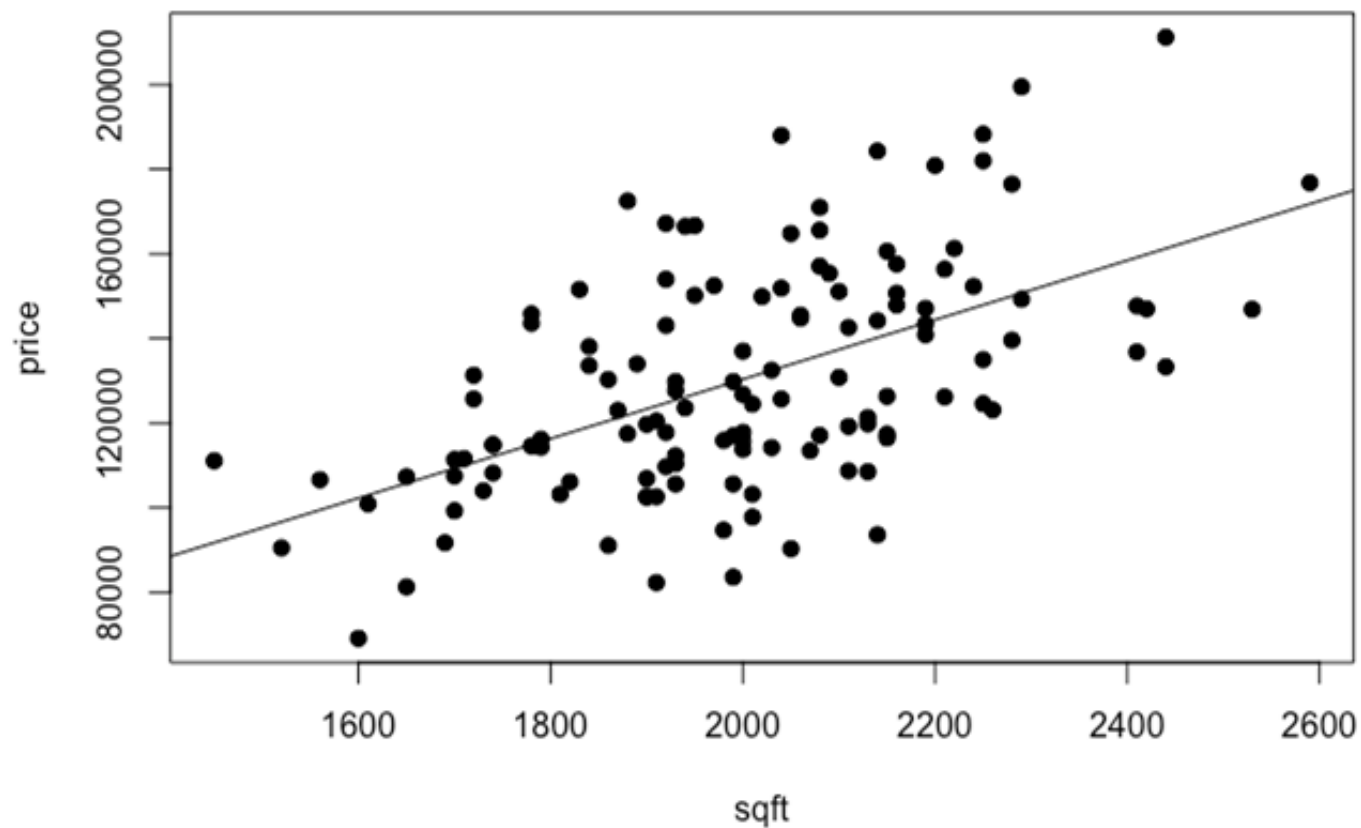
- ❑ Example

- ❑ Stock market time-series → [opening price, closing price, lowest, highest]
 - ❑ Image → Image with edges filtered
 - ❑ Document → bag-of-words

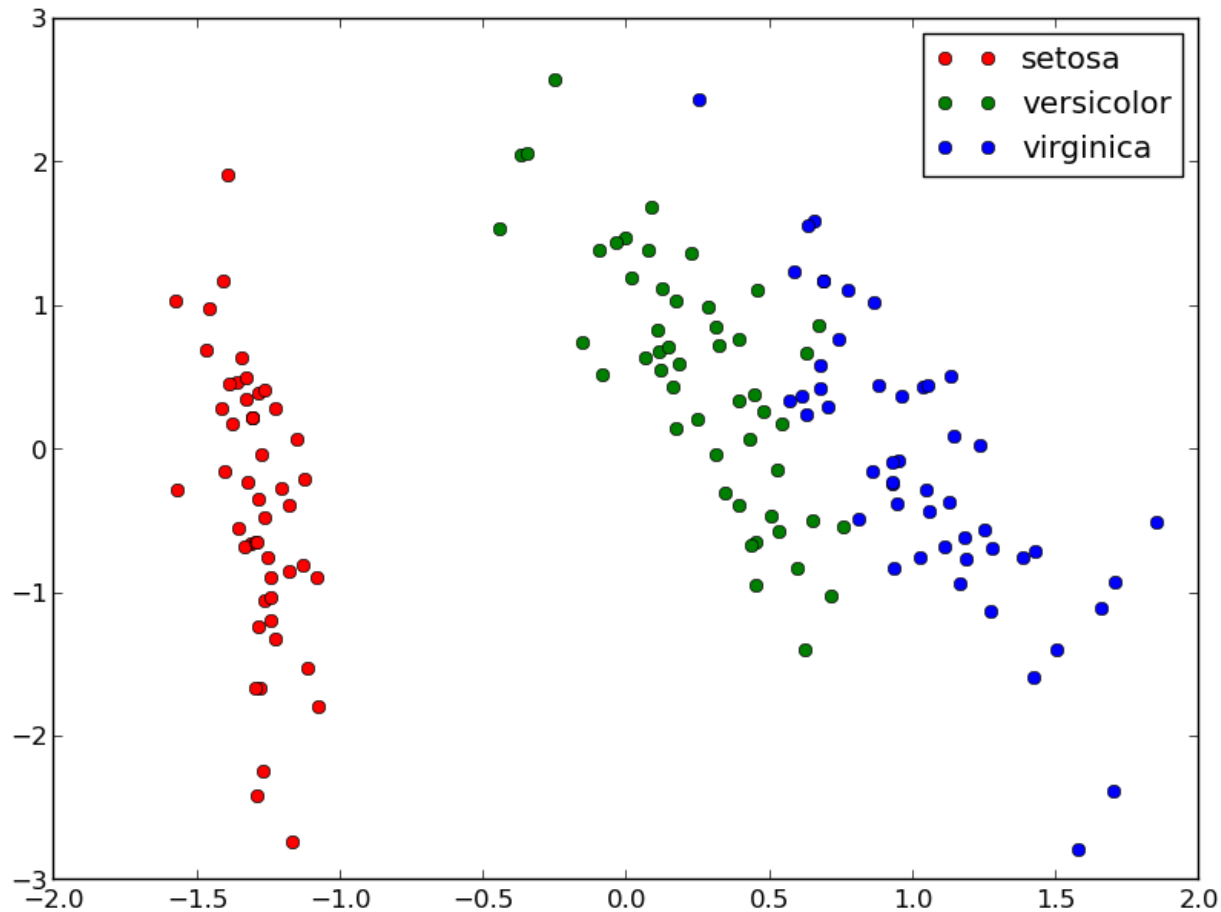
Classification vs Regression

- Regression: learn a function mapping an input to a real value
 - E.g., predict the temperature of tomorrow given some meteo signals
- Classification: learn a function mapping an input element to a class (within a finite set of possible classes)
 - E.g., predict tomorrow weather: {sunny, cloudy, rainy} given some meteor signals

Regression

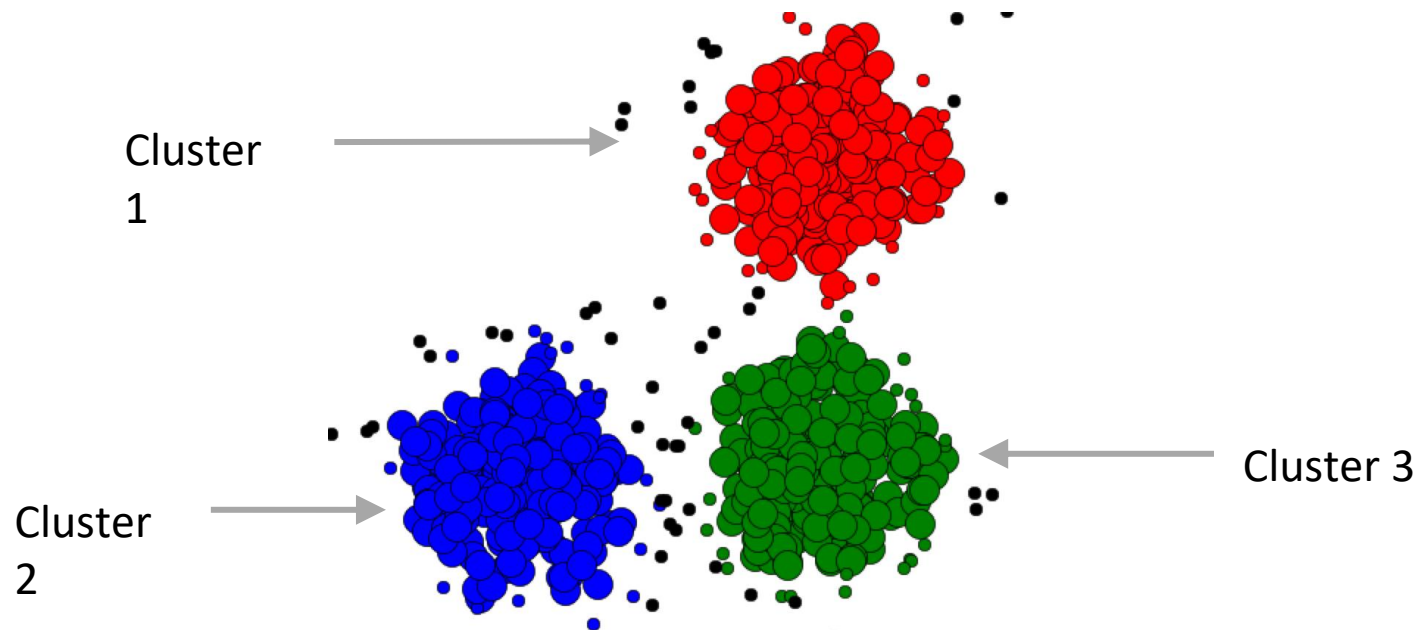


Classification



Clustering

- Separate different observed data points in similar groups (clusters). Observed data are unlabeled.



Linear algebra review

- ❑ Matrix and vector
- ❑ Summation and dot product
- ❑ Matrix multiplication
- ❑ Inversion and transposition

Matrix and vector

- Matrix is a two-dimension array, e.g.,

$$A = \begin{bmatrix} a & b & c \\ d & e & f \end{bmatrix}$$

- A is a 2x3 matrix consisting of 2 rows and 3 columns

- Vector is a matrix with multiple rows and one column

$$B = \begin{bmatrix} x \\ y \\ w \\ z \end{bmatrix}$$

- B is a vector or 4x1 matrix

Matrix and vector

□ Unit matrix

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

- Square matrix
- Diagonal from left-top to right-bottom are all one
- Other elements are zero
- Notation of unit matrix: I

Matrix and vector

□ Notations and symbols

- A_{ij} : element at i-th row and j-th column of matrix A
- Vector with n dimensions is a vector with n rows
- v_i : element at i-th row of vector v
- Matrix is represented by upper case characters, vector by lower case ones
- Scalar is a quantity having one value
- \mathbb{R} : set of real scalars
- \mathbb{R}^n : set of n-dimension vectors

Summation and dot product

- Summation of matrixes is done element wise, e.g.,

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix} + \begin{bmatrix} x & y \\ w & z \end{bmatrix} = \begin{bmatrix} a + x & b + y \\ c + w & d + z \end{bmatrix}$$

- Dimension of output matrix does not change

- Multiplication of matrix and a scalar

$$\alpha \begin{bmatrix} a & b \\ c & d \end{bmatrix} = \begin{bmatrix} \alpha a & \alpha b \\ \alpha c & \alpha d \end{bmatrix}$$

Matrix multiplication

□ Multiplication of matrix and vector

$$\begin{bmatrix} a & b \\ c & d \\ e & f \end{bmatrix} * \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} ax + by \\ cx + dy \\ ex + fy \end{bmatrix}$$

- Output is a vector
- Dimension of vector must be equal to number of columns of matrix
 - E.g., $m \times n$ matrix multiplied by $n \times 1$ vector resulting in $m \times 1$ vector
 - Vector is the second operand

Matrix multiplication

□ Multiplication of matrix and matrix

$$\begin{bmatrix} a & b \\ c & d \\ e & f \end{bmatrix} * \begin{bmatrix} x & y \\ w & z \end{bmatrix} = \begin{bmatrix} ax + bw & ay + bz \\ cx + dw & cy + dz \\ ex + fw & ey + fz \end{bmatrix}$$

- Split into multiplications of matrix and vectors and combine the outputs
- Number of columns of first matrix must be equal to number of rows of second matrix
 - E.g., $m \times n$ matrix multiplied by $n \times p$ matrix resulting in $m \times p$ matrix

Inversion and transposition

□ Inversion

- Inverted matrix of A is denoted by A^{-1}
- $A * A^{-1} = I$
- Non-squared matrix does not have inverted matrix

□ Transposition

- Transposed matrix of A is denoted by A^T
- $A = \begin{bmatrix} a & b \\ c & d \\ e & f \end{bmatrix}, A^T = \begin{bmatrix} a & c & e \\ b & d & f \end{bmatrix}$
- $A_{ij} = A^T_{ji}$

Statistics review

- ❑ Mean, median
- ❑ Variance, standard deviation
- ❑ Correlation
- ❑ Covariance
- ❑ Law of large numbers