Math 300 NTI Lesson 15

Multiple Regression - Two Numerical

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June, 2022

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Objectives

- 1. For two numerical explanatory variables in a linear regression model, conduct exploratory analysis and explain the relationship between the variables.
- 2. Fit a linear regression model to two numerical explanatory variables using the ${\tt lm}()$ function and interpret the output.

Reading

Chapter 6.2

Lesson

Remember that you will be running this more like a lab than a lecture. You want them using R and answering questions. Have them open the notes rmd and work through it together.

Work through the learning checks LC6.2 - 6.3.

- We use select() to change the names of the variables as well as to select them.
- Collinearity (or multicollinearity) is a phenomenon where one explanatory variable in a multiple regression model is highly correlated with another. This course doesn't discuss multicollinearity but it impacts the inference portion of the analysis cycle. Math 378 is a course that presents methods to handle multicollinearity.
- We preface our interpretation with the statement, "taking into account all the other explanatory variables in our model" in this section. This means we have to treat the other variables as at a constant value even though collinearity in practice may not allow this. It is only from an interpretation point of view that we use that statement.

• A phenomenon known as Simpson's Paradox, whereby overall trends that exist in aggregate either disappear or reverse when the data are broken down into groups. The next lesson discusses this in more depth.

Setup

```
library(tidyverse)
library(moderndive)
library(skimr)
library(ISLR)
```

Recreate the analysis done in the book.

Let's look at 5 random rows of data.

```
set.seed(507)
credit_ch6 %>%
  sample_n(size = 5)
```

```
## # A tibble: 5 x 6
##
        ID debt credit_limit income credit_rating
##
     <int> <int>
                          <int>
                                 <dbl>
                                                <int> <int>
## 1
       218
             955
                          5395
                                  12.5
                                                  392
                                                          65
## 2
       160
               0
                          3000
                                  53.3
                                                  235
                                                          53
## 3
       112
               0
                          2959
                                  28.6
                                                  231
                                                          60
## 4
        77
             532
                          3293
                                  30.6
                                                  251
                                                          68
## 5
       265
                          5107
                                  28.0
                                                  380
             651
                                                          55
```

glimpse(credit_ch6)

```
credit_ch6 %>%
  select(debt, credit_limit, income) %>%
  my_skim() %>%
  print()
```

```
## -- Data Summary -----
##
                            Values
## Name
                            Piped data
## Number of rows
                            400
## Number of columns
## Column type frequency:
##
    numeric
                            3
##
## Group variables
                            None
## -- Variable type: numeric -----
                                                               p25
                                                                     p50
                                                                            p75
    skim_variable n_missing complete_rate mean
                                                   sd
## 1 debt
                         0
                                      1 520.
                                                 460.
                                                        0
                                                              68.8
                                                                    460.
                                                                          863
## 2 credit_limit
                         0
                                       1 4736.
                                               2308.
                                                      855
                                                            3088
                                                                   4622.
                                                                         5873.
## 3 income
                         0
                                           45.2
                                                 35.2
                                                      10.4
                                                              21.0
                                                                     33.1
##
      p100
## 1
    1999
## 2 13913
## 3
      187.
## $numeric
##
  -- Variable type: numeric ------
                                                               p25
                                                                            p75
    skim_variable n_missing complete_rate mean
                                                                     p50
                                                   sd
## 1 debt
                         0
                                       1 520.
                                                              68.8
                                                460.
                                                        0
                                                                  460.
                                                                          863
## 2 credit limit
                         0
                                       1 4736.
                                               2308.
                                                      855
                                                            3088
                                                                   4622.
                         0
                                           45.2
                                                 35.2 10.4
                                                                     33.1
## 3 income
                                       1
                                                              21.0
## # ... with 1 more variable: p100 <dbl>
credit_ch6 %>%
 select(debt, credit_limit, income) %>%
 cor()
                    debt credit_limit
##
                                        income
## debt
               1.0000000
                           0.8616973 0.4636565
## credit_limit 0.8616973
                           1.0000000 0.7920883
## income
               0.4636565
                           0.7920883 1.0000000
```

LC 6.2 (Objective 1)

(LC6.2) Conduct a new exploratory data analysis with the same outcome variable y being debt but with credit_rating and age as the new explanatory variables x_1 and x_2 . Remember, this involves three things:

- Most crucially: Looking at the raw data values.
- Computing summary statistics, such as means, medians, and interquartile ranges.
- Creating data visualizations.

What can you say about the relationship between a credit card holder's debt and their credit rating and age?

Solution:

• Most crucially: Looking at the raw data values.

```
credit_ch6 %>%
  select(debt, credit_rating, age) %>%
  head()
```

```
## # A tibble: 6 x 3
##
      debt credit_rating
                            age
##
     <int>
                   <int> <int>
## 1
       333
                      283
                             34
## 2
       903
                      483
                             82
## 3
      580
                      514
                             71
## 4
       964
                      681
                             36
## 5
                      357
      331
                             68
## 6 1151
                      569
                             77
```

Computing summary statistics, such as means, medians, and interquartile ranges.

```
credit_ch6 %>%
  select(debt, credit_rating, age) %>%
  my_skim() %>%
  print()
```

```
## -- Data Summary -----
##
                         Values
## Name
                         Piped data
## Number of rows
                         400
## Number of columns
                         3
## Column type frequency:
##
   numeric
                         3
## Group variables
                         None
## -- Variable type: numeric ------
## skim_variable n_missing complete_rate mean sd p0 p25 p50 p75 p100
## 1 debt
                       0
                                  1 520. 460.
                                               0 68.8 460. 863 1999
## 2 credit_rating
                       0
                                   1 355. 155. 93 247. 344
                                                           437.
                       0
                                   1 55.7 17.2 23 41.8 56
                                                                 98
## 3 age
                                                            70
## $numeric
##
## -- Variable type: numeric ------
  skim_variable n_missing complete_rate mean
                                            sd p0 p25 p50 p75 p100
## 1 debt
                       0
                                  1 520. 460. 0 68.8 460. 863 1999
                                   1 355. 155. 93 247. 344 437.
## 2 credit_rating
                       0
                                                                982
## 3 age
                       0
                                   1 55.7 17.2 23 41.8 56
                                                            70
credit_ch6 %>%
 select(debt, credit_rating, age) %>%
 cor()
```

```
## debt credit_rating age

## debt 1.000000000 0.8636252 0.001835119

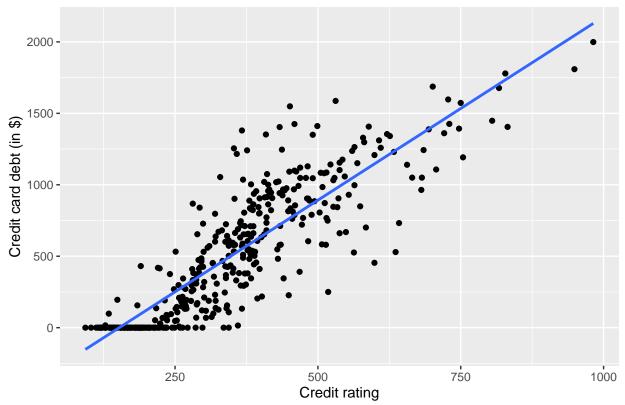
## credit_rating 0.863625161 1.0000000 0.103164996

## age 0.001835119 0.1031650 1.000000000
```

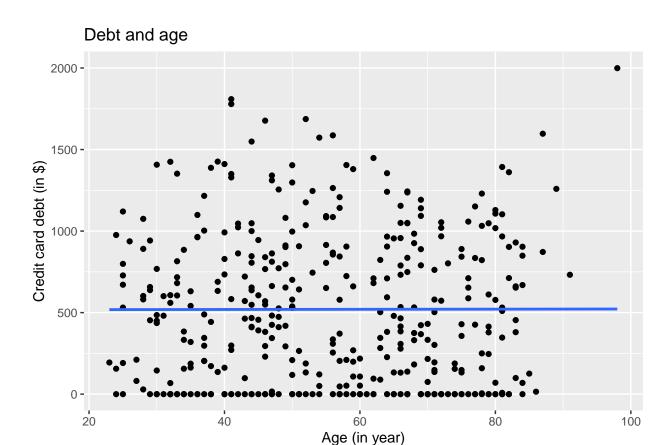
• Creating data visualizations.

```
ggplot(credit_ch6, aes(x = credit_rating, y = debt)) +
  geom_point() +
labs(
    x = "Credit rating", y = "Credit card debt (in $)",
    title = "Debt and credit rating"
) +
  geom_smooth(method = "lm", se = FALSE)
```

Debt and credit rating



```
ggplot(credit_ch6, aes(x = age, y = debt)) +
geom_point() +
labs(
    x = "Age (in year)", y = "Credit card debt (in $)",
    title = "Debt and age"
) +
geom_smooth(method = "lm", se = FALSE)
```



It seems that there is a positive relationship between one's credit rating and their debt, and very little relationship between one's age and their debt. The is a slight linear relationship between age and credit_rating.

LC 6.3 (Objective 2)

(LC6.3) Fit a new simple linear regression using $lm(debt \sim credit_rating + age, data = credit_ch6)$ where $credit_rating$ and age are the new numerical explanatory variables x_1 and x_2 . Get information about the "best-fitting" regression plane from the regression table by applying the $get_regression_table()$ function. How do the regression results match up with the results from your previous exploratory data analysis?

```
# Fit regression model:
debt_model_2 <- lm(debt ~ credit_rating + age, data = credit_ch6)</pre>
# Get regression table:
get_regression_table(debt_model_2)
## # A tibble: 3 x 7
                    estimate std_error statistic p_value lower_ci upper_ci
##
     term
     <chr>
                                                      <dbl>
##
                        <dbl>
                                  <dbl>
                                             <dbl>
                                                                <dbl>
                                                                          <dbl>
                                             -6.02
## 1 intercept
                     -270.
                                 44.8
                                                          0
                                                              -358.
                                                                        -181.
## 2 credit_rating
                         2.59
                                  0.074
                                             34.8
                                                          0
                                                                 2.45
                                                                          2.74
                                  0.668
                                             -3.52
                                                                -3.66
                                                                          -1.04
## 3 age
                        -2.35
                                                          0
```

The coefficients for both new numerical explanatory variables x_1 and x_2 , credit_rating and age, are 2.59 and -2.35 respectively, which means that debt and credit_rating are positively correlated, which matches

up with our explanatory analysis. However, debt and age are negatively correlated but in our exploratory analysis we surmised there was no relationship. When we account for credit rating, the debt tends to decrease with age, for one year increase in age, the debt on average decreases -2.35 with a credit rating held constant.

Documenting software

File creation date: 2022-06-05
R version 4.1.3 (2022-03-10)
tidyverse package version: 1.3.1
skimr package version: 2.1.4
ISLR package version: 1.4

• moderndive package version: 0.5.4