# Math 300 NTI Lesson 11

## Simple Linear Regression - Continuous x

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# **Objectives**

- 1. Explore the relationship between 2 numerical variables using summary statistics and visualizations in R. This includes using the skimr package and fitting a best fit line in a scatterplot.
- 2. Fit a linear regression model to two variables using the lm() function and interpret the output. This includes the interpretation of slope and the use of association and not cause.
- 3. Generate a table of observations, fitted values, and residuals from a linear regression object.

# Reading

Chapter 5 - 5.1

#### Lesson

Remember that you will be running this more like a lab than a lecture. You want them using R and answering questions. Have them open the notes rmd and work through it together.

Work through the learning checks LC5.1 - LC5.3.

- Regression can be used for explanatory and predictive purposes. It falls on that line between traditional statistics/econometrics and machine learning. In this course we focus on its more traditional use to interpret the relationship between predictors and a response. Math 378 is our machine learning course and expands on linear regression in this framework.
- Note the many different terms for x and y in regression. These names come from different fields. For example y is called the response, dependent variable, outcome, and output. While x is called input, predictor, independent variable, and explanatory variable. Also point out that y is numerical while x can be numerical or categorical.

- We are using new packages. The tidyverse package is a wrapper and actually loads readr, dplyr, ggplot2, and tidyr.
- In the reading, the authors' setup the problem with instructor teaching score as the response, explain why, and beauty score as the explanatory variable. What is the research question?
- $\bullet\,$  The reading introduces tilde  $\sim$  as a formula. You might want to talk about this as we use it in LC 5.1.
- The interpretation of the slope has the key phrase **average**. For a one unit change in **x**, the average value of **y** changes by the value of the slope.

#### Setup

```
library(tidyverse)
library(moderndive)
library(skimr)
library(gapminder)
```

Create the data needed for the exercises.

```
evals_ch5 <- evals %>%
  select(ID, score, bty_avg, age)
```

Let's look at 5 random rows of data.

```
set.seed(1234)
evals_ch5 %>%
  sample_n(size = 5)
```

```
## # A tibble: 5 x 4
##
        ID score bty_avg
                            age
##
     <int> <dbl>
                    <dbl> <int>
       284
             4
                     1.67
## 1
## 2
       336
            3.1
                     1.67
                             60
## 3
       406
            5
                    2.83
                             57
## 4
       101
             4.4
                     4.33
                             48
                     4.33
## 5
       111
             3.5
                             57
```

# LC 5.1 (Objective 1)

(LC5.1) Conduct a new exploratory data analysis with the same outcome variable y being score but with age as the new explanatory variable x. Remember, this involves three things:

- Looking at the raw data values.
- Computing summary statistics.
- Creating data visualizations.

What can you say about the relationship between age and teaching scores based on this exploration?

#### Solution:

• Looking at the raw data values:

```
glimpse(evals_ch5)
```

• Computing summary statistics:

my\_skim<-skim\_with(numeric = sfl(hist = NULL))</pre>

```
evals_ch5 %>%
  select(score, age) %>%
  my_skim() %>%
  print()
```

```
## -- Data Summary -----
##
                        Values
                        Piped data
## Name
## Number of rows
                        463
## Number of columns
                        2
## Column type frequency:
## numeric
## ______
## Group variables
                        None
##
## -- Variable type: numeric -----
## skim_variable n_missing complete_rate mean sd p0 p25 p50 p75 p100
## 1 score
                     0 1 4.17 0.544 2.3 3.8 4.3 4.6
## 2 age
                     0
                                1 48.4 9.80 29 42 48 57
                                                             73
## $numeric
##
## -- Variable type: numeric ------
## skim_variable n_missing complete_rate mean sd p0 p25 p50 p75 p100
## 1 score
                     0
                           1 4.17 0.544 2.3 3.8 4.3 4.6
                                                              5
                     0
                                 1 48.4 9.80 29 42
## 2 age
                                                    48 57
```

(Note that for formatting purposes, the inline histogram that is usually printed with skim() has been removed.)

• Bivariate summary:

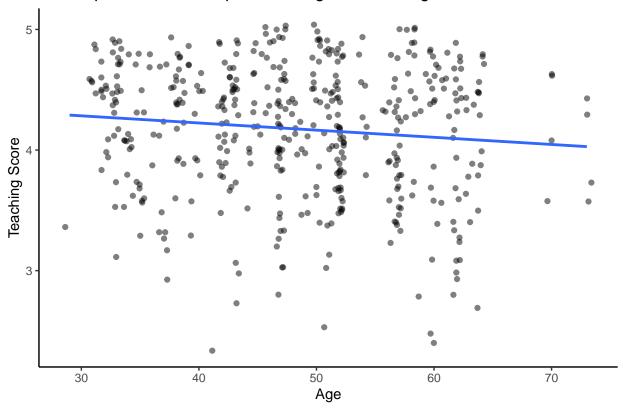
```
evals_ch5 %>%
  get_correlation(formula = score ~ age)
```

```
## # A tibble: 1 x 1
## cor
## <dbl>
## 1 -0.107
```

• Creating data visualizations:

```
ggplot(evals_ch5, aes(x = age, y = score)) +
geom_jitter(alpha=0.5) +
labs(
    x = "Age", y = "Teaching Score",
    title = "Scatterplot of relationship of teaching score and age") +
geom_smooth(method = "lm", se = FALSE) +
theme_classic()
```

# Scatterplot of relationship of teaching score and age



Based on the scatterplot, there does not appear to be a relationship between age and teaching score. If anything, there might be a slight negative linear trend. That is, as age increases, the **average** teaching score decreases slightly. Even thought the correlation coefficient is negative, it is small in absolute value and thus there may be no relationship between the variables.

#### LC 5.2 (Objective 2)

(LC5.2) Fit a new simple linear regression using lm(score ~ age, data = evals\_ch5) where age is the new explanatory variable x. Get information about the "best-fitting" line from the regression table by

applying the get\_regression\_table() function. How do the regression results match up with the results from your earlier exploratory data analysis?

#### Solution:

```
# Fit regression model:
score_age_model <- lm(score ~ age, data = evals_ch5)</pre>
```

```
# Get regression table:
get_regression_table(score_age_model)
```

```
## # A tibble: 2 x 7
##
    term
              estimate std_error statistic p_value lower_ci upper_ci
    <chr>
                <dbl>
                          <dbl>
                                    <dbl> <dbl>
                                                    <dbl>
                                    35.2
                                                    4.21
## 1 intercept
                 4.46
                          0.127
                                                             4.71
                -0.006
                          0.003
                                    -2.31 0.021 -0.011
## 2 age
                                                            -0.001
```

$$\widehat{y} = b_0 + b_1 \cdot x$$

$$\widehat{\text{score}} = b_0 + b_{\text{age}} \cdot \text{age}$$

$$= 4.462 - 0.006 \cdot \text{age}$$

For every increase of 1 year in age, there is an associated decrease of 0.006 units of the average teaching score. It matches with the results from our earlier exploratory data analysis.

#### LC 5.3 (Objective 3)

(LC5.3) Generate a data frame of the residuals of the model where you used age as the explanatory x variable.

#### Solution:

```
score_age_regression_points <- get_regression_points(score_age_model)</pre>
```

head(score\_age\_regression\_points)

```
## # A tibble: 6 x 5
##
       ID score age score_hat residual
##
    <int> <dbl> <int>
                         <dbl>
                                 <dbl>
                          4.25
## 1
       1
          4.7
                36
                                 0.452
## 2
        2 4.1
                  36
                          4.25
                                -0.148
## 3
        3 3.9 36
                          4.25
                                -0.348
## 4
        4 4.8
                  36
                          4.25
                                 0.552
        5 4.6
## 5
                  59
                          4.11
                                 0.488
## 6
        6 4.3
                  59
                          4.11
                                 0.188
```

# Documenting software

- File creation date: 2022-06-04R version 4.1.3 (2022-03-10)
- tidyverse package version: 1.3.1

skimr package version: 2.1.4gapminder package version: 0.3.0

 $\bullet$  moderndive package version: 0.5.4