# Introduction

We will again use the hate crimes data we used in Problem Set 03. The FiveThirtyEight article article about those data are in the Jan. 23, 2017 article "Higher Rates Of Hate Crimes Are Tied To Income Inequality". For this project, we will use these data to run regression models with a single **categorical** predictor (explanatory) variable **and** a single **numeric** predictor (explanatory) variable.

# Setup

First load the necessary packages

```
library(ggplot2)
library(dplyr)
library(moderndive)
library(readr)
```

Next, load the data set from where it is stored on the web:

```
hate_crimes <- read_csv("http://bit.ly/2ItxYg3")</pre>
```

You can take a glimpse at the data like so:

```
glimpse(hate_crimes)
```

```
## Rows: 51
## Columns: 9
## $ state
                                                                                    <chr> "New Mexico", "Maine", "New York", "Illinois", "Delaw~
## $ median_house_inc <chr> "low", "low", "low", "low", "high", "high", "high", "~
## $ share_pop_metro <dbl> 0.69, 0.54, 0.94, 0.90, 0.90, 1.00, 0.87, 0.86, 0.97,~
## $ hs
                                                                                    <dbl> 83, 90, 85, 86, 87, 85, 89, 90, 81, 91, 89, 89, 87, 8~
## $ hate crimes
                                                                                    <dbl> 0.295, 0.616, 0.351, 0.195, 0.323, 0.095, 0.833, 0.67~
                                                                                    <chr> "low", "lo
## $ trump_support
                                                                                    <chr> "high", "low", "low", "high", "low", "high", "high", ~
## $ unemployment
                                                                                    <chr> "low", "low", "high", "high", "high", "high", "high", ~
## $ urbanization
## $ income
                                                                                    <dbl> 46686, 51710, 54310, 54916, 57522, 58633, 58875, 5906~
```

Be sure to also examine the data in the RStudio data viewer.

A summary of the data also helps us to understand our data.

#### summary(hate\_crimes)

```
##
       state
                        median_house_inc
                                            share_pop_metro
                                                                    hs
##
    Length:51
                        Length:51
                                                   :0.3100
                                                                     :80.00
                                            Min.
                                                              Min.
##
    Class :character
                        Class :character
                                            1st Qu.:0.6300
                                                              1st Qu.:84.00
    Mode :character
                        Mode :character
                                            Median :0.7900
                                                              Median :87.00
##
##
                                            Mean
                                                   :0.7502
                                                              Mean
                                                                     :86.79
##
                                            3rd Qu.:0.8950
                                                              3rd Qu.:90.00
##
                                            Max.
                                                   :1.0000
                                                              Max.
                                                                     :92.00
##
                                                                     :3
                                                              NA's
##
                                          unemployment
                                                              urbanization
     hate_crimes
                      trump_support
```

```
##
    Min.
           :0.0670
                      Length:51
                                          Length:51
                                                              Length:51
##
    1st Qu.:0.1430
                      Class : character
                                          Class : character
                                                              Class : character
##
   Median :0.2260
                      Mode :character
                                          Mode :character
                                                              Mode :character
##
           :0.3041
   Mean
##
    3rd Qu.:0.3570
           :1.5220
##
   Max.
##
   NA's
           :4
##
        income
##
    Min.
           :35521
##
   1st Qu.:48657
   Median :54916
           :55224
##
    Mean
##
    3rd Qu.:60719
           :76165
##
   Max.
##
```

Notice that 4 states do not have data for the response variable. As a simple fix, let's remove these values. In practice, we would want to investigate the nature of why these states are missing values.

```
hate_crimes_ps4 <- hate_crimes %>%
  select(state, hs, income, urbanization) %>%
  na.omit()
```

#### Use hate\_crimes\_ps4 for all your work in this problem set.

Each case/row in these data is a state in the US. This week we will consider the response variable income, which is the numeric variable of median income of households in each state.

We will use

- A categorical explanatory variable urbanization: level of urbanization in a region
- A numerical explanatory variable hs: the percentage of adults 25 and older with a high school degree

# Income, education and urbanization

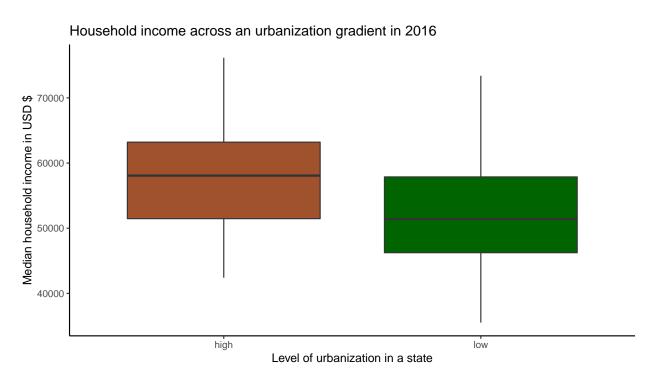
We will start by modeling the relationship between:

- y: Median household income in 2016
- $x_1$ : numerical variable percent of adults 25 and older with a high-school degree, contained in the hs variable
- $x_2$ : categorical variable level of urbanization in a state: low, or high, as contained in the variable urbanization

# Exercise 1

Create a data visualization comparing median household income at "low" and "high" levels of urbanization (you do not need to include the hs variable in this plot). Please include axis labels and title.

#### Answer:



States with a "high" level of urbanization have a higher median household income.

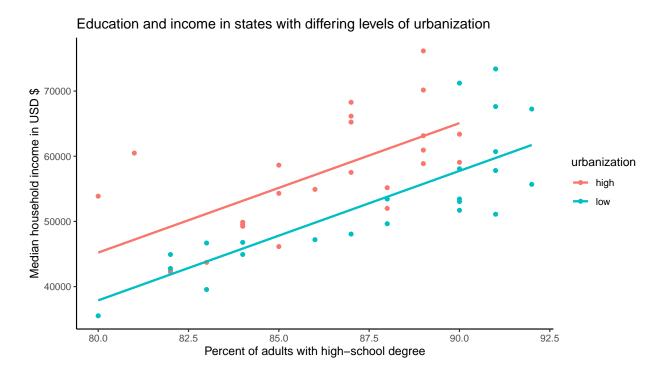
#### Exercise 2

Next, let's add the high-school degree variable into the mix by creating a scatterplot showing:

- Median household income on the y axis
- Percent of adults 25 or older with a high school degree on the x axis
- The points colored by the variable urbanization
- A line of best fit (regression line) for each level of the variable urbanization (one for "low", one for "high")

For this question, add the regression lines to the plot using the geom\_parallel\_slopes function from the moderndive package. This function will draw the regression lines based on fitting a regression model with parallel slopes (i.e., with no interaction between hs and urbanization).

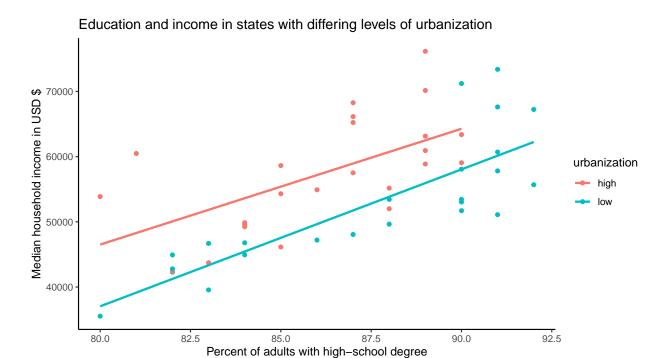
```
) +
theme_classic()
```



# Exercise 3

Now let's create a second scatterplot using the same variables, but this time draw the regression lines using <code>geom\_smooth</code>, which will allow for separate, non-parallel slopes for each urbanization group.

```
ggplot(data = hate_crimes_ps4, aes(y = income, x = hs, color = urbanization)) +
  geom_point()+
  geom_smooth(method = "lm", se = FALSE) +
  labs(
    x = "Percent of adults with high-school degree",
    y = "Median household income in USD $",
    title = "Education and income in states with differing levels of urbanization") +
  theme_classic()
```



# Exercise 4

Based on visually comparing the two models shown in Question 2 and Question 3, do you think it would be best to run a "parallel slopes" model (i.e. a model that estimates one shared slope for the two levels of urbanization), or a more complex "interaction model" (i.e. a model that estimates a separate slope for the two levels of urbanization)?

#### Answer:

The slopes do not appear to be much different, so we do not think an interaction model is warranted.

# Exercise 5

Fit the following two regression models that examine the relationship between household income (as response variable), and high-school education (hs) and urbanization as explanatory variables:

- 1. A parallel slopes model (i.e., no interaction between hs and urbanization)
- 2. A non-parallel slopes model (i.e., allow hs and urbanization to interact in your model)

Be sure to save the output from the 1m function for each model.

```
income_parallel_model <- lm(income ~ hs + urbanization, data = hate_crimes)
income_interaction_model <- lm(income ~ hs * urbanization, data = hate_crimes)</pre>
```

## Exercise 6

Use the get\_regression\_summaries function to find the unadjusted proportion of variance in income accounted for by each model, and report the value for each model

```
get_regression_summaries(income_parallel_model)
```

```
get_regression_summaries(income_interaction_model)
```

```
## # A tibble: 1 x 9
     r_squared adj_r_squared
                                    mse rmse sigma statistic p_value
                                                                              nobs
                                                                           df
##
         <dbl>
                                  <dbl> <dbl> <dbl>
                                                         <dbl>
                                                                  <dbl> <dbl> <dbl>
         0.575
                       0.546 37245066. 6103. 6374.
                                                          19.8
                                                                     0
                                                                            3
                                                                                 48
## 1
```

**Answer:** For the parallel slopes model, the proportion of variance accounted for  $(R^2)$  is .572. For the interaction model, it is .575.

### Exercise 7

Compare the **adjusted** proportion of variance account for each model. Based on this comparison, which model do you prefer? Does your preference here agree or disagree with your earlier preference based on visualizing the predictions of each model?

#### Answer:

For the parallel slopes model, the adjusted  $R^2$  is .553. For the interaction model, it is .546. Since adjusted  $R^2$  actually decreases for the more complex interaction model, we should prefer the simpler parallel slopes model.

For Exercise 8 though 10, base your answers on the model you've selected in Exercise 7.

#### Note to Instructors

Students *should* prefer the parallel slopes model, and should have said so in earlier questions. But if they don't, do not penalize them further on questions 8 through 10. For completeness, solutions for both the parallel slopes and interaction models are included for questions 8 through 10.

#### Exercise 8

What is the slope for the regression line of the states with a "high" level of urbanization? What is the intercept?

#### Answer:

#### get\_regression\_table(income\_parallel\_model)

```
## # A tibble: 3 x 7
##
                         estimate std_error statistic p_value lower_ci upper_ci
     term
##
     <chr>>
                                       <dbl>
                                                 <dbl>
                                                          <dbl>
                                                                    <dbl>
                            <dbl>
## 1 intercept
                         -113725.
                                      23553.
                                                  -4.83
                                                              0 -161163.
                                                                           -66287.
## 2 hs
                                                  7.28
                                                              0
                                                                    1437.
                                                                              2537.
                            1987.
                                        273.
## 3 urbanization: low
                           -7333.
                                       1858.
                                                 -3.95
                                                                 -11075.
                                                                             -3592.
```

• Parallel slopes: Slope is 1986.794, Intercept is -113725.193 (rounded is OK)

get\_regression\_table(income\_interaction\_model)

```
## # A tibble: 4 x 7
##
     term
                         estimate std_error statistic p_value lower_ci upper_ci
##
     <chr>
                                       <dbl>
                                                  <dbl>
                                                                    <dbl>
                            <dbl>
                                                          <dbl>
## 1 intercept
                          -95647.
                                      39938.
                                                 -2.40
                                                          0.021 -176137.
                                                                           -15158.
## 2 hs
                            1777.
                                                 3.84
                                                                     843.
                                                                             2711.
                                        463.
                          -35394.
                                                 -0.709
                                                          0.482 - 135948.
## 3 urbanization: low
                                      49894.
                                                                            65160.
## 4 hs:urbanizationlow
                             324.
                                        576.
                                                 0.563
                                                          0.576
                                                                    -836.
                                                                             1484.
```

• Interaction Model: Slope is 1777 (rounded is OK), Intercept is -95647.4

## Exercise 9

For every 1 percentage point increase of high-school educated adults in a state, what is the associated increase in the median household income?

#### Answer:

- Parallel slopes: The associated increase is the slope: \$1986
- Interaction Model: The associated increase for "low" states is the slope on hs: \$1777. For "high" states, it is \$2101

# Exercise 10

What would you predict as the median household income for a state with a **high** level of urbanization, in which 85% of adults have a high school degree? Careful with rounding!

#### Answer:

- Parallel slopes: -113725.193 + (-7333.326 \* 0) + (1986.794 \* 85) = 55152.28 (rounding OK)
- Interaction Model: -95647.4 + (-35394.00) + (1777.0 + (324 0)) \* 85 = 55,397.6 (rounding OK) Note that answers may vary substantially based on rounding

# Documenting software

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tidyverse package version: 1.3.1moderndive package version: 0.5.4