Foundations of Data Science I

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Welcome

This is a *sample* book written in **Markdown**. You can use anything that Pandoc's Markdown supports, e.g., a math equation $a^2 + b^2 = c^2$.

The $\bf bookdown$ package can be installed from CRAN or Github:

```
install.packages("bookdown")
# or the development version
# devtools::install_github("rstudio/bookdown")
```

Remember each Rmd file contains one and only one chapter, and a chapter is defined by the first-level heading #.

To compile this example to PDF, you need XeLaTeX. You are recommended to install TinyTeX (which includes XeLaTeX): https://yihui.name/tinytex/.

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Chapter 1

(PART) Data Programming

Chapter 2

Introduction to R

This lecture introduces you to basic operations when you first start using R such as navigation, the object-oriented framework, loading a package, and creating some data vectors.

2.1 Navigation

You need to know a few operations to help you maneuver the R work environment, such as listing objects (datasets and functions) that are active, changing your working directory, listing available files, and finding help.

2.1.1 Setting Your Working Directory

When you are ready to load data, R needs to know where to look for your files. You can check what is available in the current directory (i.e. folder) by asking to list all of the current files using dir().

```
dir()
```

If the file that you need is located in a different folder, you can change directories easily in R Studio by Session -> Set working director -> Choose directory (or Ctrl + Shift + H).

If you are writing a script, you want to keep track of this step so that it can be reproduced. Use the function **get.wd()** to check your current working directory, and **set.wd()** to change. You need to specify your path as an argument to this function, such as.

```
setwd( "C:/user/projects/financial model" )
```

NOTE! R uses unix style notation with forward slashes, so if you copy and paste from Windows it will look like this, with back slashes:

```
setwd( "C:\user\projects\financial model" )
```

You will need to change them around for it to work.

It is best to save all of your steps in your scripts so that the analysis can be reproduced by yourself or others. In some cases you are doing exploratory or summary work, and you may want to find a file a quickly. You can use the **file.choose()** function to open a GUI to select your file directly. This function is used as an argument inside of a load data function.

```
my.dat <- read.csv( file.choose() )</pre>
```

2.2 Commenting Code

Most computer languages have a special character that is used to "comment out" lines so that it is not run by the program. It is used for two important purposes. First, we can add text to document our functions and it will not interfere with the program. And two, we can use it to run a program while ignoring some of the code, often for debugging purposes.

The # hash tag is used for comments in R.

2.3 Help

You will use the help functions frequently to figure out what arguments and values are needed for specific functions. Because R is very customizable, you will find that many functions have several or dozens of arguments, and it is difficult to remember the correct syntax and values. But don't worry, to look them up all you need is the function name and a call for help:

```
help( dotchart ) # opens an external helpfile
```

If you just need to remind yourself which arguments are defined in a function, you can use the args() command:

```
args( dotchart )
#> function (x, labels = NULL, groups = NULL, gdata = NULL, cex = par("cex"),
#> pt.cex = cex, pch = 21, gpch = 21, bg = par("bg"), color = par("fg"),
#> gcolor = par("fg"), lcolor = "gray", xlim = range(x[is.finite(x)]),
#> main = NULL, xlab = NULL, ylab = NULL, ...)
#> NULL
```

If you can't recall a function name, you can list all of the functions from a specific package as follows:

```
help( package="stats" ) # lists all functions in stats package
```

2.4 Install Programs (packages)

When you open R by default it will launch a core set of programs, called "packages" in R speak, that are use for most data operations. To see which packages are currently active use the **search()** function.

```
search()
#> [1] ".GlobalEnv"
                            "package:bindrcpp"
                                                 "package:qqplot2"
   [4] "package:scales"
                            "package:reshape2"
                                                 "package:tidyr"
                            "package:pander"
   [7] "package:maps"
                                                 "package:dplyr"
#> [10] "package:Lahman"
                            "package:bookdown"
                                                 "package:rmarkdown"
#> [13] "package:stats"
                            "package:graphics"
                                                "package:grDevices"
                            "package:datasets"
#> [16] "package:utils"
                                                 "package:methods"
#> [19] "Autoloads"
                            "package:base"
```

These programs manage the basic data operations, run the core graphics engine, and give you basic statistical methods.

The real magic for R comes from the over 7,000 contributed packages available on the CRAN: https://cran.r-project.org/web/views/

A package consists of custom functions and datasets that are generated by users. They are *packaged* together so that they can be shared with others. A package also includes documentation that describes each function, defines all of the arguments, and documents any datasets that are included.

If you know a package name, it is easy to install. In R Studio you can select Tools -> Install Packages and a list of available packages will be generated. But it is easier to use the **install.packages()** command. We will use the Lahman Package in this course, so let's install that now.

Description This package provides the tables from Sean Lahman's Baseball Database as a set of R data.frames. It uses the data on pitching, hitting and fielding performance and other tables from 1871 through 2013, as recorded in the 2014 version of the database.

See the documentation here: https://cran.r-project.org/web/packages/Lahman/Lahman.pdf

```
install.packages( "Lahman" )
```

You will be asked to select a "mirror". In R speak this just means the server from which you will download the package (choose anything nearby). R is a community of developers and universities that create code and maintain the infrastructure. A couple of dozen universities around the world host servers that contain copies of the R packages so that they can be easily accessed everywhere.

If the package is successfully installed you will get a message similar to this:

package 'Lahman' successfully unpacked and MD5 sums checked

Once a new program is installed you can now open ("load" in R speak) the package using the library() command:

```
library( "Lahman" )
```

If you now type **search()** you can see that Lahman has been added to the list of active programs. We can now access all of the functions and data that are available in the Lahman package.

2.5 Accessing Built-In Datasets in R

One nice feature of R is that is comes with a bunch of built-in datasets that have been contributed by users are are loaded automatically. You can see the list of available datasets by typing:

```
data()
```

This will list all of the default datasets in core R packages. If you want to see all of the datasets available in installed packages as well use:

```
data( package = .packages(all.available = TRUE) )
```

2.5.1 Basic Data Operations

Let's ignore the underlying data structure right now and look at some ways that we might interact with data.

We will use the **USArrests** dataset available in the core files.

To access the data we need to load it into working memory. Anything that is active in R will be listed in the environment, which you can check using the ls() command. We will load the dataset using the data() command.

```
remove( list=ls() )

ls() # nothing currently available
#> character(0)

data( "USArrests" )

ls() # data is now avaible for use
#> [1] "USArrests"
```

Now that we have loaded a dataset, we can start to access the variables and analyze relationships. Let's get to know our dataset.

```
names ( USArrests ) # what variables do you have?
#> [1] "Murder" "Assault" "UrbanPop" "Rape"
row.names( USArrests ) # what are the obsevations (rows) in our data
#> [1] "Alabama" "Alaska" "Arizona" "Arkansas"

#> [5] "California" "Colorado" "Connecticut" "Delaware"

#> [9] "Florida" "Georgia" "Hawaii" "Idaho"

#> [13] "Illinois" "Indiana" "Iowa" "Kansas"

#> [17] "Kentucky" "Louisiana" "Maine" "Maryland"
                                                 "Minnesota" "Mississippi"
"Nebraska" "Nevada"
"New Mexico" "New York"
"Ohio" "Oklahoma"
#> [21] "Massachusetts" "Michigan"
#> [25] "Missouri" "Montana"
#> [29] "New Hampshire" "New Jersey"
#> [33] "North Carolina" "North Dakota"
#> [37] "Oregon" "Pennsylvania"
                                                  "Rhode Island" "South Carolina"
                                                  "Texas"
#> [41] "South Dakota" "Tennessee"
                                                                      "Utah"
#> [45] "Vermont" "Virginia"
                                                  "Washington"
                                                                      "West Virginia"
#> [49] "Wisconsin"
                             "Wyoming"
nrow( USArrests )
                       # how many observations are there?
#> [1] 50
dim( USArrests )
                       # a quick way to see rows and columns - the dimensions of the dataset
#> [1] 50 4
summary( USArrests ) # summary statistics of variables
                          {\it Assault} {\it UrbanPop}
         Murder
                                                                    Rape
#> Min. : 0.800 Min. : 45.0 Min. : 32.00 Min. : 7.30
#> 1st Qu.: 4.075 1st Qu.:109.0 1st Qu.:54.50 1st Qu.:15.07
```

```
Median : 7.250
                      Median :159.0
                                       Median :66.00
                                                        Median :20.10
           : 7.788
                              :170.8
                                               :65.54
                                                                :21.23
#>
    Mean
                      Mean
                                       Mean
                                                        Mean
#>
    3rd Qu.:11.250
                      3rd Qu.:249.0
                                       3rd Qu.:77.75
                                                         3rd Qu.:26.18
                                               :91.00
           :17.400
                              :337.0
                      Max.
                                                        Max.
                                                                :46.00
```

We can see that the dataset consists of four variables: Murder, Assault, UrbanPop, and Rape. We also see that our unit of analysis is the state. But where does the data come from, and how are these variables measured?

To see the documentation for a specific dataset you will need to use the help() function:

```
help( "USArrests" )
```

We get valuable information about the source and metrics:

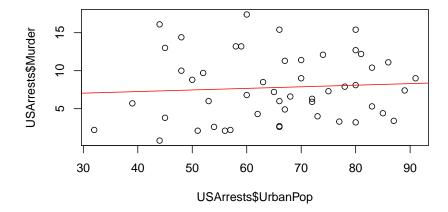
Description This data set contains statistics, in arrests per 100,000 residents for assault, murder, and rape in each of the 50 US states in 1973. Also given is the percent of the population living in urban areas.

Format A data frame with 50 observations on 4 variables.

[,1] Murder numeric Murder arrests (per 100,000) [,2] Assault numeric Assault arrests (per 100,000) [,3] UrbanPop numeric Percent urban population [,4] Rape numeric Rape arrests (per 100,000)

To access a specific variable inside of a dataset, you will use the \$ operator between the dataset name and the variable name:

```
summary( USArrests$Murder )
      Min. 1st Qu.
                    Median
                               Mean 3rd Qu.
                                               Max.
     0.800
             4.075
                     7.250
                              7.788
                                    11.250
                                             17.400
summary( USArrests$Assault )
#>
      Min. 1st Qu.
                    Median
                               Mean 3rd Qu.
                                               Max.
                     159.0
      45.0
             109.0
                              170.8
                                      249.0
                                              337.0
# Is there a relationship between urban density and crime?
plot( USArrests$UrbanPop, USArrests$Murder )
abline( lm( USArrests$Murder ~ USArrests$UrbanPop ), col="red" )
```



2.5.2 Using the Lahman Data

Let's take a look at some of the data available in the Lahman package.

```
data( package = "Lahman" )
# Data sets in package 'Lahman':
# AllstarFull
                                          AllstarFull table
# Appearances
                                          Appearances table
# AwardsManagers
                                          AwardsManagers table
# AwardsPlayers
                                          AwardsPlayers table
# AwardsShareManagers
                                          AwardsShareManagers table
# AwardsSharePlayers
                                          AwardsSharePlayers table
# Batting
                                          Batting table
# BattingPost
                                          BattingPost table
# CollegePlaying
                                          CollegePlaying table
# Fielding
                                          Fielding table
# FieldingOF
                                          FieldingOF table
# FieldingPost
                                          FieldingPost data
# HallOfFame
                                          Hall of Fame Voting Data
# LahmanData
                                          Lahman Datasets
# Managers
                                          Managers table
# ManagersHalf
                                          ManagersHalf table
                                          Master table
# Master
# Pitching
                                          Pitching table
# PitchingPost
                                          PitchingPost table
# Salaries
                                          Salaries table
# Schools
                                          Schools table
# SeriesPost
                                          SeriesPost table
# Teams
                                          Teams table
# TeamsFranchises
                                          TeamFranchises table
# TeamsHalf
                                          TeamsHalf table
# battingLabels
                                          Variable Labels
# fieldingLabels
                                          Variable Labels
                                          Variable Labels
# pitchingLabels
```

We see that we have lots of datasets to choose from here. I will use the Master dataset, which is a list of all of the Major League Baseball players over the past century, and their personal information.

```
library( Lahman )
data( Master )
names( Master )
#> [1] "playerID"
                      "birthYear"
                                     "birthMonth"
                                                    "birthDay"
                                   "birthCity"
#> [5] "birthCountry" "birthState"
                                                    "deathYear"
#> [9] "deathMonth" "deathDay"
                                     "deathCountry" "deathState"
#> [13] "deathCity"
                      "nameFirst"
                                     "nameLast" "nameGiven"
                    "height"
"finalGame"
                                     "bats"
                                                    "throws"
#> [17] "weight"
                                     "retroID"
#> [21] "debut"
                                                    "bbrefID"
#> [25] "deathDate" "birthDate"
nrow( Master ) # 18,354 players included
#> [1] 19105
```

```
summary( Master )
#> playerID
                     birthYear birthMonth birthDay
                Min. :1820 Min. : 1.000 Min. : 1.00
#> Length:19105
#> Class:character 1st Qu.:1895 1st Qu.: 4.000 1st Qu.: 8.00
#> Mode :character Median :1937 Median : 7.000 Median :16.00
                    Mean :1931 Mean : 6.629 Mean :15.61
#>
                    3rd Qu.:1969 3rd Qu.:10.000 3rd Qu.:23.00
#>
                   Max. :1996 Max. :12.000 Max. :31.00
                   NA's :132 NA's :302 NA's :449
#>
#> birthCountry birthState birthCity deathYear
#> Length:19105 Length:19105 Min. :1872
#> Class: character Class: character Class: character 1st Qu.:1942
#> Mode :character Mode :character Median :1967
                                                      Mean :1964
#>
                                                      3rd Qu.:1990
#>
                                                      Max. :2017
                                                      NA's :9664
#>
    deathMonth deathDay deathCountry
#>
                                                 {\it deathState}
#> Min. : 1.000 Min. : 1.00 Length:19105 Length:19105
\# 1st Qu.: 3.000 1st Qu.: 8.00 Class :character Class :character
#> Median : 6.000 Median :15.00 Mode :character Mode :character
#> Mean : 6.484 Mean :15.57
#> 3rd Qu.:10.000 3rd Qu.:23.00
#> Max. :12.000 Max. :31.00
#> NA's :9665 NA's :9666
\#> deathCity nameFirst nameLast \#> Length:19105 Length:19105 Length:19105
#> Class :character Class :character Class :character
#> Mode :character Mode :character Mode :character
#>
#>
#>
#>
#> nameGiven weight height bats 
#> Length: 19105 Min. : 65.0 Min. : 43.00 B : 1175
#> Class:character 1st Qu.:170.0 1st Qu.:71.00 L : 4957
#> Mode :character Median :185.0 Median :72.00 R :11788
                   Mean :186.4 Mean :72.27 NA's: 1185
#>
#>
                    3rd Qu.:200.0 3rd Qu.:74.00
                    Max. :320.0 Max. :83.00
#>
#>
                   NA's :854 NA's :785
#> throws debut finalGame retroID 
#> L : 3653 Length:19105 Length:19105 Length:19105
#> R :14472 Class :character Class :character Class :character
\#>S : 1 Mode :character Mode :character Mode :character
#> NA's: 979
#>
#>
#>
                     deathDate birthDate
#>
   bbrefID
#> Length:19105 Min. :1872-03-17 Min. :1820-04-17
\#> Class: character 1st Qu.:1942-06-05 1st Qu.:1896-11-21
#> Mode :character Median :1967-03-06 Median :1939-01-01
```

```
#>
                                :1964-10-11
                                               Mean
                                                       :1933-03-08
#>
                         3rd Qu.:1990-09-22
                                                3rd Qu.:1970-04-02
                                                        :1996-08-12
#>
                         Max.
                                :2017-02-19
                                                Max.
                                 :9666
                                                NA's
#>
                         NA's
                                                        :449
```

We can use **help(Master)** to get information about the dataset, including a data dictionary.

```
help( Master )
```

2.6 MASTER TABLE

Description

Master table - Player names, DOB, and biographical info. This file is to be used to get details about players listed in the Batting, Pitching, and other files where players are identified only by playerID.

Usage

data(Master)

Format

A data frame with 19105 observations on the following 26 variables.

- playerID: A unique code asssigned to each player. The playerID links the data in this file with records on players in the other files.
- birthYear: Year player was born
- birthMonth: Month player was born
- birthDay: Day player was born
- birthCountry: Country where player was born
- birthState: State where player was born
- birthCity: City where player was born
- deathYear: Year player died
- deathMonth: Month player died
- deathDay: Day player died
- deathCountry: Country where player died
- deathState: State where player died
- deathCity: City where player died
- nameFirst: Player's first name
- nameLast: Player's last name
- nameGiven: Player's given name (typically first and middle)
- weight: Player's weight in pounds
- height: Player's height in inches
- bats: a factor: Player's batting hand (left (L), right (R), or both (B))
- throws: a factor: Player's throwing hand (left(L) or right(R))
- **debut**: Date that player made first major league appearance
- finalGame: Date that player made first major league appearance (blank if still active)
- retroID: ID used by retrosheet, http://www.retrosheet.org/
- bbrefID: ID used by Baseball Reference website, http://www.baseball-reference.com/
- birthDate: Player's birthdate, in as.Date format
- deathDate: Player's deathdate, in as.Date format

Details

debut, finalGame were converted from character strings with as.Date.

Source

Lahman, S. (2016) Lahman's Baseball Database, 1871-2015, 2015 version, http://www.seanlahman.com/baseball-archive/statistics/

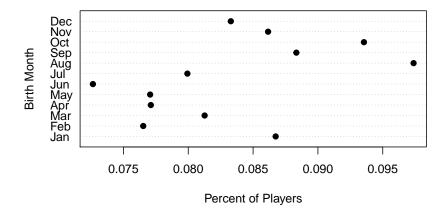
2.6.1 Example Analysis

Perhaps I am curious about some of the data. I see that we have information on the birth month of professional baseball players. If you have read Malcolm Gladwell's book *Outliers* you know there is an interesting cumulative advantage phenomenon that can occur with atheletes as they are young. If you are born near the end of the cutoff, you are on average six months older than other players in your league, and therefore slightly larger physically and more coordinated on average. Six months does not sound like much, but the slight size and coordination advantage means more playing time, which also improves skill. Over time, this small difference accumulates so that those lucky enough to be born near the cutoff become the best players.

Gladwell looked at studies of hockey. Do we see this in baseball?

```
table( Master$birthMonth )
#>
#> 1 2 3 4 5 6 7 8 9 10 11 12
#> 1631 1439 1528 1450 1449 1366 1503 1831 1661 1759 1620 1566

tab <- prop.table( table( Master$birthMonth ) )
names(tab) <- c("Jan", "Feb", "Mar", "Apr", "May", "Jun", "Jul", "Aug", "Sep", "Oct", "Nov", "Dec")
dotchart( tab, pch=19, xlab = "Percent of Players", ylab = "Birth Month" )</pre>
```



Chapter 3

Data Structures

3.1 Vectors

Vectors are the building blocks of data programming in R, so they are extremely important concepts.

Very loosely speaking a vector is a set of numbers or words. For example, [1, 2, 3] or [apple, orange, pear]. In social science, a vector is a variable in a dataset.

You will spend a lot of time creating data vectors, transforming variables, generating subsets, cleaning data, and adding new observations. These are all accomplished through operators (commands) that act on vectors.

There are four primary vector types ("classes") in R:

Class	Description
numeric character	Typical variable of only numbers A vector of letters or words, always enclosed with quotes
factor	Categories which represent groups, like treatment and control
logical	A vector of TRUE and FALSE to designate which observations fit a criteria

Each vector or dataset has a "class" that tells R the data type.

These different vectors can be combined into three different types of datasets (data frames, matrices, and lists), which will be discussed below.

```
x1 <- c(167,185,119,142)
x2 <- c("adam","jamal","linda","sriti")
x3 <- factor( c("male","male","female","female") )
x4 <- c( "treatment","control","treatment","control" )
x5 <- x4 == "treatment"
dat <- data.frame( name=x2, sex=x3, treat=x4, is.treat=x5, strength=x1 )</pre>
```

sex	treat	is.treat	strength
male	treatment	TRUE	167
$_{\mathrm{male}}$	$\operatorname{control}$	FALSE	185
female	treatment	TRUE	119
female	$\operatorname{control}$	FALSE	142
	male male female	male treatment male control female treatment	male treatment TRUE male control FALSE female treatment TRUE

R keeps track of the data type of each object:

```
class( x1 ) # c(167,185,119,142)
#> [1] "numeric"
class( x2 ) # c("adam", "jamal", "linda", "sriti")
#> [1] "character"
class( x3 ) # factor( c("male", "male", "female", "female") )
#> [1] "factor"
class( x5 ) # c( "treatment", "control", "treatment", "control" )
#> [1] "logical"
class( dat ) # data.frame( name=x2, sex=x3, treat=x4, is.treat=x5, strength=x1 )
#> [1] "data.frame"
```

We often need to know how many elements belong to a vector, which we find with the length() function.

```
x1
#> [1] 167 185 119 142
length( x1 )
#> [1] 4
```

3.2 Casting

You can easily move from one data type to another by *casting* a specific type as another type:

```
x <- 1:5

x
#> [1] 1 2 3 4 5

as.character(x)
#> [1] "1" "2" "3" "4" "5"

y <- c(TRUE, FALSE, TRUE, TRUE, FALSE)

y
#> [1] TRUE FALSE TRUE TRUE FALSE

as.numeric( y )
#> [1] 1 0 1 1 0

as.character( y )
#> [1] "TRUE" "FALSE" "TRUE" "TRUE" "FALSE"
```

But in some cases it might not make sense to cast one variable type as another.

```
z <- c("a", "b", "c")

z
#> [1] "a" "b" "c"

as.numeric( z )
#> [1] NA NA NA
```

Casting will often be induced when you try to combine different types of data. For example, when you add a character element to a numeric vector, the whole vector will be cast as a character vector.

```
x10 <- 1:5

x10
#> [1] 1 2 3 4 5

# a vector can only have one data type

x11 <- c( x10, "a")

x11 # all numbers silently recast as characters
#> [1] "1" "2" "3" "4" "5" "a"
```

When you read data in from outside sources, the input functions often will cast numeric vectors as factors if they contain a low number of elements. See the section on factors below for special instrucctions on moving from factors to numeric vectors.

3.3 The Combine Function

We often need to combine several elements into a single vector, or two vectors to form one. This is done using the c() function.

```
c(1,2,3)
#> [1] 1 2 3

c("a","b","c")
#> [1] "a" "b" "c"

x <- 1:5

y <- 10:15

z <- c(x,y)

z
#> [1] 1 2 3 4 5 10 11 12 13 14 15

c(z,"a") # combining data types
#> [1] "1" "2" "3" "4" "5" "10" "11" "12" "13" "14" "15" "a"
```

3.4 Numeric Vectors

There are some specific things to note about each vector type.

Math operators will only work on numeric vectors.

Note that if we try to run this mathematic function we get an error:

```
sum( x2 ) # Error in sum(x2) : invalid 'type' (character) of argument
```

Many functions in R are sensitive to the data type of vectors. Mathematical functions, for example, do not make sense when applied to text (character vectors). In many cases R will give an error. In some cases R will silently re-cast the variable, then perform the operation. Be watchful for when silent re-casting occurs because it might have unwanted side effects, such as deleting data or re-coding group levels in the wrong way.

3.4.1 Integers Are Simple Numeric Vectors

The integer vector is a special type of numeric vector. It is used to save memory since integers require less space than numbers that contain decimals points (you need to allocate space for the numbers to the left and the numbers to the right of the decimal). Google "computer memory allocation" if you are interested in the specifics.

If you are doing advanced programming you will be more sensitive to memory allocation and the speed of your code, but in the intro class we will not differentiate between the two types of number vectors. In *most* cases they result in the same results, unless you are doing advanced numerical analysis where rounding errors matter.

```
n <- 1:5

n
#> [1] 1 2 3 4 5

class( n )
#> [1] "integer"

n[ 2 ] <- 2.01

n # all elements converted to decimals
#> [1] 1.00 2.01 3.00 4.00 5.00

class( n )
#> [1] "numeric"
```

3.5 Character Vectors

The most important rule to remember with this data type: when creating character vectors, all text must be enclosed by quotation marks.

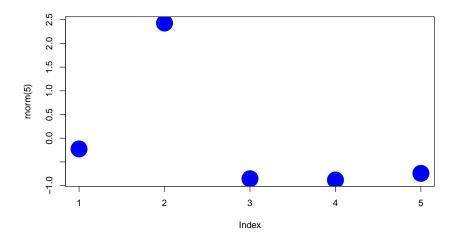
```
c( "a", "b", "c" )  # this works
#> [1] "a" "b" "c"

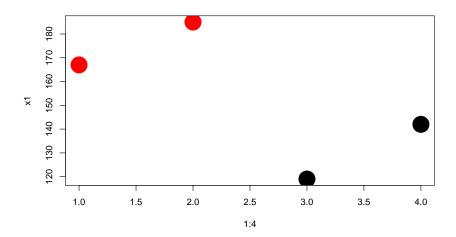
# c( a, b, c )  # this doesn't work
# Error: object 'a' not found
```

When you type characters surrounded by quotes then R knows you are creating new text ("strings" in programming speak). When you type characters that are not surrounded by quotes, R thinks that you are looking for an object in the environment, like the variables we have already created. It gets confused when it doesn't find the object that you typed.

In generate, you will use quotes when you are creating character vectors, and for arguments in functions. You do not use quotes when you are referencing an active object.

```
# these are all of the active objects
ls()
#> [1] "dat"
                    "Master"
                                "n"
                                            "tab"
                                                        "USArrests"
#> [6] "x"
                                                        "x2"
                    "x1"
                                "x10"
                                            "x11"
#> [11] "x3"
                    "x4"
                                "x5"
#> [1] "x1"
x1
#> [1] 167 185 119 142
plot( rnorm(5), col="blue", pch=19, cex=4 ) # text used for color argument, use quotes
# what if we want colors that represent groups in our data
plot( 1:4, x1, col=x3, pch=19, cex=4 )
                                       # object used for color argument, no quotes
```





Recall that x3 is the sex of study participants, so the different colors represent the different genders in the study.

3.6 Logical Vectors

Logical vectors are collections of a set of TRUE and FALSE statements.

Logical statements allow us to define groups based upon criteria, then decide whether observations belong to the group. See the section on **operators** below for a complete list of logical statements.

Logical vectors are important because organizing data into these sets is what drives all of the advanced data analytics (set theory is at the basis of mathematics and computer science).

```
dat
#>
                      treat is.treat strength
                                 TRUE
                                           167
#> 1
     adam
             male treatment
#> 2 jamal
             male
                    control
                                FALSE
                                           185
#> 3 linda female treatment
                                TRUE
                                           119
#> 4 sriti female
                                FALSE
                    control
                                           142
dat$name == "sriti"
#> [1] FALSE FALSE FALSE TRUE
dat$sex == "male"
#> [1] TRUE TRUE FALSE FALSE
dat$strength > 180
#> [1] FALSE TRUE FALSE FALSE
```

Typically logical vectors are used in combination with subset operators to identify specific groups in the data.

```
dat
#>
                       treat is.treat strength
      name
              sex
#> 1
      adam
                                  TRUE
                                             167
             male treatment
#> 2 jamal
                                 FALSE
                                             185
             male
                     control
#> 3 linda female treatment
                                  TRUE
                                             119
```

```
#> 4 sriti female control FALSE 142

# isolate data on all of the females in the dataset

dat[ dat$sex == "female" , ]

#> name sex treat is.treat strength

#> 3 linda female treatment TRUE 119

#> 4 sriti female control FALSE 142
```

When defining logical vectors, you can use the abbreviated versions of T for TRUE and F for FALSE.

```
z1 <- c(T,T,F,T,F,F)

z1
#> [1] TRUE TRUE FALSE TRUE FALSE FALSE
```

Note how NAs affect complex logical statements:

```
TRUE & TRUE

#> [1] TRUE

TRUE & FALSE

#> [1] FALSE

TRUE & NA

#> [1] NA

FALSE & NA

#> [1] FALSE
```

If one condition is TRUE, and another is NA, R does not want to throw out the data because the state of the missing value is unclear. As a result, it will preserve the observation, but it will replace all of the data with missing values:

```
dat
#>
                     treat is.treat strength
      name
             sex
#> 1 adam male treatment
                              TRUE
                                         167
#> 2 jamal male control
                              FALSE
                                         185
#> 3 linda female treatment
                              TRUE
                                         119
#> 4 sriti female
                   control
                              FALSE
                                         142
keep.these \leftarrow c(T,F,NA,F)
dat[ keep.these , ]
     name sex
                   treat is.treat strength
#> 1 adam male treatment
                             TRUE
                                       167
#> NA <NA> <NA> <NA>
                            NA
                                      NA
```

To remove these rows, replace all NAs in your selector vector with FALSE:

```
keep.these[ is.na(keep.these) ] <- FALSE

dat[ keep.these , ]
#> name sex treat is.treat strength
#> 1 adam male treatment TRUE 167
```

3.7 Factors

When there are categorical variables within our data, or groups, then we use a special vector to keep track of these groups. We could just use numbers (1=female, 0=male) or characters ("male", "female"), but factors are useful for two reasons.

First, it saves memory. Text is very "expensive" in terms of memory allocation and processing speed, so using simpler data structure makes R faster.

Second, when a variable is set as a factor, R recognizes that it represents a group and it can deploy object-oriented functionality. When you use a factor in analysis, R knows that you want to split the analysis up by groups.

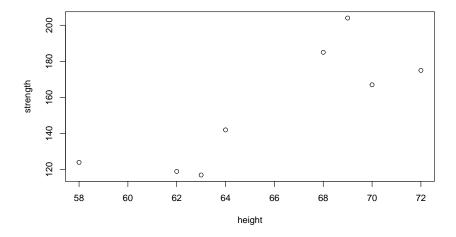
```
height <- c( 70, 68, 62, 64, 72, 69, 58, 63 )

strength <- c(167,185,119,142,175,204,124,117)

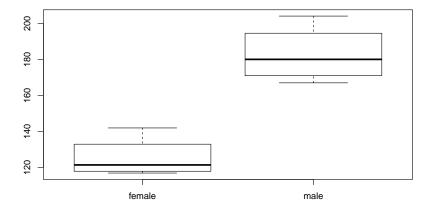
sex <- factor( c("male", "male", "female", "female", "male", "female", "female") )

plot( height, strength )  # simple scatter plot

plot( sex, strength )  # box and whisker plot
```



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Factors are more memory efficient than character vectors because they store the underlying data as a numeric vector instead of a categorical (text) vector. Each group in the data is assigned a number, and when printing items the program only has to remember which group corresponds to which number:

```
sex
#> [1] male male female female male male female female
#> Levels: female male

as.numeric( sex )
#> [1] 2 2 1 1 2 2 1 1

# male = 2
# female = 1
```

If you print a factor, the computer just replaces each category designation with its name (2 would be replaced with "male" in this example). These replacements can be done in real time without clogging the memory of your computer as they don't need to be saved.

In some instances a categorical variable might be represented by numbers. For example, grades 9-12 for high school kids. The **very important** rule to remember with factors is you can't move directly from the factor to numeric using the **as.numeric()** casting function. This will give you the underlying data structure, but will not give you the category names. To get these, you need the **as.character** casting function.

```
grades <- sample( x=9:12, size=10, replace=T )

grades
#> [1] 10 9 11 9 9 12 12 12 9 9

grades <- as.factor( grades )

grades
#> [1] 10 9 11 9 9 12 12 12 9 9

#> Levels: 9 10 11 12

as.numeric( grades )
#> [1] 2 1 3 1 1 4 4 4 1 1

as.character( grades )
```

```
#> [1] "10" "9" "11" "9" "9" "12" "12" "12" "9" "9"

# to get back to the original numeric vector

as.numeric( as.character( grades ))
#> [1] 10 9 11 9 9 12 12 12 9 9
```

Note that when subsetting a factor, it will retain all of the original levels, even when they are not in use.

In this example, there are 37 teams in the Lahman dataset (some of them defunct) and 16 teams in the National League in 2002. But after applying the year and league subsets you will still have 37 levels.

```
# there are only 16 teams in the NL in 2002

sals.2002 <- Salaries [Salaries$yearID=="2002", ]
nl.sals <- sals.2002 [ sals.2002$lgID == "NL",]
levels( nl.sals$teamID )

#> [1] "ANA" "ARI" "ATL" "BAL" "BOS" "CAL" "CHA" "CHC" "CHN" "CHW" "CIN"
#> [12] "CLE" "COL" "DET" "FLO" "HOU" "KCA" "KCR" "LAA" "LAD" "LAN" "MIA"
#> [23] "MIL" "MIN" "ML4" "MON" "NYA" "NYM" "NYN" "NYY" "OAK" "PHI" "PIT"
#> [34] "SDN" "SDP" "SEA" "SFG" "SFN" "SLN" "STL" "TBA" "TBR" "TEX" "TOR"
#> [45] "WAS" "WSN"
```

After applying a subset, in order to remove the unused factor levels you need to apply either droplevels(), or else recast your factor as a new factor.

For example:

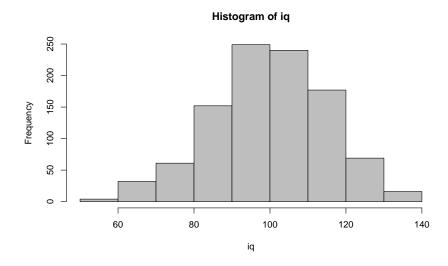
```
sals.2002 <- Salaries [Salaries$yearID=="2002", ]
nl.sals <- sals.2002 [ sals.2002$lgID == "NL",]
levels( nl.sals$teamID )
#> [1] "ANA" "ARI" "ATL" "BAL" "BOS" "CAL" "CHA" "CHC" "CHN" "CHW" "CIN"
#> [12] "CLE" "COL" "DET" "FLO" "HOU" "KCA" "KCR" "LAA" "LAD" "LAN" "MIA"
#> [23] "MIL" "MIN" "ML4" "MON" "NYA" "NYM" "NYN" "NYY" "OAK" "PHI" "PIT"
#> [34] "SDN" "SDP" "SEA" "SFG" "SFN" "SLN" "STL" "TBA" "TBR" "TEX" "TOR"
#> [45] "WAS" "WSN"
# fix in one of two equivalent ways:
# nl.sals$teamID <- droplevels( nl.sals$teamID )</pre>
# nl.sals$teamID <- factor( nl.sals$teamID )</pre>
levels( nl.sals$teamID )
#> [1] "ANA" "ARI" "ATL" "BAL" "BOS" "CAL" "CHA" "CHC" "CHN" "CHW" "CIN"
#> [12] "CLE" "COL" "DET" "FLO" "HOU" "KCA" "KCR" "LAA" "LAD" "LAN" "MIA"
#> [23] "MIL" "MIN" "ML4" "MON" "NYA" "NYM" "NYN" "NYY" "OAK" "PHI" "PIT"
#> [34] "SDN" "SDP" "SEA" "SFG" "SFN" "SLN" "STL" "TBA" "TBR" "TEX" "TOR"
#> [45] "WAS" "WSN"
nl.sals$teamID <- droplevels( nl.sals$teamID )</pre>
levels( nl.sals$teamID )
#> [1] "ARI" "ATL" "CHN" "CIN" "COL" "FLO" "HOU" "LAN" "MIL" "MON" "NYN"
#> [12] "PHI" "PIT" "SDN" "SFN" "SLN"
```

3.8 Generating Vectors

You will often need to generate vectors for data transformations or simulations. Here are the most common functions that will be helpful.

```
# repeat a number, or series of numbers
rep( x=9, times=5 )
#> [1] 9 9 9 9 9
rep(x=c(5,7), times=5)
#> [1] 5 7 5 7 5 7 5 7 5 7
rep(x=c(5,7), each=5)
#> [1] 5 5 5 5 5 7 7 7 7 7
rep( x=c("treatment","control"), each=5 ) # also works to create categories
#> [1] "treatment" "treatment" "treatment" "treatment"
#> [6] "control" "control" "control" "control"
# create a sequence of numbers
seq( from=1, to=15, by=1 )
#> [1] 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15
seq( from=1, to=15, by=3 )
#> [1] 1 4 7 10 13
1:15  # shorthand if by=1
#> [1] 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15
# create a random sample
hat <- c("a","b","c","b","f")
sample( x=hat, size=3, replace=FALSE )
#> [1] "c" "a" "b"
sample( x=hat, size=3, replace=FALSE )
#> [1] "b" "b" "a"
sample( x=hat, size=3, replace=FALSE )
#> [1] "b" "a" "c"
# for multiple samples use replacement
sample( x=hat, size=10, replace=TRUE )
#> [1] "a" "c" "c" "b" "c" "b" "c" "b" "a" "b"
```

```
# create data that follows a normal curve
iq <- rnorm( n=1000, mean=100, sd=15 )
hist( iq, col="gray" )</pre>
```



Chapter 4

Operators

Logical operators are the most basic type of data programming and the core of many types of data analysis. Most of the time we are not conducting fancy statistics, we just want to identify members of a group (print all of the females from the study), or describe things that belong to a subset of the data (compare the average price of houses with garages to houses without garages).

In order to accomplish these simple tasks we need to use logic statements. A logic statement answers the question, does an observation belong to a group.

Many times groups are simple. Show me all of the professions that make over \$100k a year, for example.

Sometimes groups are complex. Identify the African American children from a specific zip code in Chicago that live in households with single mothers.

You will use nine basic logical operators:

Operator	Description
<	less than
<=	less than or equal to
>	greater than
>=	greater than or equal to
==	exactly equal to
!=	not equal to
$x \mid y$	x OR y
x & y	x AND y
!	opposite of

Logical operators create logical vectors, a vector that contains only TRUE or FALSE. The TRUE means that the observation belongs to the group, FALSE means it does not.

```
x1 <- c(7,9,1,2)
x2 <- c("male", "male", "female", "female")
x3 <- c("treatment", "control", "treatment", "control")
x1 > 7
#> [1] FALSE TRUE FALSE FALSE
```

```
x1 >= 7
#> [1] TRUE TRUE FALSE FALSE

x1 == 9
#> [1] FALSE TRUE FALSE FALSE

x1 = 9 # don't use a single equals operator! it overwrites your variable

x1
#> [1] 9

x1 <- c(7,9,1,2)

x1 == 9 | x1 == 1
#> [1] FALSE TRUE TRUE FALSE

# x2 == male # this will not work because male is not enclosed with quotes

x2 == "female"
#> [1] FALSE FALSE TRUE TRUE

x2 == "female" & x3 == "treatment"
#> [1] FALSE FALSE TRUE FALSE
```

Note that we use operators to create logical vectors where TRUE designates observation that belong to the defined group, and FALSE designates observations outside the group. We use these logical vectors in three ways:

(1) We can create a selector variable that is used for subsets. When a logical vector is passed to the subset function it will keep all observations with a TRUE value, and drop observations with a FALSE value.

```
x1
#> [1] 7 9 1 2

x1 > 5
#> [1] TRUE TRUE FALSE FALSE

keep.these <- x1 > 5

x1[ keep.these ]
#> [1] 7 9

# you can create a selector variable with one variable, and apply it to another

x2[ keep.these ] # sex of observations where x1 > 5
#> [1] "male" "male"
```

(2) Logical vectors give us an easy way to count things within defined groups.

We can apply a sum() function to a logical vector, and the result will be a tally of all of the TRUE cases.

```
# how many females do we have in our study?
sum( x2 == "female" )
#> [1] 2
```

```
# how many females do we have in our treatment group?
sum( x2 == "female" & x3 == "treatment" )
#> [1] 1
```

(3) We use selector variables to replace observations with new values using the assignment operator. This is similar to a find and replace operation.

```
x7 <- c( "mole", "mouse", "shrew", "mouse", "rat", "shrew")
# the lab assistant incorrectly identified the shrews
x7
#> [1] "mole" "mouse" "shrew" "mouse" "rat" "shrew"
x7[ x7 == "shrew" ] <- "possum"
x7
#> [1] "mole" "mouse" "possum" "mouse" "rat" "possum"

# we don't know if linda received the treatment
x3 <- c("adam", "jamal", "linda", "sriti")
x4 <- c( "treatment", "control", "treatment", "control")
x4[ x3 == "linda" ] <- NA
x4
#> [1] "treatment" "control" NA "control"
```

The ! operator is a special case, where it is not used to define a new logical vector, but rather it swaps the values of an existing logical vector.

```
x1
#> [1] 7 9 1 2
these <- x1 > 5
these
#> [1] TRUE TRUE FALSE FALSE
! these
#> [1] FALSE FALSE TRUE TRUE
! TRUE
! TRUE
#> [1] FALSE
```

4.1 Datasets

When we combine multiple vectors together, we now have a dataset. There are three main types that we will use in this class.

Class	Description
data frame matrix list	A typical data set comprised of several variables A data set comprised of only numbers, used for matrix math The grab bag of data structures - several vectors held together

4.1.1 Data Frames

The most familiar spreadsheet-type data structure is called a data frame in R. It consists of rows, which represent observations, and columns, which represent variables.

```
data( USArrests )
dim( USArrests )
                   # number of rows by number of columns
#> [1] 50 4
names( USArrests )
                     # variable names or column names
                  "Assault" "UrbanPop" "Rape"
#> [1] "Murder"
row.names( USArrests )
#> [1] "Alabama"
                          "Alaska"
                                            "Arizona"
                                                             "Arkansas"
    [5] "California"
                          "Colorado"
                                            "Connecticut"
                                                             "Delaware"
  [9] "Florida"
                          "Georgia"
                                           "Hawaii"
                                                             "Idaho"
#> [13] "Illinois"
                          "Indiana"
                                           "Iowa"
                                                             "Kansas"
#> [17] "Kentucky"
                          "Louisiana"
                                           "Maine"
                                                             "Maryland"
#> [21] "Massachusetts"
                         "Michigan"
                                            "Minnesota"
                                                             "Mississippi"
#> [25] "Missouri"
                          "Montana"
                                           "Nebraska"
                                                             "Nevada"
#> [29] "New Hampshire"
                         "New Jersey"
                                           "New Mexico"
                                                             "New York"
                                            "Ohio"
#> [33] "North Carolina" "North Dakota"
                                                             "Oklahoma"
                                            "Rhode Island"
#> [37] "Oregon"
                          "Pennsylvania"
                                                             "South Carolina"
                                           "Texas"
#> [41] "South Dakota"
                          "Tennessee"
                                                             "Utah"
#> [45] "Vermont"
                          "Virginia"
                                            "Washington"
                                                             "West Virginia"
#> [49] "Wisconsin"
                          "Wyoming"
head( USArrests ) # print first six rows of the data
              Murder Assault UrbanPop Rape
#> Alabama
                         236
                                    58 21.2
                13.2
                10.0
#> Alaska
                          263
                                    48 44.5
#> Arizona
                 8.1
                         294
                                    80 31.0
#> Arkansas
                 8.8
                                    50 19.5
                          190
#> California
                 9.0
                         276
                                    91 40.6
#> Colorado
                 7.9
                                    78 38.7
                          204
```

4.1.2 Matrices

A matrix is also a rectangular data object that consists of collections of vectors, but it is special in the sense that it only has numeric vectors and no variable names.

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```
mat <- matrix( 1:20, nrow=5 )</pre>
mat
       [,1] [,2] [,3] [,4]
#> [1,]
        1
               6
                   11
#> [2,]
          2
               7
                   12
                       17
#> [3,] 3
             8
                 13
                       18
#> [4,] 4
             9
                 14
                       19
#> [5,] 5
              10 15
                       20
names( mat )
#> NULL
dim( mat )
#> [1] 5 4
as.data.frame( mat ) # creates variable names
#> V1 V2 V3 V4
#> 1 1 6 11 16
#> 2 2 7 12 17
#> 3 3 8 13 18
#> 4 4 9 14 19
#> 5 5 10 15 20
```

These are used almost exclusively for matrix algebra operations, which are fundamental to mathematical statistics. We will not use matrices in this course.

4.1.3 Lists

The list is the most flexible data structure. It is created by sticking a bunch of unrelated vectors or datasets together. For example, when you run a regression you generate a bunch of interesting information. This information is saved as a list.

```
x < -1:100
y \leftarrow 2*x + rnorm(100, 0, 10)
m.01 <- lm(y ~x)
names(m.01)
#> [1] "coefficients" "residuals"
                                    "effects"
                                                   "rank"
  [5] "fitted.values" "assign"
                                    "qr"
                                                   "df.residual"
  [9] "xlevels"
                     "call"
                                    "terms"
                                                   "model"
m.01$coefficients
#> (Intercept)
#> -0.5043794
              1.9985577
m.01$residuals
                                3
       1
                      2
                                                                  6
#>
   -7.3559049
                          2.6877683
                                     2.3878862
                                                1.6302649
                                                          -7.9711619
                          9
#>
           7
                8
                                     10
                                                11
                                                                 12
   -1.2802661
               6.3300627
                          0.2429119
                                    -4.6427410
                                                5.4029132
                          15
                                    16
```

```
#>
     -4.9317922
                   1.6882560
                                -0.2108935
                                             13.0434376
                                                           -1.0453205
                                                                         -2.2810515
#>
                           20
                                         21
                                                      22
                                                                    23
             19
                                                                                  24
                                 6.4237313
#>
    -8.5336548
                  -4.6084283
                                              1.3568726
                                                           -5.3062652
                                                                         -8.3790634
                                                                    29
#>
             25
                           26
                                         27
                                                      28
                                                                                  30
                   8.4616006
                                 8.1125493
#>
    17.4557162
                                             13.2877303
                                                            4.3405615
                                                                       -20.5276203
#>
             31
                           32
                                         33
                                                                    35
                                                                                  36
                                                      34
#>
    -1.6807212
                  -2.6457848
                               10.5147160
                                                            3.8898906
                                                                          2.6352188
                                              5.8145341
#>
             37
                           38
                                         39
                                                      40
                                                                                  42
                                                                    41
    -6.4526023
#>
                                                          -20.1468591
                  12.9798312
                                13.8308778
                                             -5.8406006
                                                                         -2.7500585
             43
#>
                           44
                                         45
                                                      46
                                                                    47
                                                                                  48
#>
   -20.4644534
                   6.9993682
                              -19.9155416
                                              1.7284984
                                                           -5.8948562
                                                                          0.5877659
#>
                           50
                                         51
                                                                    53
             49
                                                      52
                                                                                  54
                   3.7081200
                                                            1.6410328
#>
     5.8315446
                                 8.6977244
                                            -18.7177596
                                                                          5.4795727
#>
             55
                           56
                                         57
                                                      58
                                                                    59
                                                                                  60
     1.6497880
                  21.1232521
                                 3.9513602
                                            -14.6290282
                                                           -9.3539855
#>
                                                                        -11.2366011
#>
             61
                           62
                                         63
                                                      64
                                                                    65
                                                                                  66
#>
     6.5166020
                  -5.4553390
                                -5.2889493
                                             -9.9487999
                                                            6.2202358
                                                                         -4.1928993
                                                                    71
#>
             67
                           68
                                         69
                                                      70
                                                                                  72
#>
    -2.9061726
                   3.1056518
                                -1.5781122
                                                           -9.2307681
                                              5.9628746
                                                                          8.2549786
#>
             73
                           74
                                         75
                                                      76
                                                                    77
                                                                                  78
#>
    14.7068777
                  15.3941500
                                 6.2179172
                                             -9.9164715
                                                            3.0805612
                                                                         -0.5922107
#>
             79
                           80
                                                                    83
                                         81
                                                      82
                                                                                  84
#>
    12.3638649
                  -8.5165239
                                -8.2547947
                                              0.3930701
                                                           -3.0412042
                                                                         -8.9960434
#>
             85
                           86
                                         87
                                                      88
                                                                    89
                                                                                  90
#>
   -16.7984033
                  12.6843241
                                 8.9197865
                                              8.3100715
                                                          -10.3563143
                                                                         -8.2724792
                                                      94
#>
             91
                           92
                                                                    95
                                                                                  96
                                         93
#>
     1.1589511
                   9.3334340
                                -6.8427991
                                              7.5781800
                                                           -4.6452784
                                                                         -8.6626880
#>
             97
                           98
                                         99
                                                     100
     7.7580045
                   6.6699655
                                -6.2914860
                                              8.3101291
#>
m.01$call
\#> lm(formula = y \sim x)
```

These output are all related to the model we have run, so they are kept organized by the list so they can be used for various further steps like comparing models or checking for model fit.

A data frame is a bit more rigid that a list in that you cannot combine elements that do not have the same dimsions.

```
# new.dataframe <- data.frame( m.01$coefficients, m.01$residuals, m.01$call )
#
# these will fail because the vectors have different lengths</pre>
```

4.2 Subsets

The subset operators [] are one of the most common you will use in R.

The primary rule of subsets is to use a data operator to create a logical selector vector, and use that to generate subsets. Any observation that corresponds to TRUE will be retained, any observation that corresponds to FALSE will be dropped.

For vectors, you need to specify a single dimension.

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```
x1 <- c(167,185,119,142)
x2 <- c("adam","jamal","linda","sriti")
x3 <- factor( c("male","male","female","female") )
x4 <- c( "treatment","control","treatment","control" )
dat <- data.frame( name=x2, sex=x3, treat=x4, strength=x1 )

these <- x1 > 140  # selector vector

these
#> [1] TRUE TRUE FALSE TRUE

x1[ these ]
#> [1] 167 185 142

x2[ these ]
#> [1] "adam" "jamal" "sriti"
```

For data frames, you need two dimensions (rows and columns). The two dimensions are separated by a comma, and if you leave one blank you will not drop anything.

```
# dat[ row position , column position ]
dat
#>
     name sex treat strength
#> 1 adam male treatment 167
#> 2 jamal male control
                               185
#> 3 linda female treatment
                               119
#> 4 sriti female control
                               142
these <- dat$treat == "treatment"</pre>
dat[ these , ] # all data in the treatment group
#> name sex treat strength
#> 1 adam male treatment
                              167
#> 3 linda female treatment
                               119
dat[ , c("name", "sex") ] # select two columns of data
     name sex
#>
#> 1 adam male
#> 2 jamal male
#> 3 linda female
#> 4 sriti female
# to keep a subset as a separate dataset
dat.women <- dat[ dat$sex == "female" , ]</pre>
dat.women
```

```
#> name sex treat strength
#> 3 linda female treatment 119
#> 4 sriti female control 142
```

Note the rules listed above about subsetting factors. After applying a subset, they will retain all of the original levels, even when they are not longer useful. You need to drop the unused levels if you would like them to be omitted from functions that use the factor levels for analysis.

```
df <- data.frame( letters=LETTERS[1:5], numbers=seq(1:5) )

levels( df$letters )
#> [1] "A" "B" "C" "D" "E"

sub.df <- df[ 1:3, ]

sub.df$letters
#> [1] A B C
#> Levels: A B C D E

levels( sub.df$letters )
#> [1] "A" "B" "C" "D" "E"

droplevels( sub.df$letters )
#> [1] A B C
#> Levels: A B C
sub.df$letters )

#> [1] A B C
#> Levels: A B C
```

4.3 Variable Transformations

When we create a new variable from existing variables, it is called a 'transformation'. This is very common in data science. Crime is measures by the number of assults *per 100,000 people*, for example (crime / pop). A batting average is the number of hits divided by the number of at bats.

In R, mathematical operations are *vectorized*, which means that operations are performed on the entire vector all at once. This makes transformations fast and easy.

```
x + 5

#> [1] 6 7 8 9 10 11 12 13 14 15

x * 5

#> [1] 5 10 15 20 25 30 35 40 45 50
```

R uses a convention called "recycling", which means that it will re-use elements of a vector if necessary. In the example below the x vector has 10 elements, but the y vector only has 5 elements. When we run out of y, we just start over from the beginning. This is powerful in some instances, but can be dangerous in others if you don't realize that that it is happening.

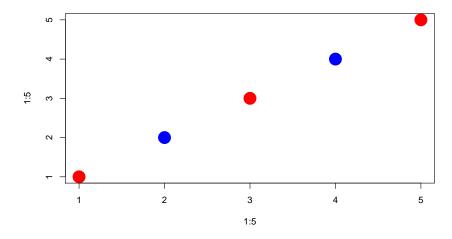
```
x <- 1:10
y <- 1:5
```

```
x + y
#> [1] 2 4 6 8 10 7 9 11 13 15

x * y
#> [1] 1 4 9 16 25 6 14 24 36 50

# the colors are recycled

plot( 1:5, 1:5, col=c("red","blue"), pch=19, cex=3 )
```



Here is an example of recycling gone wrong:

```
x1 <- c(167,185,119,142)

x2 <- c("adam", "jamal", "linda", "sriti")

x3 <- c("male", "male", "female", "female")

x4 <- c( "treatment", "contro", "treatment", "control" )

dat <- data.frame( name=x2, sex=x3, treat=x4, strength=x1 )

# create a subset of data of all female study participants

dat$sex == "female"

#> [1] FALSE FALSE TRUE TRUE

these <- dat$sex == "female"

dat[ these, ] # correct subset

#> name sex treat strength

#> 3 linda female treatment 119

#> 4 sriti female control 142
```

4.4 Missing Values: NA's

Missing values are coded differently in each data analysis program. SPSS uses a period, for example. In R, missing values are coded as "NA".

The important thing to note is that R wants to make sure you know there are missing values if you are conducting analysis. As a result, it will give you the answer of "NA" when you try to do math with a vector that includes a missing value. You have to ask it explicitly to ignore the missing value.

```
x5 < -c(1, 2, 3, 4)
#> [1] 1 2 3 4
sum( x5 )
#> [1] 10
mean(x5)
#> [1] 2.5
x5 < -c(1, 2, NA, 4)
x5
#> [1] 1 2 NA 4
# should missing values be treated as zeros or dropped?
sum( x5 )
#> [1] NA
mean(x5)
#> [1] NA
sum(x5, na.rm=T)
                    # na.rm=T argument drops missing values
#> [1] 7
mean( x5, na.rm=T ) # na.rm=T argument drops missing values
#> [1] 2.333333
```

You cannot use the == operator to identify missing values in a dataset. There is a special is.na() function

to locate all of the missing values in a vector.

```
x5
#> [1] 1 2 NA 4

x5 == NA  # this does not do what you want
#> [1] NA NA NA NA

is.na( x5 )  # much better
#> [1] FALSE FALSE TRUE FALSE

! is.na( x5 )  # if you want to create a selector vector to drop missing values
#> [1] TRUE TRUE FALSE TRUE

x5[! is.na(x5)]
#> [1] 1 2 4

x5[ is.na(x5)] <- 0  # replace missing values with zero</pre>
```

4.5 The 'attach' Function

Never Use This!

This is a convenient function for making variable names easily accessible, but it is problematic because of: scope

conflicting variable names

```
x <- 1:5
y <- 6:10

dat <- data.frame(x,y)

rm(x)
rm(y)

# I want to transform x in my dataset

attach( dat )

2*x
#> [1] 2 4 6 8 10

x <- 2*x

detach( dat )

x
#> [1] 2 4 6 8 10

dat # whoops! I didn't save my work in the dataset
#> x y
```

```
#> 1 1 6

#> 2 2 7

#> 3 3 8

#> 4 4 9

#> 5 5 10
```

You will see the **attach()** function used on occassion, and it is tempting because you can write the variable names directly. But in general, try to avoid the **attach()** function and don't form bad habits by using it now because when your scripts become more complicated then can cause problems.

Chapter 5

Merging Data

5.1 Packages Used in This Chapter

```
library( pander )
library( dplyr )
library( maps )
```

5.2 Relational Databases

Modern databases are huge - think about the amount of information stored at Amazon in the history of each transation, the database where Google logs every single search from every person around the world, or Twitter's database of all of the tweets (millions each day).

When databases become large, flat spreadsheet style formats are not useful because they create a lot of redundant information, are large to store, and are not efficient to search. Large datasets are instead stored in relational databases - sets of tables that contain unique IDs that allow them to be joined when necessary.

For example, consider a simple customer database. We don't want to store customer info with our transactions because we would be repeating their name and street address every time they make a new purchase. As a result, we store customer information and transaction information separately.

Customer Database

CUSTOMER.ID	FIRST.NAME	LAST.NAME	ADDRESS	ZIP.CODE
178 934	Alvaro Janette	Jaurez Johnson	123 Park Ave 456 Candy Ln	57701 57701
269	Latisha	Shane	1600 Penn Ave	20500

Transactions Database

CUSTOMER.ID	PRODUCT	PRICE
178	video	5.38
178	shovel	12
269	book	3.99
269	purse	8
934	mirror	7.64

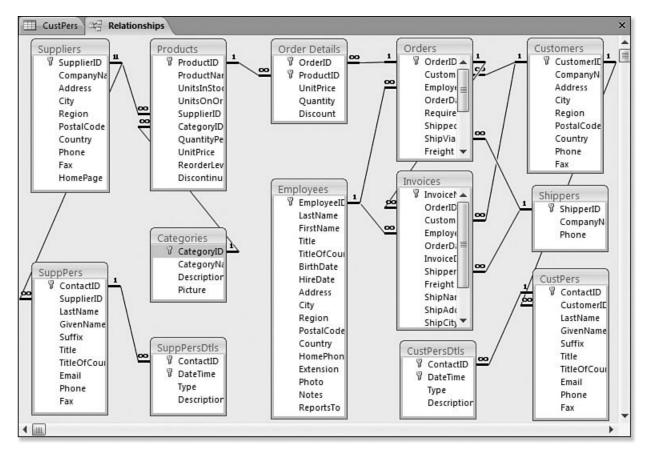
CUSTOMER.ID	PRODUCT	PRICE	_
			-

If we want to make the information actionable then we need to combine these datasets. For example, perhaps we want to know the average purchase amount from an individual in the 57701 zip code. We cannot answer that question with either dataset since the zip code is in one dataset, and the price is in another. We need to merge the data.

```
merge( customer.info, purchases )
     CUSTOMER.ID FIRST.NAME LAST.NAME
                                            ADDRESS ZIP. CODE PRODUCT PRICE
#> 1
            178
                    Alvaro
                              Jaurez 123 Park Ave
                                                      57701
                                                              video 5.38
#> 2
            178
                    Alvaro
                              Jaurez 123 Park Ave
                                                      57701
                                                             shovel 12.00
                   Latisha
#> 3
            269
                               Shane 1600 Penn Ave
                                                      20500
                                                               book 3.99
#> 4
            269
                   Latisha
                               Shane 1600 Penn Ave
                                                      20500
                                                              purse 8.00
#> 5
            934
                   Janette Johnson 456 Candy Ln
                                                      57701 mirror 7.64
full.dat <- merge( customer.info, purchases )</pre>
full.dat$PRICE[ full.dat$ZIP.CODE == "57701" ]
#> [1] 5.38 12.00 7.64
mean( full.dat$PRICE[ full.dat$ZIP.CODE == "57701" ] )
#> [1] 8.34
```

In reality, each purchase would have a purchase ID that is linked to shipping addresses, customer complaints, seller ratings, etc. Each seller would have their own data table with info. Each purchase would be tied to a payment type, which has its own data table. The system gets quite complex, which is why it is important to pay attention to the details of putting the data back together again.

5.3. SET THEORY 45



We will cover a few details of data merges that will help you avoid common and very subtle mistakes that can lead to incorrect inferences.

5.3 Set Theory

In order to merge data **correctly** you need to understand some very basic principles of set theory.

5.3.1 Set Theory Functions

Let's assume we have two sets: set1=[A,B], set2=[B,C]. Each element in this set represents a group of observations that occurs in the dataset. So B represents people that occur in both datasets, A represents people that occur only in the first dataset, and C represents people that only occur in the second dataset.

We can then describe membership through three operations:

Operation	Description
union intersection difference	The universe of all elements across all both sets: [A,B,C] The elements shared by both sets: [B] The elements in my first set, not in my second [A] or [C]

Let's see how this might work in practice with an example of members of a study:

```
name <- c("frank","wanda","sanjay","nancy")
group <- c("treat","treat","control","control")
gender <- c("male","female","female")

data.frame( name, group, gender ) %>% pander
```

name	group	gender
frank wanda sanjay nancy	treat treat control control	male female male female

For this example let's define set 1 as the treatment group, and set 2 as all women in the study. Note that set membership is always defined as binary (you are in the set or out), but it can include multiple criteria (the set of animals can contains cats, dogs, and mice).

```
treated <- name[ group == "treat" ]

treated
#> [1] "frank" "wanda"

females <- name[ gender == "female" ]

females
#> [1] "wanda" "nancy"
```

Now we can specify group belonging using some convenient set theory functions: union(), setdiff(), and intersect().

```
union( treated, females )
#> [1] "frank" "wanda" "nancy"

intersect( treated, females )
#> [1] "wanda"

setdiff( treated, females )
#> [1] "frank"

setdiff( females, treated )
#> [1] "nancy"
```

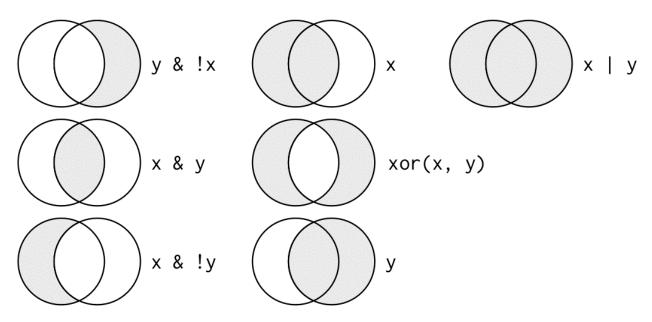
It is very important to note that union() and intersect() are symmetric functions, meaning intersect(x,y) will give you the same result as intersect(y,x). The setdiff() function is not symmetric, however.

5.3.2 Set Theory Using Logical Operators

Typically you will define your groups using logical operators, which perform the exact same function as set theory functions but are a little more expressive and flexible.

Let's use the same example above where x="treatment" and y="female", then consider these cases:

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Who belongs in each group?

```
# x
name[ group == "treat" ]
#> [1] "frank" "wanda"

# x & y
name[ group == "treat" & gender == "female" ]
#> [1] "wanda"

# x & ! y
name[ group == "treat" & gender != "female" ]
#> [1] "frank"

# x / y
name[ group == "treat" | gender == "female" ]
#> [1] "frank" "wanda" "nancy"
```

Who belongs in these groups?

- !x & !yx & ! (x & y)
- (x | y) &! (x & y)

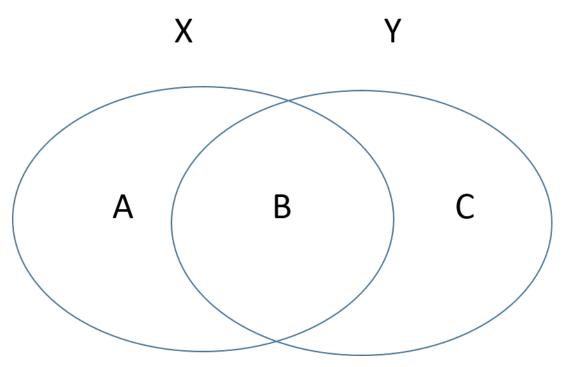
5.4 Merging Data

The Merge Function

The merge function joins two datasets. The function requires two datasets as the arguments, and they need to share a unique ID variable. Recall the example from above:

```
merge( customer.info, purchases )
     CUSTOMER.ID FIRST.NAME LAST.NAME
                                            ADDRESS ZIP. CODE PRODUCT PRICE
#> 1
             178
                     Alvaro
                               Jaurez 123 Park Ave
                                                       57701
                                                               video 5.38
#> 2
             178
                     Alvaro
                               Jaurez 123 Park Ave
                                                       57701
                                                              shovel 12.00
#> 3
             269
                                Shane 1600 Penn Ave
                                                       20500
                                                                book 3.99
                    Latisha
             269
                    Latisha
                                Shane 1600 Penn Ave
                                                       20500
                                                               purse 8.00
                                                       57701 mirror
#> 5
             934
                    Janette
                              Johnson 456 Candy Ln
                                                                     7.64
```

The important thing to keep in mind is that the default merge operation uses the **intersection** of the two datasets. It will drop all elements that don't occur in both datasets. We may want to fine-tune this as to not lose valuable data and potentially bias our analysis. As an example, no illegal immigrants will have social security numbers, so if you are merging using the SSN, you will drop this group from the data, which could impact your results.



With a little help from the set theory examples above, we can think about which portions of the data we wish to drop and which portions we wish to keep.

Argument	Usage
all=F	DEFAULT - new dataset contains intersection of X and Y (B only)
all=T	New dataset contains union of X and Y (A, B & C)
all.x=T	New dataset contains A and B, not C
all.y=T	New dataset contains B and C, not A

Here is some demonstrations with examples adapted from the R help file.

```
authors

#> surname nationality deceased

#> 1 Tukey US yes

#> 2 Tierney US no
```

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```
#> 3 Ripley UK
#> 4 McNeil Australia
books
#>
                                 title
     Tukey Exploratory Data Analysis
#> 2 Venables Modern Applied Statistics
#> 3 Ripley Spatial Statistics
#> 4 Ripley Stochastic Simulation
#> 5 McNeil Interactive Data Analysis
\#> 6 R Core Team An Introduction to R
# adding books to the author bios dataset (set B only)
merge(authors, books, by.x = "surname", by.y = "name")
#> surname nationality deceased
\textit{\#> 1} \quad \textit{McNeil} \quad \textit{Australia} \qquad \quad \textit{no Interactive Data Analysis}
#> 2 Ripley UK no Spatial Statistics
#> 3 Ripley UK no Stochastic Simulation
#> 4 Tukey US yes Exploratory Data Analysis
# adding author bios to the books dataset (set B only)
merge(books, authors, by.x = "name", by.y = "surname")
#> name title nationality deceased
#> 1 McNeil Interactive Data Analysis Australia no
no
                                        UK
                                                no
                                       US yes
# keep books without author bios, lose authors without books ( sets A and B )
merge( books, authors, by.x = "name", by.y = "surname", all.x=T )
      name
                                title nationality deceased
#> 1 McNeil Interactive Data Analysis Australia no
\#> 2 R Core Team An Introduction to R <NA>
                                                    \langle NA \rangle
                                            UK
UK
                                                     no
                                            US
#> 5
       Tukey Exploratory Data Analysis
                                                    yes
#> 6 Venables Modern Applied Statistics <NA> <NA>
# keep authors without book listed, lose books without author bios ( sets B and C )
merge( books, authors, by.x = "name", by.y = "surname", all.y=T )
```

```
#>
                                      title nationality deceased
            name
          McNeil Interactive Data Analysis
#> 1
                                              Australia
#> 2
          Ripley
                        Spatial Statistics
                                                      UK
                                                               no
#> 3
                                                      UK
          Ripley
                     Stochastic Simulation
                                                               no
#> 4 Shakespeare
                                       <NA>
                                                 England
                                                              yes
#> 5
         Tierney
                                       <NA>
                                                      US
#> 6
           Tukey Exploratory Data Analysis
                                                      US
                                                              yes
# dont' throw out any data
                              ( sets A and B and C )
merge( books, authors, by.x = "name", by.y = "surname", all=T )
#>
                                      title nationality deceased
            name
#> 1
          McNeil Interactive Data Analysis
                                             Australia
#> 2 R Core Team
                     An Introduction to R
                                                    <NA>
                                                             <NA>
#> 3
          Ripley
                        Spatial Statistics
                                                      UK
                                                               no
                                                      UK
#> 4
          Ripley
                     Stochastic Simulation
                                                               no
#> 5 Shakespeare
                                       <NA>
                                                 England
                                                              yes
#> 6
         Tierney
                                       <NA>
                                                      US
                                                               no
#> 7
           Tukey Exploratory Data Analysis
                                                      US
                                                              yes
#> 8
        Venables Modern Applied Statistics
                                                    <NA>
                                                             <NA>
```

Also note that the order of your datasets in the argument list will impact the inclusion or exclusion of elements.

```
\label{eq:merge} \begin{split} & merge(~x,~y,~all=F~)~EQUALS~merge(~y,~x,~all=F~)\\ & merge(~x,~y,~all.x=T~)~DOES~NOT~EQUAL~merge(~y,~x,~all.x=T~) \end{split}
```

5.4.1 The by.x and by.y Arguments

When you use the default **merge()** function without specifying the variables to merge upon, the function will check for common variable names across the two datasets. If there are multiple, it will join the shared variables to create a new unique key. This might be problematic if that was not the intent.

Take the example of combining fielding and salary data in the Lahman package. If we are not explicit about the merge variable, we may get odd results. Note that they two datasets share four ID variables.

```
library( Lahman )
data( Fielding )
data( Salaries )

intersect( names(Fielding), names(Salaries) )
#> [1] "playerID" "yearID" "teamID" "lgID"

# merge id

int <- intersect( names(Fielding), names(Salaries) )

paste( int[1],int[2],int[3],int[4], sep="." )
#> [1] "playerID.yearID.teamID.lgID"
```

To avoid problems, be explicit using the by.x and by.x arguments to control which variable is used for the merge.

```
head( merge( Salaries, Fielding ) )
    yearID teamID lqID playerID salary stint POS G GS InnOuts PO A E DP
                                        1
                   NL barkele01 870000
                                              P 20 18
                                                               2 9 1 0
#> 1
      1985
              ATL
                                                         221
                                       1  P 37 37
1  C 70 67
1  P 66 2
1  C 91 76
1  1B 39 27
      1985
              ATL
                  NL bedrost01 550000
                                              P 37 37
                                                          620 13 23 4
#> 3
      1985
             ATL NL benedbr01 545000
                                                        1698 314 35 4 1
#> 4
      1985
             ATL NL campri01 633333
                                                         383 7 13 4 3
#> 5
              ATL NL ceronri01 625000
                                                         2097 384 48 6 4
      1985
#> 6
      1985
              ATL
                   NL chambch01 800000
                                                         814 299 25 1 31
   PB WP SB CS ZR
#> 1 NA NA NA NA NA
#> 2 NA NA NA NA NA
#> 3 1 9 65 24
#> 4 NA NA NA NA NA
#> 5 6 20 69 29 1
#> 6 NA NA NA NA NA
head( merge( Salaries, Fielding, by.x="playerID", by.y="playerID" ) )
     playerID yearID.x teamID.x lgID.x salary yearID.y stint teamID.y
#> 1 aardsda01
                 2010
                           SEA
                                  AL 2750000
                                                 2009
                                                          1
                                                                SEA
                           SEA
#> 2 aardsda01
                 2010
                                                 2015
                                 AL 2750000
                                                          1
                                                                ATL
#> 3 aardsda01
                2010
                           SEA
                                 AL 2750000
                                                 2006
                                                          1
                                                                CHN
#> 4 aardsda01
              2010
                           SEA
                                  AL 2750000
                                                 2008
                                                          1
                                                                BOS
#> 5 aardsda01
                 2010
                           SEA
                                                 2013
                                                                NYN
                                   AL 2750000
                                                          1
#> 6 aardsda01
                 2010
                           SEA
                                   AL 2750000
                                                 2012
                                                                NYA
                                                          1
    lgID.y POS G GS InnOuts PO A E DP PB WP SB CS ZR
#> 1
        AL
            P 73 0
                        214 2 5 0 1 NA NA NA NA NA
            P 33 0
                         92 0 1 1 0 NA NA NA NA NA
        NL
#> 3
        NL
           P 45 0
                        P 47 0
#> 4
        AL
                        146 3 6 0 O NA NA NA NA NA
#> 5
             P 43 0
        NL
                        119
                            1 5 0 O NA NA NA NA NA
#> 6
        AL
            P 1 0
                      3 000 0 NA NA NA NA NA
```

5.5 Non-Unique Observations in ID Variables

In some rare instances, you will need to merge to datasets that have non-singular elements in the unique key ID variables, meaning each observation / individual appears more than one time in the data. Note that in this case, for each occurance of an observation / individual in your X dataset, you will merge once with each occurance of the same observation / individual in the Y dataset. The result will be a multiplicative expansion of the size of your dataset.

For example, if John appears on four separate rows of X, and three separate rows of Y, the new dataset will contain 12 rows of John $(4 \times 3 = 12)$.

```
dataset X contains four separate instances of an individual [X1, X2, X3, X4]
```

dataset Y contains three separate instances of an individual [Y1, Y2, Y3]

After the merge we have one row for each pair:

```
X1-Y1
```

X1-Y2

X1-Y3

X2-Y1 X2-Y2 X2-Y3 X3-Y1 X3-Y2 X3-Y3 X4-Y1 X4-Y2 X4-Y3

For example, perhaps a sales company has a database that keeps track of biographical data, and sales performance. Perhaps we want to see if there is peak age for sales performance. We need to merge these datasets.

```
bio <- data.frame( name=c("John","John","John"),</pre>
                  year=c(2000,2001,2002),
                   age=c(43,44,45))
performance <- data.frame( name=c("John", "John", "John"),</pre>
                           year=c(2000,2001,2002),
                           sales=c("15k","20k","17k") )
# correct merge
merge( bio, performance, by.x=c("name","year"), by.y=c("name","year") )
#> name year age sales
#> 1 John 2000 43
                     15k
#> 2 John 2001 44
                     20k
#> 3 John 2002 45
                    17k
# incorrect merge
merge( bio, performance, by.x=c("name"), by.y=c("name") )
#> name year.x age year.y sales
#> 1 John 2000 43
                       2000
                              15k
           2000 43
#> 2 John
                       2001
                              20k
                              17k
#> 3 John
          2000 43
                       2002
#> 4 John
          2001 44
                       2000
                              15k
#> 5 John
                       2001
           2001 44
                              20k
#> 6 John
            2001
                       2002
                              17k
                 44
#> 7 John
            2002 45
                       2000
                              15k
#> 8 John
            2002 45
                       2001
                              20k
#> 9 John
           2002 45
                       2002
                              17k
```

It is good practice to check the size (number of rows) of your dataset before and after a merge. If it has expanded, chances are you either used the wrong unique IDs, or your dataset contains duplicates.

5.5.1 Example of Incorrect Merge

Here is a tangible example using the Lahman baseball dataset. Perhaps we want to examine the relationship between fielding position and salary. The *Fielding* dataset contains fielding position information, and the *Salaries* dataset contains salary information. We can merge these two datasets using the *playerID* field.

If we are not thoughtful about this, however, we will end up causing problems. Let's look at an example using Kirby Pucket.

```
kirby.fielding <- Fielding[Fielding$playerID == "puckeki01" , ]</pre>
head( kirby.fielding )
         playerID yearID stint teamID lqID POS
                                             G GS InnOuts PO A E DP
#> 83848 puckeki01 1984 1 MIN AL OF 128 128 3377 438 16 3 4
#> 85157 puckeki01 1985
                          1 MIN AL OF 161 160 4213 465 19 8 5
#> 86489 puckeki01 1986
                             MIN AL OF 160 157
                                                      4155 429 8 6 3
                          1
#> 87896 puckeki01 1987
                           1
                              MIN AL OF 147 147
                                                      3820 341 8 5 2
#> 89264 puckeki01 1988
                        1 MIN AL OF 158 157
                                                    4049 450 12 3 4
#> 90685 puckeki01 1989
                          1 MIN AL OF 157 154 3985 438 13 4 3
        PB WP SB CS ZR
#> 83848 NA NA NA NA NA
#> 85157 NA NA NA NA NA
#> 86489 NA NA NA NA NA
#> 87896 NA NA NA NA NA
#> 89264 NA NA NA NA NA
#> 90685 NA NA NA NA NA
nrow( kirby.fielding )
#> [1] 21
kirby.salary <- Salaries[ Salaries$playerID == "puckeki01" , ]</pre>
head( kirby.salary )
       yearID teamID lgID playerID salary
#> 280
        1985
                MIN AL puckeki01 130000
#> 917
         1986
                MIN AL puckeki01 255000
#> 1610 1987 MIN AL puckeki01 465000
#> 2244 1988 MIN AL puckeki01 1090000
        1989
                MIN AL puckeki01 2000000
#> 2922
#> 3717
        1990
                MIN
                     AL puckeki01 2816667
nrow( kirby.salary )
#> [1] 13
kirby.field.salary <- merge(kirby.fielding, kirby.salary, by.x="playerID", by.y="playerID")
head( select( kirby.field.salary, yearID.x, yearID.y,
                                                   POS,
                                                           G, GS, salary ) )
#> yearID.x yearID.y POS G GS salary
#> 1
       1984
               1985 OF 128 128 130000
                1986 OF 128 128 255000
#> 2
        1984
#> 3
        1984
                1987 OF 128 128 465000
#> 4
      1984
               1988 OF 128 128 1090000
#> 5
       1984
               1989 OF 128 128 2000000
#> 6
               1990 OF 128 128 2816667
       1984
nrow( kirby.field.salary )
#> [1] 273
21*13
#> [1] 273
```

What we have done here is taken each year of fielding data, and matched it to **every** year of salary data. We can see that we have 21 fielding observations and 13 years of salary data, so our resulting dataset is 273 observation pairs.

This merge also makes it difficult to answer the question of the relationship between fielding position and salary if players change positions over time.

The correct merge in this case would be a merge on a playerID-yearID pair. We can create a unique key by combining playerID and yearID using **paste()**:

```
head( paste( kirby.fielding$playerID, kirby.fielding$yearID, sep=".") )
#> [1] "puckeki01.1984" "puckeki01.1985" "puckeki01.1986" "puckeki01.1987"
#> [5] "puckeki01.1988" "puckeki01.1989"
```

But there is a simple solution as the merge function also allows for multiple variables to be used for a merge() command.

5.6 The %in% function

Since we are talking about intersections and matches, I want to briefly introduce the **%in%** function. It is a combination of the two.

The **intersect()** function returns a list of unique matches between two vectors.

```
data(Salaries)
data(Fielding)
intersect( names(Salaries), names(Fielding) )
#> [1] "yearID" "teamID" "lgID" "playerID"
```

The **match()** function returns the position of matched elements.

```
x <- c("A", "B", "C", "B")

y <- c("B", "D", "A", "F")

match( x, y)

#> [1] 3 1 NA 1
```

The %in% function returns a logical vector, where TRUE signifies that the element in y also occurs in x. In other words, does a specific element in y belong to the intersection of x,y.

This is very useful for creating subsets of data that belong to both sets.

```
x <- c("A","B","C")
y <- c("B","D","A","B","F","B")
y %in% x # does each element of y occur anywhere in x?
#> [1] TRUE FALSE TRUE TRUE FALSE TRUE
```

```
y[ y %in% x] # keep only data that occurs in both
#> [1] "B" "A" "B" "B"
```

5.7 The Match Function

Often times we do not need to merge data, we may just need sort data in one dataset so that it matches the order of another dataset. This is accomplished using the **match()** function.

Note that we can rearrange the order of a dataset by referencing the desired position.

```
x <- c("Second", "Third", "First")

x
#> [1] "Second" "Third" "First"

x[ c(3,1,2) ]
#> [1] "First" "Second" "Third"
```

The **match()** function returns the *positions* of matches of its *first* vector to the *second* vector listed in the arguments. Or in other words, the *order* that vector 2 would need to follow to match vector 1.

```
x <- c("A", "B", "C")
y <- c("B", "D", "A")
cbind( x, y )
#> [1,] "A" "B"
#> [2,] "B" "D"
#> [3,] "C" "A"
match( x, y )
#> [1] 3 1 NA
match( y, x) # not a symmetric operation!
#> [1] 2 NA 1
# In the y vector:
# [3]=A
# [1]=B
# [NA] =D (no match)
order.y <- match(x, y)
y[ order.y ]
#> [1] "A" "B" NA
```

We can see that match() returns the correct order to put y in so that it matches the order of x. In the re-ordered vector, the first element is the original third element A, the second element is the original first element B, and there is no third element because D did not match anything in x.

Note the order of arguments in the function:

match (data I want to match to ,data I need to re-order)

We can use this position information to re-order y as follows:

```
x <- sample( LETTERS[1:15], size=10 )</pre>
y <- sample( LETTERS[1:15], size=10 )
cbind( x, y )
      x y
#> [1,] "E" "J"
#> [2,] "N" "L"
#> [3,] "C" "C"
#> [4,] "B" "N"
#> [5,] "F" "F"
#> [6,] "G" "M"
#> [7,] "A" "I"
#> [8,] "J" "G"
#> [9,] "O" "D"
#> [10,] "H" "B"
order.y <- match(x, y)
y.new <- y[ order.y ]</pre>
cbind( x, y.new )
    x y.new
#> [1,] "E" NA
#> [2,] "N" "N"
#> [3,] "C" "C"
#> [4,] "B" "B"
#> [5,] "F" "F"
#> [6,] "G" "G"
#> [7,] "A" NA
#> [8,] "J" "J"
#> [9,] "O" NA
#> [10,] "H" NA
# Note the result if you confuse the order or arguments
order.y <- match( y, x )
y.new <- y[ order.y ]</pre>
cbind( x, y.new )
#>
   x y.new
#> [1,] "E" "G"
#> [2,] "N" NA
#> [3,] "C" "C"
#> [4,] "B" "L"
#> [5,] "F" "F"
#> [6,] "G" NA
#> [7,] "A" NA
```

```
#> [8,] "J" "M"
#> [9,] "O" NA
#> [10,] "H" "N"
```

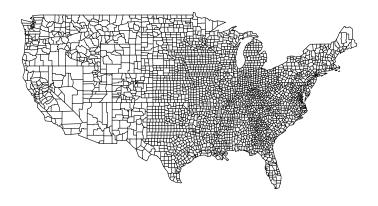
This comes in handy when we are matching information between two tables. For example, in GIS the map regions follow a specific order but your data does not. Create a color scheme for levels of your data, and then re-order the colors so they match the correct region on the map. In this example, we will look at unemployment levels by county.

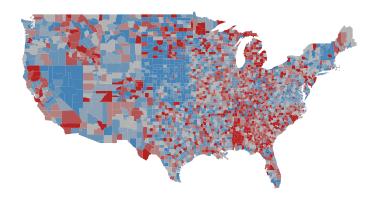
```
library( maps )
data( county.fips )
data( unemp )
map( database="county" )
# assign a color to each level of unemployment, red = high, gray = medium, blue = low
color.function <- colorRampPalette( c("steelblue", "gray70", "firebrick") )</pre>
color.vector <- cut( rank(unemp$unemp), breaks=7, labels=color.function( 7 ) )</pre>
color.vector <- as.character( color.vector )</pre>
head( color.vector )
#> [1] "#B28282" "#B28282" "#B22222" "#B25252" "#B28282" "#B22222"
# doesn't look quite right
map( database="county", col=color.vector, fill=T, lty=0 )
# what went wrong here?
# our unemployment data (and thus the color vector) follows a different order
cbind( map.id=county.fips$fips, data.id=unemp$fips, color.vector )[ 2500:2510 , ]
         map.id data.id color.vector
#> [1,] "48011" "47149" "#B28282"
#> [2,] "48013" "47151" "#B22222"
#> [3,] "48015" "47153" "#B22222"
#> [4,] "48017" "47155" "#B28282"
#> [5,] "48019" "47157" "#B28282"
#> [6,] "48021" "47159" "#B22222"
#> [7,] "48023" "47161" "#B25252"
#> [8,] "48025" "47163" "#B3B3B3"
#> [9,] "48027" "47165" "#B28282"
#> [10,] "48029" "47167" "#B25252"
#> [11,] "48031" "47169" "#B25252"
# place the color vector in the correct order
this.order <- match( county.fips$fips, unemp$fips )
```

```
color.vec.ordered <- color.vector[ this.order ]

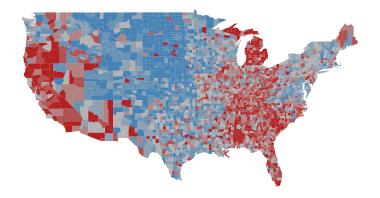
# colors now match their correct counties

map( database="county", col=color.vec.ordered, fill=T, lty=0 )
title( main="Unemployment Levels by County in 2009")</pre>
```





Unemployment Levels by County in 2009



Note that elements can be recycled from your y vector:

```
x <- c("A", "B", "C", "B")
y <- c("B","D","A","F")
cbind( x, y )
#>  x  y
#> [1,] "A" "B"
#> [2,] "B" "D"
#> [3,] "C" "A"
#> [4,] "B" "F"
match( x, y )
#> [1] 3 1 NA 1
order.y <- match( x, y )
y.new <- y[ order.y ]</pre>
cbind( x, y.new )
\#> x y.new
#> [1,] "A" "A"
#> [2,] "B" "B"
#> [3,] "C" NA
#> [4,] "B" "B"
```

Chapter 6

Analysis with Groups in R

6.0.1 Packages Used in this Chapter

```
library( pander )
library( dplyr )
library( tidyr )
library( reshape2 )
library( scales )
library( ggplot2 )
library( Lahman )
```

6.0.2 Hypothetical Experimental Data

We will demonstrate some functions using this hypothetical dataset:

```
head( d ) %>% pander
```

id	race	blood.type	gender	age	study.group	speed
1	white	A	male	50	treatment	509.6
2	white	В	female	46	treatment	654.7
3	white	A	female	29	treatment	658.5
4	black	A	female	59	treatment	645.8
5	white	A	female	87	treatment	45.22
6	white	A	female	36	treatment	679

6.1 Group Structure

The two most important skills as you first learn a data programming language are:

- 1. Translating English phrases into computer code using logical statements
- 2. Organizing your data into groups

This lecture focuses on efficienty splitting your data into groups, and then analyzing your data by group.

6.1.1 What Are Groups?

A group represents a set of elements with identical characteristics - mice all belong to one group and elephants belong to another. Easy enough, right?

In data analysis, it is a little more complicated because a group is defined by a set of features. Each group still represents a set of elements with identical characteristics, but when we have multiple features there is a unique group for each combination of features.

The simple way to think about this is that the cross-tab of features generates a grid (table), and each cell represents a unique group:

Male	Male	
Treatment	Control	
Female	Female	
Treatment	Control	

We might be interested in simple groups (treatment cases versus control cases), or complex groups (does the treatment effect women and men differently?).

In previous lectures you have learned to identify a group with a logical statement, and analyze that group discretely.

```
mean( speed[ study.group == "treatment" & gender=="female" ] )
#> [1] 614.0334
```

In this lecture you will learn to define a group structure, then analyze all of your data using that structure.

```
tapply( speed, INDEX = list( study.group, gender ), FUN = mean )
```

	female	male
control	462.5	364.1
treatment	614	504.5

6.1.2 Main Take-Away

R has been designed to do efficient data analysis by defining a group structure, then quickly applying a function to all unique members.

The base R packages do this with a set of functions in the **apply()** family. The **tapply()** function allows you to specify an outcome to analyze and a group, then ask for results from a function.

```
tapply( X=speed, INDEX=list( study.group, gender ), FUN=mean )
```

	female	male
control	462.5	364.1
treatment	614	504.5

The **dplyr** package makes this process easier using some simple verbs and the "pipe" operator.

da+	9/59/	group by study group gon	ndor)	9/ >9/	<pre>summarize(ave.speed = mean(speed))</pre>
uat	10/10	group_by(study.group, gen	ider)	10/10	summarize(ave.speed - mean(speed))

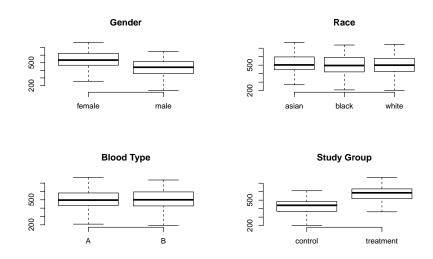
study.group	gender	ave.speed
control	male female	$364.1 \\ 462.5$
$\begin{array}{c} {\rm treatment} \\ {\rm treatment} \end{array}$	$rac{ ext{male}}{ ext{female}}$	$504.5 \\ 614$

6.1.3 Example

Let's think about a study looking at reading speed. The treatment is a workshop that teaches some speed-reading techniques. In this study we have data on:

- gender (male, female)
- race (black, white, asian)
- blood.type (A,B)
- age (from 18 to 93)

Examining descriptive statistics we can see that reading speed varies by gender and the treatment group, but not by race or blood type:



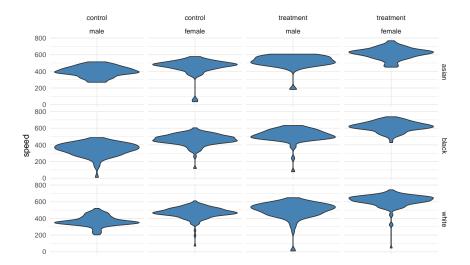
The question is, how many unique groups can we create with these four factors?

Each individual factor contains a small number of levels (only 2 or 3 in this case), which makes the group structure look deceptively simple at first glance. When we start to examine combinations of factors we see that group structure can get complicated pretty quickly.

If we look at gender alone, we have two levels: male and female. So we have two groups. If we look at our study groups alone we have two groups: treatment and control.

If we look at gender and the study groups together, we now have a 2 x 2 grid, or four unique groups.

If the race factor has three levels, how many unique groups will we have considering the study design, gender, and race together?

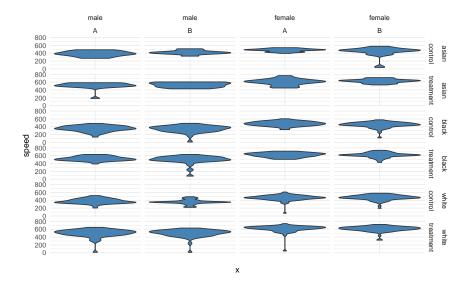


We can calculate the size of the grid by multiplying number of levels for each factor. We see here we have 12 unique groups:

```
nlevels( gender ) * nlevels( study.group ) * nlevels( race )
#> [1] 12
```

If we add blood type, a factor with two levels (A and B), we now have 24 unique groups:

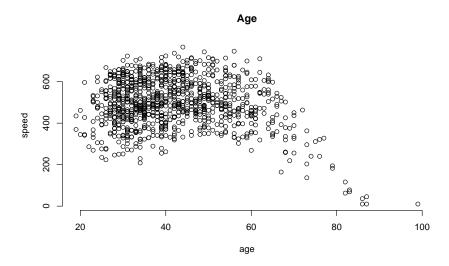
```
p + facet_grid( race + study.group ~ gender + blood.type)
```



What about age? It is a continuous variable, so it's a little more tricky.

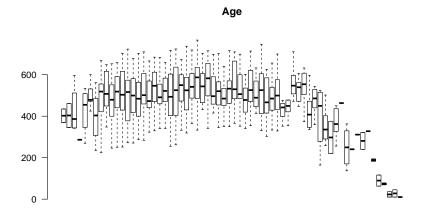
We can certainly analyze the relationship between age and speed using correlation tools.

```
plot( age, speed, bty="n", main="Age" )
```



But we can also incorporate this independent variable into a group structure. We can treat each distinct age as a separate group. The ages in this study range from 18 to 93, so we have 65 distinct ages represented.

```
plot( factor(age), speed, las=2, frame.plot=F, outline=F, main="Age", xaxt="n" )
```

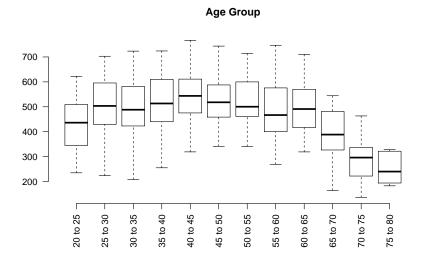


If we think about the overall group structure, then, we have unique groups defined by gender, race, blood type, and study design, and another 65 age groups. So in total we now have $24 \times 65 = 1,560$ groups! That is getting complicated.

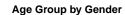
This group design is problematic for two reasons. From a pragmatic standpoint, we can't report results from 1,500 groups in a table. From a more substantive perspective, we although we have 1,500 distinct cells in our grid, many may not include observations that represent the unique combination of all factors. So this group design is not very practical.

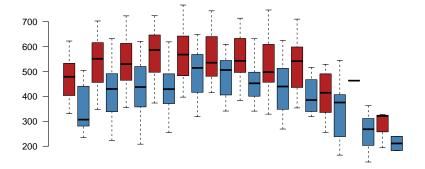
A similar problem arises if our data includes time. If our data includes the time of events recorded by hours, days of the week, months, and years, we can have generate complicated group structures if we try to analyze every unique combination.

We can simplify our analysis by thinking about age ranges instead of ages, or in other words by binning our continuous data. If we split it into five-year ranges, for example, we have gone from 65 distinct ages to 12 distinct age groups.



We have now simplified our analysis from 1,560 to 288 possible groups. Combinations of groups will also be easier:





6.2 Analysis by Group

Let's demonstrate some analysis of groups using the Lahman package and some **dplyr** verbs. Let's do some analysis of player salaries (*Salaries* dataset), and start with a simple group structure - teams in the National League and time.

- 1. Which team has the highest average player salary?
- 2. Which team has the most players paid over \$5 million a season?
- 3. Which team has raised it's pay the most over the past decade?

Let's start by thinking about group structure. We have teams, and we have seasons. Teams is stored as a factor, and seasons as a numeric value, so we can consider group for each by counting levels and unique values:

```
nlevels( Salaries$teamID )
#> [1] 46
length( unique( Salaries$yearID ) )
#> [1] 32
```

So we can potentially calculate $32 \times 46 = 1{,}472$ average player salaries.

6.2.1 Highest Ave Player Salary

For our first question, we will select only teams from the National League. Let's use the most recent year of data to calculate average pay.

```
Salaries %>% filter( lgID == "NL", yearID == 2016 ) %>%
             group_by( teamID) %>%
             summarize( Ave_Salary = mean(salary) )
#> # A tibble: 15 x 2
#>
    teamID Ave_Salary
#>
    <fct>
                 <db1>
#> 1 ARI
              3363041.
#> 2 ATL
              2362010.
#> 3 CHC
              5312678.
#> 4 CIN
              3066899.
#> 5 COL
              3413487
#> 6 LAD
              6322525.
#> # ... with 9 more rows
```

Since the salaries are large, they are a little hard to read. Let's clean up the table a bit.

```
Salaries %>%
    filter( lgID == "NL", yearID == 2016 ) %>%
    group_by( teamID ) %>%
    summarize( Ave_Salary=dollar( mean(salary,na.rm=T) ) ) %>%
    arrange( desc(Ave_Salary) ) %>%
    pander()
```

teamID	Ave_Salary
SFG	\$6,890,151
LAD	\$6,322,525
WSN	\$5,448,179
CHC	\$5,312,678

teamID	Ave_Salary
NYM	\$4,958,857
STL	\$4,614,629
SDP	\$3,756,475
PIT	\$3,706,387
COL	\$3,413,487
ARI	\$3,363,041
CIN	\$3,066,899
MIA	\$2,761,222
ATL	\$2,362,010
MIL	\$2,292,508
PHI	\$2,033,793

6.2.2 Most Players Paid Over \$5 Million

This question requires you to utilize a logical statement in order to translate from the question to code. We need to inspect each salary, determine whether it is over the \$5m threshold, then count all of the cases. The operation will look something like this:

```
sum( Salaries$salary > 5000000 )
#> [1] 3175
```

It gets a little trickier when we want to do the operation simultaneously across groups. Our team group structure is already defined, so let's define our logical vector and count cases that match:

```
dat.NL <- filter( Salaries, yearID == 2010 & lgID == "NL" ) %>% droplevels()
gt.5m <- dat.NL$salary > 5000000
table( dat.NL$teamID, gt.5m )
#>
        gt.5m
         FALSE TRUE
#>
#>
             23
                   3
     ARI
#>
     ATL
             21
                    6
     CHN
             19
                    8
#>
             21
                    5
#>
     CIN
             23
                    6
#>
     COL
#>
     FLO
             23
     HOU
             24
#>
                    7
#>
     LAN
             20
             25
#>
     MIL
#>
     NYN
             19
#>
     PHI
             18
                   10
#>
     PIT
             27
                    0
#>
     SDN
             25
                    1
#>
     SFN
             21
                    7
#>
     SLN
             19
                    6
     WAS
             26
#>
                    4
```

This solution works, but the table provides too much information. We can use dply to simplify and format the table nicely for our report:

```
Salaries %>%
  filter( yearID == 2010 & lgID == "NL" ) %>%
  group_by( teamID ) %>%
  summarise( gt_five_million = sum( salary > 5000000 ) ) %>%
  arrange( desc(gt_five_million) ) %>%
  pander
```

teamID	$gt_five_million$
PHI	10
NYN	9
$_{\rm CHN}$	8
LAN	7
SFN	7
ATL	6
COL	6
SLN	6
CIN	5
FLO	4
HOU	4
MIL	4
WAS	4
ARI	3
SDN	1
PIT	0

6.2.3 Fielding Positions

Which fielding position is the highest paid?

```
merge( Salaries, Fielding ) %>%
  filter( yearID == 2016 ) %>%
  group_by( POS ) %>%
  summarize( Mean_Salary = dollar( mean(salary) ) ) %>%
  pander
```

POS	Mean_Salary
1B	\$5,570,032
2B	\$3,162,075
3B	\$3,579,088
\mathbf{C}	\$2,521,903
OF	\$3,546,115
P	\$3,401,676
SS	\$2,510,833

6.2.4 Country of Birth

Which country has produced the highest paid baseball players?

```
merge( Salaries, Master ) %>%
  filter( yearID == 2016 ) %>%
  group_by( birthCountry ) %>%
  summarize( Mean_Salary = dollar( mean(salary) ) ) %>%
  pander
```

birthCountry	Mean_Salary
Aruba	\$650,000
Australia	\$523,400
Brazil	\$1,548,792
CAN	\$7,854,167
Colombia	\$3,125,289
Cuba	\$5,532,484
Curacao	\$5,724,167
D.R.	\$5,102,318
Germany	\$511,500
Japan	\$8,247,012
Mexico	\$4,617,038
Netherlands	\$2,425,000
Nicaragua	\$2,375,000
P.R.	\$3,241,378
Panama	\$2,946,550
Saudi Arabia	\$522,500
South Korea	\$5,326,190
Taiwan	\$6,750,000
USA	\$4,189,640
V.I.	\$507,500
Venezuela	\$4,521,051

6.2.5 Pay Raises

To examine pay raises, we will now use more than one year of data. Since the question asks about pay raises over the past decade, we will filter the last ten years of data.

And how since we are looking at patterns over teams and over time, we need to define a group structure with two variables:

teamID	yearID	mean
ARI	2007	\$1,859,555
ARI	2008	\$2,364,383
ARI	2009	\$2,812,141
ARI	2010	\$2,335,314
ARI	2011	\$1,986,660
ARI	2012	\$2,733,512
ARI	2013	\$3,004,400
ARI	2014	\$3,763,904

teamID	yearID	mean
ARI	2015	\$2,034,250
ARI	2016	\$3,363,041
ATL	2007	\$3,117,530
ATL	2008	\$3,412,189
ATL	2009	\$3,335,385
ATL	2010	\$3,126,802
ATL	2011	\$3,346,257
ATL	2012	\$2,856,205
ATL	2013	\$3,254,501
ATL	2014	\$4,067,042
ATL	2015	\$2,990,885
ATL	2016	\$2,362,010

This might seem like an odd format. We might expect something that looks more like our grid structure:

```
dat.NL <- filter( Salaries, yearID > 2010 & lgID == "NL" ) %>% droplevels()
tapply( dat.NL$salary, INDEX=list(dat.NL$teamID, dat.NL$yearID), FUN=mean, na.rm=T ) %>% pander
```

	2011	2012	2013	2014	2015	2016
ARI	1986660	2733512	3004400	3763904	2034250	3363041
\mathbf{ATL}	3346257	2856205	3254501	4067042	2990885	2362010
\mathbf{CHC}	NA	NA	NA	NA	NA	5312678
\mathbf{CHN}	5001893	3392194	3867989	2426759	4138547	NA
\mathbf{CIN}	2531571	2935843	4256178	3864911	4187862	3066899
\mathbf{CLE}	NA	NA	NA	4500000	NA	NA
\mathbf{COL}	3390310	2692054	2976363	3180117	3827544	3413487
\mathbf{FLO}	2190154	NA	NA	NA	NA	NA
\mathbf{HOU}	2437724	2332731	NA	NA	NA	NA
\mathbf{LAD}	NA	NA	NA	NA	NA	6322525
\mathbf{LAN}	3472967	3171453	6980069	6781706	7441103	NA
MIA	NA	4373259	1400079	1549515	2835688	2761222
\mathbf{MIL}	2849911	3755921	3077881	3748778	3477586	2292508
\mathbf{NYM}	NA	NA	NA	NA	NA	4958857
NYN	4401752	3457555	1648278	3168777	3870667	NA
PHI	5765879	5817965	6533200	5654530	4295885	2033793
\mathbf{PIT}	1553345	2248286	2752214	2756357	3065259	3706387
\mathbf{SDN}	1479650	1973025	2342339	2703061	4555435	NA
\mathbf{SDP}	NA	NA	NA	NA	NA	3756475
\mathbf{SFG}	NA	NA	NA	NA	NA	6890151
\mathbf{SFN}	4377716	3920689	5006441	5839649	6100056	NA
\mathbf{SLN}	3904947	3939317	3295004	4310464	4586212	NA
\mathbf{STL}	NA	NA	NA	NA	NA	4614629
\mathbf{WAS}	2201963	2695171	4548131	4399456	5365085	NA
\mathbf{WSN}	NA	NA	NA	NA	NA	5448179

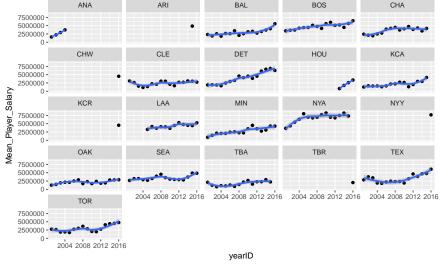
Later on we will look at the benefits of "tidy data", but the basic idea is that you can "facet" your analysis easily when your groups are represented as factors instead of arranged as a table. For example, here is a time series graph that is faceted by teams:

```
Salaries %>% filter( yearID > 2000 & lgID == "AL" ) %>% group_by( teamID, yearID ) %>% summarize( Mean_Player_Salary=mean(salary) ) -> t1

qplot( data=t1, x=yearID, y=Mean_Player_Salary, geom=c("point", "smooth") ) + facet_wrap( ~ teamID, nc

ANA ARI BAL BOS CHA

7500000-
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CHW CLE DET HOU KCA
```



Now you can quickly see that Detroit is the team that has raised salaries most aggressively.

If we need to, we can easily convert a tidy dataset into something that looks like a table using the **spread()** function:

```
Salaries %>% filter( yearID > 2006 & lgID == "NL" ) %>%
    group_by( teamID, yearID ) %>%
    summarize( mean = dollar(mean(salary)) ) %>%
    spread( key=yearID, value=mean, sep="_" ) %>%
    select( 1:6 ) %>% na.omit() %>%
    pander
```

teamID	yearID_2007	yearID_2008	yearID_2009	yearID_2010	yearID_2011
ARI	\$1,859,555	\$2,364,383	\$2,812,141	\$2,335,314	\$1,986,660
ATL	\$3,117,530	\$3,412,189	\$3,335,385	\$3,126,802	\$3,346,257
$_{\rm CHN}$	\$3,691,494	\$4,383,179	\$5,392,360	\$5,429,963	\$5,001,893
CIN	\$2,210,483	\$2,647,061	\$3,198,196	\$2,760,059	\$2,531,571
COL	\$2,078,500	\$2,640,596	\$2,785,222	\$2,904,379	\$3,390,310
FLO	\$984,097	\$660,955	\$1,315,500	\$2,112,212	\$2,190,154
HOU	\$3,250,333	\$3,293,719	\$3,814,682	\$3,298,411	\$2,437,724
LAN	\$3,739,811	\$4,089,260	\$4,016,584	\$3,531,778	\$3,472,967
MIL	\$2,629,130	\$2,790,948	\$3,083,942	\$2,796,837	\$2,849,911
NYN	\$3,841,055	\$4,593,113	\$5,334,785	\$4,800,819	\$4,401,752
PHI	\$2,980,940	\$3,495,710	\$4,185,335	\$5,068,871	\$5,765,879
PIT	\$1,427,327	\$1,872,684	\$1,872,808	\$1,294,185	\$1,553,345
SDN	\$2,235,022	\$2,376,697	\$1,604,952	\$1,453,819	\$1,479,650
SFN	\$3,469,964	\$2,641,190	\$2,965,230	\$3,522,905	\$4,377,716
SLN	\$3,224,529	\$3,018,923	\$3,278,830	\$3,741,630	\$3,904,947
WAS	\$1,319,554	\$1,895,207	\$2,140,286	\$2,046,667	\$2,201,963

yearID	$teamID_ARI$	${\rm teamID_ATL}$	${\rm teamID_CHC}$	$teamID_CHN$	${\rm teamID_CIN}$
2007	\$1,859,555	\$3,117,530	NA	\$3,691,494	\$2,210,483
2008	\$2,364,383	\$3,412,189	NA	\$4,383,179	\$2,647,061
2009	\$2,812,141	\$3,335,385	NA	\$5,392,360	\$3,198,196
2010	\$2,335,314	\$3,126,802	NA	\$5,429,963	\$2,760,059
2011	\$1,986,660	\$3,346,257	NA	\$5,001,893	\$2,531,571
2012	\$2,733,512	\$2,856,205	NA	\$3,392,194	\$2,935,843
2013	\$3,004,400	\$3,254,501	NA	\$3,867,989	\$4,256,178
2014	\$3,763,904	\$4,067,042	NA	\$2,426,759	\$3,864,911
2015	\$2,034,250	\$2,990,885	NA	\$4,138,547	\$4,187,862
2016	\$3,363,041	\$2,362,010	\$5,312,678	NA	\$3,066,899