

# Panel Model Selection

```
library( dplyr )  
library( stargazer )
```

## OVERVIEW OF PANEL MODELS

```
# e <- rnorm(30)
# this one works well:
e <- c(-0.217265337508781, 0.0996074731855418, 0.0800275276849036,
-0.178488399013339, -0.496420526595239, -1.7168471976976, -0.405092050237224,
-0.115710342436631, -0.371092702457788, 0.822415948208485, 0.85135450577188,
0.171227422217835, 0.123875567283242, 1.40368293360846, 1.2581671356454,
0.62810338038335, -0.887705537863198, 0.757750779879804, 1.08763122728127,
0.575576369638848, 0.28709316244214, -0.375428732568683, 0.663417542179713,
1.04134503360736, -0.16471947215554, 2.4753832533224, -1.11870402193226,
0.32517135445685, -1.07233215548999, -0.0896477846333077)
```

```
id <- rep( 1:3, each=10 )
org.id <- factor(id)
```

```
# MODEL 1 - OLS
```

```
x1 <- 9 + 1:10 + 0*id
y1 <- 25 + x1 + 0*id + e
```

```
x <- x1
y <- y1
m1 <- lm( y ~ x )
```

```
# MODEL 2 - Random Effect
```

```
x2 <- 9 + 1:10 + 0*id
y2 <- 5 + x2 + 10*id + e
```

```
x <- x2
y <- y2
m2.ols <- lm( y ~ x )
m2.re <- lm( y ~ x + org.id )
```

```
# MODEL 3
```

```
x3 <- 1:10 + 5*id
y3 <- 5 + x3 + 10*id + e
```

```
x <- x3
y <- y3
m3.ols <- lm( y ~ x )
m3.fe <- lm( y ~ x + org.id )
```

```
# MODEL 4 - Dynamic
```

```
y4 <- y3[c(F,rep(T,9))]
y.lagged <- y3[c(rep(T,9),F)]
x4 <- x3[c(F,rep(T,9))]
```

```
x <- x4
```

```

y <- y4
m4 <- lm( y ~ x + y.lagged )

```

```

par( mfrow=c(1,3) )

```

```

plot( x1, y1, pch=19, col=org.id, cex=2,
      ylim=c(20,60), xlim=c(0,30),
      bty="n", axes=F,
      xlab="Fertilizer", ylab="Tons of Corn Per Acre",
      line=1.5, cex.lab=1.5 )
axis( side = 1, labels = FALSE )
axis( side = 2, labels = FALSE )
title( main="Scenario 1: All Farms Equal", line=1, cex.main=2 )

```

```

plot( x2, y2, pch=19, col=org.id, cex=2,
      ylim=c(20,60), xlim=c(1,30),
      bty="n", axes=F,
      xlab="Fertilizer", ylab="Tons of Corn Per Acre",
      line=1.5, cex.lab=1.5 )
axis( side = 1, labels = FALSE )
axis( side = 2, labels = FALSE )
title( main="Scenario 2: Land Quality Varies", line=1, cex.main=2 )

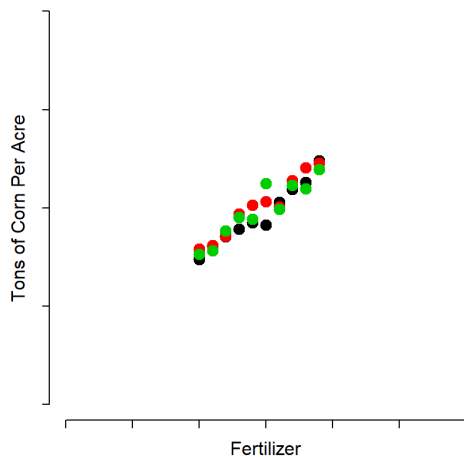
```

```

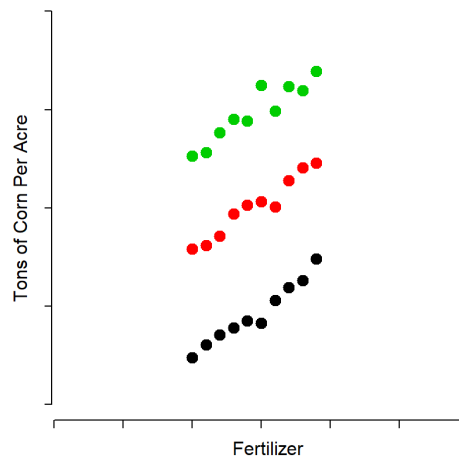
plot( x3, y3, pch=19, col=org.id, cex=2,
      ylim=c(20,60), xlim=c(1,30),
      bty="n", axes=F,
      xlab="Fertilizer", ylab="Tons of Corn Per Acre",
      line=1.5, cex.lab=1.5 )
axis( side = 1, labels = FALSE )
axis( side = 2, labels = FALSE )
title( main="Scenario 3: Land Management Varies", line=1, cex.main=2 )

```

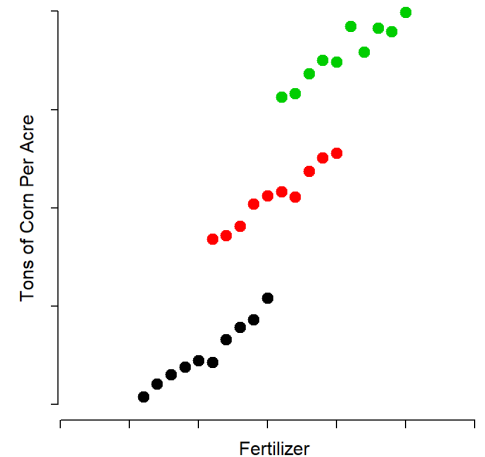
**Scenario 1: All Farms Equal**



**Scenario 2: Land Quality Varies**



**Scenario 3: Land Management Varies**



```

par( mfrow=c(1,3), mar=c(5.1, 4.1, 4.1, 15) )

plot( x1, y1, pch=19, col=gray(0.5,0.5), cex=3,
      ylim=c(20,70), xlim=c(0,25),
      bty="n", axes=F,
      xlab="Pooled Model is UNBIASED + EFFICIENT", ylab="",
      line=1.5, cex.lab=1.5, col.lab="gray20", cex.lab=1.5 )
axis( side = 1, labels = FALSE )
axis( side = 2, labels = FALSE )
title( main="Scenario 1", line=1, cex.main=2 )
abline( m1, lwd=2 )
b <- m1$coefficients
mtext( " Pooled Model", side=4, outer=F, at=b[1]+25*b[2]+3, cex=1.5, las=2 )

plot( x2, y2, pch=19, col=gray(0.5,0.5), cex=3,
      ylim=c(20,70), xlim=c(1,25),
      bty="n", axes=F,
      xlab="Pooled Model is UNBIASED + INEFFICIENT", ylab="",
      line=1.5, cex.lab=1.5, col.lab="gray20", cex.lab=1.5 )
axis( side = 1, labels = FALSE )
axis( side = 2, labels = FALSE )
title( main="Scenario 2", line=1, cex.main=2 )
abline( m2.ols, lwd=2 )
for(i in 1:3){ abline( lm(y2[id==i]~x2[id==i]), lty=3, lwd=3, col="darkgray" ) }

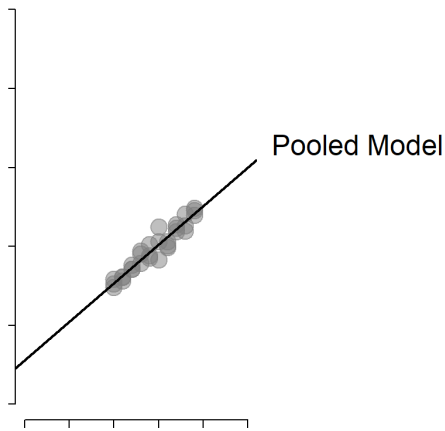
# mtext( " OLS Slope", side=4, outer=F, at=m2.ols$fitted.values[30]+3, cex=1.5, las=2 )
b <- m2.re$coefficients
mtext( " RE Slope", side=4, outer=F, at=b[1]+25*b[2]+2, cex=1, las=2 )
mtext( " Pooled Model", side=4, outer=F, at=b[1]+25*b[2]+b[3]+2, cex=1.5, las=2 )
mtext( " RE Slope", side=4, outer=F, at=b[1]+25*b[2]+b[4]+2, cex=1, las=2 )

plot( x3, y3, pch=19, col=gray(0.5,0.5), cex=3,
      ylim=c(20,70), xlim=c(1,25),
      bty="n", axes=F,
      xlab="Pooled Model is BIASED + INEFFICIENT", ylab="",
      line=1.5, cex.lab=1.5, col.lab="gray20", cex.lab=1.5 )
axis( side = 1, labels = FALSE )
axis( side = 2, labels = FALSE )
title( main="Scenario 3", line=1, cex.main=2 )
abline( m3.ols, lwd=2 )
for(i in 1:3){ abline( lm(y3[id==i]~x3[id==i]), lty=3, lwd=3, col="darkgray" ) }

mtext( " Pooled Model", side=4, outer=F, at=m3.ols$fitted.values[30]+5, cex=1.5, las=2 )
b <- m3.fe$coefficients
mtext( " FE Slope", side=4, outer=F, at=b[1]+25*b[2]+2, cex=1, las=2 )
mtext( " FE Slope", side=4, outer=F, at=b[1]+25*b[2]+b[3]+2, cex=1, las=2 )
mtext( " FE Slope", side=4, outer=F, at=b[1]+25*b[2]+b[4]+2, cex=1, las=2 )

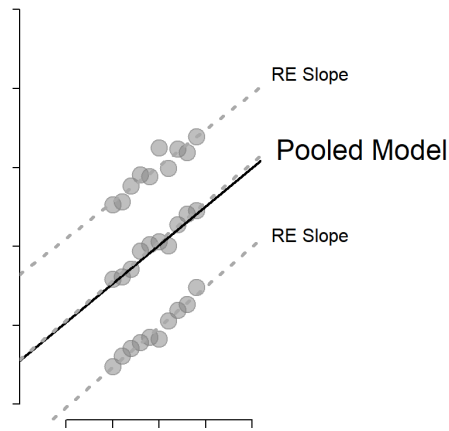
```

Scenario 1



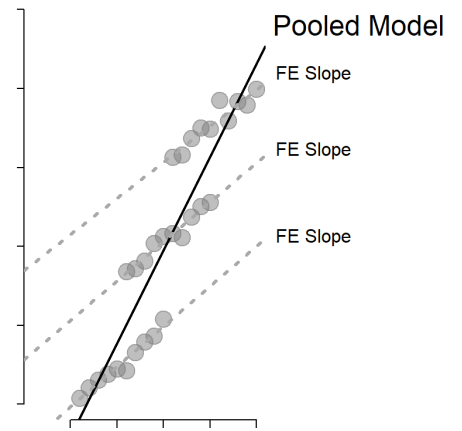
Pooled Model is UNBIASED + EFFICIENT

Scenario 2



Pooled Model is UNBIASED + INEFFICIENT

Scenario 3



Pooled Model is BIASED + INEFFICIENT

```
stargazer( m1, m2.ols, m2.re, m3.ols, m3.fe, m4,
  type="text",
  intercept.bottom=FALSE,
  column.labels = c("Scenario 1", "Scenario 2", "Scenario 3"),
  column.separate = c(1,2,3),
  add.lines = list(c("True Slope",
    "1","1","1","1","1","1"),
    c("Fixed Effects?","NO","NO","YES","NO","YES","NO"),
    c("Dynamic Model","NO","NO","NO","NO","NO","YES") ),
  omit=c("Constant","org.id"),
  omit.stat=c("f","ser","adj.rsq","rsq","n"),
  dep.var.labels.include = FALSE,
  dep.var.caption = "",
  digits=2 )
```

```
stargazer( m1, m2.ols, m2.re, m3.ols, m3.fe, m4,
  type="html",
  intercept.bottom=FALSE,
  column.labels = c("Scenario 1", "Scenario 2", "Scenario 3"),
  column.separate = c(1,2,3),
  add.lines = list(c("True Slope",
    "1","1","1","1","1","1"),
    c("Fixed Effects?","NO","NO","YES","NO","YES","NO"),
    c("Dynamic Model","NO","NO","NO","NO","NO","YES") ),
  omit=c("Constant","org.id"),
  omit.stat=c("f","ser","adj.rsq","rsq","n"),
  dep.var.labels.include = FALSE,
  dep.var.caption = "",
  digits=2,
  out="Baseline.doc")
```

Scenario 1

Scenario 2

Scenario 3

(1)

(2)

(3)

(4)

(5)

(6)

x	0.98 <sup>***</sup>	0.98 <sup>*</sup>	0.98 <sup>***</sup>	2.36 <sup>***</sup>	0.98 <sup>***</sup>	0.13
	(0.06)	(0.55)	(0.05)	(0.19)	(0.05)	(0.14)
y.lagged						0.94 <sup>***</sup>
						(0.05)
True Slope	1	1	1	1	1	1
Fixed Effects?	NO	NO	YES	NO	YES	NO
Dynamic Model	NO	NO	NO	NO	NO	YES
Note:				<i>p</i> <0.1; <b><i>p</i></b> <0.05; <i>p</i> <0.01		

## TIME EFFECTS

```

time.effect <- rep( c(-1,1,2,3,2,1,0,-1,-2,0), 3 )
e.new <-
  c(0.717752254188994, 1.46351044875319, 0.545085270634742, 0.398709885310457,
    0.509880154168709, 1.12550062156401, -1.38757100156204, 0.199452611009322,
    0.909229008764255, -0.191497620829187, 1.92890813350955, -0.195505507481137,
    -0.206714709910741, 0.700838318157092, -0.651743403883677, 0.743503199376542,
    1.07098487453718, -0.298184876026821, -0.322110555305533, 1.33356616169561,
    2.22524178992114, 0.34393523837206, -0.00781897594284145, -0.454827433881235,
    1.91734908738423, 2.51779087685677, 0.066017323821991, 0.345542463689957,
    0.258480442909562, 0.415665805192596)
e2 <- e.new + time.effect
time <- factor( rep( 2001:2010, 3 ) )

```

*# MODEL ZERO - NO TIME EFFECTS*

```

x0 <- 9 + 1:10 + 0*id
y0 <- 25 + x1 + 0*id + e.new

```

```

x <- x0
y <- y0
m0.ols <- lm( y ~ x )
m0.time <- lm( y ~ x + time )

```

*# MODEL 1 - OLS*

```

x1 <- 9 + 1:10 + 0*id
y1 <- 25 + x1 + 0*id + e2

```

```

x <- x1
y <- y1
m1.ols <- lm( y ~ x )
m1.time <- lm( y ~ x + time )

```

*# MODEL 2 - Random Effect*

```

x2 <- 9 + 1:10 + 0*id
y2 <- 5 + x2 + 10*id + e2

```

```

x <- x2
y <- y2
m2.ols <- lm( y ~ x )
m2.re <- lm( y ~ x + org.id )
m2.time <- lm( y ~ x + org.id + time )

```

*# MODEL 3*

```

x3 <- 1:10 + 5*id
y3 <- 5 + x3 + 10*id + e2

```

```

x <- x3
y <- y3
m3.ols <- lm( y ~ x )

```

```
m3.fe <- lm( y ~ x + org.id )
m3.time <- lm( y ~ x + org.id + time )
```

```
# MODEL 4 - Dynamic
```

```
y4 <- y3[c(F,rep(T,9))]
y.lagged <- y3[c(rep(T,9),F)]
x4 <- x3[c(F,rep(T,9))]
time2 <- factor( rep( 2002:2010, 3 ) )

x <- x4
y <- y4
m4 <- lm( y ~ x + y.lagged )
m4.time <- lm( y ~ x + y.lagged + time2 )
```

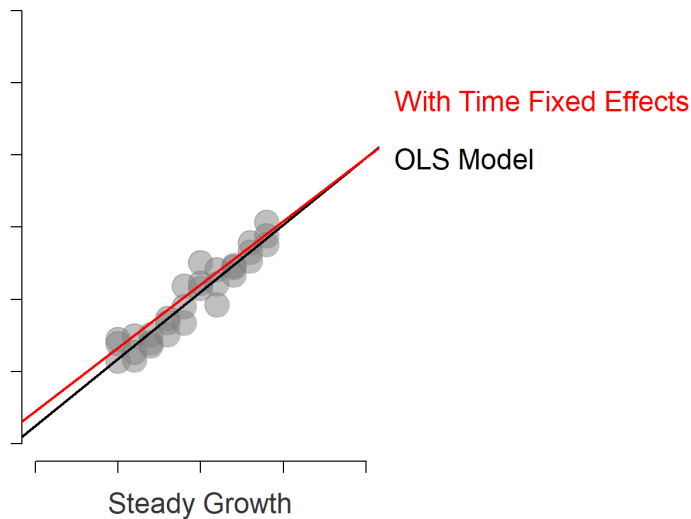
```
par( mar=c(5.1, 4.1, 4.1, 15), mfcol=c(1,2) )
```

```
plot( x0[1:30], y0[1:30], pch=19, col=gray(0.5,0.5), cex=3,
      ylim=c(30,60), xlim=c(5,25),
      bty="n", axes=F,
      xlab="Steady Growth", ylab="",
      line=1.5, cex.lab=1.5, col.lab="gray20", cex.lab=1.5 )
axis( side = 1, labels = FALSE )
axis( side = 2, labels = FALSE )
title( main="Case A: No Time Effects", line=1, cex.main=2 )
abline( m0.ols, lwd=2 )
b <- m0.ols$coefficients
mtext( " OLS Model", side=4, outer=F, at=b[1]+25*b[2]-0, cex=1.5, las=2 )
abline( m0.time, col="red", lwd=2 )
mtext( " With Time Fixed Effects", side=4, outer=F, at=b[1]+25*b[2]+4, cex=1.5, las=2, col="red" )
```

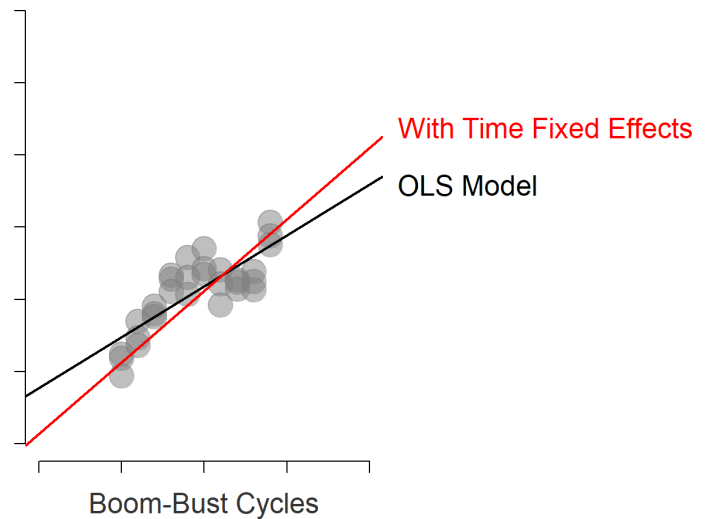
```
plot( x1[1:30], y1[1:30], pch=19, col=gray(0.5,0.5), cex=3,
      ylim=c(30,60), xlim=c(5,25),
      bty="n", axes=F,
      xlab="Boom-Bust Cycles", ylab="",
      line=1.5, cex.lab=1.5, col.lab="gray20", cex.lab=1.5 )
axis( side = 1, labels = FALSE )
axis( side = 2, labels = FALSE )
title( main="Case B: Time Effects", line=1, cex.main=2 )
abline( m1.ols, lwd=2 )
b <- m1.ols$coefficients
mtext( " OLS Model", side=4, outer=F, at=b[1]+25*b[2]-0, cex=1.5, las=2 )
abline( m1.time, col="red", lwd=2 )
mtext( " With Time Fixed Effects", side=4, outer=F, at=b[1]+25*b[2]+4, cex=1.5, las=2, col="red" )
```



## Case A: No Time Effects



## Case B: Time Effects



```
stargazer( m1.ols, m1.time, m2.re, m2.time, m3.fe, m3.time,
  type="text",
  intercept.bottom=FALSE,
  column.labels = c("Scenario 1", "Scenario 2", "Scenario 3"),
  column.separate = c(2,2,2),
  add.lines = list(c("True Slope",
    "1","1","1","1","1","1"),
    c("Org Fixed Effects?",
    "YES","YES","YES","YES","YES","YES"),
    c("Time Fixed Effects?",
    "NO","YES","NO","YES","NO","YES") ),
  omit=c("org.id","time","time2"),
  omit.stat=c("f","ser","adj.rsq","rsq","n"),
  dep.var.labels.include = FALSE,
  dep.var.caption = "",
  digits=2 )
```

```
stargazer( m1, m1.time, m2.re, m2.time, m3.fe, m3.time,
  type="html",
  intercept.bottom=FALSE,
  column.labels = c("Scenario 1", "Scenario 2", "Scenario 3"),
  column.separate = c(2,2,2),
  add.lines = list(c("True Slope",
    "1","1","1","1","1","1"),
    c("Org Fixed Effects?",
    "YES","YES","YES","YES","YES","YES"),
    c("Time Fixed Effects?",
    "NO","YES","NO","YES","NO","YES") ),
  omit=c("Constant","org.id","time","time2"),
  omit.stat=c("f","ser","adj.rsq","rsq","n"),
  dep.var.labels.include = FALSE,
  dep.var.caption = "",
  digits=2,
  out="TimeFixedEffects.doc")
```

	Scenario 1		Scenario 2		Scenario 3	
	(1)	(2)	(3)	(4)	(5)	(6)
x	0.98 <sup>***</sup>	0.99 <sup>***</sup>	0.70 <sup>***</sup>	0.99 <sup>***</sup>	0.70 <sup>***</sup>	0.99 <sup>***</sup>
	(0.06)	(0.08)	(0.10)	(0.08)	(0.10)	(0.08)
True Slope	1	1	1	1	1	1
Org Fixed Effects?	YES	YES	YES	YES	YES	YES
Time Fixed Effects?	NO	YES	NO	YES	NO	YES
<i>Note:</i>				<i>p</i> <0.1; <b><i>p</i></b> <0.05; <i>p</i> <0.01		

```

par( mfrow=c(1,3) )

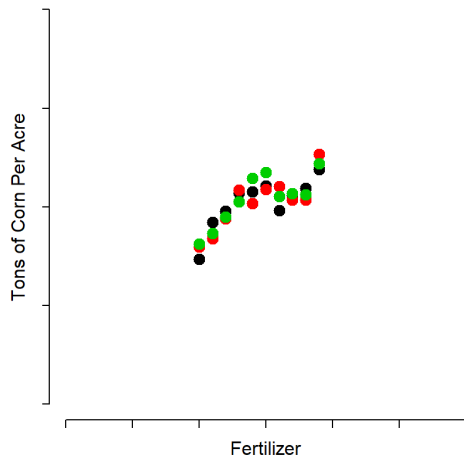
plot( x1, y1, pch=19, col=org.id, cex=2,
      ylim=c(20,60), xlim=c(0,30),
      bty="n", axes=F,
      xlab="Fertilizer", ylab="Tons of Corn Per Acre",
      line=1.5, cex.lab=1.5 )
axis( side = 1, labels = FALSE )
axis( side = 2, labels = FALSE )
title( main="Scenario 1: All Farms Equal", line=1, cex.main=2 )

plot( x2, y2, pch=19, col=org.id, cex=2,
      ylim=c(20,60), xlim=c(1,30),
      bty="n", axes=F,
      xlab="Fertilizer", ylab="Tons of Corn Per Acre",
      line=1.5, cex.lab=1.5 )
axis( side = 1, labels = FALSE )
axis( side = 2, labels = FALSE )
title( main="Scenario 2: Land Quality Varies", line=1, cex.main=2 )

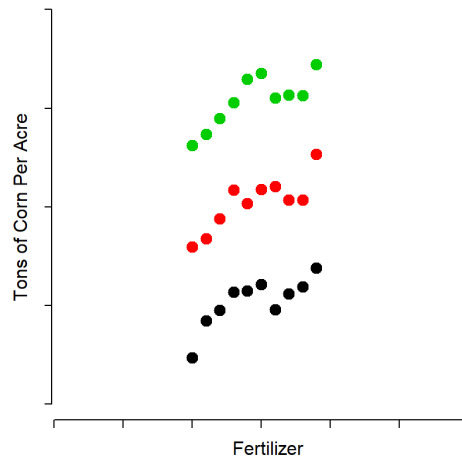
plot( x3, y3, pch=19, col=org.id, cex=2,
      ylim=c(20,60), xlim=c(1,30),
      bty="n", axes=F,
      xlab="Fertilizer", ylab="Tons of Corn Per Acre",
      line=1.5, cex.lab=1.5 )
axis( side = 1, labels = FALSE )
axis( side = 2, labels = FALSE )
title( main="Scenario 3: Management Varies", line=1, cex.main=2 )

```

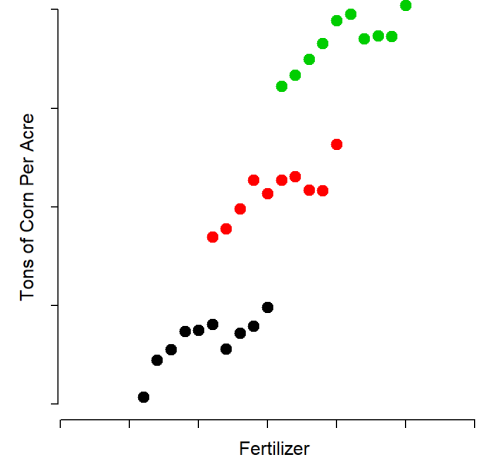
Scenario 1: All Farms Equal



Scenario 2: Land Quality Varies



Scenario 3: Management Varies



# FIXED EFFECTS BY DE-MEANING DATA

*# MODEL 1 - OLS*

```
x1 <- 9 + 1:10 + 0*id
y1 <- 25 + x1 + 0*id + e
```

```
x <- x1
y <- y1
m1.ols <- lm( y ~ x )
```

*# MODEL 3*

```
x3 <- 1:10 + 5*id
y3 <- 5 + x3 + 10*id + e
```

```
x3.mean <- ave( x3, org.id )
x3.centered <- x3 - x3.mean
```

```
y3.mean <- ave( y3, org.id )
y3.centered <- y3 - y3.mean
```

```
x <- x3
y <- y3
m3.ols <- lm( y ~ x )
m3.fe <- lm( y ~ x + org.id )
```

```
x <- x3.centered
y <- y3.centered
m3.centered <- lm( y ~ x )
```

```
stargazer( m1.ols, m3.fe, m3.centered,
  type="text",
  intercept.bottom=FALSE,
  column.labels = c("OLS on Data w No Groups",
                    "FE on Data w Groups",
                    "OLS on De-Meaned Data"),
  column.separate = c(1,1,1),
  add.lines = list(c("True Slope",
                    "1","1","1") ),
  omit=c("Constant","org.id","time","time2"),
  omit.stat=c("f","ser","adj.rsq","rsq","n"),
  dep.var.labels.include = FALSE,
  dep.var.caption = "",
  digits=2 )
```

```
stargazer( m1.ols, m3.fe, m3.centered,
  type="html",
  intercept.bottom=FALSE,
  column.labels = c("OLS on Data <br> w No Groups",
                    "FE on Data <br> w Groups",
                    "OLS on <br> De-Meaned Data"),
  column.separate = c(1,1,1),
  add.lines = list(c("True Slope",
                    "1","1","1") ),
  omit=c("Constant","org.id","time","time2"),
  omit.stat=c("f","ser","adj.rsq","rsq","n"),
  dep.var.labels.include = FALSE,
  dep.var.caption = "",
  digits=2,
  out="DemeanedData.doc" )
```

	OLS on Data w No Groups	FE on Data w Groups	OLS on De-Meaned Data
	(1)	(2)	(3)
x	0.98*** (0.06)	0.98*** (0.05)	0.98*** (0.05)
True Slope	1	1	1

*Note:*

$p < 0.1$ ;  $p < 0.05$ ;  $p < 0.01$

## ## GRAPHICS

```
par( mfrow=c(1,3) )

plot( x1, y1, pch=19, col=gray(0.5,0.5), cex=3,
      ylim=c(34,46), xlim=c(mean(x1)-5,mean(x1)+5),
      bty="n", axes=F,
      xlab="", ylab="",
      cex.lab=1.5 )
axis( side = 1, cex.axis=2, at=c(10.5,12.5,14.5,16.5,18.5), labels=c(10,12,14,16,18) )
axis( side = 2, cex.axis=2 )
title( main="Scenario 1: No Group Structure)", line=1, cex.main=2 )
abline( h=40, lty=3, col="gray", lwd=3 )
abline( v=mean(x), lty=3, col="gray", lwd=3 )
text( 17, 39, expression( paste( "( ", bar( x ), " , ", bar( y ), " )" ) ),
      cex=2, col="black" )

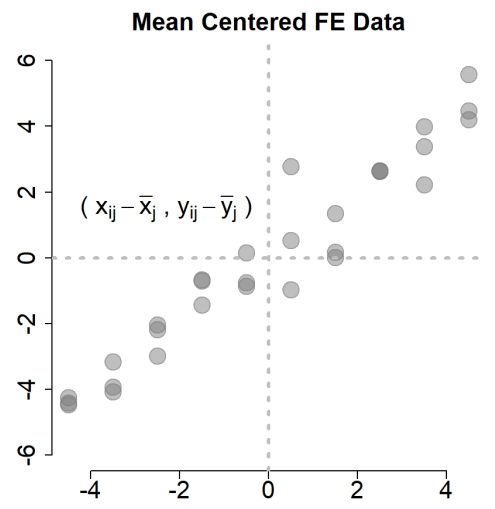
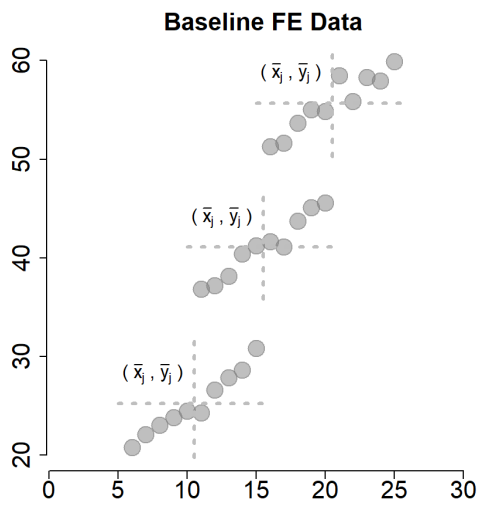
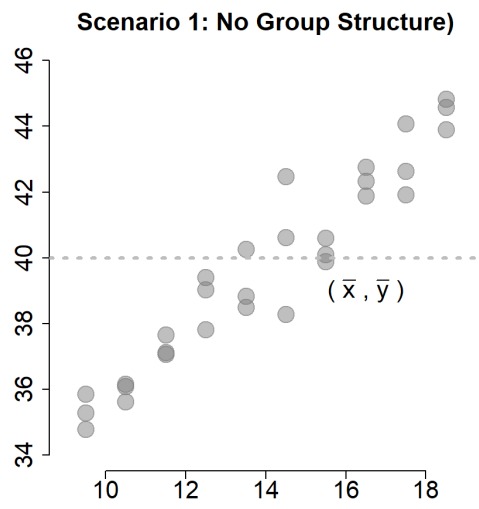
plot( x3, y3,
      pch=19, col=gray(0.5,0.5), cex=3,

      ylim=c(20,60), xlim=c(1,30),
      bty="n", axes=F,
      xlab="", ylab="",
      cex.lab=1.5 )
axis( side = 1, cex.axis=2 )
axis( side = 2, cex.axis=2 )
title( main="Baseline FE Data", line=1, cex.main=2 )
for( i in 1:3 )
{
  segments( x0=min(x3[id==i])-1, x1=max(x3[id==i])+1,
            y0=mean(y3[id==i]),
            lty=3, col="gray", lwd=3 )

  segments( x0=mean(x3[id==i]),
            y0=min(y3[id==i])-1, y1=max(y3[id==i])+1,
            lty=3, col="gray", lwd=3 )

  text( mean(x3[id==i])-3, mean(y3[id==i])+3,
        expression( paste( "( ", bar( x )[j], " , ", bar( y )[j], " )" ) ),
        cex=1.5, col="black" )
}

plot( x3.centered, y3.centered,
      pch=19, col=gray(0.5,0.5), cex=3,
      ylim=c(-6,6),
      bty="n", axes=F,
      xlab="", ylab="",
      cex.lab=1.5 )
axis( side = 1, cex.axis=2 )
axis( side = 2, cex.axis=2 )
title( main="Mean Centered FE Data", line=1, cex.main=2 )
abline( h=0, lty=3, col="gray", lwd=3 )
abline( v=0, lty=3, col="gray", lwd=3 )
text( -2.3, 1.5, expression( paste( "( ", x[ij] - bar( x )[j], " , ", y[ij] - bar( y )[j], " )" ) ),
      cex=2, col="black" )
```



# TAXONOMY OF BIAS FROM GROUP STRUCTURE

```
# SIMPSON'S PARADOX
```

```
# MODEL 1 - OLS
```

```
x1  <- 9 + 1:10 + 0*id  
y1  <- 25 + x1 + 0*id + e
```

```
x <- x1  
y <- y1  
m1 <- lm( y ~ x )
```

```
# MODEL 2 - Random Effect
```

```
x2  <- 9 + 1:10 + 0*id  
y2  <- 5 + x2 + 10*id + e
```

```
x <- x2  
y <- y2  
m2.ols <- lm( y ~ x )  
m2.re <- lm( y ~ x + org.id )
```

```
# FE CASE 1
```

```
x11  <- 1:10 + 5*id  
y11  <- 5 + x11 + 10*id + e  
  
x <- x11  
y <- y11  
m11.ols <- lm( y ~ x )  
m11.fe <- lm( y ~ x + org.id )
```

```
# FE CASE 2
```

```
x12  <- 1:10 + 5*id  
y12  <- 10 + 15*id + e  
  
x <- x12  
y <- y12  
m12.ols <- lm( y ~ x )  
m12.fe  <- lm( y ~ x + org.id )
```

```
# FE CASE 3
```

```
x13  <- 1:10 + 5*id  
y13  <- 60 + x13 - 18*id + e  
  
x <- x13  
y <- y13  
m13.ols <- lm( y ~ x )  
m13.fe  <- lm( y ~ x + org.id )
```

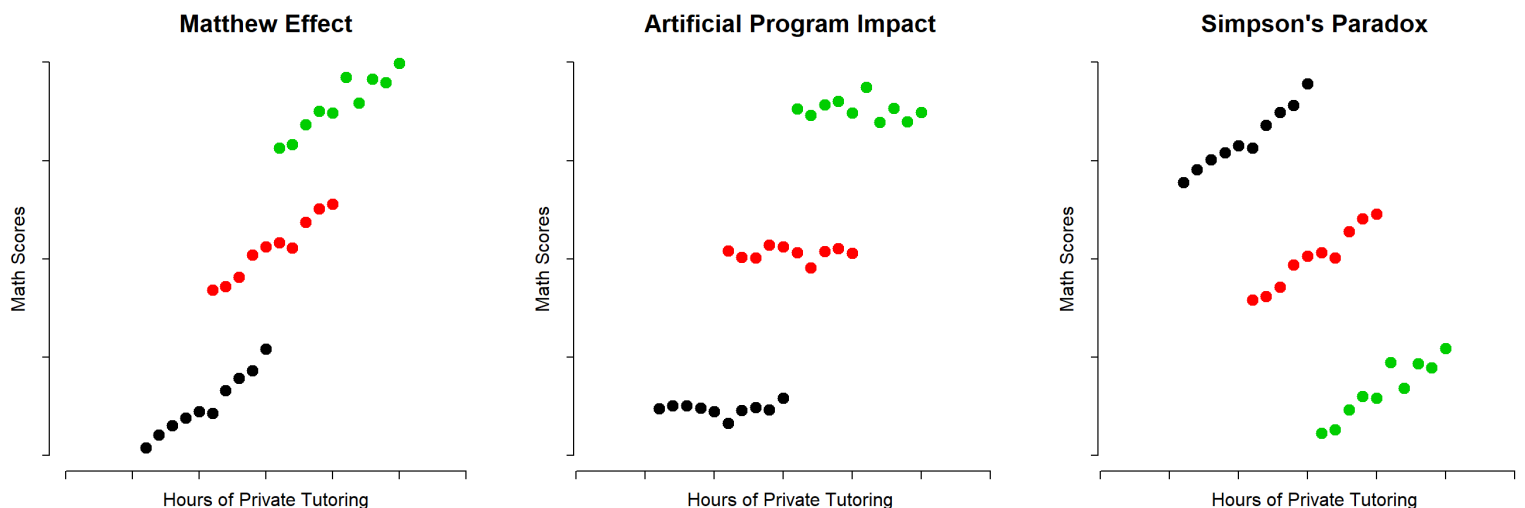
```
## GRAPHICS
```

```
par( mfrow=c(1,3) )
```

```
plot( x11, y11, pch=19, col=org.id, cex=2,
      ylim=c(20,60), xlim=c(0,30),
      bty="n", axes=F,
      xlab="Hours of Private Tutoring", ylab="Math Scores",
      line=1.5, cex.lab=1.5 )
axis( side = 1, labels = FALSE )
axis( side = 2, labels = FALSE )
title( main="Matthew Effect", line=1, cex.main=2 )
```

```
plot( x12, y12, pch=19, col=org.id, cex=2,
      ylim=c(20,60), xlim=c(1,30),
      bty="n", axes=F,
      xlab="Hours of Private Tutoring", ylab="Math Scores",
      line=1.5, cex.lab=1.5 )
axis( side = 1, labels = FALSE )
axis( side = 2, labels = FALSE )
title( main="Artificial Program Impact", line=1, cex.main=2 )
```

```
plot( x13, y13, pch=19, col=org.id, cex=2,
      ylim=c(20,60), xlim=c(1,30),
      bty="n", axes=F,
      xlab="Hours of Private Tutoring", ylab="Math Scores",
      line=1.5, cex.lab=1.5 )
axis( side = 1, labels = FALSE )
axis( side = 2, labels = FALSE )
title( main="Simpson's Paradox", line=1, cex.main=2 )
```





###

```
par( mfrow=c(1,3), mar=c(5.1, 4.1, 4.1, 15) )

plot( x11, y11, pch=19, col=gray(0.5,0.5), cex=3,
      ylim=c(20,70), xlim=c(1,25),
      bty="n", axes=F,
      xlab="Program Impact Over-Stated", ylab="",
      line=1.5, cex.lab=1.5, col.lab="gray50", cex.lab=1.5 )
axis( side = 1, labels = FALSE )
axis( side = 2, labels = FALSE )
title( main="Matthew Effect", line=1, cex.main=2 )
abline( m11.ols, lwd=2 )
for(i in 1:3){ abline( lm(y11[id==i]~x11[id==i]), lty=3, lwd=3, col="darkgray" ) }

mtext( " Pooled Model", side=4, outer=F, at=m11.ols$fitted.values[30]+5, cex=1.5, las=2 )
b <- m11.fe$coefficients
mtext( " FE Slope", side=4, outer=F, at=b[1]+25*b[2]+2, cex=1, las=2 )
mtext( " FE Slope", side=4, outer=F, at=b[1]+25*b[2]+b[3]+2, cex=1, las=2 )
mtext( " FE Slope", side=4, outer=F, at=b[1]+25*b[2]+b[4]+2, cex=1, las=2 )

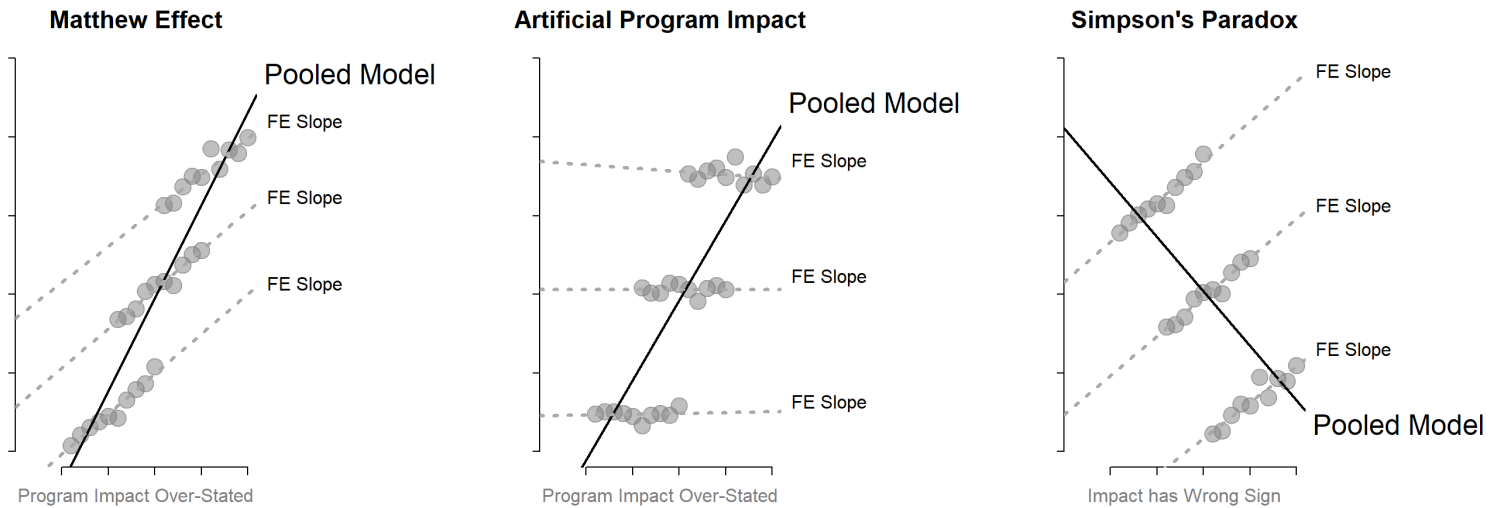
plot( x12, y12, pch=19, col=gray(0.5,0.5), cex=3,
      ylim=c(20,70), xlim=c(1,25),
      bty="n", axes=F,
      xlab="Program Impact Over-Stated", ylab="",
      line=1.5, cex.lab=1.5, col.lab="gray50", cex.lab=1.5 )
axis( side = 1, labels = FALSE )
axis( side = 2, labels = FALSE )
title( main="Artificial Program Impact", line=1, cex.main=2 )
abline( m12.ols, lwd=2 )
for(i in 1:3){ abline( lm(y12[id==i]~x12[id==i]), lty=3, lwd=3, col="darkgray" ) }

mtext( " Pooled Model", side=4, outer=F, at=m12.ols$fitted.values[30]+5, cex=1.5, las=2 )
b <- m12.fe$coefficients
mtext( " FE Slope", side=4, outer=F, at=b[1]+25*b[2]+2, cex=1, las=2 )
mtext( " FE Slope", side=4, outer=F, at=b[1]+25*b[2]+b[3]+2, cex=1, las=2 )
mtext( " FE Slope", side=4, outer=F, at=b[1]+25*b[2]+b[4]+2, cex=1, las=2 )

plot( x13, y13, pch=19, col=gray(0.5,0.5), cex=3,
      ylim=c(20,70), xlim=c(1,25),
      bty="n", axes=F,
      xlab="Impact has Wrong Sign", ylab="",
      line=1.5, cex.lab=1.5, col.lab="gray50", cex.lab=1.5 )
axis( side = 1, labels = FALSE )
axis( side = 2, labels = FALSE )
title( main="Simpson's Paradox", line=1, cex.main=2 )
abline( m13.ols, lwd=2 )
for(i in 1:3){ abline( lm(y13[id==i]~x13[id==i]), lty=3, lwd=3, col="darkgray" ) }

mtext( " Pooled Model", side=4, outer=F, at=m13.ols$fitted.values[30]-3, cex=1.5, las=2 )
b <- m13.fe$coefficients
mtext( " FE Slope", side=4, outer=F, at=b[1]+25*b[2]+2, cex=1, las=2 )
```

```
mtext( " FE Slope", side=4, outer=F, at=b[1]+25*b[2]+b[3]+2, cex=1, las=2 )
mtext( " FE Slope", side=4, outer=F, at=b[1]+25*b[2]+b[4]+2, cex=1, las=2 )
```



```
stargazer( m11.ols, m11.fe, m12.ols, m12.fe, m13.ols, m13.fe,
  type="text",
  intercept.bottom=TRUE,
  column.labels = c("Matthew Effect",
    "Artificial Impact",
    "Simpson's Paradox"),
  column.separate = c(2,2,2),
  add.lines = list(c("True Slope",
    "1","1","0","0","1","1"),
    c("Fixed Effects?",
    "NO","YES","NO","YES","NO","YES") ),
  omit=c("Constant","org.id","time","time2"),
  omit.stat=c("f","ser","adj.rsq","rsq","n"),
  dep.var.labels.include = FALSE,
  dep.var.caption = "",
  digits=2 )
```

```
stargazer( m11.ols, m11.fe, m12.ols, m12.fe, m13.ols, m13.fe,
  type="html",
  intercept.bottom=TRUE,
  column.labels = c("Matthew Effect",
    "Artificial Impact",
    "Simpson's Paradox"),
  column.separate = c(2,2,2),
  add.lines = list(c("True Slope",
    "1","1","0","0","1","1"),
    c("Fixed Effects?",
    "NO","YES","NO","YES","NO","YES") ),
  omit=c("Constant","org.id","time","time2"),
  omit.stat=c("f","ser","adj.rsq","rsq","n"),
  dep.var.labels.include = FALSE,
  dep.var.caption = "",
  digits=2,
  out="BiasModels.doc")
```

	Matthew Effect		Artificial Impact		Simpson's Paradox	
	(1)	(2)	(3)	(4)	(5)	(6)
x	2.36 <sup>***</sup>	0.98 <sup>***</sup>	2.03 <sup>***</sup>	-0.02	-1.39 <sup>***</sup>	0.98 <sup>***</sup>
	(0.19)	(0.05)	(0.27)	(0.05)	(0.32)	(0.05)
True Slope	1	1	0	0	1	1
Fixed Effects?	NO	YES	NO	YES	NO	YES

*Note:*  $p<0.1$ ;  **$p<0.05$** ;  $p<0.01$