BIAS FROM SPECIFICATION OR MEASUREMENT

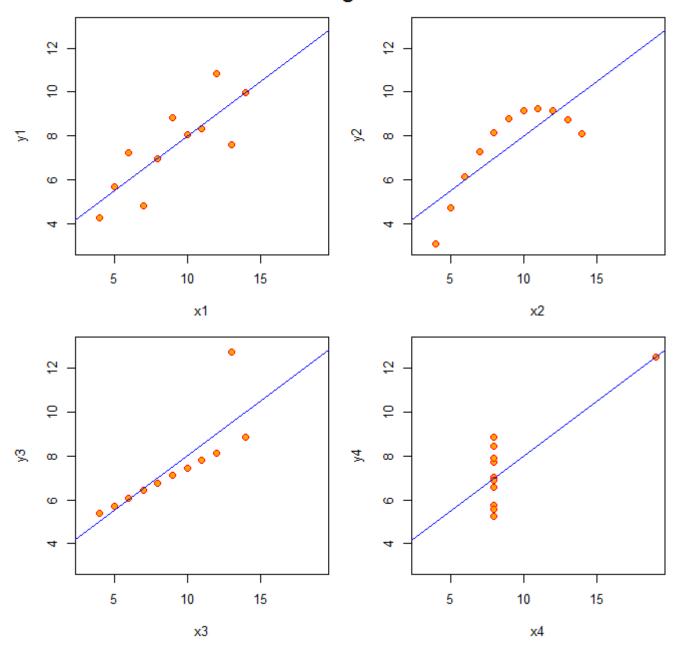
ANSCOMBE'S QUARTET A LESSON IN MODEL FIT

Anscombe's Quartet

	x1	y1	x2	y2	х3	у3	x4	y4
1	10	8.04	10	9.14	10	7.46	8	6.58
2	8	6.95	8	8.14	8	6.77	8	5.76
3	13	7.58	13	8.74	13	12.74	8	7.71
4	9	8.81	9	8.77	9	7.11	8	8.84
5	11	8.33	11	9.26	11	7.81	8	8.47
6	14	9.96	14	8.1	14	8.84	8	7.04
7	6	7.24	6	6.13	6	6.08	8	5.25
8	4	4.26	4	3.1	4	5.39	19	12.5
9	12	10.84	12	9.13	12	8.15	8	5.56
10	7	4.82	7	7.26	7	6.42	8	7.91
11	5	5.68	5	4.74	5	5.73	8	6.89
Mean	9	7.5	9	7.5	9	7.5	9	7.5
Variance	11	4.12	11	4.12	11	4.12	11	4.12
Correlation	0.816		0.816		0.816		0.816	
Regression	y = 3 + 0.5x		y = 3 + 0.5x		y = 3 + 0.5x		y = 3 + 0.5x	

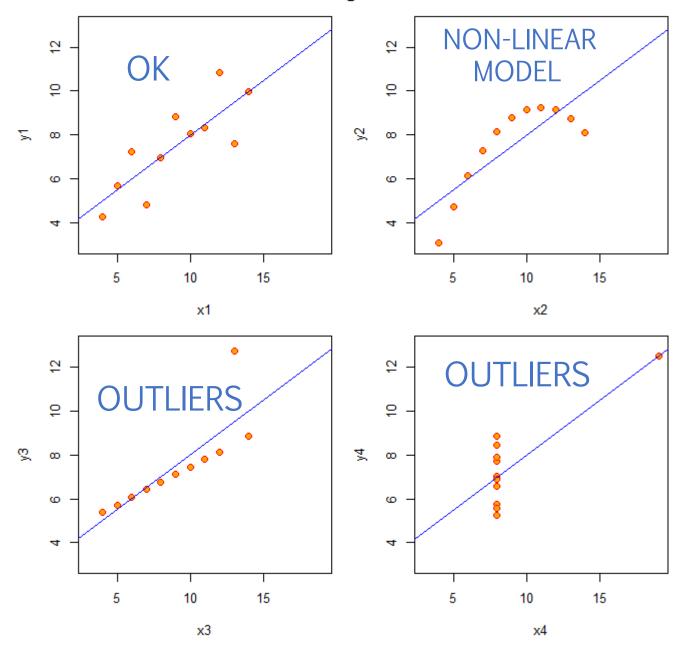
Four datasets that produce IDENTICAL descriptive stats, correlations, and regression models

Anscombe's 4 Regression data sets



BUT THEY ARE VERY DIFFERENT RELATIONSHIPS!

Anscombe's 4 Regression data sets

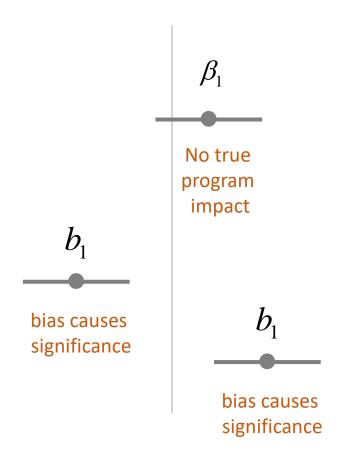


Anscombe's Quartet is often cited because (a) whoever created this example is a genius, and (b) it is a vivid demonstration of causes and consequences of SPECIFICATION BIAS.

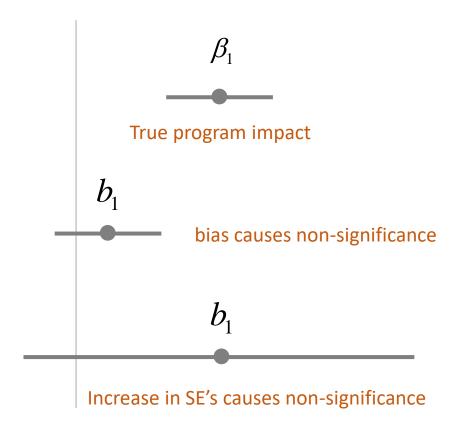
We will consider what happens to slopes when outliers are present, or we use a linear specification when the relationship is non-linear.

CLASSES OF INFERENTIAL FAILURE TYPE I AND TYPE II ERRORS

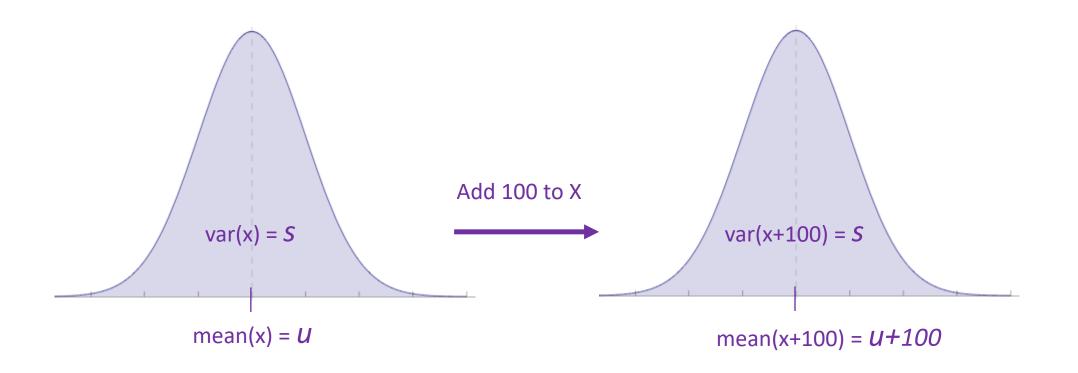
TYPE I ERROR FALSE POSITIVE CLAIMING PROGRAM HAS IMPACT WHEN IT DOESN'T



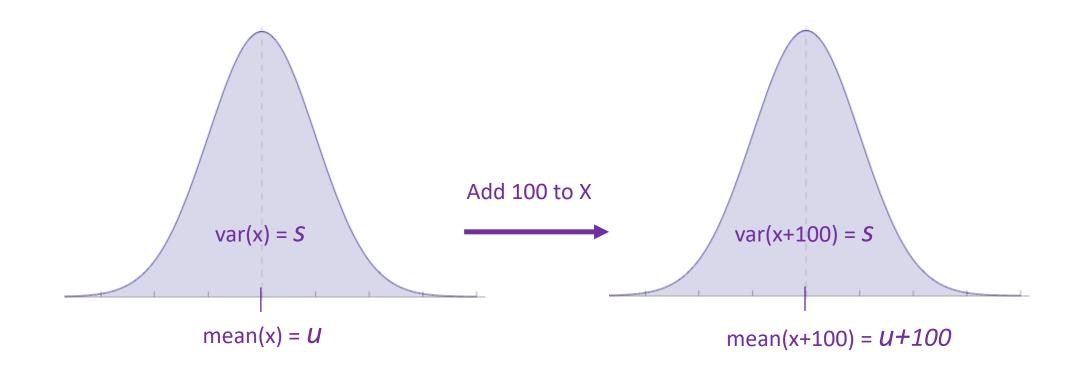
TYPE II ERROR
FALSE NEGATIVE
FAILING TO IDENTIFY TRUE
PROGRAM IMPACT

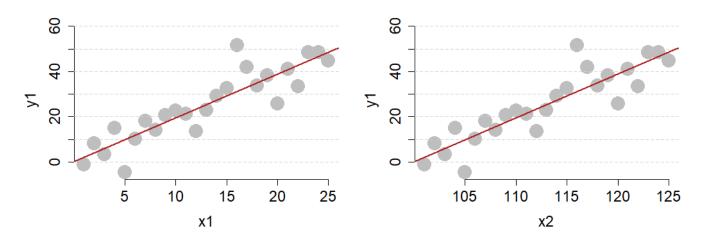


IMPLICATIONS OF MEASUREMENT ERROR

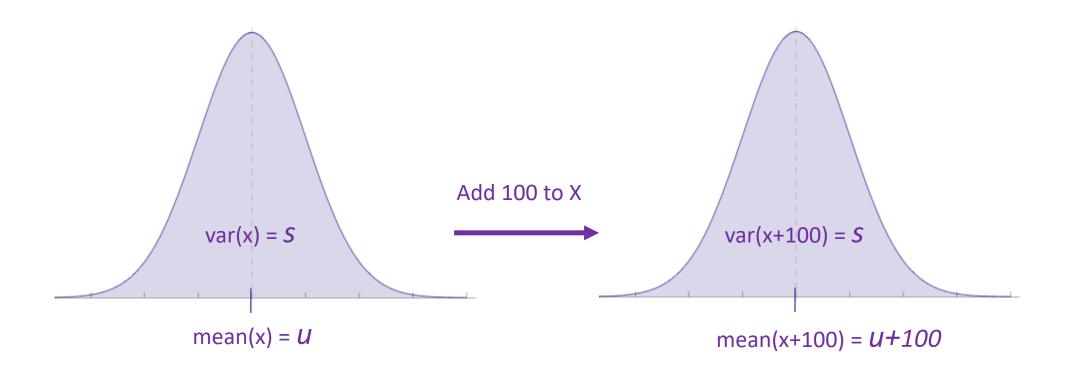


"Linear Transformations" X2 = X1 + 100Variance of X is unchanged





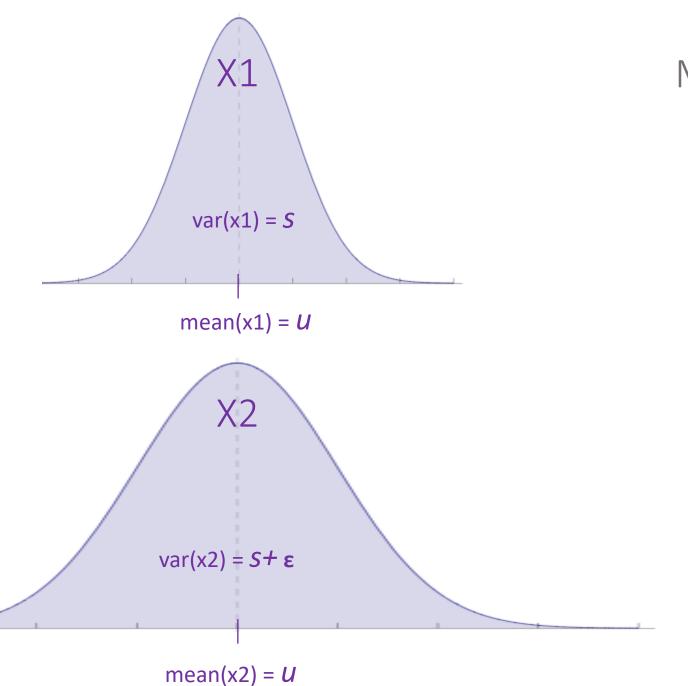
After linear transformations: Regressions are unaffected



"Linear Transformations"

$$X2 = X1 + 100$$

Must add the **same constant** to every value of X Just moves the distribution to right or left



Measurement Error

$$X2 = X1 + \epsilon$$

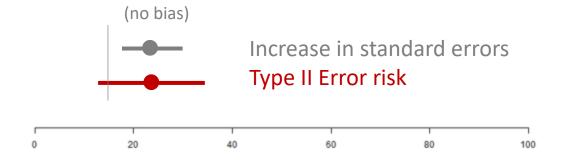


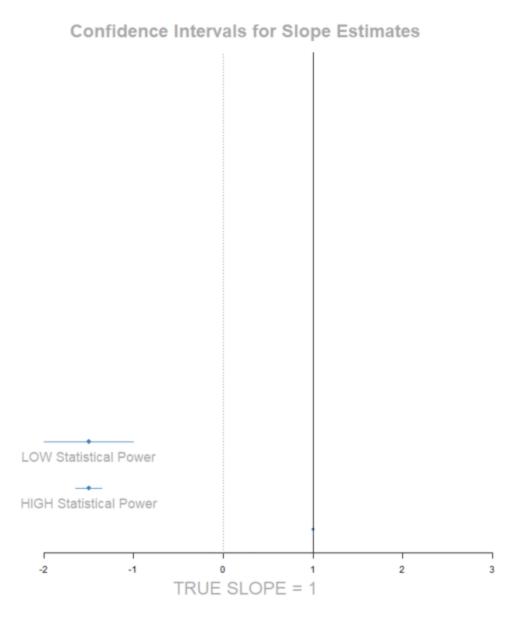
Add random error to every X.

Random means each X is equally likely to be overmeasured as undermeasured.

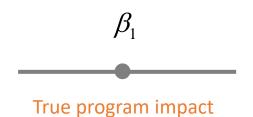
X2 has the same mean as X1, but more variance

ADDING MEASUREMENT ERROR TO THE DV





ADDING MEASUREMENT ERROR TO THE INDEPENDENT VARIABLE: "ATTENUATION BIAS"



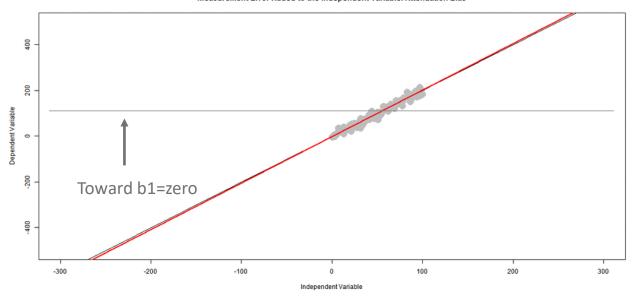
slope with measurement error



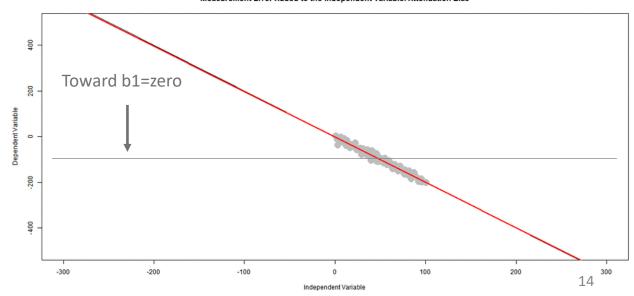
$$b_1 \downarrow = \frac{\operatorname{cov}(x_1, y)}{\operatorname{var}(x_1) \uparrow}$$

$$SE_{b1} \downarrow = \frac{residual}{samplesize \cdot var(x_1) \uparrow}$$

Measurement Error Added to the Independent Variable: Attenuation Bias



Measurement Error Added to the Independent Variable: Attenuation Bias

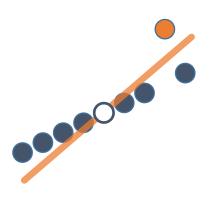


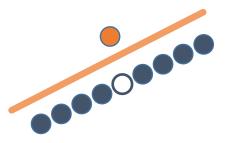
OUTLIERS

SLOPES TOO LARGE SE LARGER

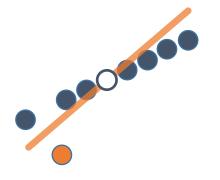
SLOPES OK SE LARGER

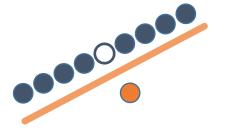
SLOPES TOO SMALL SE LARGER





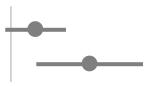




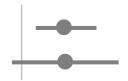




Extreme of X:
Risk of bias in slope ↑
Risk of false positive

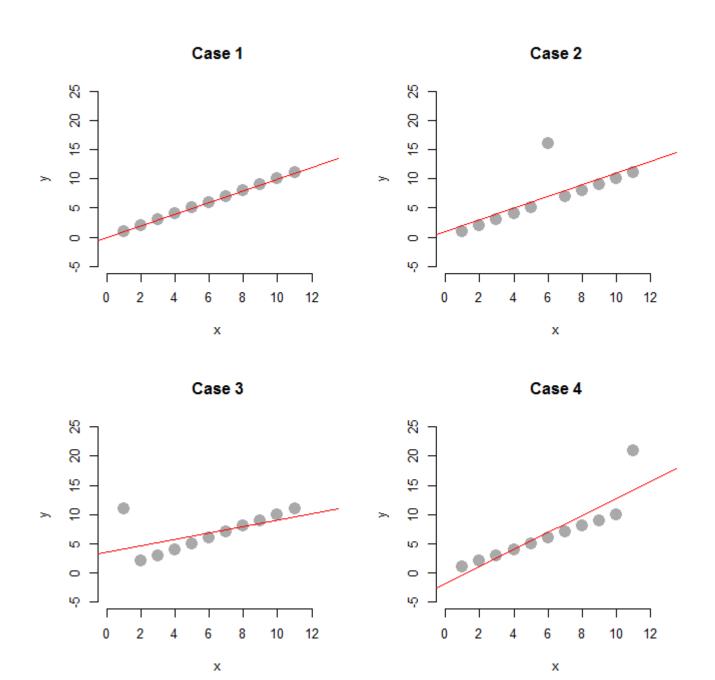


Middle of X: Don't bias slope Increased risk of false negative



Extreme of X:
Risk of bias in slope ↓
Increased risk of false negative

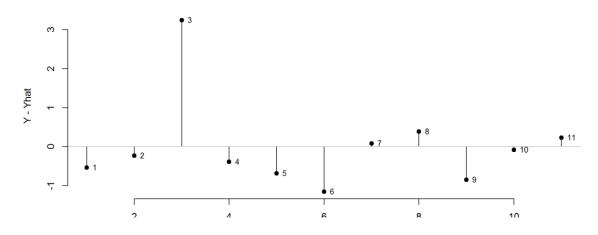


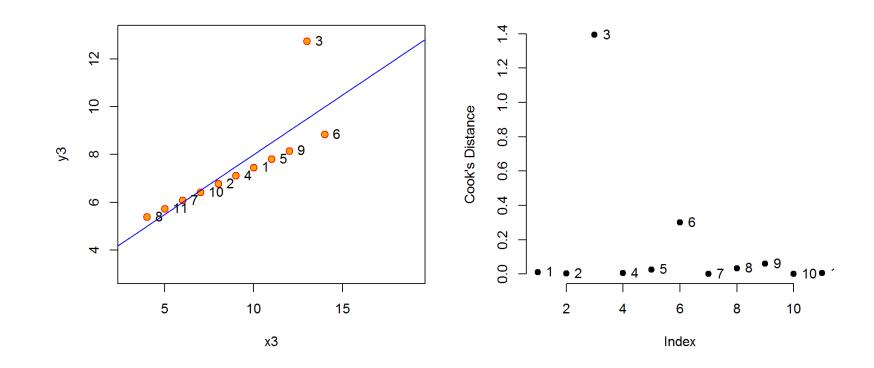


	Depe	Dependent variable:				
		у				
	(1)	(2)	(3)	(4)		
X	1.00***	1.00***	0.55*	1.45***		
	(0.00)	(0.30)	(0.26)	(0.26)		
Constant	0.00***	0.91	3.64*	-1.82		
	(0.00)	(2.06)	(1.78)	(1.78)		

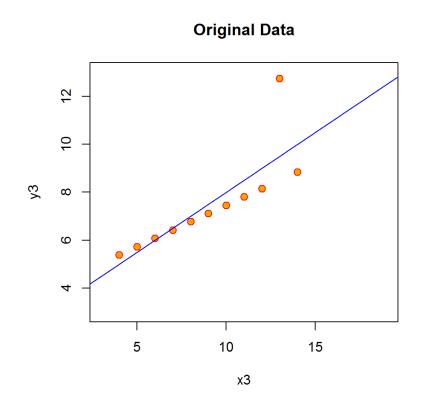
Residual Analysis

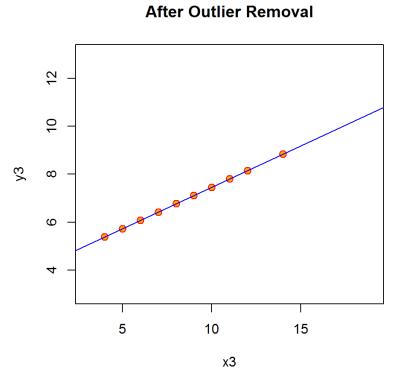
IDENTIFYING
OUTLIERS
USING
RESIDUALS
AND COOK'S
DISTANCE



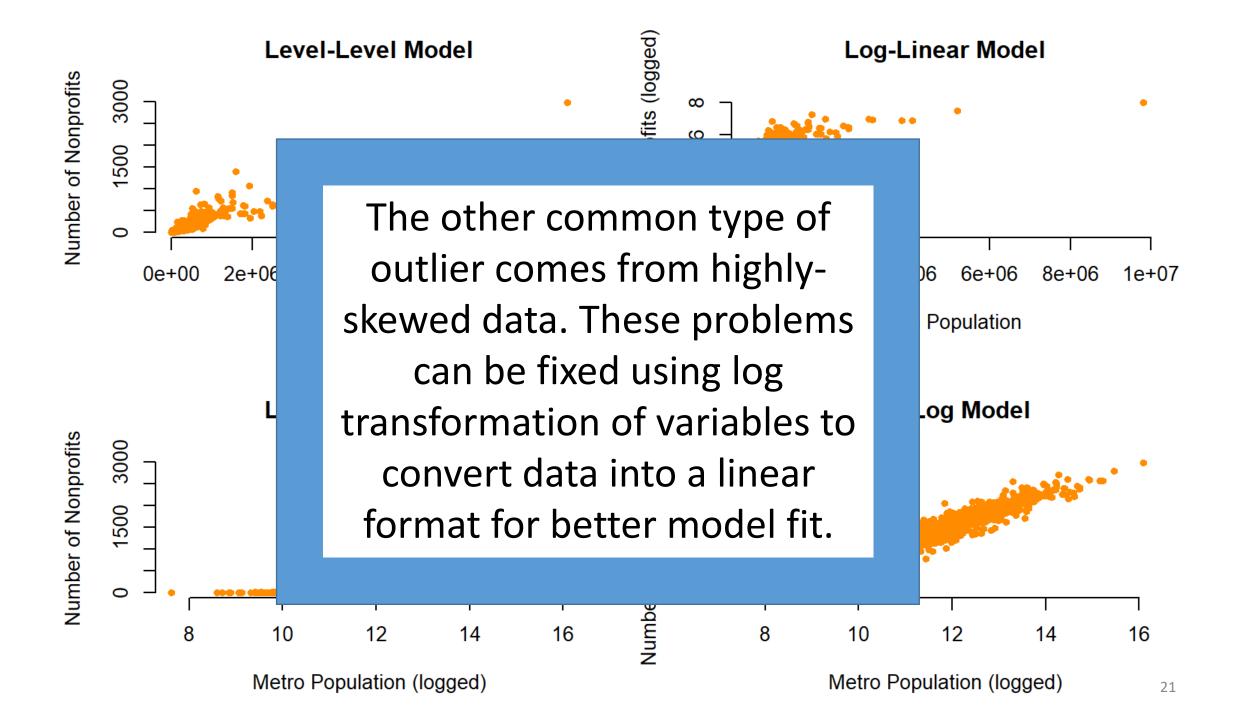


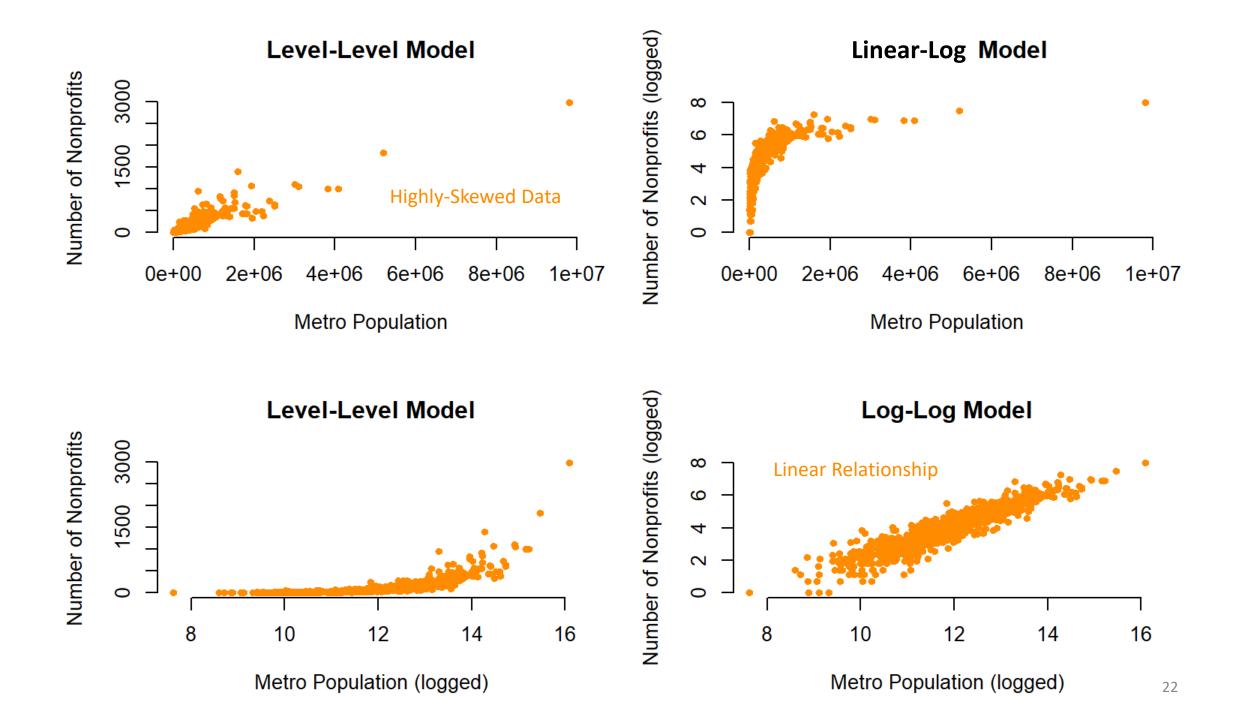
	Dependent variable:		
	у3		
	(1)	(2)	
x3	0.50***	0.35***	
	(0.12)	(0.0003)	
Constant	3.00**	4.01***	
	(1.12)	(0.003)	
Observations	11	10	
R^2	0.67	1.00	
Adjusted R ²	0.63	1.00	
Note:	<i>p<0.1; p<0.05; p<0.01</i>		





LOGGED REGRESSION MODELS



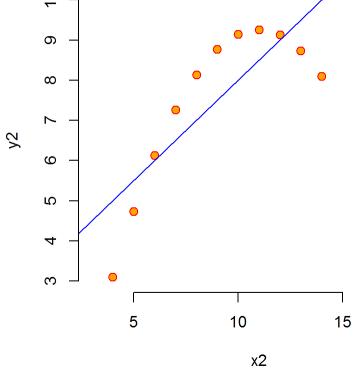


NON-LINEAR RELATIONSHIPS QUADRATIC MODELS

Linear: $Y = b0 + b1(X_1) + e$

Quadratic: $Y = b0 + b1(X_1) + b2(X_1)^2 + e$





Quadratic Fit

