



Agenda

- Employee and Manager
- Problem with a given diff.
- Array pair divisible by k
- Pair sum divisible by k
- Largest Subarray with zero sum
- Equilibrium index

Employee and Manager

Map

key
(emp)

A

B

C

D

E

F

Value
(Manager)

C ✓

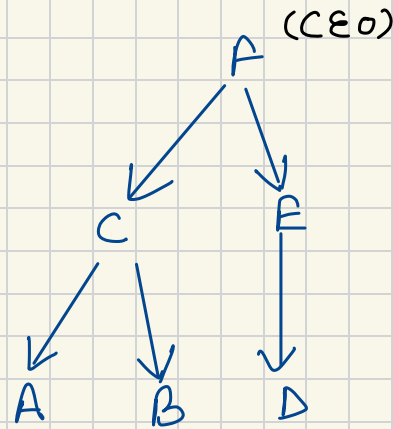
C

F

E

F

F



o/p

A → 0

B → 0

C → 2

D → 0

E → 1

F → 5

Direct Reportees

Mgr

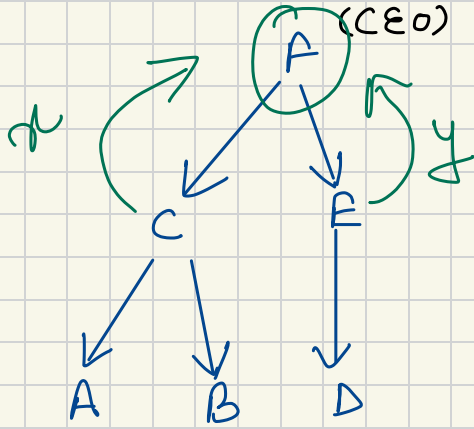
F → {C, E}

C → {A, B}

E → {D}

$$\text{total F Manages} = (x+1) + (y+1)$$

no. of Emp under a person .



$$\text{No. of Emp under you} = \sum_i' (\text{no. of Emp Managed by your direct reporter}) + 1$$

$$f(x) = \sum_i f(x_i) + 1$$

Recursive Relation -

```

HashMap<String, ArrayList<String>> directs = new HashMap<>();
String ceo = "";
for (String e : emp.keySet())
{
    String mngr = emp.get(e);

    if (e.equals(mngr) == true)
    {
        ceo = e;
        continue;
    }

    if (directs.containsKey(mngr) == true)
    {
        ArrayList<String> prevEmp = directs.get(mngr);
        prevEmp.add(e);
        directs.put(mngr, prevEmp);
    }
    else
    {
        ArrayList<String> empUnderMe = new ArrayList<>();
        empUnderMe.add(e);
        directs.put(mngr, empUnderMe);
    }
}

```

Key Value
(Emp)(Manager)

→ A C
→ B C
→ C F
→ D E
→ E F
→ F F

Manager	Emp
C	{A, B}
F	{C, E}
E	{D}

CEO = F

Mngr	Emp
C	{A, B}
F	{C, E}
E	{D}

CEO = F

faith₀ returns no. of Emp under someone

```

    fun (F)
    {
        int total = 0;
        for (Direct Reportees)
        {
            int x = fun(DR)
            total += (x + 1)
        }
    }
  
```

Problem with a given Difference

int[] arr = { 5, 10, 3, 2, 50, 80 } B = 78

Brute force

```
for (int i = 0 → n)
{
    for (int j = i + 1 → n)
    {
        if (arr[i] - arr[j] == B || arr[j] - arr[i] == B)
            return true;
    }
}
return false;
```

TC: $O(N^2)$

SC: $O(1)$

`int[] arr = { 5, 10, 3, 2, 50, 80 }`

$B = 78$

(x, y)

$$x - y = B \quad \left\{ \begin{array}{l} x = y + B \end{array} \right.$$

$$y - x = B \quad \left\{ \begin{array}{l} x = y - B \end{array} \right.$$

✓ $y = 80$

$$x = 80 + 78 = 158$$

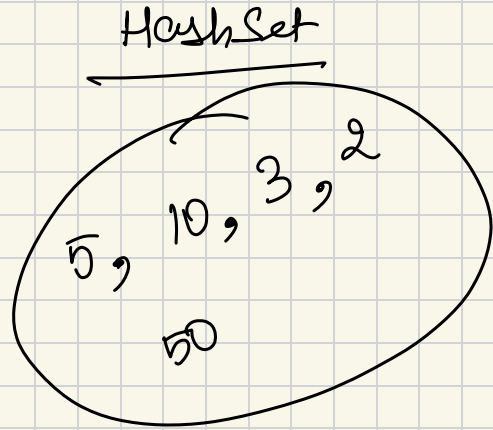
$$x = 80 - 78 = 2$$

find()
↓
 $O(1)$

$y = 2$

$$x = 2 + 78 = 80$$

$$x = 2 - 78 = -76$$



Array Pair divisible by K.

$\text{int}[] \text{arr} = \{ 1, 2, 3, 4, 5, 6, 7, 8, 9, 10 \}$ $K=5$

$n/2 \rightarrow$ pairs such sum of each pair is divisible by K

(9, 1)	(8, 2)	(7, 3)	(6, 4)	(5, 10)
↓	↓	↓	↓	↓
10	10	10	10	15

$$\text{arr} = \{ 1, \cancel{6}, \cancel{14}, 24, \cancel{19}, \cancel{21} \}_6 \quad K=5$$

✓ 3

(1, 2)

return true/false

(14, 6) (21, 19) (1, 24)

$(x + y)$ divisible by K

$$x + y = a * K$$

$$(d_1 * K + r_1) + (d_2 * K + r_2) = a * K$$

$$K * (d_1 + d_2) + (r_1 + r_2) = a * K$$

$K * (d_1 + d_2)$ is divisible by K

$(r_1 + r_2)$ has to be divisible by K

$$\underline{\underline{0 \leq r_1, r_2 < K}}$$

$$\begin{array}{r} K \overline{) x (d} \\ \hline r \end{array}$$

$$x = K * d + r$$

{ equal to K }
or
equal to 0

to make two numbers (x, y) divisible by k

$$\text{or } \left. \begin{array}{l} (x_1 + x_2) = K \\ (x_1 + x_2) = 0 \end{array} \right\}$$

$(14, 21)$

$\downarrow \quad \downarrow$

rem = $\underbrace{4 \quad 1}$

\nearrow

$k = 5$

$[14, 21] \rightarrow \text{divisible by } k$

$\{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$ $K=5$

rem

↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓
1 2 3 4 0 1 2 3 4 0

$$r_1 + r_2 = K$$

$$1 + r_2 = 5$$

$$r_2 = 4$$

$$2 + r_2 = 5$$

$$r_2 = 3$$

you need equal
freq of complementary
rem.

freq of rem

1 → 2
2 → 2
3 → 2
4 → 2
0 → 2

Largest Subarray with sum equal to zero

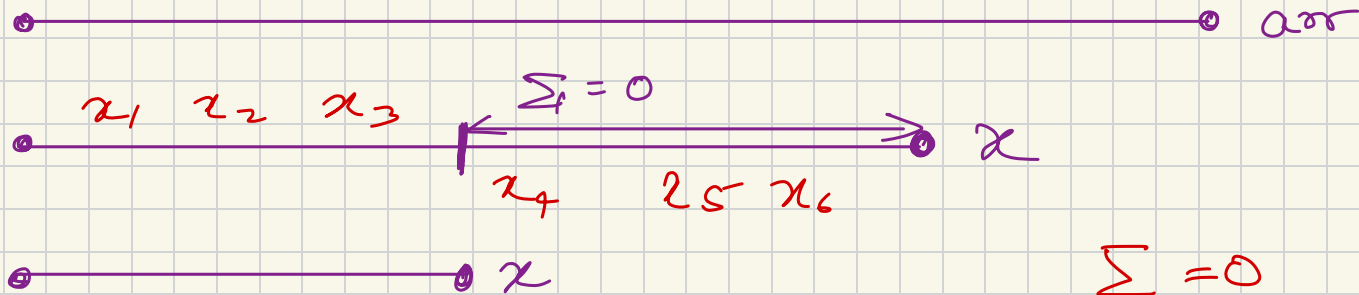
$$\text{arr}[] = \{ 15, -2, 2, -8, 1, 7, -11, -4 \}$$

Brute Force

→ Calc. all subarray sum
if (sum == 0)
store maxLen

TC: $O(N^2)$
SC: $O(1)$

$$\text{arr}[] = \left\{ \begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ 15 & -2 & 2 & -8 & 1 & 7 & -11 & -4 \end{matrix} \right\}$$



$$\boxed{x_1 + x_2 + x_3} + \boxed{x_4 + x_5 + x_6} = x$$

$\Sigma = 0$

$$x_1 + x_2 + x_3 = x$$

$$\text{arr}[] = \{ 15, -2, 2, -8, 1, 7, -11, -4 \}$$

$$\text{len} = \cancel{0} \cancel{1} \cancel{2} \cancel{3} \cancel{4} \cancel{5} \cancel{6} \cancel{7} \cancel{8}$$

sum of arr

Index	0	1	2	3	4	5	6	7
sum of arr	0	15	13	15	7	8	15	4

$$\text{len of Subarray} = i - \{ \text{index sum was first seen} \}$$

```

class Solution {
    public int maxLen(int arr[])
    {
        ✓ int rsum = 0;
        HashMap<Integer, Integer> map = new HashMap<>();
        ✓ map.put(rsum, -1);

        int maxlen = 0; 1 2 3
        for (int i = 0; i < arr.length; i++)
        {
            ✓ rsum += arr[i];
            if (map.containsKey(rsum) == true)
            {
                ✓ int len = i - map.get(rsum);
                maxlen = Math.max(maxlen, len);
            }
            else
            {
                map.put(rsum, i);
            }
        }

        return maxlen;
    }
}

```

$\{ \overset{0}{15}, \overset{1}{-2}, \overset{2}{2}, \overset{3}{7}, \overset{4}{1}, \overset{5}{-8}, \overset{6}{-11}, \overset{7}{-4} \}$
 ↑ ↑ ↑ ↑ ↑ ↑ ✗ ↑

rsum	indexSeenFirst
0	-1
15	→ 0
13	1
22	3
23	4
4	6

~~rsum = 15~~ ~~13~~ ~~22~~ ~~23~~

~~22~~ ~~23~~ ~~0~~

$2 - 0 = 2$

$5 - 0 = 5$

$7 - (-1) = 8$

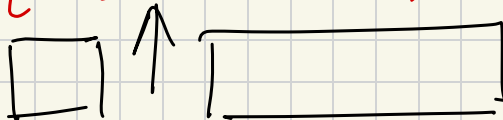
Equilibrium Index

$\text{int}[] \text{arr} = \{ \overset{0}{9}, \overset{1}{3}, \overset{2}{7}, \overset{3}{6}, \overset{4}{9}, \overset{5}{10} \}$

equilibrium index, is an index where sum of all the ele.
on left of that index is equal sum of all the ele.
on right of that index.

int[] arr = { 9, 3, 7, 6, 9, 10 }

0 1 2 3 4 5



The diagram shows a small square box on the left and a larger rectangular box on the right. An upward-pointing arrow is positioned between them, pointing towards the second element (3) of the array above.

stand at each index (i)

- get sum of left array
[0, i-1]

- get sum of right array
[i+1, n)

TC: $O(N \times N) = O(N^2)$

SC: $O(1)$

$\text{int}[] \text{arr} = \{ 9, 3, 7, 6, 9, 10 \}$

$\text{int}[] \text{sum} = \{ 0, 9, 12, 19, 25, 34 \}$

$\text{int}[] \text{sum} = \{ 35, 32, 25, 19, 10, 0 \}$

$\left. \begin{array}{l} \text{TC: } O(N) \\ \text{SC: } O(N) \end{array} \right\}$

✓ Yes Same

✓ Equilibrium Point

int[] arr = { 0 1 2 3 4 5
 9, 3, 7, 6, 9, 10 }

✓ totalSum = 44
 ✓ sum = ~~0~~ ~~9~~ ~~19~~

TC: O(N)
 SC: O(1)



$$rsum = 44 - 9 - 0 = 35$$

$$rsum = 44 - 3 - 9 = 32$$

$$\underline{lsum + x + rsum = totalSumArray}$$

$$rsum = totalSumArray - x - lsum$$

$$rsum = 44 - 7 - 12 = 25$$

$$rsum = 44 - 6 - 9 = 19$$

H.W.

- Count No. of Pairs with Absolute Diff. K
- Find the repeating and Missing Number.

Valid Anagram

str1

accio

Brute force

sort string:

accio accio

freq

a → 1

c → 2

i → 1

o → 1

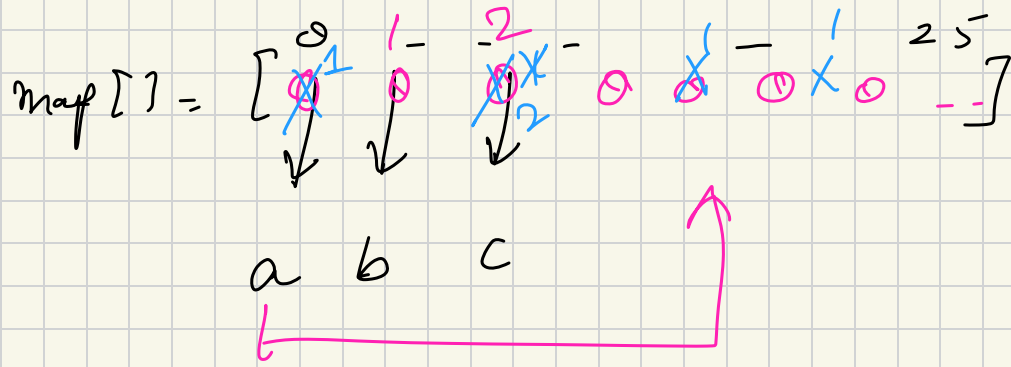
str2

ociaac

o → 1
c → 2
i → 1
a → 1

TC: $O(N \log N)$
SC: $O(1)$

TC: $O(N) + O(N) + O(26) = O(N)$
SC: $O(52) = \underline{\underline{O(1)}}$



$$'m' - 'a' =$$

$$'c' - 'a' = 2$$

accio
↑↑↑↑↑

$$'a' - 'a' = 0$$

$$'c' - 'a' = 2$$