



# Hashing

- a technique used for searching purposes.

Searching TC:  $O(1)$

① Linear Search

↳ TC:  $O(N)$

② Binary Search

↳ TC:  $O(\log_2 N)$

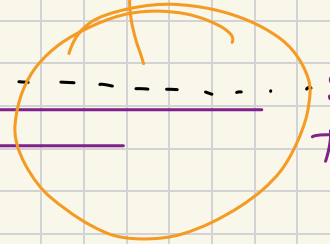
if by user

8, 3, 13, 6, 7, 4, 10, 50

Boolean

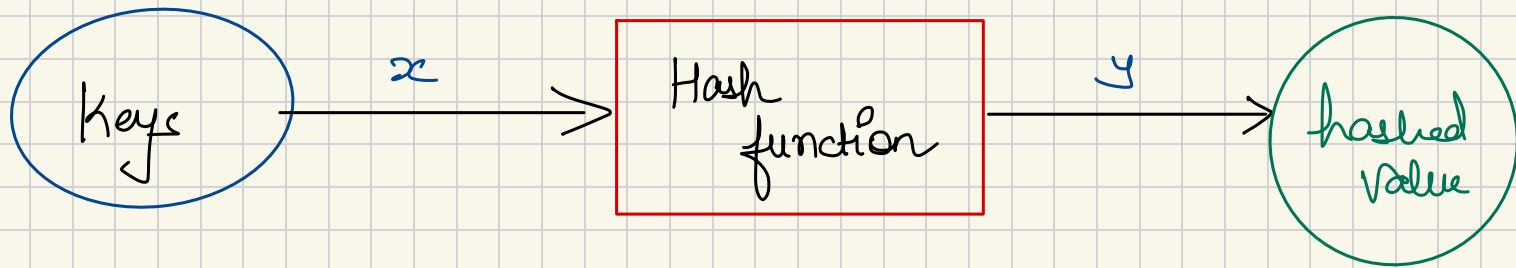
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	...	50
			T	T		T	T	T		T			T					...	T

memory  
wasted



```
search(int tar) → {  
    if (arr[tar] == true)  
        return true;  
    else  
        return false;  
}
```

high memory usage!  
hashing was introduced



hash f<sup>n</sup>

step 1  $g(x) = k$

          ↓                ↓

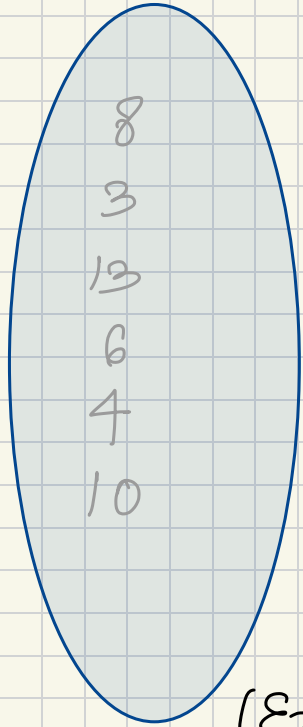
          key             Integer value

step 2  $h(k) = y$

appl<sup>i</sup>

    ↳ 09986

Key Space



hash fun

$$\underline{\underline{f(K) = K}}$$

$$f(8) = 8$$

$$f(3) = 3$$

$$f(13) = 13$$

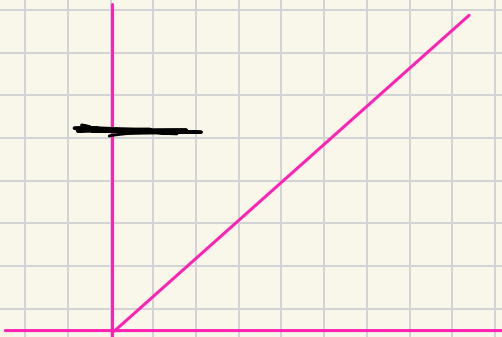
$$f(6) = 6$$

$$f(4) = 4$$

$$f(10) = 10$$

One-One  
relation

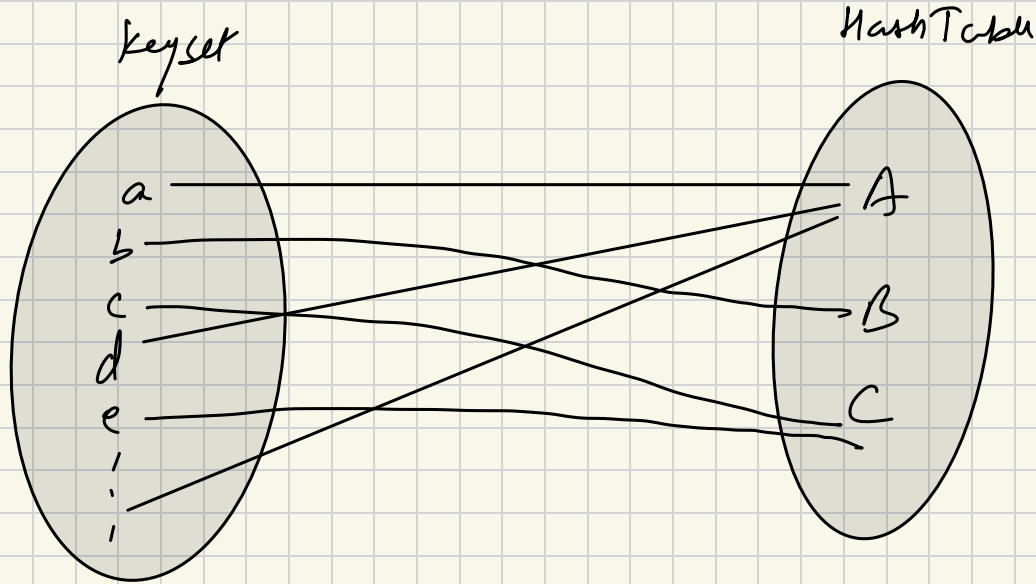
(Extra Memory is used)



hash Table

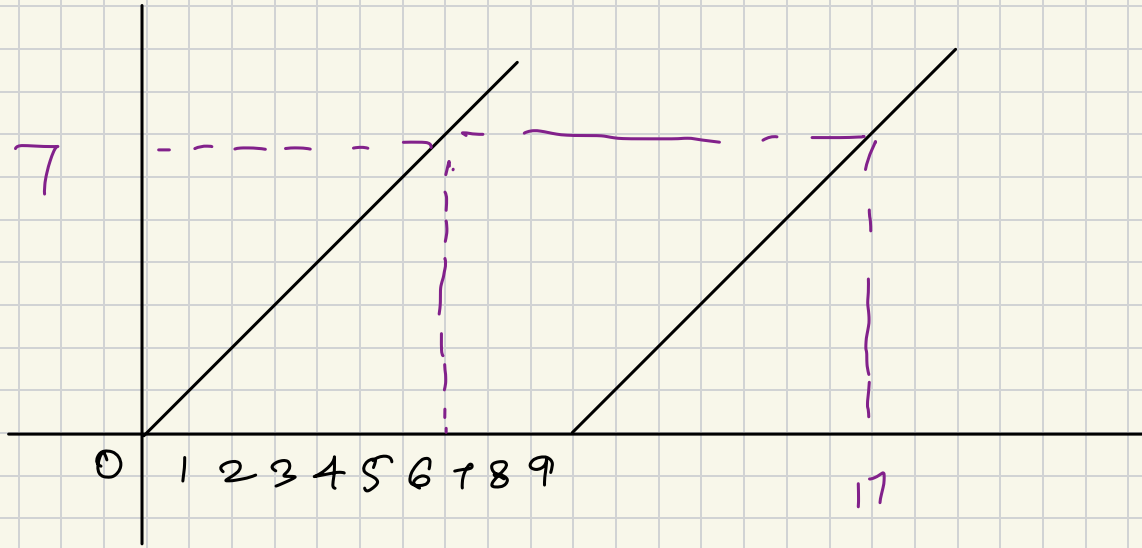
0	
1	
2	
3	3
4	4
5	
6	6
7	
8	8
9	
10	10
11	
12	
13	13
14	
15	
16	
17	

# Many to One Relations



hash fun

$$f(K) = K \% 10$$



Key Space

hash fun

hash Table

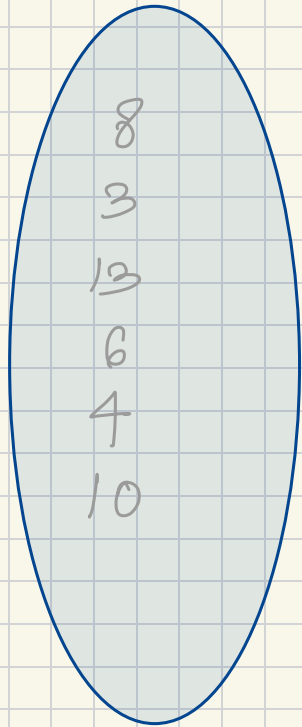
$$f(k) = k \% 10$$

$$f(8) = 8 \% 10 = 8$$

$$f(3) = 3 \% 10 = 3$$

$$f(13) = 13 \% 10 = 3$$

collision



0	
1	
2	
3	3
4	
5	
6	
7	
8	8
9	



## Methods to remove collision

Open hashing

① Chaining

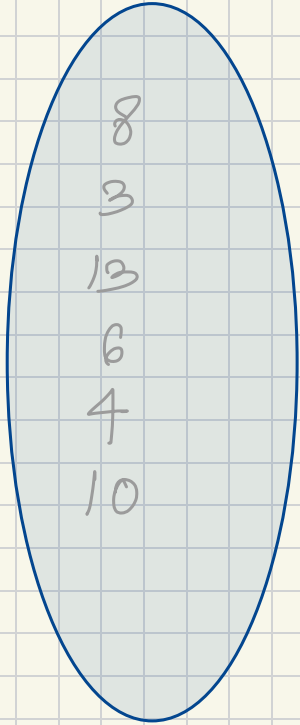
Closed hashing

① Linear Probing

② Quadratic Probing

# Chaining

Key Space



hash fun

$$f(k) = k \% 10$$

$$f(8) = 8 \% 10 = 8$$

$$f(3) = 3 \% 10 = 3$$

$$f(13) = 13 \% 10 = 3$$

$$f(6) = 6 \% 10 = 6$$

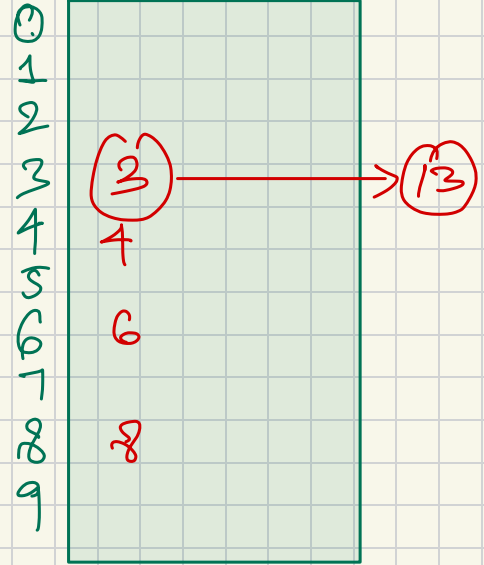
$$f(4) = 4 \% 10 = 4$$

search (13)

$$\left\{ \begin{array}{l} 13 \% 10 = 3 \end{array} \right.$$

searching.  
TC: O(1)  
=

hash Table



$$f(k) = \cancel{k} \% 10$$

$$\underline{f(k)} = k \% \text{ size}$$

$$\text{size} = \text{length } L^*$$

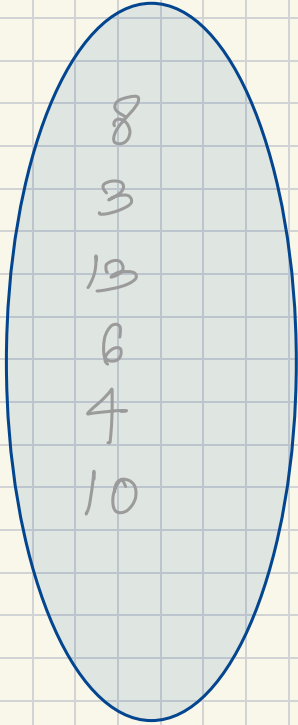
$$0 - 15500 \approx 15\%$$

$$7500$$

$$f(k), k \% 7500$$

# Quadratic Probing

Key Space



hash fun

$$f'(k) = \{f(k) + g(i)\} \% 10$$

$$f(k) = k \% 10 \quad g(i) = 0, 1, 2, \dots$$

$$f'(8) = (8 + 0) \% 10 = 8$$

$$f'(3) = (3 + 0) \% 10 = 3$$

$$f'(13) = (3 + 0) \% 10 = 3$$

$$f'(13) = (3 + 1) \% 10 = 4$$

$$f'(6) = (6 + 0) \% 10 = 6$$

$$f'(4) = (4 + 0) \% 10 = 4$$

$$f'(4) = (4 + 1) \% 10 = 5$$

$$f'(40) = (0 + 0) \% 10 = 0$$

hash Table

0	10
1	
2	
3	3
4	13
5	4
6	6
7	
8	8
9	

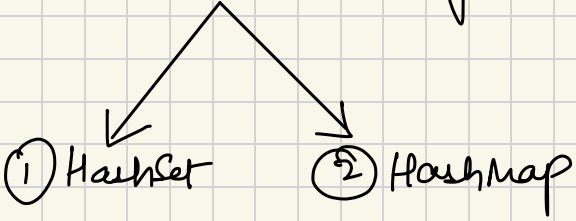
## Quadratic Probing

$$f'(k) = \{ f(k) + g(i) \} \% \text{size}$$

$$f(k) = k \% \text{size}$$

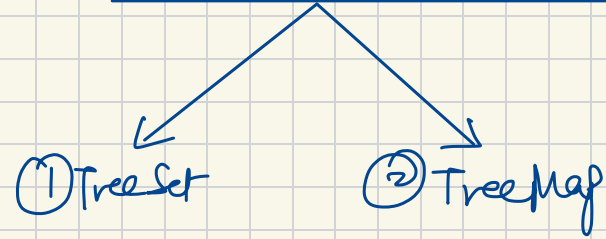
$$g(i) = i^2 \quad \hookrightarrow 0, 1, 4, 9, 16, 25, 36, \dots$$

## Based on hashing



searching TC:  $O(1)$   
insertion TC:  $O(1)$

## Based on Red-Black Tree



searching TC:  $O(\log_2 N)$   
insertion TC:  $O(\log_2 N)$

HashSet

↳ set of unique entities

- ✓ Holds unique entities
- ✓ preserving of entities O/D

keySet = { ~~1~~, ~~2~~, ~~3~~, ~~7~~, ~~5~~, ~~7~~, ~~6~~, ~~5~~, ~~2~~, ~~2~~, ~~1~~ }

1, 2, 3, 5, 7, 6

→ HashSet

## Hash Map

ds to store (key, value) pairs

- Key ① Unique entity
- ② Hashing is applied over keys

implement a shopping cart

<u>key</u>	<u>value</u>
item	qty
lays	3
eggs	6
oranges	3