



Hashing (searching technique)

pool of
Numbers $\}$

$\}$ \int int target

- ① Linear Search $Tc: O(N)$ $Sc: O(1)$
 - ② Binary Search $Tc: O(\log_2 N)$ $Sc: O(1)$
 - ③ Hashing $Tc: O(1)$, $Sc: O(1)$
- } Store No. inside an array
- } Store No. ^P inside a hashTable

NOTE: Hashing allows searching ^o in $Tc: O(1)$, $Sc: O(1)$

~~if~~ 8, 3, 13, 16, 17, 14, 10, 50

Boolean[] arr = {
0 1 2 3 4 5
T T T T T

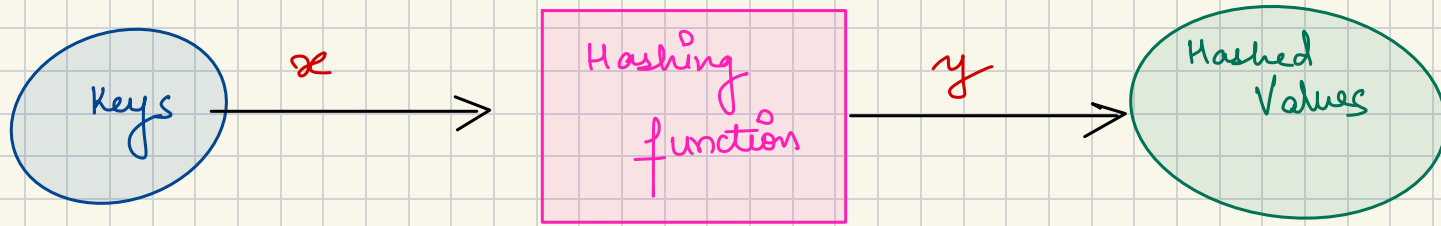
50
T

```
search (int key)
{
    if (arr[key] == true)
        return "found";
    else
        return "Not found";
}
```

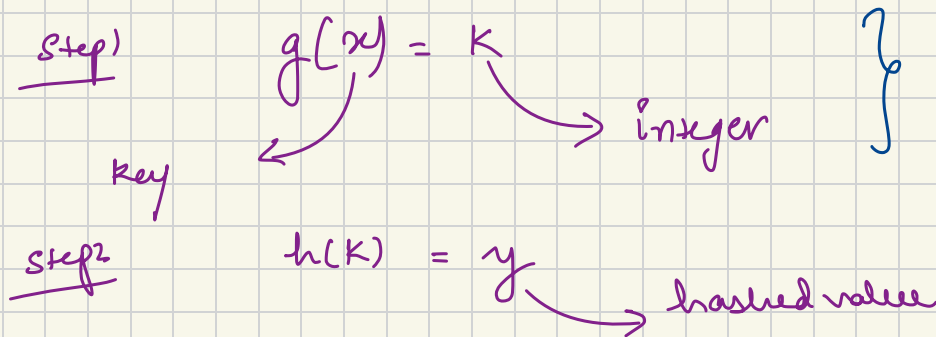
} TC: O(1)
SC: O(1)

{
• high memory was consumed
• hence hashing was introduced

Basic Mechanism of Hashing



Hash f^n , { 2-steps f^n }



Key Space.

Hash f^n

$$h(k) = k \quad (\text{one to one } f^n)$$

$$h(8) = 8$$

$$h(3) = 3$$

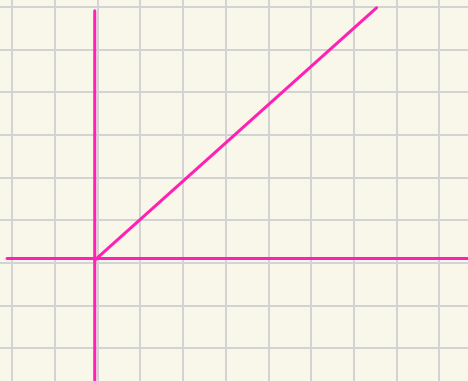
$$h(13) = 13$$

$$h(6) = 6$$

$$h(4) = 4$$

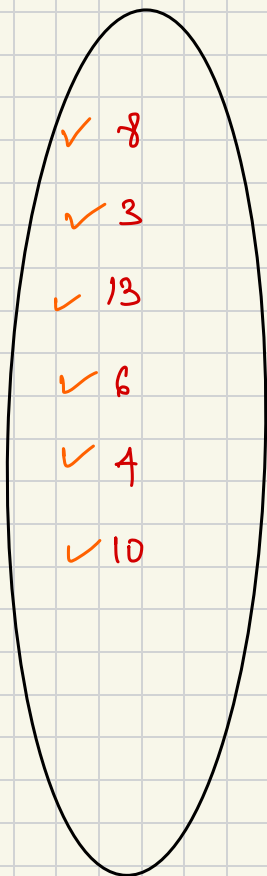
$$h(10) = 10$$

high memory was
consumed }



Hash Table

0	
1	
2	
3	3
4	4
5	
6	6
7	
8	8
9	
10	10
11	
12	
13	13
14	
15	
16	



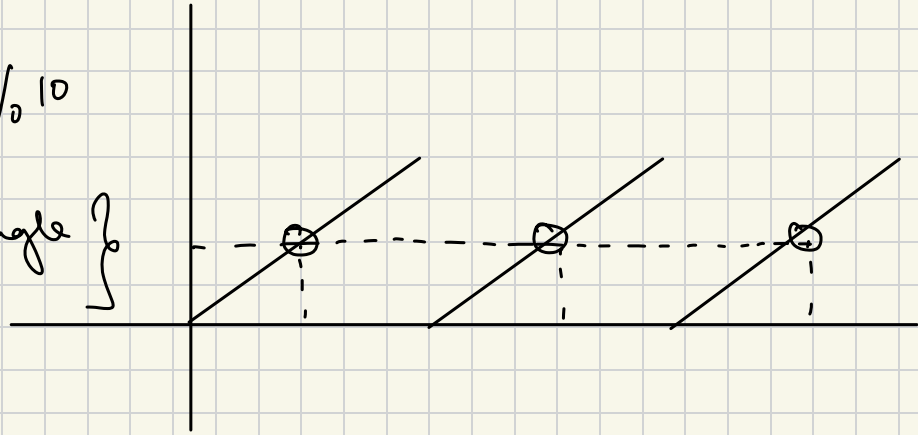
pair list

• unique hashed value for each key { one to one }

many to one fⁿ

$$h(K) = K \% 10$$

for multiple keys, there is single }
hashed values



Key Space.

Hash fⁿ

$$h(k) = k \% 10$$

Hash Table

✓ 8

✓ 3

✓ 16

13

$$h(8) = 8 \% 10 = 8$$

$$h(3) = 3 \% 10 = 3$$

$$h(16) = 16 \% 10 = 6$$

$$h(13) = 13 \% 10 = 3$$

Collision

0

1

2

3

4

5

6

7

8

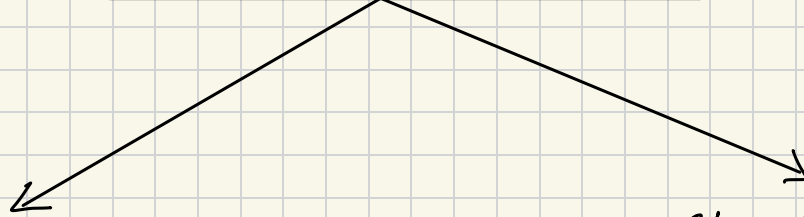
9

3

16

8

Methods to remove collision



Open Hashing

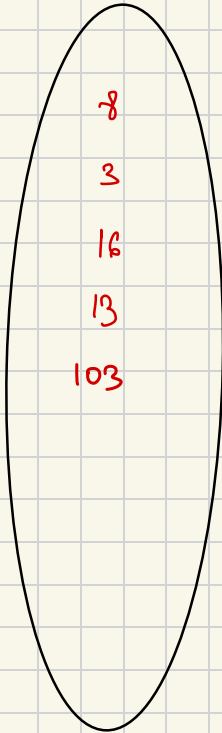
① Chaining

Closed Hashing

- ① Linear Probing
- ② Quadratic Probing

Chaining

Key Space



Hash fⁿ

$$h(k) = k \% 10$$

$$h(8) = 8 \% 10 = 8$$

$$h(3) = 3 \% 10 = 3$$

$$h(16) = 16 \% 10 = 6$$

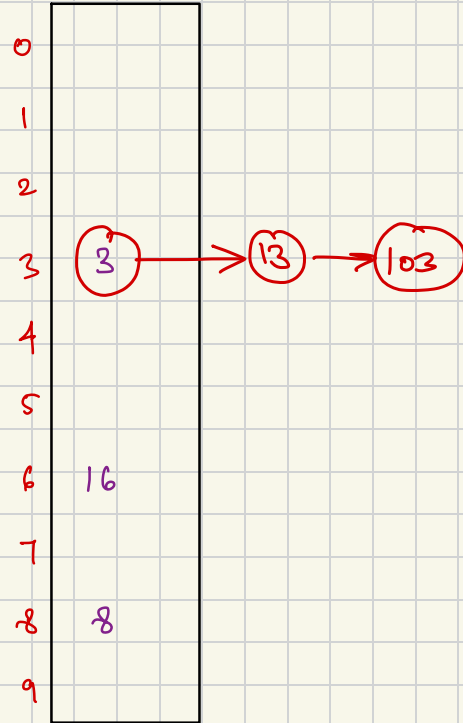
$$h(13) = 13 \% 10 = 3$$

$$h(103) = 103 \% 10 = 3$$

Search (103)

TC: $O(1)$
SC: $O(1)$

Hash Table



Hash fⁿ

$$h(n) = n \% 10 \times$$

load factor

0 - 10000
↳ 75% of Range

7500

Linear Probing

Key Space



Hash fⁿ

$$h'(k) = \{h(k) + g(i)\} \% 10$$

$$h(k) = k \% 10$$

$$g(i) = i; \quad i \in 0, 1, 2, \dots$$

$$\begin{aligned} h'(8) &= \{h(8) + g(0)\} \% 10 \\ &= (8 + 0) \% 10 = 8 \end{aligned}$$

$$\begin{aligned} h'(3) &= \{h(3) + g(0)\} \% 10 \\ &= (3 + 0) \% 10 = 3 \end{aligned}$$

$$\begin{aligned} h'(16) &= \{h(16) + g(0)\} \% 10 \\ &= (6 + 0) \% 10 = 6 \end{aligned}$$

$$h'(13) = \{h(13) + g(0)\} \% 10 = (3 + 0) \% 10 = 3$$

$$h'(13) = \{h(13) + g(1)\} \% 10 = (3 + 1) \% 10 = 4$$

Hash Table

0	
1	
2	
3	3
4	13
5	
6	16
7	
8	8
9	

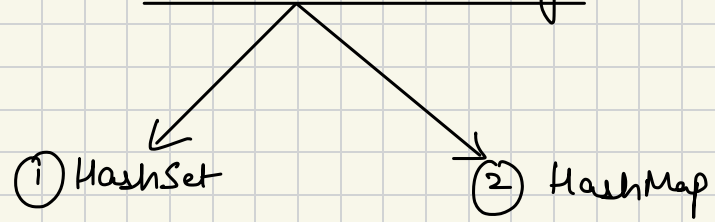
Quadratic Probing .

$$h'(k) = \{ h(k) + g(i) \} \% L.f.$$

$$h(k) = k \% L.f.$$

$$g(i) = i^2 \quad ; \quad 0, 1, 4, 9, 16, 25, \dots$$

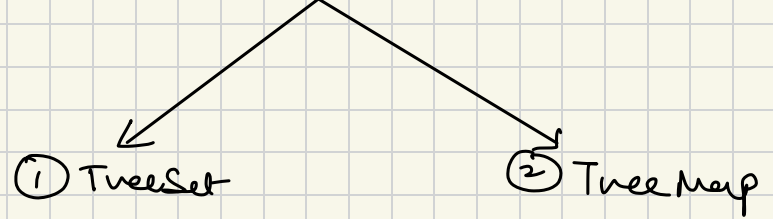
Based on hashing



TC: $O(1)$ Searching

TC: $O(1)$ Insertion

Red-Black trees



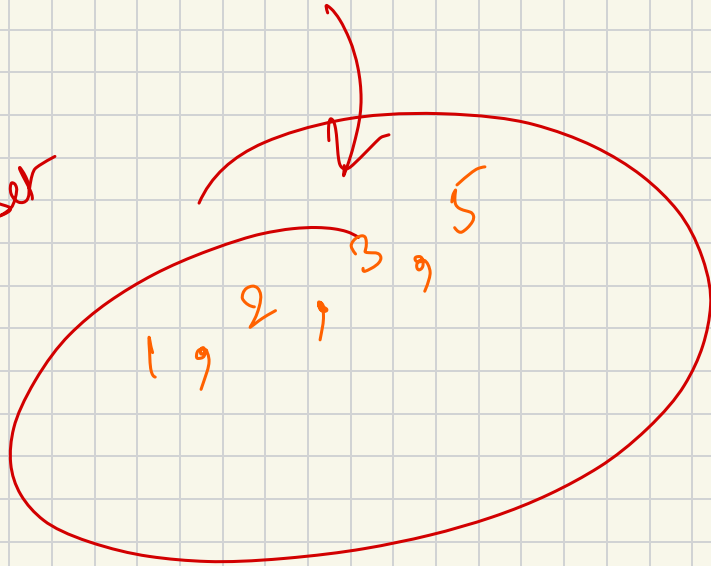
TC: $O(\log N)$

HashSet

↳ set of unique entities

keySet = { 1, 2, 3, 3, 5, 2, 1, 3, 5 }

HashSet



Hash Map

↓

stores (key, value) pair

implement shopping cart for E-commerce

String
key (item)

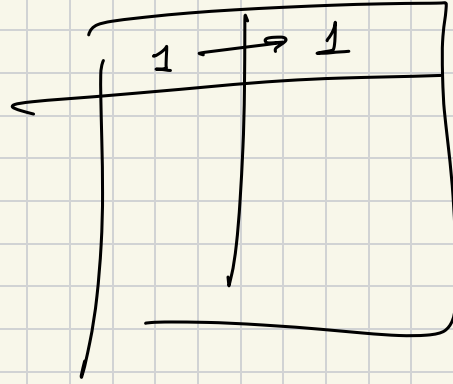
Integer
value (qty)

(unique entity)

Hashing is
done on keys

{	Lays	5
	eggs	12
	oranges	2
	yogurt	4

$\{1, 2, 3, +, +, 3\}$



¹⁰
 \checkmark ~~203~~ ~~204~~ ~~205~~ ~~206~~ ~~207~~ ~~208~~ ~~203~~ ~~204~~ ~~205~~ ~~206~~
¹³
 \checkmark ~~203~~ ~~204~~ ~~204~~ ~~205~~ ~~206~~ ~~207~~ ~~205~~ ~~208~~ ~~203~~ ~~206~~ 205 206 204

⁴
~~1~~ ~~1~~ ~~5~~
⁴
~~1~~ ~~2~~ ³ ⁴
 \checkmark \checkmark

3, 4, 1

H'W

① Valid Anagrams

② Employees and Managers

}