






Agenda.

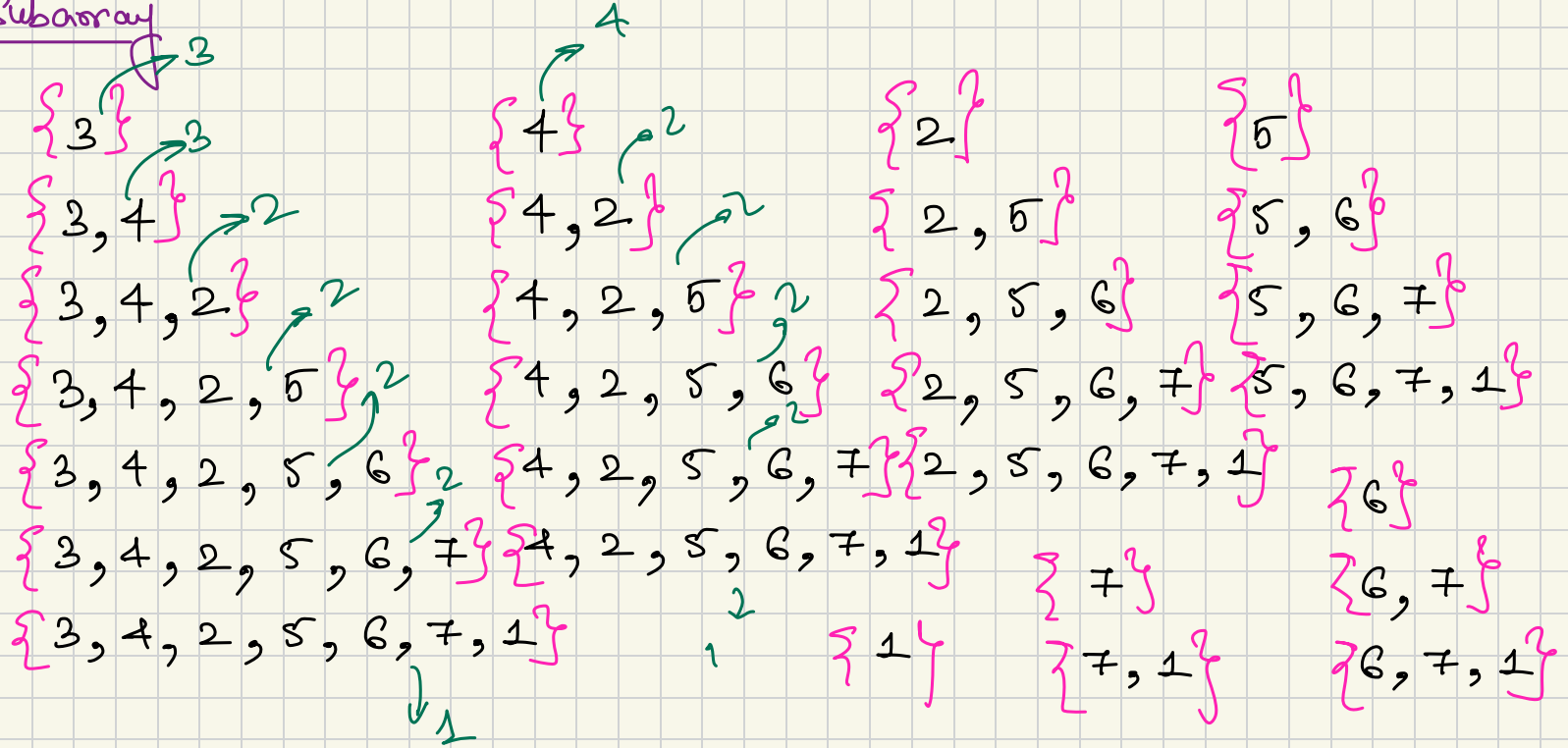
- Sum of subarray minimums  Hard
- Trapping Rain Water  Hard
- Minimum Stack  Med

Sum of Subarray Minimums

int[] arr = { 3, 4, 2, 5, 6, 7, 1 }

$$\sum \text{min value}$$

Subarray



Brute Force

- Nested loop : try to get all subarray min
- Inc. the sum.

TC: $O(N^2)$

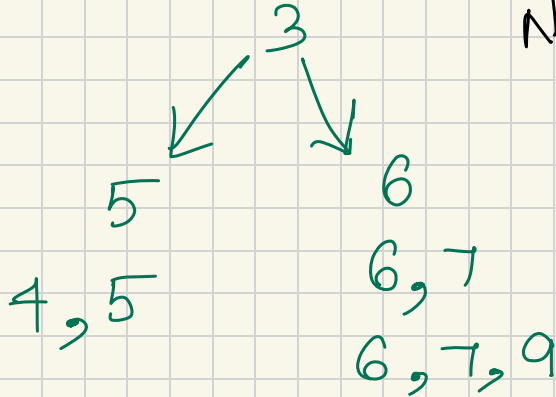
SC: $O(1)$

$$\text{arr} = \{ \overset{0}{2}, \overset{1}{4}, \overset{2}{5}, \overset{3}{3}, \overset{4}{6}, \overset{5}{7}, \overset{6}{9}, \overset{7}{1} \}$$

\uparrow nseli \uparrow \uparrow nseri

$$\sum \text{min of Subarray} = 2 \times a + 4 \times b + 5 \times c + 3 \times d + \dots$$

No. of Subarray Ele is min.



No of Subarray

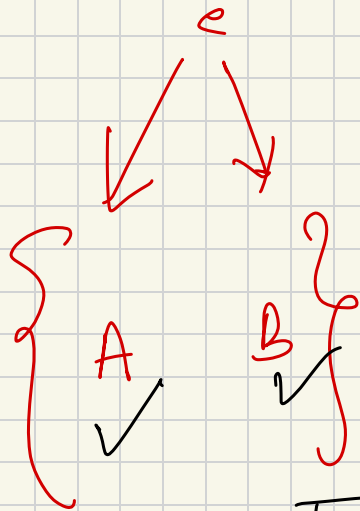
$$= 1 + 2 \times 1 + 1 \times 3$$

$$+ 2 \times 1 \times 3$$

$$= 1 + 2 + 3 + 6 = 12$$

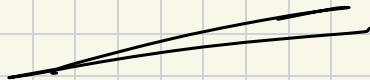
$$\begin{aligned}
 &1 + 0 \times 1 + 1 \times 2 \\
 &\quad + 0 \times 1 \times 2 \\
 &\quad = 1 + 2 \\
 &\quad = 3
 \end{aligned}$$

$\swarrow 6$ $\searrow 7$
 7, 9



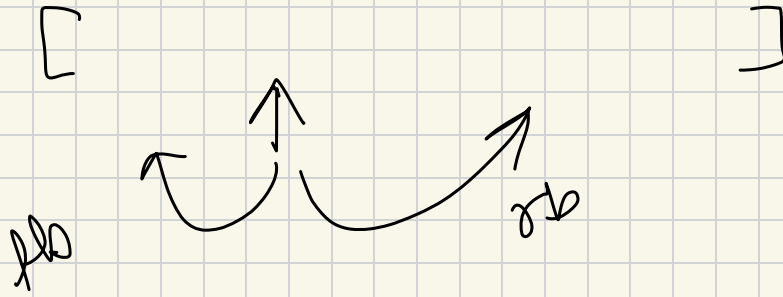
Total Subarray

$$X = 1 + A \times 1 + 1 \times B + A \times 1 \times B$$



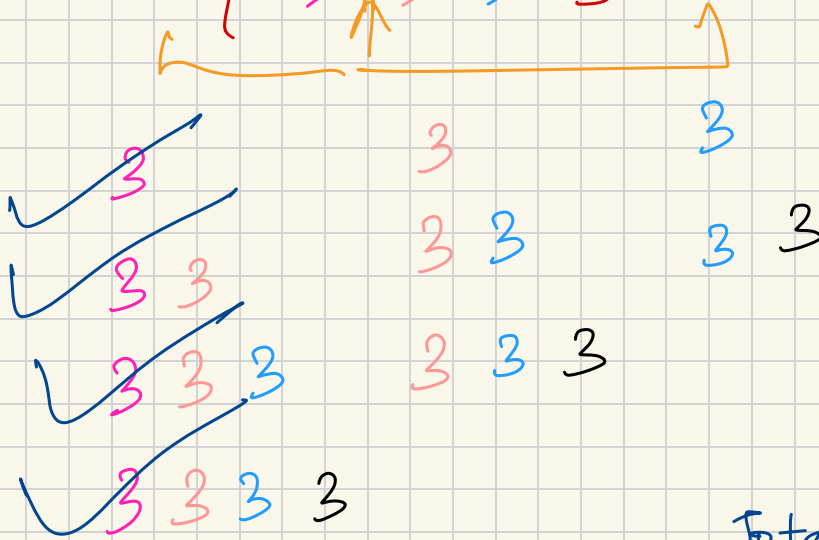
Sum 2

$$\sum_{i=0}^n X_i \times \text{arr}[T_i]$$



No. of inclusion from left = $i - lb - 1$ }
from right = $rb - i - 1$ }

$\text{int}[] = \{ 3, 3, 3, 3 \}$



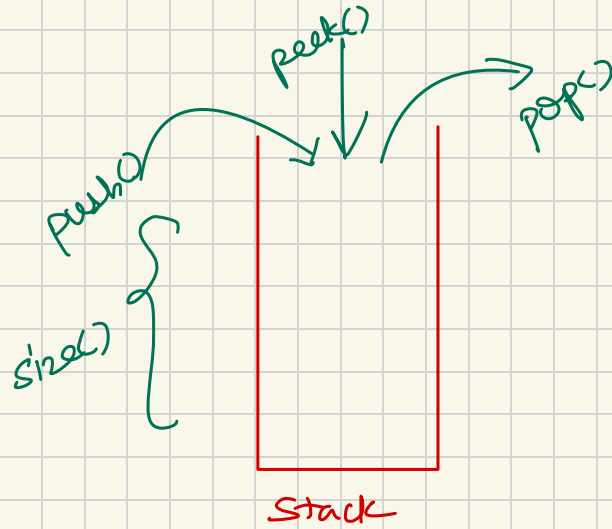
$$\begin{aligned}
 & 1 \times 1 + 1 \times 2 + 1 \times 1 \times 2 \\
 &= 1 + 1 + 2 + 2 \\
 &= 6
 \end{aligned}$$

3

$$\begin{aligned}
 \text{Total} &= 1 + 0 \times 1 + 1 \times 3 + 0 \times 1 \times 3 \\
 &= 4
 \end{aligned}$$

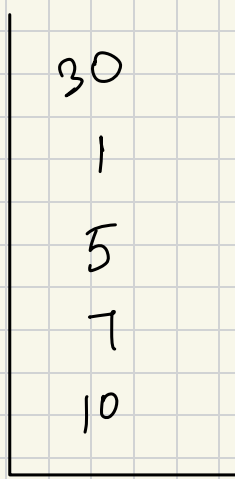
- o Next Smaller and equal element on left.
- o Next Smaller element on right.

Min Stack



getMin() : Method

returns Min Value present in the stack in $O(1)$



St.

Test Case

push(10)

push(7)

push(5)

push(2)

getMin() \rightsquigarrow 2

pop()

getMin() \rightsquigarrow 5

push(1)

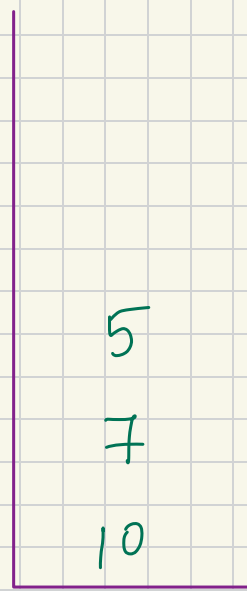
getMin() \rightsquigarrow 1

push(30)

getMin() \rightsquigarrow 1

push(10) ✓
push(7) ✓
push(5) ✓
push(2) ✓
getMin() ~→ 2 ✓
pop() ✓
getMin() ~→ 5 ✓
push(1)
getMin() ~→ 1
push(30)
getMin() ~→ 1

TC: O(N)



St.



temp

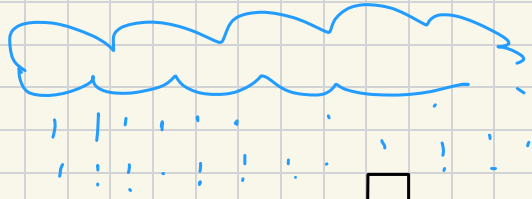
push(10)
push(7)
push(5)
push(2)
getMin() \rightsquigarrow 2
pop()
getMin() \rightsquigarrow 5
push(1)
getMin() \rightsquigarrow 1
push(30)
getMin() \rightsquigarrow 1

30, 1
1, 1
5, 5
7, 7
10, 10

Stack

class Pair
{
 minValue;
 element;
}

Trapping Rainwater



water stored = 6 sq. units

lust = { 0 1 0 2 1 0 1 2 3 1 2 0 }

$0 \quad 1 \quad 2 \quad 3 \quad 4 \quad 5 \quad 6 \quad 7 \quad 8 \quad 9 \quad 10 \quad 11$
 $hst[] = \{0, 1, 0, 2, 1, 0, 1, 2, 3, 1, 2, 0\}$

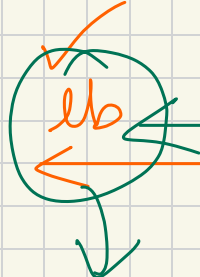
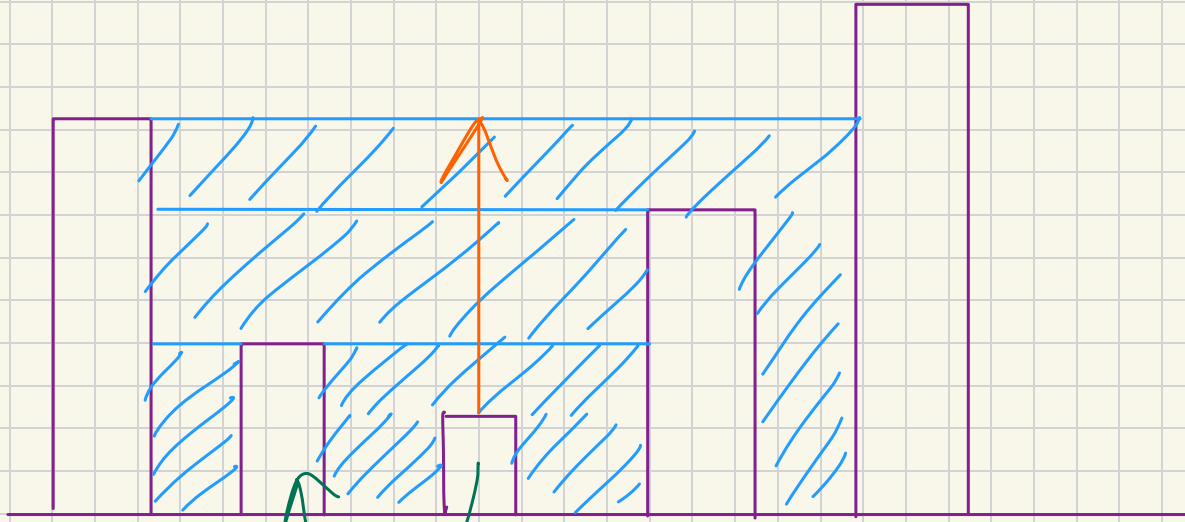
Brute force

for (int i = 0 \longrightarrow n)

$\left\{ \begin{array}{l} \text{getTallest}(0, i-1) \\ \text{getTallest}(i+1, n) \end{array} \right.$

Calc. water above you

$i=0 \quad 1 \quad \dots \quad n-1$
 $\downarrow \quad \downarrow \quad \dots \quad \downarrow$
 $\sum_{i=0}^{n-1} 2N$
 $2N = 2N \times N = 2N^2$
 $\left. \begin{array}{l} TC: O(N^2) \\ SC: O(1) \end{array} \right\} = O(N^2)$



tallest Building On Left



tallest Building On
right

0 1 2 3 4 5 6 7 8 9 10 11
hist[] = {0, 1, 0, 2, 1, 0, 1, 2, 3, 1, 2, 0}

~~↑~~ ~~↑~~ ~~↑~~ ~~↑~~ ~~↑~~ ~~↑~~ ↑

→ 0 0 1 1 2 2 2 → lmax
✓ Tc: O(n)

↑ ↑ ↑

2 0 0

← rmax (O(n))

Reverse String Paranthesis

$= (ab(cd)e((fg)h)) \rightarrow \underline{\underline{ghfedba}}$