



✓ Hashing. {Theory}

Searching $(TC: O(1))$ ✓

A technique for searching purpose.

✓ (1) Linear Search

$TC: O(N), SC: O(1)$

✓ (2) Binary Search

$TC: O(\log_2 N), SC: O(1)$

} Storing $\{P\}$ in an array }

IP $\rightarrow 8, 3, 13, 16, 7, 4, 10, \dots, 50$

Hash Table.

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	50
			T	T			T	T	T			T		T									T

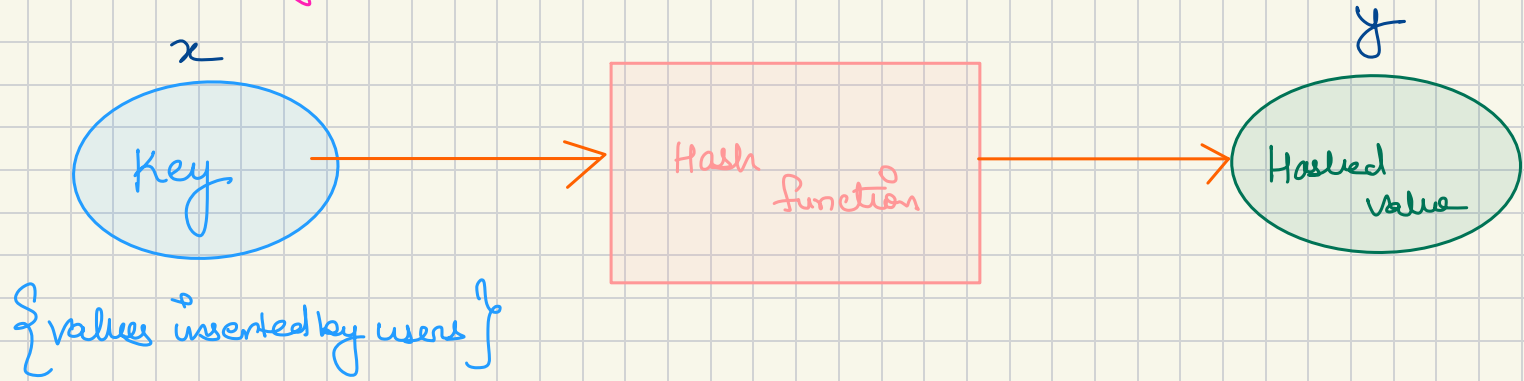
```

search(key) 8
{
    if (arr[key] == true)
        return "found";
    else
        return "not found";
}
  
```

TC: $O(1)$, SC: $O(1)$

high memory required,
hashing was introduced
to reduce this
memory

Basic Hashing Mechanism



Hash funⁿ { 2-step funⁿ }

Key \rightarrow can be anything

✓ step 1

$$g(x) = k$$

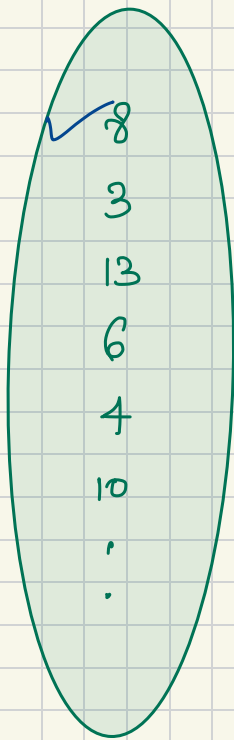
Key \swarrow Integer value

step 2

$$f(k) = y$$

hashed value

Key Space



hash funⁿ
 $f(k) = k$ (one to one fⁿ)

$$f(8) = 8$$

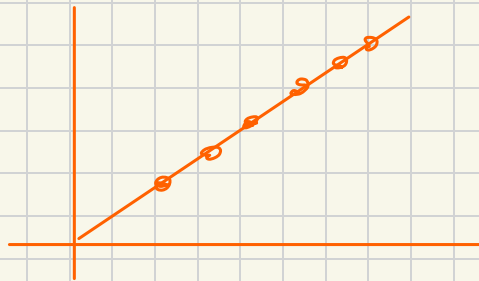
$$f(3) = 3$$

$$f(13) = 13$$

$$f(6) = 6$$

$$f(4) = 4$$

$$f(10) = 10$$



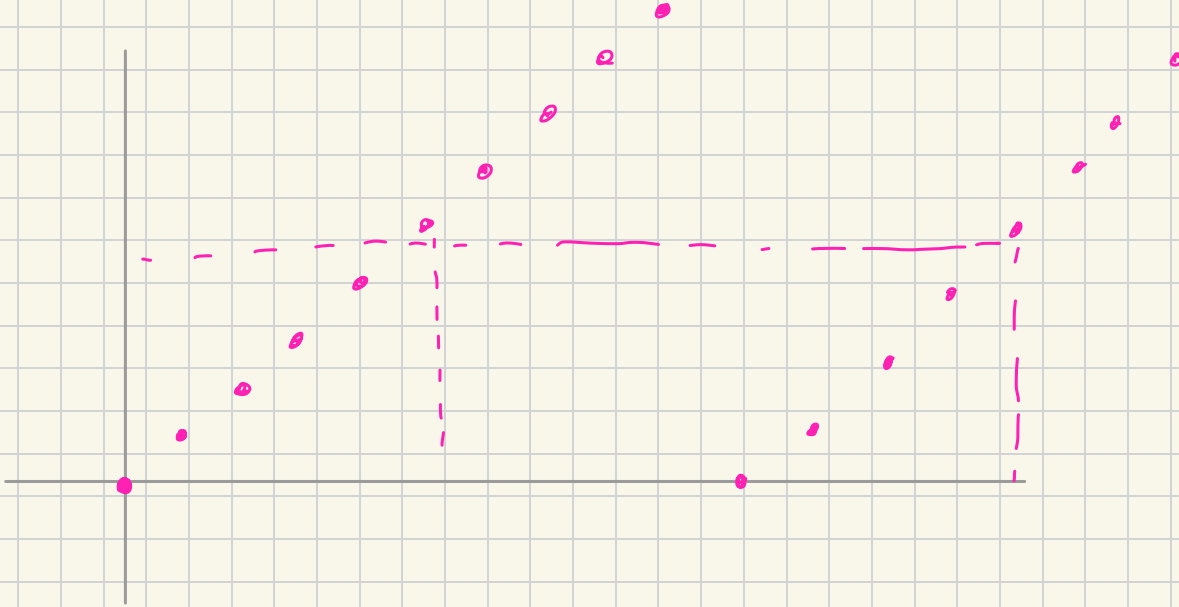
Hash Table

0	
1	
2	
3	3
4	4
5	
6	6
7	
8	8
9	
10	10
11	
12	
13	13
14	
15	
16	
17	
18	
19	
20	
21	

many to one relationship

$$f(k) = k \% 10$$

hashed value: $[0, 9]$
↓
size = 10



Key Space

8
3
13
6
4
10
.
.

hash funⁿ
 $P(K) = K \% 10$

$$F(8) = 8 \% 10 = 8$$

$$F(3) = 3 \% 10 = 3$$

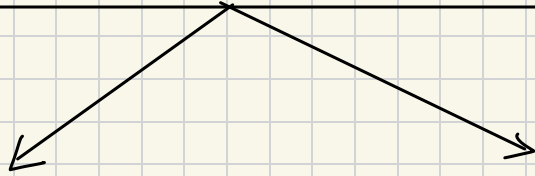
$$F(13) = 13 \% 10 = 3$$

Hash Table

0	
1	
2	
3	3
4	
5	
6	
7	
8	8
9	

Collision!

Methods to remove collision



open hashing

① chaining

closed hashing

- ① linear probing
- ② quadratic probing

chaining

Key Space

8
3
13
6
4
10
33

hash fun

$$P(K) = K \% 10$$

$$P(8) = 8 \% 10 = 8$$

$$P(3) = 3 \% 10 = 3$$

$$P(13) = 13 \% 10 = 3$$

$$P(6) = 6 \% 10 = 6$$

$$P(4) = 4 \% 10 = 4$$

$$P(10) = 10 \% 10 = 0$$

$$P(33) = 33 \% 10 = 3$$

searching(33)
→ hash value. 3

avg TC : $O(1)$

Hash Table

0	10
1	
2	
3	3 → 13 → 33
4	4
5	
6	6
7	
8	8
9	

Range of i/p: $0 - 100$

size: 75% of Range

$$f(k) = k \% 75$$

Linear Probing

Key Space

- 8
- 3
- 13
- ✓ 6
- ✓ 4
- ✓ 10
- ✓ 33
- .

hash fun

$$f'(k) = \{f(k) + g(i)\} \% 10$$

$$f(k) = k \% 10$$

$$g(i) = 0, 1, 2, \dots$$

$$f'(8) = \{8 + 0\} \% 10 = 8$$

$$f'(3) = \{3 + 0\} \% 10 = 3$$

$$f'(13) = \{3 + 0\} \% 10 = 3$$

$$f'(13) = \{3 + 1\} \% 10 = 4$$

searching(33)

→ hash value 3

avg TC: $O(1)$

Hash Table

0	10
1	
2	
3	3
4	13
5	4
6	6
7	33
8	8
9	

Quadratic Probing

$$f'(k) = \{ f(k) + g(i) \} \% \text{ size}$$

where, $f(k) = k \% \text{ size}$

$$g(i) = i^2, \quad i \in 0, 1, 2, \dots$$

Based on Hashing

① HashSet

② HashMap

TC: $O(1)$ \leadsto Searching }

TC: $O(1)$ \leadsto Inserting }

Based on Red/Black trees

① TreeMap

② TreeSet

TC: $O(\log N)$ \leadsto Searching }

TC: $O(\log^2 N)$ \leadsto Inserting }

HashSet

↳ data structure to store unique values {entities}

3, 13, 9, 3, 7, 1, 2, 2, 3, 13

random order

HashSet

{3, 13, 9, 7, 1, 2}

↳ searching $T.C: O(1)$
↳ inserting $T.C: O(1)$

HashMap.

↳ ds which stores key-value pairs!

shopping cart?

key (string)

Value (Integer)

lays	→	2
coke	→	5
eggs	→	2
oranges	→	4

values can be any value,

unique entity
TC: O(1)

↓
searching /
inserting /
deleting

find All Duplicates In an Array 6

find the Ele, Occ. K times 6

Valid Anagram

str1 = "accio"

str2 = "oicac"

rearrangement

Brute force

Sorting

str1 = "accio"

{leno}

str2 = "accio"

{leno}

Anagram!

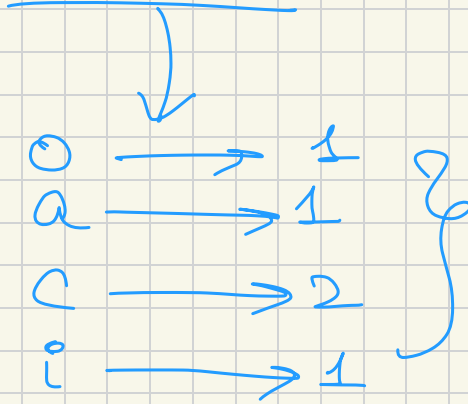
$\begin{cases} TC: O(N \log N) \\ SC: O(N) \end{cases}$

str1 = "accio"



a	→	1
c	→	2
i	→	1
o	→	1

str2 = "ociac"



o	→	1
a	→	1
c	→	2
i	→	1

Anagram!