

Question -

Sum of subarray minimums $\text{mod} = 10^9 + 7$

$\text{arr} = [3, 1, 2, 4]$

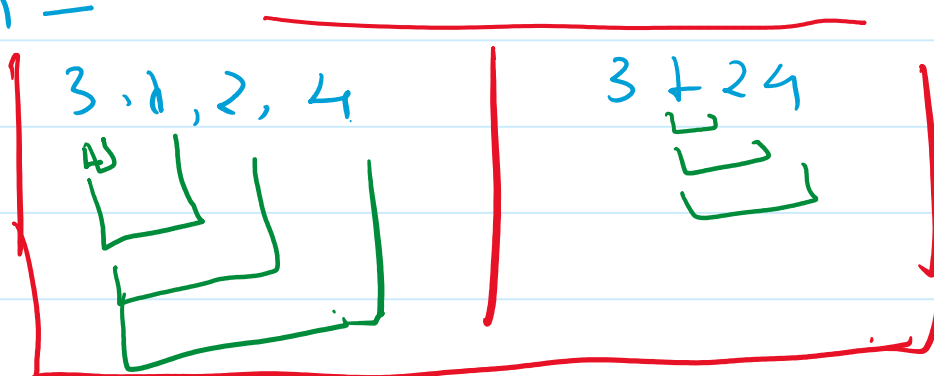
3	→	3	1	→	1	2	→	2	4	→	4
3, 1	→	1	1, 2	→	1	2, 4	→	2			
3, 1, 2	→	1	1, 2, 4	→	1						
3, 1, 2, 4	→	1									

= 17

Method - 1. Brute force approach

- 1.1. Generate all subarray (subsequence)
- 1.2. find minimum from an subsequence.
- 1.3. Sum all subsequence and return it.

Dry Run -



Code

```

sum = 0    mod = (int)(1e9 + 7)
for (i = 0 → n-1)
    mini = arr[i]
    for (j = i → n-1)
        mini = min(mini, arr[j]);
        sum = (sum + mini) % mod;
    }
return sum;

```

$\text{TC} \rightarrow O(N^2)$
 $\text{SC} \rightarrow O(1)$

2nd optimal solution -

Approach

Sum of subarray minimums $\text{mod} = 10^9 + 7$

$\text{arr} = [3, 1, 2, 4]$

3	→	3	1	→	1	2	→	2	4	→	4
3, 1	→	1	1, 2	→	1	2, 4	→	2			
3, 1, 2	→	1	1, 2, 4	→	1						
3, 1, 2, 4	→	1									

+ 3 + 6 + 4 + 4 = 17

- Some points

+ Handling of mod -

$(10^9 + 7) \Rightarrow \text{long MOD} = 1_000_000_007$

+ Counting the Number of time element is smaller

- use knowledge of NGE, NSE arr.

+ final result

- No. of subarr. * (element)

Here $3 * 1 + 1 * 6 + 2 * 2 + 4 * 1 = 17$ Answer

Dry run - & Understanding & Approach.

AN = {1, 4, 6, 2, 3, 7, 8, 1}

↑

What are the Contribution of 3, in given the smaller element

(this can be)

{3}

{3, 2}

{3, 7, 8}

{3, 7, 8, 1} X

X → 1 smallest

Similar

{4, 6, 2, 3}

in all

Case

3 is smaller

(4)
1, 4, 6, 2, 3, 7, 8, 1
3

Total NO. of subarray generate in which '3' is smallest. ⇒ (4 × 3) How?

{4, 6, 2, 3}	{6, 7, 3}	{7, 3}	{3, }
{4, 6, 7, 3, 7}	{6, 7, 3, 7}	{7, 3, 7}	{3, 7}
{4, 6, 2, 3, 7, 8}	{6, 7, 3, 7, 8}	{7, 3, 8}	{3, 7, 8}

this is 12 subarray generated by containing element '3'

Formula for it = left subarray × right subarray

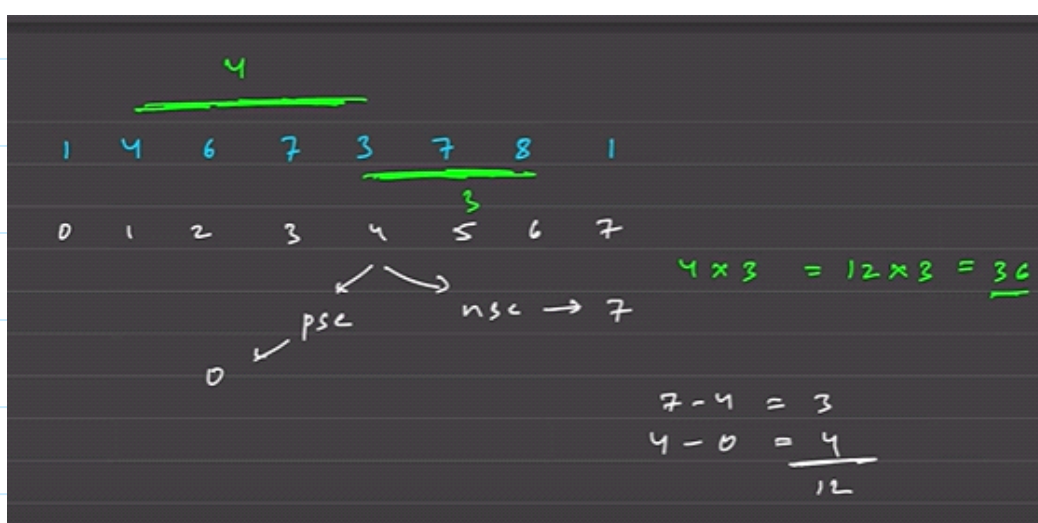
Sum of smallest in subarray containing '3'

= 3 × (4 × 3)
 ↑ ↑ ↘
 left right
 ex.

How to find out left smallest, Right smallest

Use concept of NGE, prevSE

→ instance of storing value store idx, (useful)

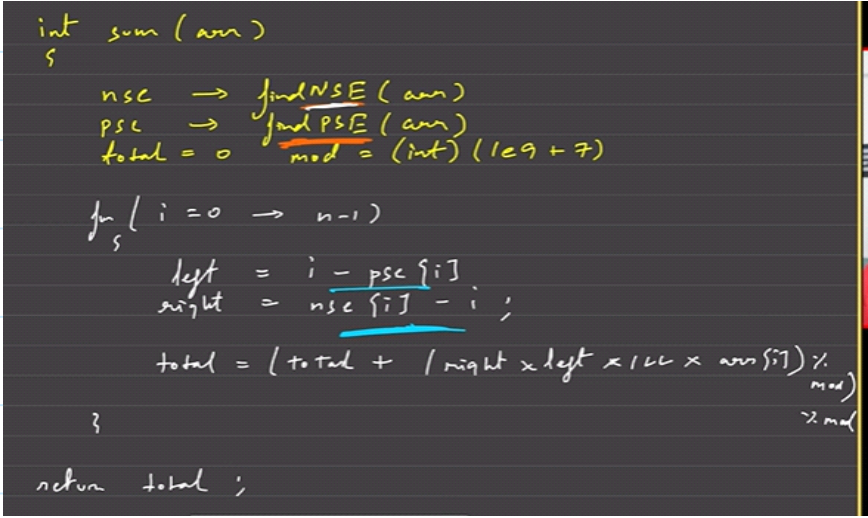


Use the next smallest element and previous smallest element ...

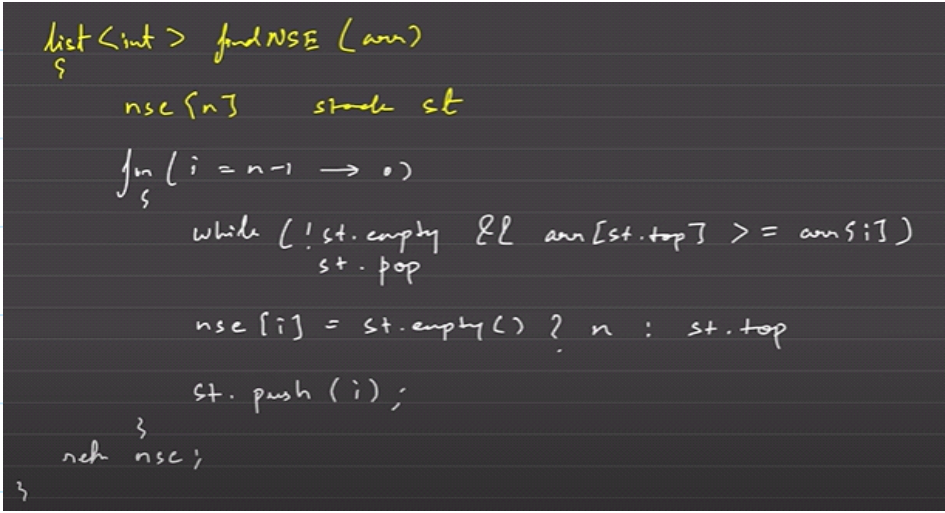
nsc → N → instance of not found store 'N'
 pse → -1 → Previous smallest not found store '-1'

```
import java.util.*;
class Solution {

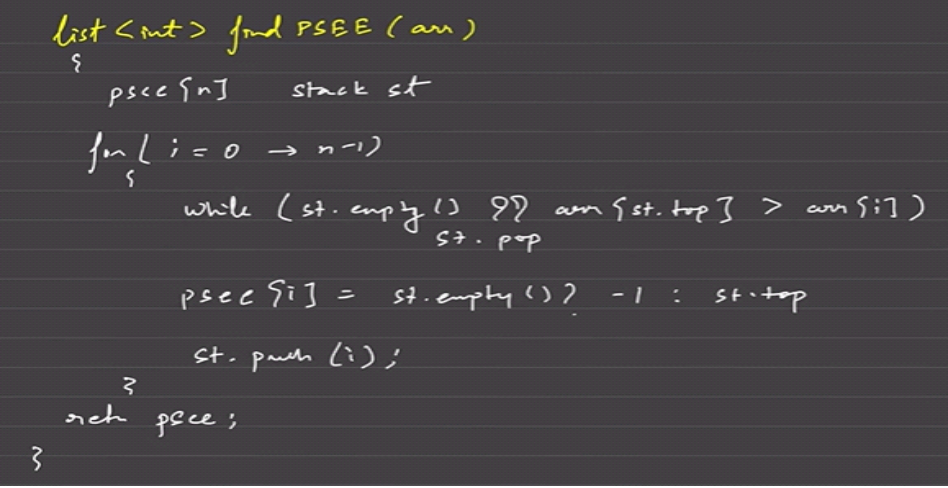
    public int sumSubarrayMins(int[] arr) {
        int n = arr.length;
        int[] nextSmaller = nextSmaller(arr); // TC - O(2N)
        int[] prevSmaller = prevSmaller(arr); // SC - O(2N)
        int MOD = 1_000_000_007;
        long ans = 0;
        for (int i = 0; i < n; i++) {
            long leftDist = (i - prevSmaller[i]);
            long rightDist = (nextSmaller[i] - i);
            long count = leftDist * rightDist;
            ans = (ans + ((count * arr[i]) % MOD)) % MOD;
        }
        return (int) ans;
    }
}
```



```
public static int[] nextSmaller(int[] arr) {
    int[] ans = new int[arr.length];
    Stack<Integer> stack = new Stack<>();
    int n = arr.length;
    for (int i = n - 1; i >= 0; i--) {
        while (!stack.isEmpty() && arr[i] <= arr[stack.peek()])
            stack.pop();
        ans[i] = stack.isEmpty() ? n : stack.peek();
        stack.push(i);
    }
    return ans;
}
```

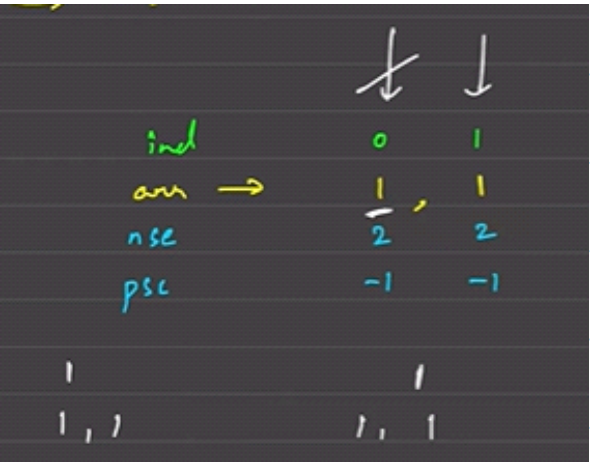


```
public static int[] prevSmaller(int[] arr) {
    int[] ans = new int[arr.length];
    Stack<Integer> stack = new Stack<>();
    int n = arr.length;
    for (int i = 0; i < n; i++) {
        while (!stack.isEmpty() && arr[i] < arr[stack.peek()])
            stack.pop();
        ans[i] = stack.isEmpty() ? -1 : stack.peek();
        stack.push(i);
    }
    return ans;
}
```



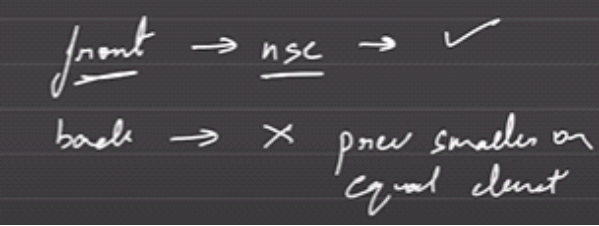
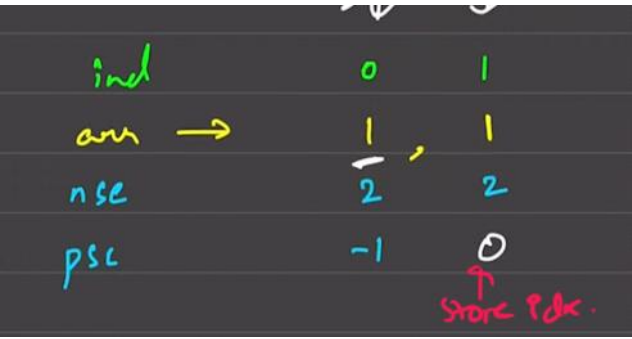
Edge case :
suppose arr={1,1}

then sub array



problem :Is that ... two time consider ... {1,1} :

For that problem resolution ...



Front store the "next smallest "
But .. Previous store ... only ...
Previous smaller or equal element

**Overall time complexity : is : ... $O(5N)$
Space complexity is : $O(5N)$ **

Space complexity can we reduce butkeep the same space complexity .. Because of the ..easy to understand format ...