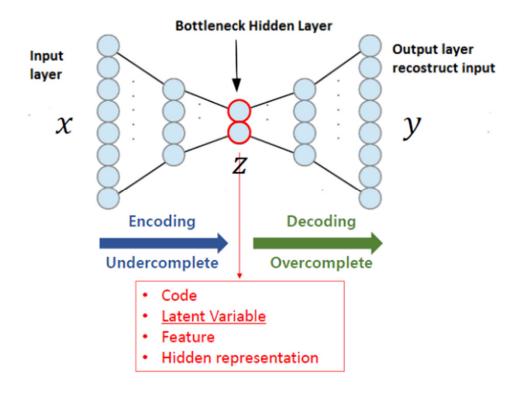
# AutoRec & ConvMF

SoC 19, SeungAn Jung

#### AutoRec - Intro

- Autoencoder paradigm into CF model
- AutoRec has representational and computational advantages over existing neural approaches to CF
- Outperforms SOTA CF
  - RBM-CF
    - Generative Model Discriminative Model
    - MLE RMSE
    - Only applicable for discrete ratings Agnostic to rating
  - LLORMA
    - Embed both users and items into shared latent space only users/itmes
    - Linear latent representation nonlinear latent representation

### AutoRec - AutoEncoder



#### AutoRec - Model

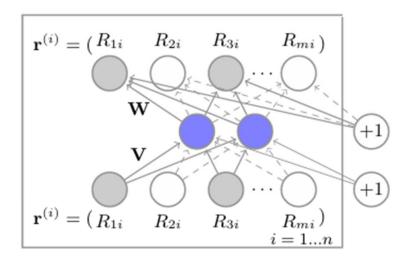


Figure 1: Item-based AutoRec model. We use plate notation to indicate that there are n copies of the neural network (one for each item), where  $\mathbf{W}$  and  $\mathbf{V}$  are tied across all copies.

$$\begin{split} \min_{\theta} \sum_{\mathbf{r} \in \mathbf{S}} ||\mathbf{r} - h(\mathbf{r}; \theta)||_2^2, \\ h(\mathbf{r}; \theta) &= f\left(\mathbf{W} \cdot g(\mathbf{V}\mathbf{r} + \boldsymbol{\mu}) + \mathbf{b}\right) \end{split}$$

$$\min_{\theta} \sum_{i=1}^{n} ||\mathbf{r}^{(i)} - h(\mathbf{r}^{(i)}; \theta))||_{\mathcal{O}}^{2} + \frac{\lambda}{2} \cdot (||\mathbf{W}||_{F}^{2} + ||\mathbf{V}||_{F}^{2}), \quad (2)$$

$$\hat{R}_{ui} = (h(\mathbf{r}^{(i)}; \hat{\theta}))_u.$$

### AutoRec - Evaluation

- Model
  - AutoRec
  - RBM-CF
  - LLORMA
- Dataset
  - Movielens 1M, 10M, Netflix datasets
- Metric: RMSE

### AutoRec - Evaluation

	ML-1M	ML-10M
U-RBM	0.881	0.823
I-RBM	0.854	0.825
U-AutoRec	0.874	0.867
I-AutoRec	0.831	0.782
	(a)	

$f(\cdot)$	$g(\cdot)$	RMSE
Identity	Identity	0.872
Sigmoid	Identity	0.852
Identity	Sigmoid	0.831
Sigmoid	Sigmoid	0.836
	(b)	

	ML-1M	ML-10M	Netflix		
BiasedMF	0.845	0.803	0.844		
I-RBM	0.854	0.825	-		
U- $RBM$	0.881	0.823	0.845		
LLORMA	0.833	0.782	0.834		
I-AutoRec	0.831	0.782	0.823		
(c)					

Table 1: (a) Comparison of the RMSE of I/U-AutoRec and RBM models. (b) RMSE for I-AutoRec with choices of linear and nonlinear activation functions, Movielens 1M dataset. (c) Comparison of I-AutoRec with baselines on MovieLens and Netflix datasets. We remark that I-RBM did not converge after one week of training. LLORMA's performance is taken from [2].

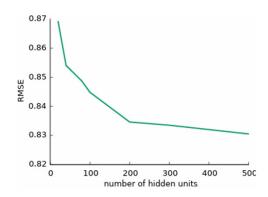


Figure 2: RMSE of I-AutoRec on Movielens 1M as the number of hidden units k varies.

#### ConvMF - Intro

#### Convolutional Matrix Factorization for Document Context-Aware Recommendation

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#### ConvMF - Intro

- Rating matrix becomes sparse -> MF becomes inaccurate
  - -> Improving accuracy by additionally utilizing textual information e.g., reviews, abstracts, synopses
  - LDA, SDAE -> Bag of words models
    - Ignore "contextual information" of document such as surrounding words and word orders.

"people trust the man" vs "people betray his trust finally"

-> PMF + CNN

## ConvMF - Background

#### 1. Matrix Factorization

$$\mathcal{L} = \sum_{i}^{N} \sum_{j}^{M} I_{ij} (r_{ij} - u_{i}^{T} v_{j})^{2} + \lambda_{u} \sum_{i}^{N} \|u_{i}\|^{2} + \lambda_{v} \sum_{j}^{M} \|v_{j}\|^{2}$$

#### 2. CNN

- convolution layer for generating local feature
- pooling layer for representing data as more concise way

### ConvMF - Model

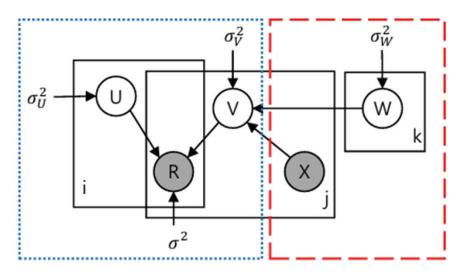


Figure 1: Graphical model of ConvMF model: PMF part in left (dotted-blue); CNN part in right (dashed-red)

### ConvMF - Probabilistic Model

$$\begin{split} p(R|U,V,\sigma^2) &= \prod_{i}^{N} \prod_{j}^{M} N(r_{ij}|u_{i}^{T}v_{j},\sigma^2)^{I_{ij}} \\ p(U|\sigma_{U}^{2}) &= \prod_{i}^{N} N(u_{i}|0,\sigma_{U}^{2}I) \\ p(V|W,X,\sigma_{V}^{2}) &= \prod_{j}^{M} N(v_{j}|cnn(W,X_{j}),\sigma_{V}^{2}I) \\ p(W|\sigma_{W}^{2}) &= \prod_{j}^{M} N(w_{k}|0,\sigma_{W}^{2}I) \\ p(W|\sigma_{W}^{2}) &= \prod_{j}^{M} N(w_{k}|0,\sigma_{W}^{2}I) \end{split}$$

#### ConvMF - CNN

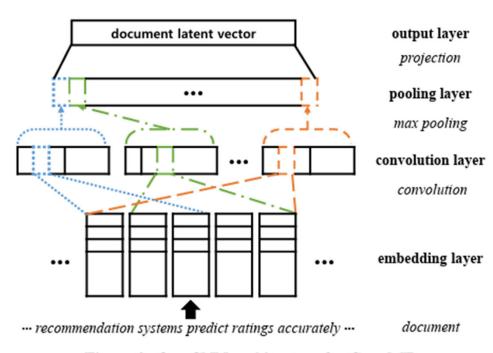


Figure 2: Our CNN architecture for ConvMF

## ConvMF - Optimization

#### MAP

$$\begin{aligned} \max_{U,V,W} p(U,V,W|R,X,\sigma^2,\sigma_U^2,\sigma_V^2,\sigma_W^2) & \mathcal{L}(U,V,W) = \sum_{i}^{N} \sum_{j}^{M} \frac{I_{ij}}{2} (r_{ij} - u_i^T v_j)_2 + \frac{\lambda_U}{2} \sum_{i}^{N} \|u_i\|_2 \\ &= \max_{U,V,W} [p(R|U,V,\sigma^2)p(U|\sigma_U^2)p(V|W,X,\sigma_V^2)p(W|\sigma_W^2)] \\ &+ \frac{\lambda_V}{2} \sum_{i}^{M} \|v_j - cnn(W,X_j)\|_2 + \frac{\lambda_W}{2} \sum_{k}^{|w_k|} \|w_k\|_2, \end{aligned}$$

• Coordinate descent per iteration

$$u_i \leftarrow (VI_iV^T + \lambda_U I_K)^{-1}VR_i$$
  
$$v_j \leftarrow (UI_jU^T + \lambda_V I_K)^{-1}(UR_j + \lambda_V cnn(W, X_j))$$

## ConvMF - Optimization

$$\mathcal{E}(W) = \frac{\lambda_V}{2} \sum_{j=1}^{M} \|(v_j - cnn(W, X_j))\|^2 + \frac{\lambda_W}{2} \sum_{k=1}^{M} \|w_k\|^2 + \text{constant}$$

Optimize W : Backpropagation with given target value  $v_i$ 

$$r_{ij} \approx \mathbb{E}[r_{ij}|u_i^T v_j, \sigma^2]$$
  
=  $u_i^T v_j = u_i^T (cnn(W, X_j) + \epsilon_j)$ 

- Model
  - PMF
  - CTR
  - CDL
  - ConvMF
  - ConvMF+

Dataset	# users	# items	# ratings	density
ML-1m ML-10m	6,040 69,878	3,544 10,073	993,482 9,945,875	4.641% 1.413%
AIV	29,757	15,149	135,188	0.030%

Table 1: Data statistic on three real-world datasets

- Dataset
  - MovieLens 1m, 10m, Amazon Instant Video(AIV)
- Metric: RMSE

	Dataset				
Model	ML-1m	ML-10m	AIV		
PMF	0.8971	0.8311	1.4118		
CTR	0.8969	0.8275	1.5496		
CDL	0.8879	0.8186	1.3594		
ConvMF	0.8531	0.7958	1.1337		
ConvMF+	0.8549	0.7930	1.1279		
Improve	3.92%	2.79%	16.60%		

Table 3: Overall test RMSE

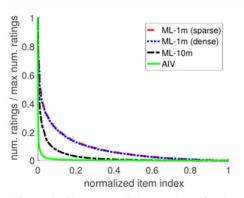


Figure 3: Skewness of the number of ratings for items on each dataset

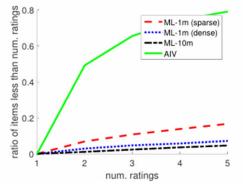


Figure 4: Ratio of items that have less than num. ratings (N) to each entire dataset

	ML-1m		ML-10m		AIV	
Model	$\lambda_U$	$\lambda_V$	$\lambda_U$	$\lambda_V$	$\lambda_U$	$\lambda_V$
PMF	0.01	10000	10	100	0.1	0.1
CTR	100	1	10	100	10	0.1
CDL	10	100	100	10	0.1	100
ConvMF	100	10	10	100	1	100
ConvMF+	100	10	10	100	1	100

Table 2: Parameter Setting of  $\lambda_U$  and  $\lambda_V$ 

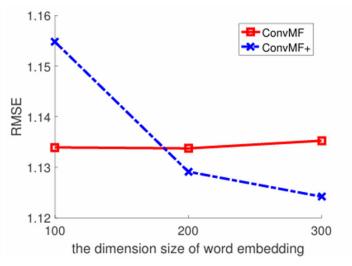


Figure 5: The effects of the dimension size of word embedding on Amazon dataset

	Phrase captured by $W_c^{11}$	$\max(c^{11})$	Phrase captured by $W_c^{86}$	$\max(c^{86})$		
Verb	people trust the man	0.0704	betray his <b>trust</b> finally	0.1009	◆	noun
	Test phrases for $W_c^{11}$	$c_{test}^{11}$	Test phrases for $W_c^{86}$	c <sub>test</sub> <sup>86</sup>		
	people <b>believe</b> the man	0.0391	betray his believe finally	0.0682		
	people faith the man	0.0374	betray his faith finally	0.0693		
	people tomas the man	0.0054	betray his tomas finally	0.0480		

Table 5: Case study on two shared weights of ConvMF

## Conclusion

- AutoRec
  - CF + NN(AutoEncoder)
- ConvMF
  - PMF + CNN