

APPLICATIONS



OF DATA SCIENCE

Community Detection

Applications of Data Science - Class 10

Giora Simchoni

gsimchoni@gmail.com and add #dsapps in subject

Stat. and OR Department, TAU

2023-04-28

APPLICATIONS



Intro

APPLICATIONS



OF DATA SCIENCE

Why detect communities?

- Understand hidden structure
- Identify separate functionalities
- Categorize (e.g. for automating Search & Browse)
- Divide & Conquer (e.g. for visualization)
- Optimize (e.g. with software)
- Reduce size of large networks
- Sheer Coolness

What's a "good" community?

- Either "ground truth" (supervised)
- Many edges within (dense), few edges between (sparse)
(unsupervised)

Spectral Partitioning

APPLICATIONS



OF DATA SCIENCE

Start with dividing the network into 2 communities ("bisection").



What is the number of ways to divide n nodes into two distinct groups?

The *cut size* between two sets of nodes is the number of edges between them:

$$R = \frac{1}{2} \sum_{ij \text{ in different groups}} A_{ij}$$

Define \mathbf{s} the vector which indicates to which community a network belongs:

$$s_i = \begin{cases} +1 & \text{if node } i \text{ belongs to community 1} \\ -1 & \text{if node } i \text{ belongs to community 2} \end{cases}$$

Then:

$$\frac{1}{2}(1 - s_i s_j) = \begin{cases} 1 & \text{if nodes } i, j \text{ belong to different communities} \\ 0 & \text{if nodes } i, j \text{ belong to the same community} \end{cases}$$

So we can sum over all i, j to express R :

$$R = \frac{1}{4} \sum_{ij} A_{ij}(1 - s_i s_j) = \frac{1}{4} \sum_{ij} (A_{ij} - A_{ij}s_i s_j)$$

Do you see where we're going with this?

$$\sum_{ij} A_{ij} = \sum_i \sum_j A_{ij} = \sum_i k_i = \sum_i k_i s_i^2 = \sum_{ij} k_i \delta_{ij} s_i s_j$$

Where δ_{ij} is the *Kronecker delta*, which is 1 if $i = j$ and 0 otherwise.

Then the cut size can be written as:

$$R = \frac{1}{4} \sum_{ij} (k_i \delta_{ij} - A_{ij}) s_i s_j = \frac{1}{4} \sum_{ij} L_{ij} s_i s_j = \frac{1}{4} \mathbf{s}^\top \mathbf{L} \mathbf{s}$$

Where L is the network Laplacian defined earlier.

And so we want to minimize $\frac{1}{4} \mathbf{s}^\top \mathbf{L} \mathbf{s}$ s.t. $s_i = \pm 1$.

Now suppose n_1 and n_2 , no. of nodes expected in community 1 and 2 are known (not unrealistic, especially with equal sizes and when you want to avoid degenerate scenarios).

$$\sum_i s_i = \mathbf{1}^\top \cdot \mathbf{s} = n_1 - n_2$$

Relaxation:

We get rid of having $s_i = \pm 1$, instead we'll require its $L2$ norm to be: $\sum_i s_i^2 = \mathbf{s}^\top \mathbf{s} = n$

Applying Lagrange multipliers we get:

$$\frac{\partial R}{\partial s} = \frac{\partial}{\partial s} \mathbf{s}^\top \mathbf{L} \mathbf{s} + \lambda(n - \mathbf{s}^\top \mathbf{s}) + 2\mu((n_1 - n_2) - \mathbf{1}^\top \cdot \mathbf{s})$$

Equating to 0 to find the minimum and performing the derivatives we get:

$$\mathbf{Ls} = \lambda \mathbf{s} + \mu \mathbf{1}$$

(Here if we have time I can show you how we get to...)

Finally, the solution for \mathbf{s} is:

$$\mathbf{s} = \mathbf{v}_2 + \frac{n_1 - n_2}{n}$$

Where \mathbf{v}_2 is the Fiedler vector: eigenvector of L , which corresponds to λ , the second smallest (after zero) eigenvalue of L .

But \mathbf{s} needs to be at ± 1 , so bottom line we take the n_1 most positive values in \mathbf{v}_2 and put the relevant nodes in community 1, and the rest of the n_2 nodes in community 2.

It can be shown that $R = \frac{n_1 n_2}{n} \lambda$, hence λ , the second smallest eigenvalue of L (a.k.a *algebraic connectivity*) determines the cut size, how easy it is to divide the network into two communities of sizes n_1 and n_2



What if $\lambda = 0$? What if we didn't assume we knew n_1 and n_2 ?

Regarding implementation, I do not think Spectral Clustering is implemented in NetworkX, however you can either implement it yourself or use [SpectralClustering\(\)](#) from Scikit-Learn.

The `SpectralClustering()` of Scikit-Learn isn't identical to what we defined though. I believe that after obtaining \mathbf{v}_2 , there is no way of specifying n_1 and n_2 , instead all nodes with positive values in \mathbf{v}_2 are taken for community 1 and all nodes with negative values are taken to community 2.

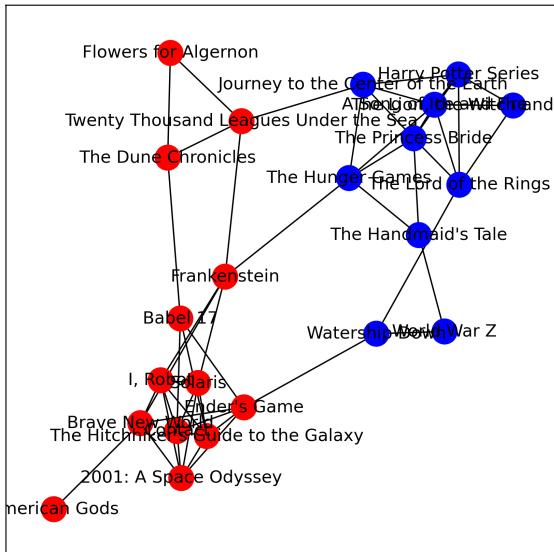
```
import pandas as pd
import numpy as np
import networkx as nx
import matplotlib.pyplot as plt
from sklearn.cluster import SpectralClustering

scifi_edgelist = pd.read_csv('../data/sci_fi_final_edgelist.csv')
G = nx.from_pandas_edgelist(scifi_edgelist, 'book', 'book2', ['cor'
A = nx.to_numpy_array(G)
sc = SpectralClustering(2, affinity='precomputed', n_init=100,
    assign_labels='discretize')
communities = sc.fit_predict(A)

communities[:10]
```

```
## array([1, 1, 1, 1, 1, 0, 0, 1, 1, 0], dtype=int64)
```

```
color_dict = {0: 'blue', 1: 'red'}
nx.draw_networkx(G, nodelist = G.nodes,
    node_color = [color_dict[comm] for comm in communities])
plt.show()
```



Girvan-Newman (Betweennees)

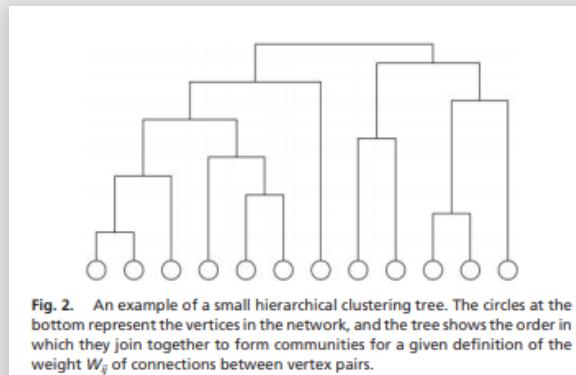
APPLICATIONS



OF DATA SCIENCE

[Girvan & Newman \(2002\)](#) suggested a divisive strategy of repeatedly removing "strongest" edges from the network, slowly uncovering the community structure of the network, until we're left with n communities for n nodes.

This will create a dendrogram of nodes, from a point where all are connected to where all are "leaves":



To choose the community structure best for you either cut the dendrogram where you get k communities or use some other metric.

But what criterion to choose for "strongest" edges?

Girvan & Newman suggested *edge betweenness* which is the same as *betweenness centrality* we have defined, using edges:

$$x_e = \sum_{u,v} \frac{\tau(u,v|e)}{\tau(u,v)}$$

Where $\tau(u, v)$ is the number of shortest paths from node u to node v and $\tau(u, v|e)$ is the number of those shortest paths which pass through edge e .

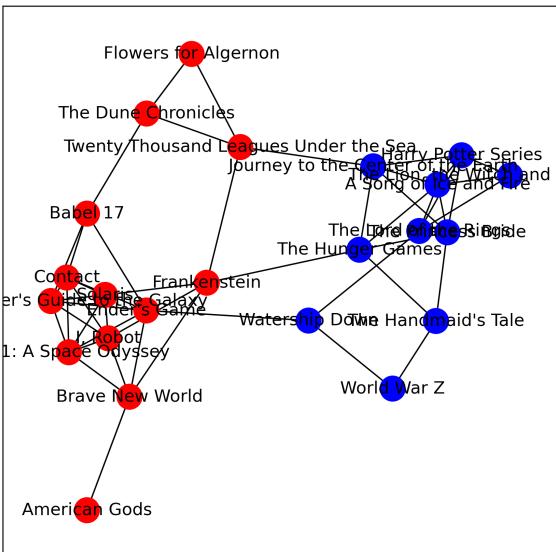
To summarize:

1. Calculate the betweenness for all edges in the network.
2. Remove the edge with the highest betweenness.
3. Recalculate betweennesses for all edges affected by the removal.
4. Repeat from step 2 until no edges remain.



Why recalculate betweenness at each iteration?

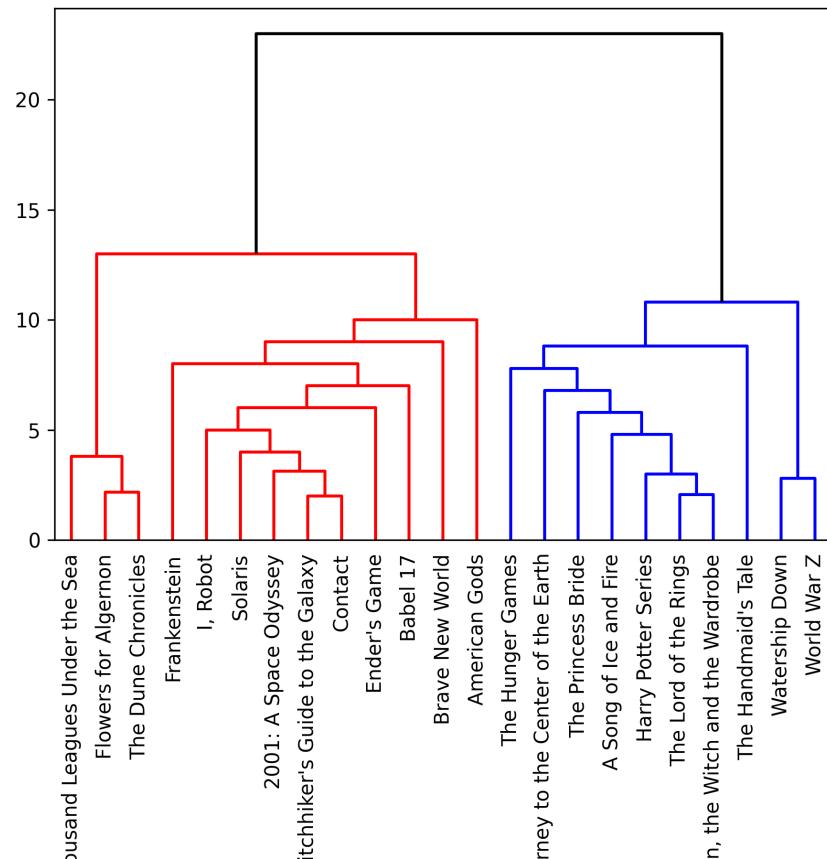
```
communities = nx.community.girvan_newman(G) # returns an iterator
communities = list(next(community)) # we take the first tuple for
                                    # each community
nx.draw_networkx(G, nodelist = G.nodes,
                  node_color = get_node_colors_by_communities(community, G.nodes))
plt.show()
```



APPLICATIONS



Getting the actual dendrogram turned out to be quite laborious, you can see [here](#) how I got it to work or see the slides source (this chunk is hidden because it's a lot of code...)



Label Propagation

APPLICATIONS



OF DATA SCIENCE

Proposition 1: Synchronous

Completely different, beautiful, democratic idea:

1. Initialize a unique label (community) for each node
2. For each node (in parallel): choose the the most common label in neighbors
3. If there is a tie: choose label at random
4. Go back to 2 until some stopping criteria (e.g. no change)

Pros	Cons
Relatively fast (in parallel)	May not converge
	Reproducibility issue



Can you think of a network that will never converge?

Proposition 2: Asynchronous

1. Initialize a unique label (community) for each node
2. Decide on a nodes permutation
3. For each node (one after the other): choose the the most common label in neighbors
4. If there is a tie: choose label at random
5. Go back to 2 until some stopping criteria (e.g. no change)

Pros	Cons
Better convergence	Even worse reproducibility issue, no single solution "Monster communities"
	Relatively slow

Improving Convergence

- Smarter tie breakers:
 - If the node is labelled with one of the tied labels in its neighborhood - keep it
 - Set an order on labels (e.g. $1, \dots, l$) and always choose the max label
 - Or both
- Stopping Criterion
 - Unfortunately "no change in labels" may be too an optimistic criterion to achieve.
 - "Equilibrium": if in the current structure each node has a label no different than the majority label in its neighborhood - stop. In other words: if in the next iteration nodes will change label only due to ties - stop.

Detour: The Network Coloring Problem

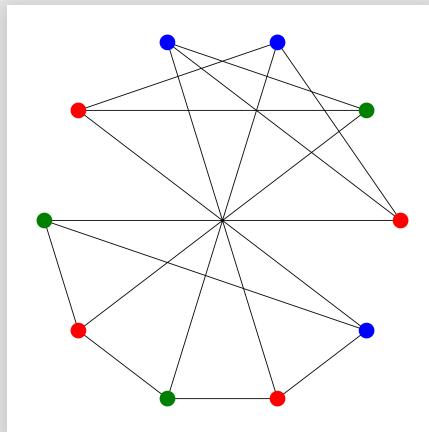
APPLICATIONS



OF DATA SCIENCE

Can you color a network using as few colors as possible, where no two adjacent nodes share the same color?

```
F = nx.petersen_graph()
color_dict = nx.coloring.greedy_color(F)
colors = ['green', 'red', 'blue']
node_colors = [colors[color_ind] for node, color_ind in color_dict.items()]
nx.draw_shell(F, nodelist=F.nodes, node_color=node_colors)
plt.show()
```



Think of a not-so-fast simple algorithm to get this done (A fast algorithm can make this in $O(\max(\deg(G)))$ time!)

The smallest number of colors required to color a given network G is called its *chromatic number*, $\chi(G)$

💡 What is an "easy" upper bound on $\chi(G)$?

What is it good for?

- Scheduling: imagine each node is a university course and two courses share an edge if they have common students. How would you schedule exam times, such that no student has to attend two exams at the same time?
- Political map coloring: no two adjacent countries share a color
- A network G is bipartite iff $\chi(G) = 2$
- Sudoku: $9 \times 9 = 81$ cells (nodes), two cells are connected if they are in the same row/column/square. Can you put in each cell 1 out of 9 numbers (colors) such that no two adjacent cells share the same number?
- And...

End of Detour

APPLICATIONS



OF DATA SCIENCE

Proposition 3: Both ("Semi-Synchronous")

Cordasco & Gargano (2010):

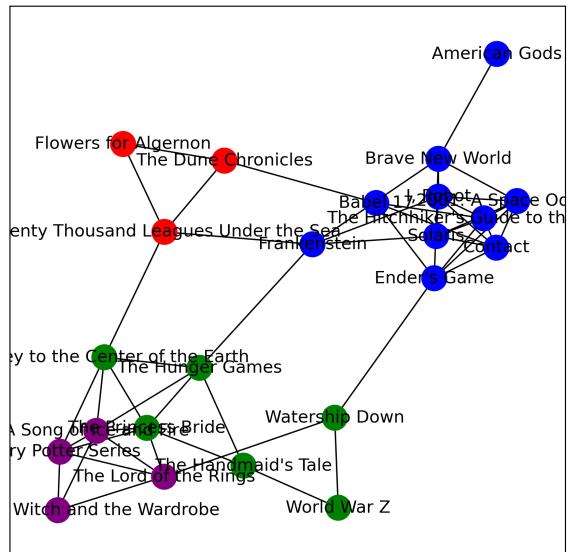
1. Initialize a unique label (community) for each node
2. Network coloring: assign a "color" to the nodes of the network such that no two adjacent nodes share the same color
3. **In each color group** (one after the other), for each node (in parallel): choose the the most common label in neighbors
4. If there is a tie: choose a label by one of the "smarter" tie breakers
5. Go back to 3 until some stopping criteria ("Equilibrium")



Do you see the sense in iterating the nodes in parallel *in each color group*?

```
communities = nx.community.label_propagation_communities(G)

plt.figure()
nx.draw_networkx(G, nodelist = G.nodes,
    node_color = get_node_colors_by_communities(community, G.nodes)
plt.show()
```



Modularity Maximization

APPLICATIONS



OF DATA SCIENCE

Modularity

$$Q = \frac{1}{(2m)} \sum_{vw} \left[A_{vw} - \frac{k_v k_w}{(2m)} \right] \delta(c_v, c_w)$$

Diagram illustrating the components of the Modularity formula:

- Total no. of ends of edges in undirected graph
- Value in adjacency matrix for $[v,w]$. 1 if edge exists, or 0
- Degree of node
- 1 if v and w belong to same community, 0 otherwise

Modularity in words: “the fraction of the edges that fall within the given groups minus the expected fraction if edges were distributed at random.”

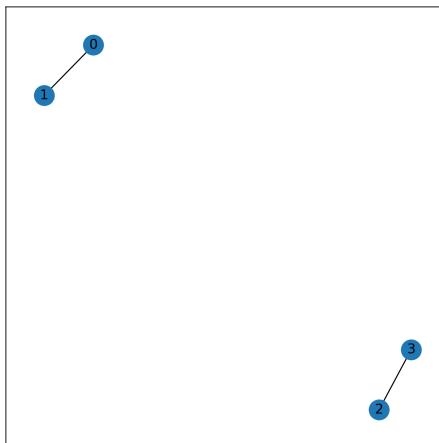


Statisticians might know this from the "observed minus expected" approach for Goodness of Fit statistics.

If the number of within-community edges is no better than random,
 $Q = 0$ (why?).

In general Q ranges from -0.5 to (nearly) 1. You can see the full proof [here](#), but you can also develop some intuition:

```
F = nx.Graph()
F.add_nodes_from(range(4))
F.add_edges_from([(0, 1), (2, 3)])
nx.draw_networkx(F)
plt.show()
```



```
print(nx.community.modularity(F, [{0, 1}, {2, 3}]))
```

0.5

```
print(nx.community.modularity(F, [{0, 2}, {1, 3}]))
```

-0.5

```
F = nx.Graph()
F.add_nodes_from(range(8)) # Add more communities
F.add_edges_from([(0, 1), (2, 3), (4, 5), (6, 7)])
print(nx.community.modularity(F, [{0, 1}, {2, 3}, {4, 5}, {6, 7}]))
```

0.75

```
print(nx.community.modularity(F, [{0, 2, 4, 6}, {1, 3, 5, 7}]))
```

-0.5

 A good Q is said to be above 0.3. What do you think of that?

What would you do with a weighted network?

Bisection, inspired by Spectral Partitioning

Define M to be the *modularity matrix*:

$$M_{ij} = A_{ij} - \frac{k_i k_j}{2m}$$

Note that:

$$\sum_i M_{ij} = \sum_i A_{ij} - \frac{k_j}{2m} \sum_i k_i = k_j - \frac{k_j}{2m} 2m = 0$$

Define as in Spectral Partitioning community vector \mathbf{s} :

$$s_i = \begin{cases} +1 & \text{if node } i \text{ belongs to community 1} \\ -1 & \text{if node } i \text{ belongs to community 2} \end{cases}$$

Follow the same logic and you'll get:

$$Q = \frac{1}{4m} \mathbf{s}^\top \mathbf{M} \mathbf{s}$$

So our goal is to maximize $\mathbf{s}^\top \mathbf{M} \mathbf{s}$ s.t. $s_i = \pm 1$.

And as before we will relax \mathbf{s} to have a norm of n : $\sum_i s_i^2 = \mathbf{s}^\top \mathbf{s} = n$

Applying Lagrange multiplier, taking derivative, equating to zero:

$$\frac{\partial Q}{\partial s} = \frac{\partial}{\partial s} \mathbf{s}^\top \mathbf{M} \mathbf{s} + \lambda(n - \mathbf{s}^\top \mathbf{s}) = 0$$

$$\mathbf{M} \mathbf{s} = \lambda \mathbf{s}$$

Which means that \mathbf{s} is an eigenvector of \mathbf{M} with eigenvalue λ .

Since we can now write: $Q = \frac{1}{4m} \mathbf{s}^\top \mathbf{M} \mathbf{s} = \frac{1}{4m} \lambda \mathbf{s}^\top \mathbf{s} = \frac{\lambda n}{4m}$

It is clear we need the maximum eigenvalue λ , corresponding to the leading eigenvector \mathbf{u}_1 of \mathbf{M} .

But s still needs to be ± 1 , and so usually:

$$s_i = \begin{cases} +1 & \text{if } [u_1]_i > 0 \\ -1 & \text{if } [u_1]_i < 0 \end{cases}$$

This "Spectral bisection" modularity maximization version isn't implemented in NetworkX, probably because you don't necessarily desire only two communities, and finding the leading eigenvector of a M takes time $O(n^2)$, not that fast for large networks.

Still, modularity is widely used.

Greedy Modularity Maximization

Clauset, Newman & Moore (2004) suggested an *agglomerative* strategy of greedily combining communities to find the partition with maximum modularity:

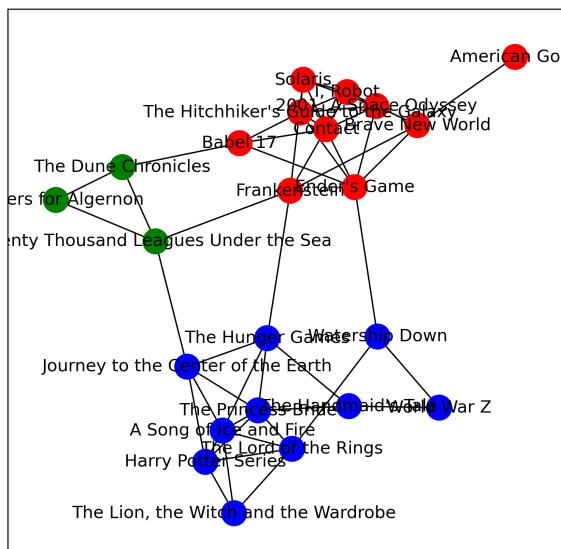
1. Start with n communities: each node as a community of its own
2. Choose the pair of communities that grouping together would result in maximum increase or minimum decrease in Modularity
3. Go back to 2 until only one community is left
4. Review resulting dendrogram choosing the partition (cut) with maximum modularity

The authors show that for sparse networks where $n \sim m$ the complexity is $O(n \log^2(n))$

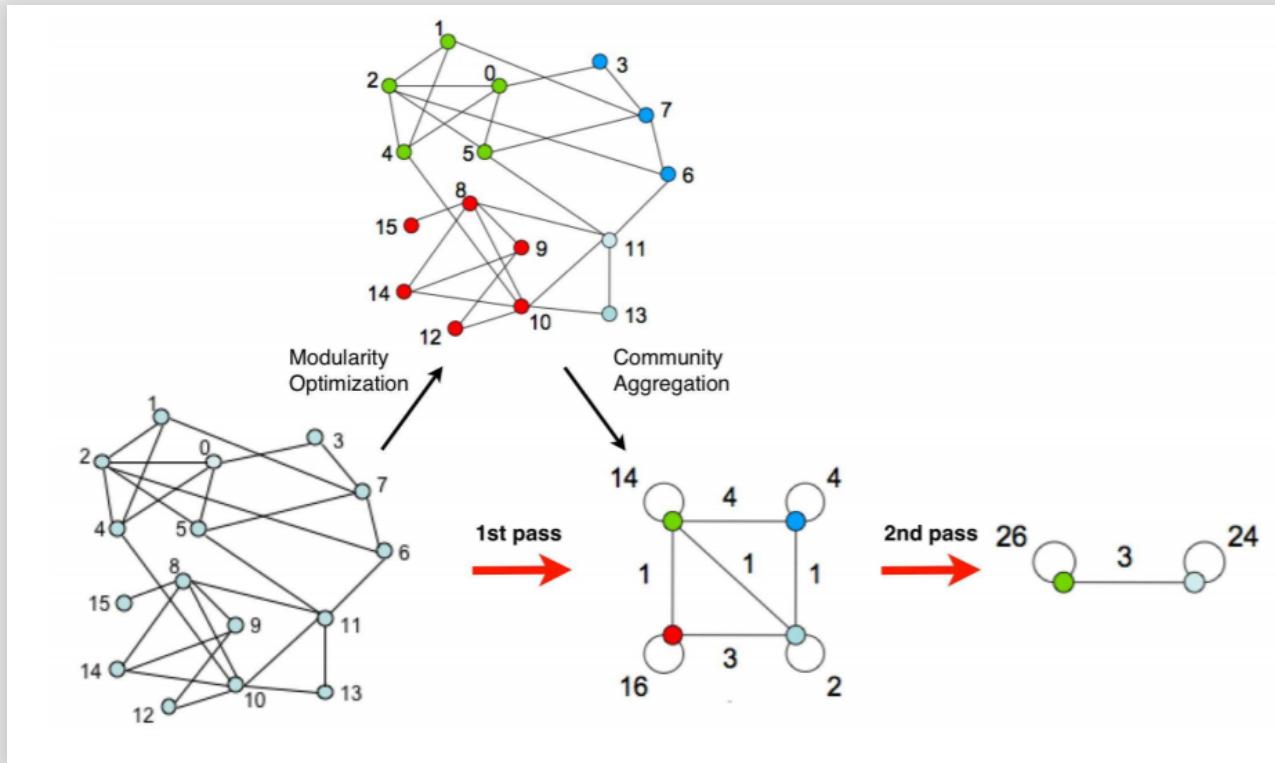
```
communities = nx.community.greedy_modularity_communities(G)
print(nx.community.modularity(G, communities))
```

0.47616301422529794

```
nx.draw_networkx(G, nodelist = G.nodes,
    node_color = get_node_colors_by_communities(community, G.nodes)
plt.show()
```



The Louvain Method (What everyone uses...)



[Blondel et. al. \(2008\)](#) were all researchers at Louvain Uni., so...

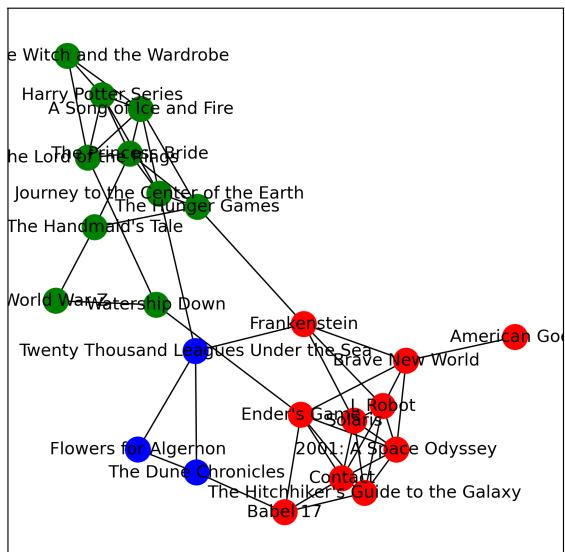
1. Start with n communities: each node as a community of its own
2. For each node i , go over all its neighbors communities: Switch node i 's community with the community for which $\max_j(\Delta Q)$ is reached, s.t. $\max_j(\Delta Q) > 0$ (otherwise leave node i). Keep going (passing all nodes as many times necessary) until no improvement in Q is possible
3. Build a new network: amalgamate each community into a single node, where all its within edges are summed into a single self-loop edge with weight $\times 2$
4. Go back to 2 until no improvement in Q is possible

The Louvain method is extremely fast, "empirical" complexity appears to be linear. It is also available in NetworkX since v2.7:

```
communities = nx.community.louvain_communities(G)
print(nx.community.modularity(G, communities))
```

```
## 0.47616301422529794
```

```
nx.draw_networkx(G, nodelist = G.nodes,
    node_color = get_node_colors_by_communities(community, G.nodes)
plt.show()
```



The Leiden Method (What everyone will use?...)

<https://arxiv.org/abs/1810.08473>

The Leiden method is supposed to not only reach better quality results than Louvain (modularity and more), but is also much faster.

You'll read about it in HW5, and see the [leidenalg](#) package.

Graph Embeddings

APPLICATIONS



OF DATA SCIENCE

Embeddings aren't new.

- A different name for "Embeddings" could be "Dimensionality Reduction".
- In modern Machine Learning, we often get a high-dimensional dataset (say $X_{n \times p}$ and p is very large) some methods cannot handle. One go-to strategy is to reduce the dimension of this dataset matrix by PCA or NMF.
- In Network Analysis too, imagine a huge adjacency matrix A . Especially for the purpose of Community Detection (a.k.a clustering) what if you could reduce the dimensionality of A first, then perform your clustering method of choice (e.g. K-Means)?
- These reduced-dimension vectors are "Embeddings".
- The only question left is: how to reduce the dimensionality?

Detour: word2vec

APPLICATIONS



OF DATA SCIENCE

Bag of Words Model (BOW)

💡 What is the dimensionality of "words"?

- In the Oxford English dictionary there are 171K words. When expanding to jargon etc. the estimate is 1M words
- Now suppose you have 3,000 Yelp reviews classified as "positive" or "negative", which you would use to train a classification model to deploy on the Yelp website
- Each sentence is comprised of a few words
- If a word is a categorical variable which can receive 1 in 1M levels, using the classic approach of dummy variables, in order to build a simple $X_{n \times p}$ matrix for say, logistic regression, you would need to build a 3K x 1M matrix

Don't do it (why?).

The road to word2vec

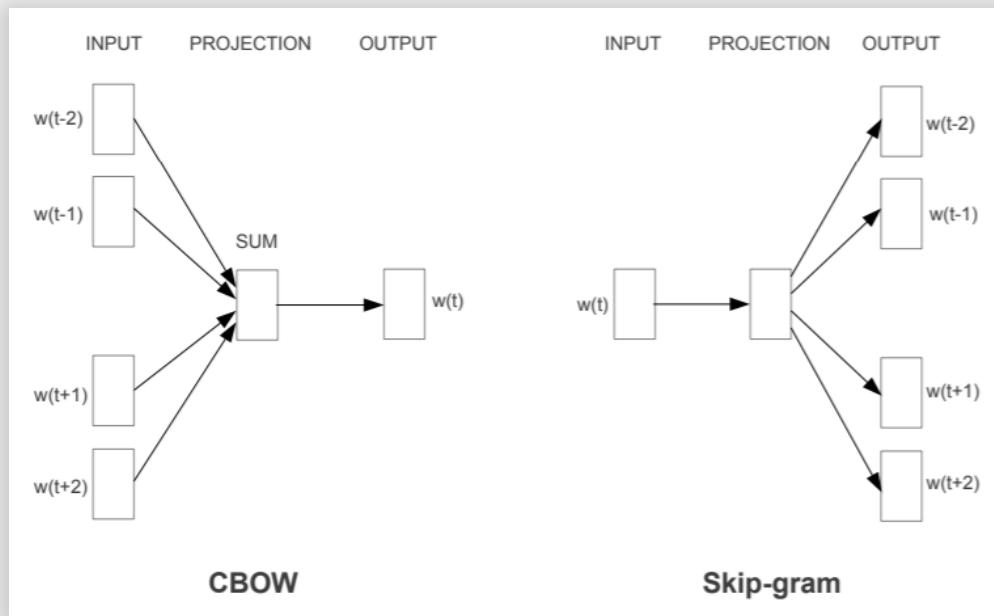
"Regular" dimensionality reduction methods do not work well on text data.

1. They tend to be slow.
2. They ignore (and therefore lose) semantic meaning and grammatical function of a word, as can be seen by unsatisfactory performance in NLP tasks such as translation, finding synonyms and analogies.

Q: What model *would* preserve semantic/syntactic meaning?

A: A model which would be excellent at predicting a word out of context (or the opposite!).

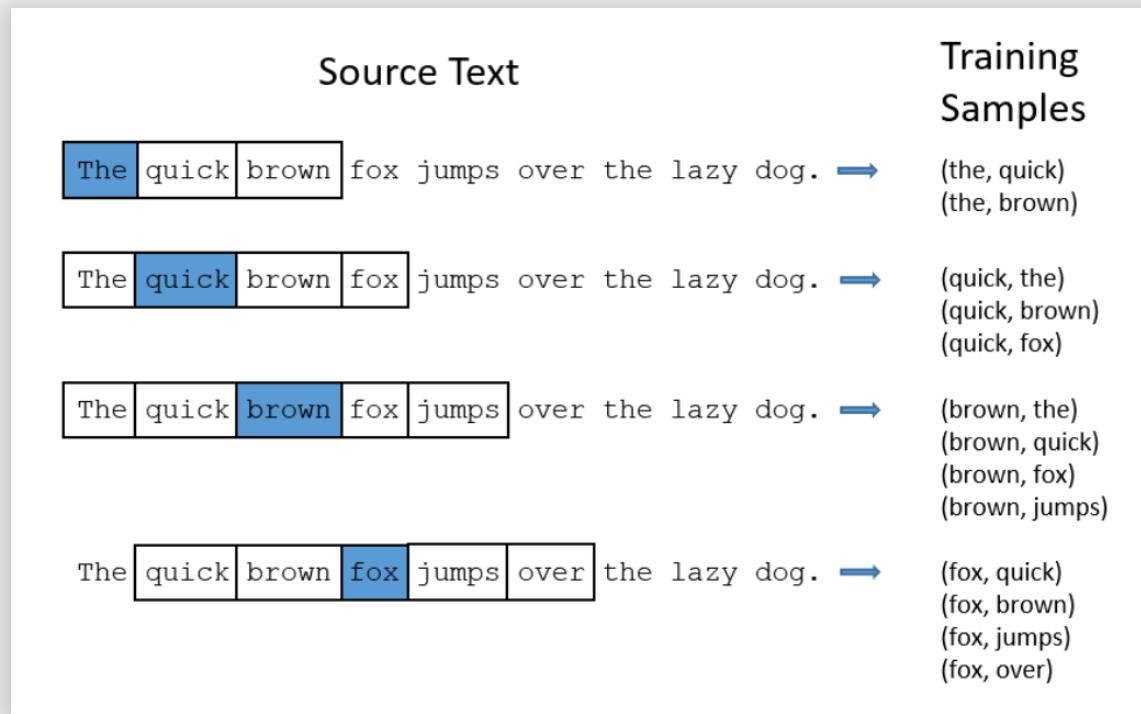
That's exactly what [Mikolov et. al. \(2013\)](#) did:



They had a 2-layer (not that deep) neural network predict:

1. CBOW - a few past and future context-words from a single middle-word
2. Skip-Gram - a single middle-word from a few past and future context-words

Skip-Gram

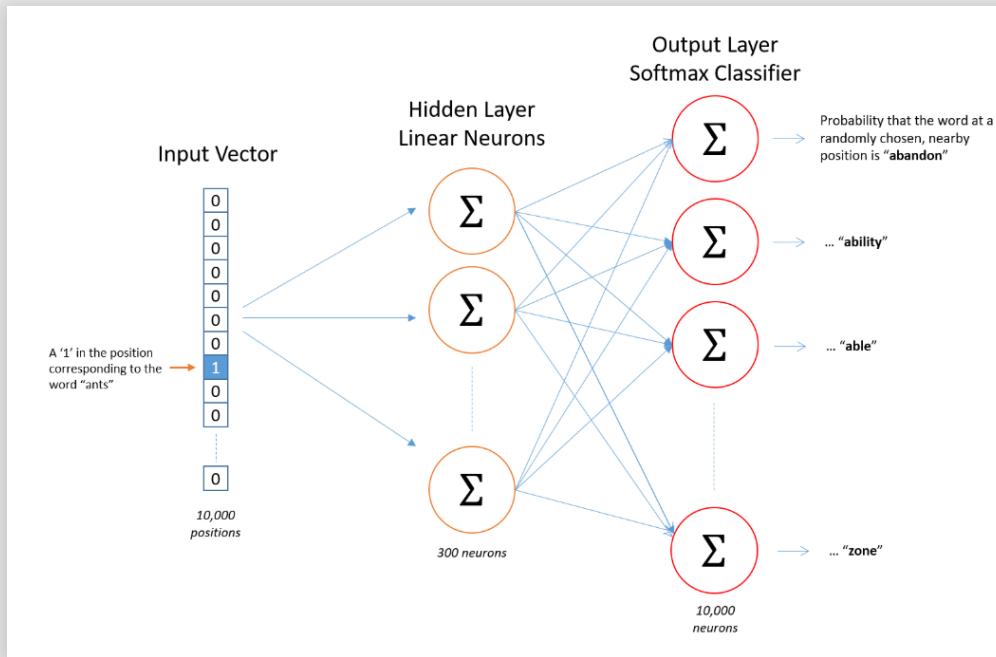


Actually these aren't all the pairs, the final version also includes "negative sampling" of non-correct words.

Source: [Chris McCormick](#)

Network Architecture

So for a vocabulary size of 10K words...



Q: How well did this network do in predicting words?

A: I have no idea. Because...

word2vec

The model was only trained to find the weight matrix W of dimension $|V| \times D$ where:

- $|V|$ is the vocabulary size, the length of the dummy vectors input to the network
- D the size of the hidden layer

In the above example this would be a $10K \times 300$ matrix where for each word there would be a 300-long *word vector* or *embedding* hopefully representing its semantic/syntactic better than traditional dimensionality reduction methods.

This form of learning is also called *Representation Learning*.

Now take these "embeddings" and do whatever with them, from regression to clustering.

Or just do the usual trick of "King - Man + Woman = ?" to get "Queen"...

Note that it doesn't always work!

Table 8: *Examples of the word pair relationships, using the best word vectors from Table 4 (Skip-gram model trained on 783M words with 300 dimensionality).*

Relationship	Example 1	Example 2	Example 3
France - Paris	Italy: Rome	Japan: Tokyo	Florida: Tallahassee
big - bigger	small: larger	cold: colder	quick: quicker
Miami - Florida	Baltimore: Maryland	Dallas: Texas	Kona: Hawaii
Einstein - scientist	Messi: midfielder	Mozart: violinist	Picasso: painter
Sarkozy - France	Berlusconi: Italy	Merkel: Germany	Koizumi: Japan
copper - Cu	zinc: Zn	gold: Au	uranium: plutonium
Berlusconi - Silvio	Sarkozy: Nicolas	Putin: Medvedev	Obama: Barack
Microsoft - Windows	Google: Android	IBM: Linux	Apple: iPhone
Microsoft - Ballmer	Google: Yahoo	IBM: McNealy	Apple: Jobs
Japan - sushi	Germany: bratwurst	France: tapas	USA: pizza

End of Detour

APPLICATIONS



OF DATA SCIENCE

node2vec

Grover & Leskovec (2016):

learn a mapping of nodes to a low-dimensional space of features that maximizes the likelihood of preserving network neighborhoods of nodes.

In short, if:

- a word is a node
- a sentence or a window of words is a neighborhood

We could just use word2vec to get *meaningful* node emebeddings!

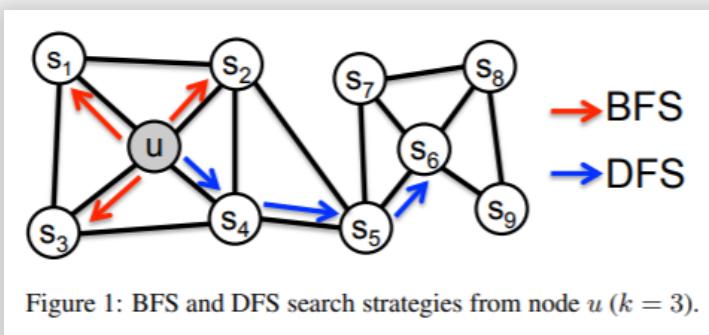
Then, in this low-dimensional space perform node clustering to communities with your clustering method of choice (original article uses K-Means).

How to sample a neighborhood?

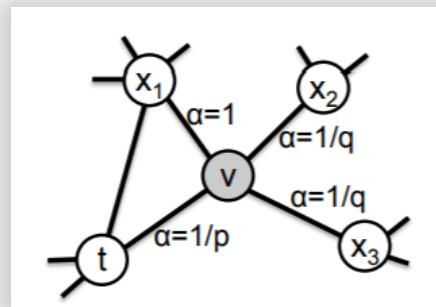
The researchers differentiate between two similarities between a pair of nodes:

- Homophily: which are your immediate neighbors? similar to semantics?
- Structural Equivalence: what is your *role* in the neighborhood? similar to syntaxics?

In addition they point out that the two common search strategies BFS and DFS "play a key role in producing representations that reflect either of the above equivalences".



The biased random walk procedure



For each node v , the "search bias" α_{vx} of advancing to the following node x after coming from node t is computed before hand, using parameters p and q :

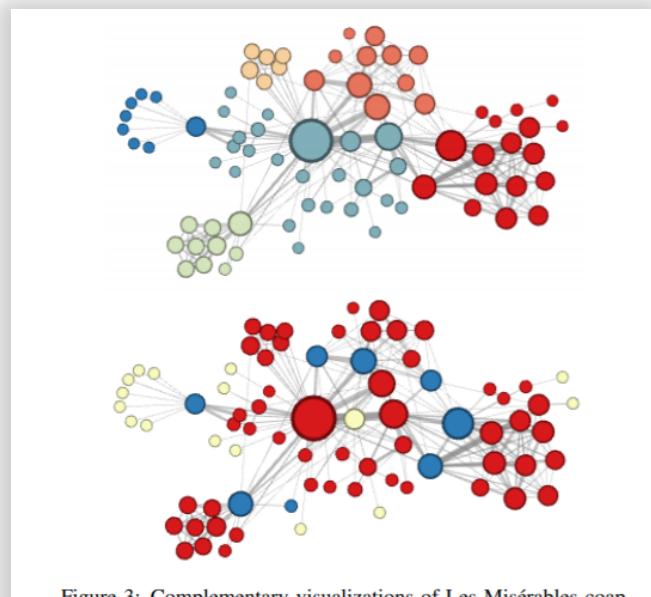
- if node x is t itself: $1/p$
- if node x is connected to t : 1
- if node x isn't connected to t : $1/q$

Obviously these aren't probabilities, these are weights whose sum needs to be normalized to 1.

The biased random walk procedure

Which p, q to use?

- low p , high q : we are unlikely to progress, and stick to the local neighborhood of t (related to BFS, emphasis on Homophily)
- high p , low q : we are unlikely to go back to t , we are progressing (related to DFS, emphasis on Structural Equivalence)



node2vec isn't implemented in NetworkX but has been implemented by Elior Cohen in the [node2vec](#) library, based on [gensim](#) word2vec fitting.

Initialize the random walk probabilities, say $p = q = 1$ and the dimensionality of the embeddings is 64:

```
from node2vec import Node2Vec

node2vec = Node2Vec(G, dimensions=64, walk_length=30, num_walks=200, p=1, q=1)

## Computing transition probabilities: 0% | 0/23 [00:00<?, ?it/s]
## Computing transition probabilities: 100%|#####
## Generating walks (CPU: 1): 0% | 0/200 [00:00<?, ?it/s]
## Generating walks (CPU: 1): 4% | 3 / 200 [00:00<00:03, 60.97it/s]
## Generating walks (CPU: 1): 7% | 7 / 200 [00:00<00:03, 55.26it/s]
## Generating walks (CPU: 1): 10% | # 20 / 200 [00:00<00:03, 56.32it/s]
## Generating walks (CPU: 1): 13% | # 3 26 / 200 [00:00<00:03, 52.73it/s]
## Generating walks (CPU: 1): 16% | # 6 32 / 200 [00:00<00:03, 52.46it/s]
## Generating walks (CPU: 1): 19% | # 9 38 / 200 [00:00<00:03, 52.54it/s]
## Generating walks (CPU: 1): 22% | # 2 44 / 200 [00:00<00:02, 52.47it/s]
## Generating walks (CPU: 1): 25% | # 5 50 / 200 [00:00<00:02, 52.67it/s]
## Generating walks (CPU: 1): 28% | # 8 56 / 200 [00:01<00:02, 52.78it/s]
## Generating walks (CPU: 1): 31% | # 1 62 / 200 [00:01<00:02, 52.52it/s]
```

Perform SGD to fit the $W_{23 \times 64}$ matrix which we call X here for what's coming next:

```
model = node2vec.fit(window=6, min_count=1, batch_words=4)

X = model.wv.vectors

print(X.shape)

## (23, 64)
```

Perform K-means on X , specifying $k = 2$:

```
from sklearn.cluster import KMeans

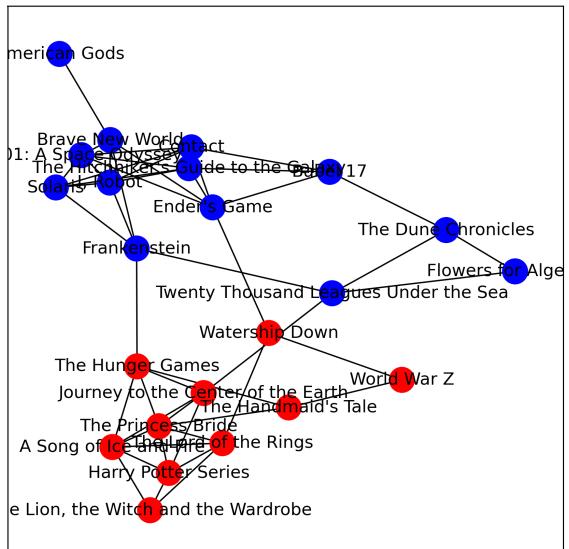
kmeans = KMeans(n_clusters=2, random_state=0).fit(X)
```

```

color_dict = {0: 'blue', 1: 'red'}
book_color_dict = {book: color_dict[color] for book, color in zip
node_colors = [book_color_dict[book] for book in G.nodes]

nx.draw_networkx(G, nodelist = G.nodes, node_color = node_colors)
plt.show()

```



Other methods

APPLICATIONS



OF DATA SCIENCE

Adjacency matrix based:

- Hierarchical Clustering
- K-Means
- Whatever you find in Scikit-Learn...

Heuristics:

- Kernighan-Lin

Modularity Maximization:

- Simulated Annealing
- Genetic Algorithms

Nonnegative Matrix Factorization:

- BigCLAM

Graph Embeddings (Deep Learning):

- Graph Neural Networks
- SDNE

Game Theory:

- GLEAM