# **Aphros documentation**

Release 0.1.2

**Petr Karnakov** 

**Sergey Litvinov** 

# **CONTENTS**

1	Introduction	1
2	Communication	3
3	Convection-diffusion equation 3.1 Implicit solver	6
4	4.2 Projection	10 10 11
5		13 15
6	6.1Advection solver6.2Diffusion solver6.3Taylor-Couette flow	17 19 22 25 26
7	Geometric primitives	29
8	8.1 Code blocks	33 33 34
9	Output	35
10	10.1 AWK for CSV files	37 37 38 38
11	11.1 CSV IO	39 40 41 43

12	Log		47
	12.1	Surface tension as gradient	17
	12.2	Particle normal displacement	
			48
			48
	12.5	Number of particles and strings	48
			49
			49
			49
			50
	12.10	Registered modules in Ubuntu	50
	12.11	VTK merge, comparison of floats with tolerance	50
		Explicit part of viscous stress	51
13	Conti	ributing	53
	13.1	Style guide	53
Bib	oliogra	phy	55

**CHAPTER** 

### **ONE**

#### INTRODUCTION

**Aphros** is a finite volume solver for incompressible multiphase flows with surface tension. Key features:

- implementation in C++14
- abstractions for mesh elements (cells, faces and nodes), range-based loops over them and the corresponding data fields (cell-, face- and node-based fields)
- convenient and fast development (no need to write 3D loops) using only standard features of the language (without code generators or domain-specific languages)
- scalability to thousands of compute nodes using MPI/OpenMP thanks to the Cubism library for distributed computing on structured grids
- coroutines to enable encapsulation in the block-wise processing framework
- individual solvers can be used separately as regular classes or functions
- fluid solver based on SIMPLE or Bell-Colella-Glaz methods
- · conservative split advection solver based on PLIC
- method of particles for curvature estimation that outperforms standard techniques at low resolutions which is well-suited for simulation with many small bubbles and drops
- multilayer volume-of-fluid scheme for coalescence prevention which has the computational cost that does not depend on the number of bubbles in the simulation and therefore can describe processes such as generation of foam

#### COMMUNICATION

The grid is decomposed into subdomains, one for each MPI rank. Each subdomain is further divided into cubic blocks of fixed size. The program is built following the SPMD (single program multiple data) model. Each MPI rank processes its blocks sequentially. The code is divided into *stages* which are executed in parallel on all blocks with synchronization after every stage. This implements *coroutines*. The code can issue communication requests which are collected during each stage and executed before transferring to the next stage.

The following function consists of two stages:

```
void F(Mesh& m) {
    auto sem = m.GetSem();
    struct {
        FieldCell<Scal> fc;
    }* ctx(sem);

    if (sem()) {
        fc.Reinit(m, m.GetId());
        m.Comm(&fc);
    }

    if (sem()) {
        fc.Reinit(m, 0);
    }
}
```

Mesh *m* provides functionality for parallel communication. Pointer *ctx* will be initialized to point at an instance of the user-defined *struct* persistent across stages of one call of the function. The instance is created before the execution of the first stage and destroyed after the last stage.

Communication requests include:

```
void Comm(std::unique_ptr<CommRequest>&& r)

void Reduce(std::unique_ptr<Op>&& o)

void GatherToLead(std::vector<T>* buf)

void Dump(const FieldCell<Scal>* field, std::string name)
```

**CHAPTER** 

THREE

#### CONVECTION-DIFFUSION EQUATION

Abstract class ConvDiffVect describes the interface of a solver for the vector convection-diffusion equation

$$\rho \left( \frac{\partial \mathbf{u}}{\partial t} + (\mathbf{v} \cdot \nabla) \mathbf{u} \right) = \nabla \cdot (\mu \nabla \mathbf{u}) + \mathbf{f}$$

in the discrete form

$$\rho_c \left( \frac{\delta \mathbf{u}_c}{\delta t} + \frac{1}{V_c} \sum_{f \in c} v_f \mathbf{u}_f S_f^c \right) = \frac{1}{V_c} \sum_{f \in c} \mu_f \frac{\delta \mathbf{u}_f}{\delta n} S_f^c + \mathbf{f}_c$$
(3.1)

where c is a cell index,  $\phi_c$  is a cell-average,  $f \in c$  are neighbour faces of cell c,  $\phi_f$  is a face-average,  $S_f^c$  is the signed face area (positive if  $\mathbf{n}_f$  is an outer normal to c) and  $V_c$  is the cell volume.

The constructor takes pointers to fields of density  $\rho$ , viscosity  $\mu$ , force f and volume flux  $\mathbf{v} \cdot \mathbf{S}_f$ :

```
// par: parameters
// fcr: density
// ffd: diffusion coefficient
// fcs: source
// ffv: volume flux
ConvDiffVect(
    double time, double dt, M& m_, const EB& eb_, Par par_,
    const FieldCell<Scal>* fcr, const FieldFaceb<Scal>* ffd,
    const FieldCell<Vect>* fcs, const FieldFaceb<Scal>* ffv)
```

After an implementation is constructed, the solution is advanced by calling MakeIteration() and the current velocity field is returned by

```
virtual const FieldCell<Vect>& GetVelocity(Step) const
```

The interface also exposes functions

```
virtual void Assemble(
    const FieldCell<Vect>& fcw, const FieldFaceb<Scal>& ffv)
```

```
// linear system returned by GetDiag() and GetConst()
virtual void Assemble(
   const FieldCell<Vect>& fcw, const FieldFaceb<Scal>& ffv)
```

```
// linear system returned by GetDiag() and GetConst()
virtual void Assemble(
   const FieldCell<Vect>& fcw, const FieldFaceb<Scal>& ffv)
```

to assemble the linear system for a given velocity field fcw from the previous iteration and the volume flux ffv and access its scalar component d. Furthermore, the current solution can be explicitly corrected with

```
virtual void CorrectVelocity(Step, const FieldCell<Vect>&)
```

Both these features are required for the pressure correction equation.

### 3.1 Implicit solver

Class ConvDiffVectImp implements an implicit solver corresponding to the discrete equation

$$\rho_c^s \left( \frac{\delta \mathbf{u}_c^{s+1}}{\delta t} + \frac{1}{V_c} \sum_{f \in c} v_f^s \mathbf{u}_f^{s+1} S_f^c \right) = \frac{1}{V_c} \sum_{f \in c} \mu_f^s \frac{\delta \mathbf{u}_f^{s+1}}{\delta n} S_f^c + \mathbf{f}_c^s$$

which requires solving a linear system at every iteration.

In addition to the requirements of the base class, the constructor takes mappings describing the boundary conditions and the initial fields:

```
// ffv: volume flux
ConvDiffVect(
    double time, double dt, M& m_, const EB& eb_, Par par_,
    const FieldCell<Scal>* fcr, const FieldFaceb<Scal>* ffd,
    const FieldCell<Vect>* fcs, const FieldFaceb<Scal>* ffv)
```

with the initial velocity fcvel, face conditions mfc, cell conditions mcc, density fcr, viscosity fcd, force fcs, and volume flux ffv. Parameters of the solver are provided by

```
struct ConvDiffPar {
   Scal relax = 1.; // relaxation factor [0,1] (1 -- no relaxation)
   bool second = true; // second order in time
   ConvSc sc = ConvSc::quick; // scheme for convective flux (see convdiffi.h)
   Scal df = 1.; // deferred correction factor
   Scal th = 1e-10; // threshold for flow direction
   bool stokes = false; // Stokes flow, disable convective fluxes and time
   bool symm = false; // use symmetric solver for linear system
   bool explconv = false; // explicit convective fluxes in case Conv::imp
};
```

where sc defines the interpolation scheme

Table 3.1: Interpolation schemes.

ConvSc::fou	First Order Upwind
ConvSc::cd	Central Differences (midpoint)
ConvSc::sou	Second Order Upwind
ConvSc::quick	QUICK

# 3.2 Explicit solver

Class ConvDiffVectExp implements an explicit solver corresponding to the discrete equation

$$\rho_c^s \Big( \frac{\delta \mathbf{u}_c^{s+1}}{\delta t} + \frac{1}{V_c} \sum_{f \in c} v_f^s \mathbf{u}_f^s S_f^c \Big) = \frac{1}{V_c} \sum_{f \in c} \mu_f^s \frac{\delta \mathbf{u}_f^s}{\delta n} S_f^c + \mathbf{f}_c^s.$$

Here the solution is advanced by explicit formulas and the linear system is constructed only to implement Assemble() and GetVelocityEquations() of the base class.

3.2. Explicit solver 7

**CHAPTER** 

**FOUR** 

#### **NAVIER-STOKES EQUATIONS**

Abstract class FluidSolver describes the interface of a solver for the Navier-Stokes equations

$$\nabla \cdot \mathbf{u} = S_v$$

$$\rho \left( \frac{\partial \mathbf{u}}{\partial t} + (\mathbf{v} \cdot \nabla) \mathbf{u} \right) = -\nabla p + \nabla \cdot \mu (\nabla \mathbf{u} + \nabla \mathbf{u}^T) + \mathbf{f}$$

where the continuity equation is discretized as

$$\sum_{f \in c} v_f S_f^c = S_v$$

and the momentum equation as (3.1), where  $S_v$  is the volume source term.

The constructor takes pointers to fields of density  $\rho$ , viscosity  $\mu$ , force f and volume source  $S_v$ :

After an implementation is constructed, the solution is advanced by calling MakeIteration() and the current solution is provided by

```
virtual const FieldCell<Vect>& GetVelocity(Step) const
```

```
virtual const FieldCell<Scal>& GetPressure(Step) const
```

```
virtual const FieldEmbed<Scal>& GetVolumeFlux(Step) const
```

The volume flux satisfies the continuity equation and the cell-based velocity satisfies the momentum equation.

#### 4.1 SIMPLE

Class Simple implements the solver using the SIMPLE method.

In addition to the requirements of the base class, the constructor takes mappings describing the boundary conditions and the initial fields.

```
// par: parameters
Simple(M& m, const EB& eb, const Args& args)
```

with the initial velocity fcw, face conditions mfc, cell conditions mcc, density fcr, viscosity fcd, force fcf, projections of well-balanced force fcbp, volume source fcsv and mass source fcsm. Parameters of the solver are provided by

```
struct SimplePar {
 using Scal = typename Vect::Scal;
 Scal vrelax = 0.8; // velocity relaxation factor [0,1]
 Scal prelax = 1.; // pressure relaxation factor [0,1]
 Scal rhie = 1.; // Rhie-Chow factor [0,1] (0 disable, 1 full)
 bool second = true; // second order in time
 Vect meshvel = Vect(0); // relative mesh velocity
 size_t inletflux_numid = 0; // reduction for id from 0 to numid-1
 ConvSc convsc = ConvSc::quick; // convection scheme
 Scal convdf = 1.; // deferred correction factor
 bool stokes = false;
 bool explconv = false; // explicit convection for Conv::imp
 bool convsymm = false; // symmetric solver for linear system in convdiff
 Conv conv = Conv::imp; // convection-diffusion solver
 Scal outlet_relax = 1;
 bool explviscous = true; // enable explicit viscous terms
```

# 4.2 Projection

Class Proj implements the solver using Chorin's projection.

In addition to the requirements of the base class, the constructor takes mappings describing the boundary conditions and the initial fields.

```
// par: parameters
Proj(M& m, const EB& eb, const Args& args)
```

with the initial velocity fcw, face conditions mfc, cell conditions mcc, density fcr, viscosity fcd, force fcf, projections of well-balanced force fcbp, volume source fcsv and mass source fcsm. Parameters of the solver are provided by

```
struct ProjPar {
  using Scal = typename Vect::value_type;
  Scal vrelax = 1; // velocity relaxation factor [0,1]
  Scal prelax = 1.; // pressure relaxation factor [0,1]
  bool second = true; // second order in time
  Vect meshvel = Vect(0); // relative mesh velocity
  size_t inletflux_numid = 0; // reduction for id from 0 to numid-1
  ConvSc convsc = ConvSc::quick; // convection scheme
  Scal convdf = 1.; // deferred correction factor
```

(continues on next page)

# 4.3 Boundary conditions

The boundary conditions are specified by a map from IdxFace to CondFaceFluid, instances of which can be generated with function solver::Parse() from a string. Value of id is written to field fluidcond in bc.vtk (see *Output*).

<b>,</b>							
class	Parse() format	description	id				
NoSlipWallFixed	wall <x y="" z=""></x>	no-slip wall with fixed velocity	1				
InletFixed	inlet <x y="" z=""></x>	inlet with given velocity	3				
InletFlux	inletflux <x id="" y="" z=""></x>	inlet with given total flux	3				
OutletAuto	outlet	outlet	4				
SlipWall	slipwall	free-slip wall	2				

Table 4.1: Fluid boundary conditions.

**CHAPTER** 

**FIVE** 

#### **MULTILAYER VOF**

Multilayer VOF is a method for solving the advection equation that can represent multiple interfaces in the same cell. This enables simulations of foams, suspensions, and other multiphase systems where bubbles and drops that do not coalesce.

The split conservative advection scheme Weymouth and Yue [1] operates on a volume fraction field and uses the PLIC reconstruction to compute the fluxes. In three dimensions, one advection step is split into three sub-steps, or sweeps. To ensure conservation, a divergence term is added explicitly. The normals are estimated using the mixed Youngs-centered scheme.

The multilayer VOF implements the same advection scheme but operates on *multilayer fields*. A multilayer field (u,q) stores mappings between *colors q* and *values u*. The colors are real numbers, and *none=-1* denotes an empty color. Assuming that each cell can contain at most L=4 values, the mappings are represented as L-tuples up to reordering. For example, the following tuples encode a field (u,q) with three values in cell c1 and two values in cell c2

```
u[c1]: {0.2, 0.4, 0.1, 0}
q[c1]: { 0, 1, 2, none}
u[c2]: {0.3, 0.7, 0, 0}
q[c2]: { 1, 2, none, none}
```

The ordering of tuples is insignificant, so simultaneous permutation of values and colors gives equivalent representations

```
u[c1]: {0.4, 0.1, 0.2, 0}
q[c1]: { 1, 2, 0, none}
u[c2]: {0.7, 0, 0.3, 0}
q[c2]: { 2, none, 1, none}
```

A conventional field can be constructed from a multilayer field by selecting values with a given color. For example, selecting the values with color qs=2 gives a conventional field us

```
us[c1]: 0
us[c2]: 0.7
```

The following pseudocode implements the multilayer VOF method. One advection step is split in the spatial directions and in three dimensions consists of three substeps, or sweeps.

```
void Step() {
  for (d: {0, 1, 2}) {
     {u, q} = Sweep(d, u, v, q, n, a);
     {n, a} = Plic(u);
  }
  q = Recolor(u, q);
}
```

Given the PLIC reconstruction of the interface, one sweep computes fluxes, updates the volume fractions and propagates the colors to downwind cells

```
auto Sweep(d, u, v, q, n, a) {
  // v: mixture flux
  // w: phase flux
 // qf: phase color from upwind cell
 for (f : faces) {
   for (1 : layers) {
      c = AdjacentCell(f, v[f] > 0 ? 0 : 1); // upwind cell
     w(f, 1) = PlicFlux(n(c, 1), a(c, 1), h, v, dt, d);
      qf(f, 1) = q(c, 1);
      cd = AdjacentCell(f, v > 0 ? 1 : 0); // downwind cell
      if (FindLayer(q, cd, q(c, l)) == kLayerNone) {
       ld = FindLayer(q, cd, kClNone);
        if (ld != kLayerNone) {
          q(cd, 1d) = q(c, 1);
      }
    }
 for (c : cells) {
   for (1 : layers) {
      fm = AdjacentCell(c, 0);
      fp = AdjacentCell(c, 1);
      ds = (v[fp] - v[fm]) * dt / volume;
      wm = w(c, FindLayer(qf, fm, q(c, l)));
      wp = w(c, FindLayer(qf, fp, q(c, l)));
      dl = (wp - wm) * dt / vol;
     u(c, 1) += udiv(c, 1) * ds - d1;
      if (u(c, 1) == 0) {
       q(c, 1) = kClNone;
      }
    }
 }
 return {u, q};
```

Function Plic() builds the PLIC reconstruction in interfacial cells and returns normals n and plane constants a:

```
auto Plic() {
    for (c : cells) {
        for (l : layers) {
            uu = Stencil3(c, u, q, q(c, l));
            n(c, l) = Normal(uu);
      }
      auto navg = Avg(n, q, c);
      for (l : layers) {
            n(c, l) = (n.dot(navg) > 0 ? -navg : navg);
      }
            a(c, l) = PlaneConstant(u(c, l), n(c, l), h);
    }
    return {n, a};
}
```

Normals n are estimated using the standard Youngs-centered scheme Normal () applied to stencil values assembled by Stencil3 (), which selects values with given color (or zero if the requested color is not found) on the 3x3x3

stencil. After all advection sweeps, Recolor() detects new connected components and recomputes the colors as described in *Connected-component labeling*.

The complete implementation of the multilayer VOF is given in src/solver/vofm.ipp.

### 5.1 Connected-component labeling

After each advection step, the colors need to be updated to detect new connected components. The following function initializes the color field with unique values, then iteratively joins the colors from adjacent cells by taking the minimal color until equilibration.

To reduce the number of iterations, function RecolorCorners () runs the same algorithm for corners from cubic subdomains. The colors propagate through the domain faster.

```
auto RecolorCorners(u, q, q_new) {
    // map: mapping from old color to new color
    for (c: corners of subdomains) {
        for (l: layers) {
            cn = AdjacentCell(c, d);
            ln = FindLayer(q, cm, q(c, l));
            ql = q_new(c, l);
            q2 = q_new(cn, ln);
            map[max(ql, q2)] = min(q1, q2);
        }
    }
}
changed = true;
while (changed) {
    changed = false;
    for (q1 in map) {
```

(continues on next page)

```
if (map[q1] in map) {
    map[q1] = map[map[q1]];
    changed = true;
}

for (f : faces) {
    cm = AdjacentCell(f, 0);
    cp = AdjacentCell(f, 1);
    for (1 : layers) {
        q_new(cm, 1) = map[q(cm, 1)];
        q_new(cp, 1) = map[q(cp, 1)];
}

return q_new;
}
```

#### **EMBEDDED BOUNDARIES**

The method of embedded boundaries allows one to solve equations in complex geometries on a Cartesian mesh. The surface of a solid body is represented by *cut cells*. A cut cell is obtained by cutting a regular cubic cell with a plane. Discretization of the equations with the finite volume method remains the same, except that the discrete conservation law now includes additional boundaries in cut cells.

The functionality related to embedded boundaries is provided in header embed. h.

```
#include <aphros/solver/embed.h>
```

A new type FieldEmbed transparently combines FieldFace and FieldCell. The cell-field stores the values on embedded boundaries. Given a mesh m, a combined field is initialized on the mesh similar to other fields with an optional default value:

```
FieldEmbed<Scal> fe(m, 0); // [f]ield [e]mbed
```

The field can be accessed both by cell- and face-indices. The following code traverses all internal cells and faces and assigns a value to the field:

```
for (IdxCell c : m.Cells()) {
   fe[c] = 1;
}
for (IdxFace f : m.Faces()) {
   fe[f] = 1;
}
```

A new class Embed<M> defines new iterators and geometric routines that take into account cut cells. The cells and faces are divided into three groups:

- regular cells (whole cells inside the domain),
- cut cells (cells crossed by the domain boundary),
- excluded cells (cells outside the domain).

The same classification applies to faces

- regular faces (whole faces inside the domain),
- cut faces (faces crossed by the domain boundary),
- excluded faces (cells outside the domain).

An instance of Embed<M>, commonly named as eb, is constructed from a mesh and needs to be initialized from a level-set function  $\varphi$  stored in a node-field:

```
void F(const FieldNode<Scal>& phi) {
  auto sem = m.GetSem();
  struct {
    std::unique_ptr<Embed<M>> eb_;
    } * ctx(sem);
  if (sem()) {
    eb_.reset(new Embed<M>(m));
  }
  if (sem.Nested()) {
    eb_->Init(phi);
  }
}
```

Regular cells are those for which  $\varphi>0$  in all adjacent nodes, excluded cells are those for which  $\varphi<0$  in all adjacent nodes, and other cells are cut cells. The Embed<M> class defines ranges eb.Cells() and eb.Faces() such that they include regular and cut cells but not excluded cells. Another range eb.CFaces() traverses only cut cells. The name CFaces comes from *Cell Faces*. Together, eb.Faces() and eb.CFaces() include all indices for which an embed-field can be defined. The following code assigns a value to the embed-field in cut cells, regular faces and cut faces:

```
for (IdxCell c : eb.CFaces()) {
   fe[c] = 1;
}
for (IdxFace f : eb.Faces()) {
   fe[f] = 1;
}
```

Class Embed<M> also defines geometric routines such as eb.GetVolume() and eb.GetArea(). The following code computes the total volume of the domain and the total area of all boundaries:

```
Scal vol = 0;
for (IdxCell c : eb.Cells()) {
  vol += eb.GetVolume(c);
}
Scal area = 0;
for (IdxFace f : eb.Faces()) {
  area += eb.GetArea(f);
}
for (IdxCell c : eb.CFaces()) {
  area += eb.GetArea(c);
}
```

The range of neighbor indices eb.Nci() is limited to non-excluded neighbor faces. The name Nci stands for *Neighbor Cell Index*. The following code sums up the values over all faces of one cut cell c:

```
IdxCell c;
Scal sum = fe[c];
for (size_t q : eb.Nci()) {
   IdxFace f = eb.GetFace(c, q);
   sum += fe[f];
}
```

The header defines numerical routines for interpolation and computation of gradients. Some of them require boundary conditions.

```
MapEmbedCond mec; // boundary conditions
FieldEmbed<Scal> feu(m);
```

(continues on next page)

```
FieldCell<Scal> fcu(m);
FieldCell<Scal> fci = eb.Interpolate(feu);
FieldEmbed<Scal> fei = eb.Interpolate(fcu, mec);
FieldCell<Vect> fcg = eb.Gradient(feu);
FieldEmbed<Scal> feg = eb.Gradient(fcu, mec);
```

#### 6.1 Advection solver

The routines described above are sufficient to implement an advection solver.

```
// Advection solver.
// fcu: quantity to advect
// mebc: boundary conditions
// vel: advection velocity
// dt: time step
void Advection0(
   FieldCell<Scal>& fcu, const MapEmbed<BCond<Scal>>& mebc,
   const FieldEmbed<Scal>& fev, Scal dt, const Embed<M>& eb) {
 const auto fcg =
     UEmbed<M>::GradientLinearFit(UEmbed<M>::Interpolate(fcu, mebc, eb), eb);
     UEmbed<M>::InterpolateUpwind(fcu, mebc, ConvSc::fou, fcg, fev, eb);
 // Compute flux.
 FieldEmbed<Scal> fevu(eb, 0);
 for (auto f : eb.Faces()) {
   fevu[f] = feu[f] * fev[f];
 for (auto c : eb.CFaces()) {
   fevu[c] = feu[c] * fev[c];
 // Advance in time.
 for (auto c : eb.Cells()) {
   Scal sum = fevu[c]; // sum of fluxes
   for (auto q : eb.Nci(c)) {
     sum += fevu[eb.GetFace(c, q)] * eb.GetOutwardFactor(c, q);
   fcu[c] -= sum * dt / eb.GetVolume(c);
  }
```

6.1. Advection solver 19

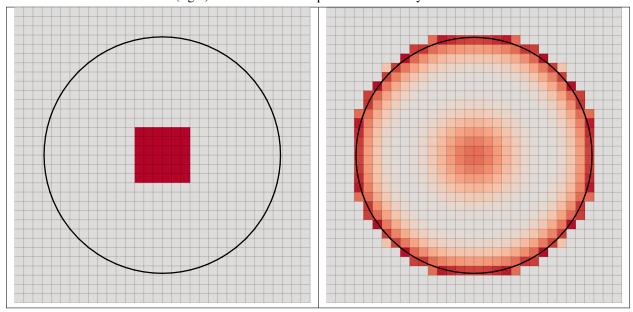


Table 6.1: Results of advection solver Advection0(): initial (left) and final (right). Instabilities develop near the boundary.

See full example in examples/103\_embed\_advection/main.cpp.

The previous implementation suffers from the problem of small cells. Stability requires that the change of the conserved quantity at one time step does not exceed the cell volume. Therefore, small cells lead to strong restrictions on the time step. One common remedy is redistribution of the conserved quantity to neighboring cells. Function <code>eb.RedistributeCutCells()</code> redistributes a conserved quantity from cut cells to their neighboring cells such that the integral of the quantity does not change. Using this function in the advection solver results in

```
// Advection solver with redistribution from cut cells
// and first order upwind scheme.
void Advection1(
   FieldCell<Scal>& fcu, const MapEmbed<BCond<Scal>>& mebc,
   const FieldEmbed<Scal>& fev, Scal dt, const Embed<M>& eb) {
 const auto fcg =
     UEmbed<M>::GradientLinearFit(UEmbed<M>::Interpolate(fcu, mebc, eb), eb);
 const auto feu =
     UEmbed<M>::InterpolateUpwind(fcu, mebc, ConvSc::fou, fcg, fev, eb);
  // Compute flux.
 FieldEmbed<Scal> fevu(eb, 0);
 for (auto f : eb.Faces()) {
    fevu[f] = feu[f] * fev[f];
 for (auto c : eb.CFaces()) {
    fevu[c] = feu[c] * fev[c];
  // Compute the change at one time step.
 FieldCell<Scal> fct(eb, 0);
 for (auto c : eb.Cells()) {
   Scal sum = fevu[c];
    for (auto q : eb.Nci(c)) {
      sum += fevu[eb.GetFace(c, q)] * eb.GetOutwardFactor(c, q);
    fct[c] = -sum * dt;
```

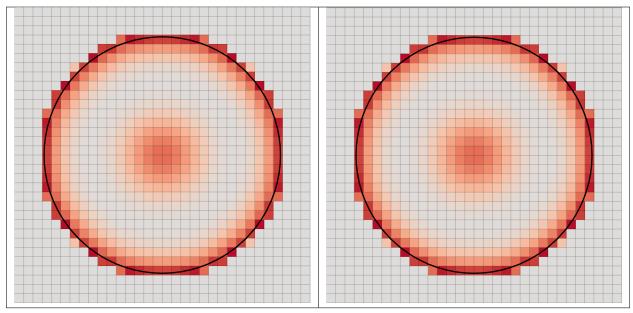
(continues on next page)

```
}
fct = UEmbed<M>::RedistributeCutCells(fct, eb);
// Advance in time.
for (auto c : eb.Cells()) {
   fcu[c] += fct[c] / eb.GetVolume(c);
}
```

```
// Advection solver with redistribution from cut cells
// and second order upwind scheme.
void Advection2(
   FieldCell<Scal>& fcu, const MapEmbed<BCond<Scal>>& mebc,
   const FieldEmbed<Scal>& fev, Scal dt, const Embed<M>& eb) {
 const auto fcg =
     UEmbed<M>::GradientLinearFit(UEmbed<M>::Interpolate(fcu, mebc, eb), eb);
 auto feu = UEmbed<M>::InterpolateUpwind(fcu, mebc, ConvSc::sou, fcg, fev, eb);
 // Compute flux.
 FieldEmbed<Scal> fevu(eb, 0);
 for (auto f : eb.Faces()) {
   fevu[f] = feu[f] * fev[f];
 for (auto c : eb.CFaces()) {
   fevu[c] = feu[c] * fev[c];
  // Compute the change at one time step.
 FieldCell<Scal> fct(eb, 0);
 for (auto c : eb.Cells()) {
   Scal sum = fevu[c];
   for (auto q : eb.Nci(c)) {
     sum += fevu[eb.GetFace(c, q)] * eb.GetOutwardFactor(c, q);
   fct[c] = -sum * dt;
 fct = UEmbed<M>::RedistributeCutCells(fct, eb);
 // Advance in time.
 for (auto c : eb.Cells()) {
   fcu[c] += fct[c] / eb.GetVolume(c);
 }
}
```

6.1. Advection solver 21

Table 6.2: Results of first order upwind scheme Advection1() (left) and second order upwind scheme Advection2() (right). Resdistribution from cut cells stabilizes the method in both cases.



The fraction of redistributed quantities eb.RedistributeCutCells() does not depend on the velocity or the time step. While this makes a stable method, the unnecessary redistribution of values may reduce the accuracy. Another approach would be to use a local stability criterion depending on the velocity

$$\frac{v_f \Delta t}{S_f |\mathbf{x}_c - \mathbf{x}_f|} < CFL_0$$

#### 6.2 Diffusion solver

The diffusion equation illustrates another problem of small cells which arises in computation of gradients. The diffusive fluxes are proportional to the normal gradient of the quantity. Approximations of normal gradients contain the distance between the face and cell centroids in the denominator.

$$\left(\frac{\delta u}{\delta n}\right) = \frac{u_c - u_f}{(\mathbf{x}_c - \mathbf{x}_f) \cdot \mathbf{n}_f}$$

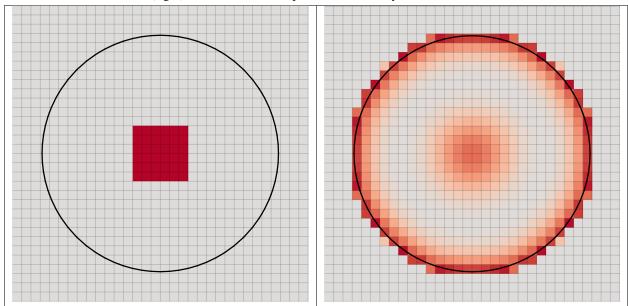
The following function implements a diffusion solver using this approximation

```
// Diffusion solver.
// fcu: quantity to advect
// mebc: boundary conditions
// diff: diffusion coefficient
// dt: time step
void Diffusion0(
    FieldCell<Scal>& fcu, const MapEmbed<BCond<Scal>>& mebc, Scal diff, Scal dt,
    const Embed<M>& eb) {
    const auto feg = UEmbed<M>::Gradient(fcu, mebc, eb);
    // Compute flux.
    FieldEmbed<Scal> fed(eb, 0);
    for (auto f : eb.Faces()) {
```

(continues on next page)

```
fed[f] = feg[f] * diff * eb.GetArea(f);
for (auto c : eb.CFaces()) {
 fed[c] = feg[c] * diff * eb.GetArea(c);
// Advance in time.
for (auto c : eb.Cells()) {
 Scal sum = fed[c]; // sum of fluxes
 for (auto q : eb.Nci(c)) {
   sum += fed[eb.GetFace(c, q)] * eb.GetOutwardFactor(c, q);
 fcu[c] += sum * dt / eb.GetVolume(c);
}
```

Table 6.3: Results of diffusion solver Diffusion0(): initial (left) and final (right). Instabilities develop near the boundary.



See full example in examples/104\_embed\_diffusion/main.cpp.

```
// Diffusion solver with redistribution to neighbor cells.
void Diffusion1(
   FieldCell<Scal>& fcu, const MapEmbed<BCond<Scal>>& mebc, Scal diff, Scal dt,
   const Embed<M>& eb) {
 const auto feg = UEmbed<M>::Gradient(fcu, mebc, eb);
 // Compute flux.
 FieldEmbed<Scal> fed(eb, 0);
 for (auto f : eb.Faces()) {
   fed[f] = feg[f] * diff * eb.GetArea(f);
 for (auto c : eb.CFaces()) {
   fed[c] = feg[c] * diff * eb.GetArea(c);
  // Compute the change at one time step.
 FieldCell<Scal> fct(eb, 0);
```

6.2. Diffusion solver

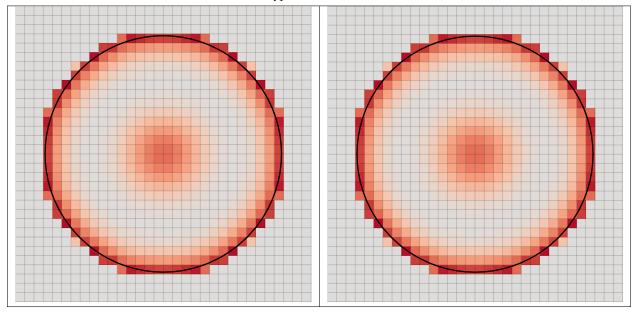
(continues on next page)

23

```
for (auto c : eb.Cells()) {
    Scal sum = fed[c];
    for (auto q : eb.Nci(c)) {
        sum += fed[eb.GetFace(c, q)] * eb.GetOutwardFactor(c, q);
    }
    fct[c] = sum * dt;
}
fct = UEmbed<M>::RedistributeCutCells(fct, eb);
// Advance in time.
for (auto c : eb.Cells()) {
    fcu[c] += fct[c] / eb.GetVolume(c);
}
```

```
// Diffusion solver with redistribution to neighbor cells
// and LoopFaces() to avoid code duplicatoin.
void Diffusion2(
   FieldCell<Scal>& fcu, const MapEmbed<BCond<Scal>>& mebc, Scal diff, Scal dt,
   const Embed<M>& eb) {
 const auto feg = UEmbed<M>::Gradient(fcu, mebc, eb);
  // Compute flux.
 FieldEmbed<Scal> fed(eb, 0);
 eb.LoopFaces([\&] (auto cf) { // lambda-function applied to faces and
                              // embedded faces
   fed[cf] = feg[cf] * diff * eb.GetArea(cf);
 });
  // Compute the change at one time step.
 FieldCell<Scal> fct(eb, 0);
 for (auto c : eb.Cells()) {
   Scal sum = fed[c];
   for (auto q : eb.Nci(c)) {
      sum += fed[eb.GetFace(c, q)] * eb.GetOutwardFactor(c, q);
   fct[c] = sum * dt;
 fct = UEmbed<M>::RedistributeCutCells(fct, eb);
 // Advance in time.
 for (auto c : eb.Cells()) {
   fcu[c] += fct[c] / eb.GetVolume(c);
  }
```

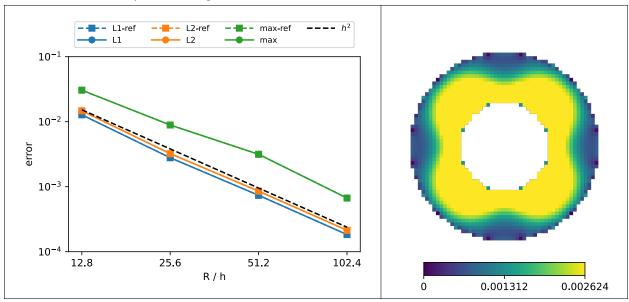
Table 6.4: Results of diffusion solver Diffusion1 () (left) using linear fit to cell centers to compute the gradient which eliminates the instabilities. Solver Diffusion2 () (right) produces the same results and illustrates the usage of ExecFaces () to execute the same lambdafunction on indices of two types



# 6.3 Taylor-Couette flow

See full example in examples/201\_taylor\_couette.

Table 6.5: Error norms with grid refinement (left) and error field at R/h=25.6 (right).



# 6.4 Hydrostatic

## 6.4.1 Single-phase

See full example in examples/203\_hydrostatic.

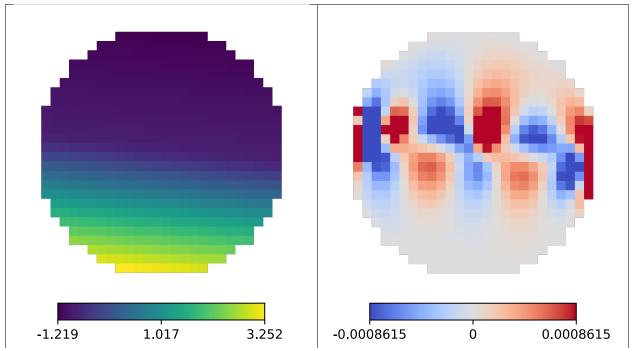


Table 6.6: Pressure (left) and velocity (right).

## 6.4.2 Multiphase

See full example in examples/203\_hydrostatic.

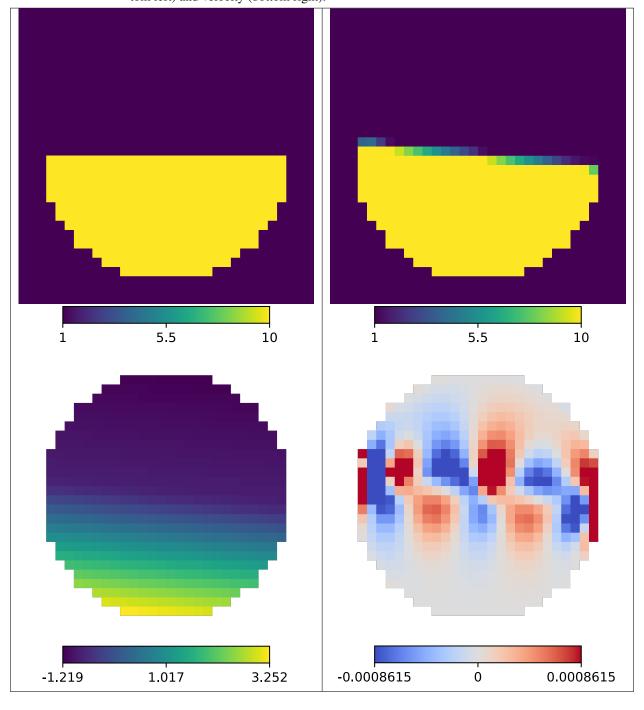


Table 6.7: Initial density (top left), final density (top right), pressure (bottom left) and velocity (bottom right).

6.4. Hydrostatic 27

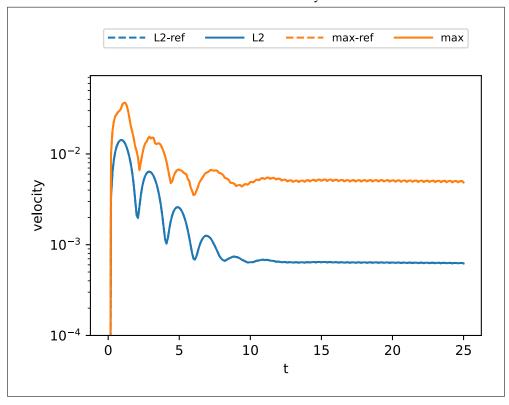


Table 6.8: Evolution of velocity norms.

#### **GEOMETRIC PRIMITIVES**

Header func/primlist.h provides routines to define level-set functions for a list of geometric primitives such as spheres and boxes. A primitive is described by

```
struct Primitive {
 using Vect = Vect_;
 using Scal = typename Vect::Scal;
 static constexpr size_t dim = Vect::dim;
 Primitive(std::string name_)
     : name(name_), inter([](const Rect<Vect>&) -> bool { return true; }) {}
 Primitive() : Primitive("") {}
 friend std::ostream& operator<<(std::ostream& o, const Primitive<Vect>& p) {
   o << "name='" << p.name << "'";
   o << " mod='" << (p.mod_minus ? "-" : "") << (p.mod_and ? "&" : "") << "'";
   return o;
 std::string name;
 bool mod_minus = false;
 bool mod_and = false;
 std::function<Scal(const Vect&)> ls; // level-set
 std::function<br/>bool(const Rect<Vect>&)> inter; // true if intersects rectangle
 std::function<Vect(const Vect&)> velocity; // velocity
 Vect c; // center XXX adhoc for GetSphereOverlap
 Vect r; // radius XXX adhoc for GetSphereOverlap
```

Function GetPrimitives () parses a stream with a list of primitives.

```
// Parses a list of primitives in stream buf.
// edim: effective dimension, 2 or 3 (ignores z-component if edim=2)
static std::vector<Primitive> GetPrimitives(std::istream& buf, size_t edim)
```

Available primitives and their parameters:

- **sphere** Ellipsoid with principal axes aligned with the coordinate axes. Parameters: cx cy cz (center), rx ry rz (half-size);
- **box** Rectangular box with sides aligned with the coordinate planes. Parameters: cx cy cz (center), rx ry rz (half-size);
- ring Torus. Parameters: cx cy cz (center), nx ny nz (normal), r (radius), th (thickness);
- **smooth\_step** Smooth step Almgren *et al.* [2]. Parameters: cx cy cz (center), nx ny nz (normal), tx ty tz (tangent), ln (size along normal), lt (size along tangent);

- **cylinder** Right circular cylinder. Parameters: cx cy cz (center), nx ny nz (normal), r (radius), n0 n1 (range along normal relative to center);
- polygon Cylinder bounded by parallel planes with the plane section specified as a sequence of non-intersecting polygons. Parameters: ox oy oz (origin), nx ny nz (normal), ux uy uz (direction of 2D x-axis), n0 n1 (range along normal relative to origin), scale (factor applied to 2D vertices), x y ... (2D vertices of all polygons, first and last vertices of each polygon must coincide);
- ruled Ruled surface bounded by parallel planes with two plane sections on the opposite sides specified as two sequences of non-intersecting polygons. Parameters: ox oy oz (origin), nx ny nz (normal), ux uy uz (direction of 2D x-axis), n0 n1 (range along normal relative to origin, sides 0 and 1), scale0 scale1 (factors applied to 2D vertices on sides 0 and 1), x y ... (2D vertices of all polygons on side 0, first and last vertices of each polygon must coincide), x y ... (same but on side 1).

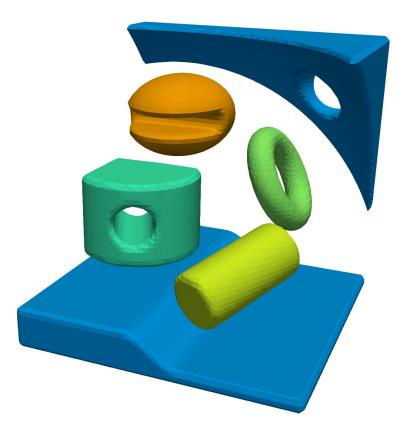
Each primitive defines a level-set function which is positive inside the body. By default, the resulting level-set function is composed from the list of primitives using the union operation (taking the maximum value). To change the default operation, modifiers can be added before the name of the primitive:

- -: minus, multiply level-set by -1;
- &: intersection, take the minimum with the current level-set.

#### Example of a list of primitives

```
# cx cy cz rx ry rz
box 0.7 0.3 0.4 0.25 0.2 0.15
&cylinder 0.55 0.25 0.5 0 0 1 0.22
&-cylinder 0.7 0.3 0.4 1 0.5 0 0.07 -1 1
# cx cy cz rx ry rz
sphere 0.3 0.3 0.7 0.25 0.2 0.15
&-box 0.45 0.3 0.7 0.1 0.2 0.03
# cx cy cz nx ny nz r th
ring 0.3 0.7 0.5 0 1 0.5
                          0.15 0.05
# cx cy cz nx ny nz tx ty tz
smooth_step 0.5 0.5 0.1 0 0 1 0 1 0
# cx cy cz tx ty tz r t0 t1
                    -2 1 0.5
cylinder 0.75 0.7 0.3
                                0.1
                                     -0.20.2
-sphere 1 0.2 0 1.3
&-cylinder 0.1 0.8 0.8 -2 1 0.5
                                0.1 - 0.2 0.2
```

(see setup in examples/200\_primlist)



Parameter  $list_ls$  in the configuration defines the method of computing the volume fraction field from the level-set functions

- set int list\_ls 0 step-wise approximation (1 if level-set is positive, 0 otherwise);
- set int list\_ls 1 linear approximation with normal and plane constant computed from the level-set at the cell
  center, does not support modifiers;
- set int list\_ls 2 using the overlap library to compute the exact volume fraction cut by an ellipsoid (only
   valid for primitive sphere);
- set int list\_ls 3 linear approximation with normal and plane constant computed from the level-set on mesh
  nodes, supports modifiers.

**EIGHT** 

### **BOUNDARY CONDITIONS**

Header func/init\_u.h provides routines to describe boundary conditions based on primitives. The list of boundary conditions is a list of code blocks with primitives.

### 8.1 Code blocks

A code block is described by

```
struct CodeBlock {
  std::string name;
  std::string content;
};
```

and has the following format

```
NAME {
   CONTENT
}
```

where NAME does not contain { or } and CONTENT may contain only matching { . . . }.

Examples of code blocks

```
name {
  content
}

name { content }

name with spaces {
  content { inside {inside} braces }
}
```

The following function extracts a list of blocks from a stream

```
// Parses a stream and returns a list of code blocks.
std::vector<CodeBlock> ParseCodeBlocks(std::istream& f)
```

Leading and trailing whitespaces are stripped.

## 8.2 Groups of primitives

Boundary conditions are selected inside groups of primitives organized as code blocks. The name of the block is the boundary condition to set and the content is a list of primitives describing a single level set function. Affected are cut cells and faces on the domain boundary.

```
wall 0 0 0 {
   box 0 0 0 10
}
wall 1 0 0 {
   sphere 0.7 0.5 0.5 0.2
}
slipwall {
   sphere 0.3 0.5 0.5 0.2
}
inlet 1 0 0 {
   sphere 0.5 0.7 0.5 0.2
}
symm {
   sphere 0.5 0.5 0.7 0.2
   sphere 0.5 0.5 0.3 0.2
}
```

The following function parses parses a file and returns a MapEmbed object containing face and cut-cell conditions.

```
MapEmbed<size_t>, MapEmbed<size_t>, std::vector<std::string>>
ParseGroups(
std::istream& fin, const MEB& eb, const FieldCell<bool>& fc_innermask)
```

NINE

### **OUTPUT**

Simulations produce output of various types:

- statistics (stdout)
- fields (HDF5, plain or XML VTK)
- PLIC polygons (polydata legacy VTK)
- marching cubes triangles (polydata legacy VTK)
- boundary conditions (polydata legacy VTK)

Boundary conditions are written to bc.vtk if enabled by set int dumpbc 1. It contains cell fields block (block id), cond (conditions for advection) and condfluid (conditions for fluid, see *Fluid boundary conditions*.).

The output is implemented in function

```
void DumpBcPoly(
    const std::string filename, const MapEmbed<size_t>& me_group,
    const MapEmbed<typename MEB::Scal>& me_contang, const MEB& meb,
    typename MEB::M& m)
```

36 Chapter 9. Output

**TEN** 

### **TOOLS**

### 10.1 AWK for CSV files

### 10.1.1 Synopsis

ap.cawk [-v var=value] ['prog'] [CSV ..]

### 10.1.2 Description

### 10.1.3 Examples

```
$ cat example.csv
x,y
1,10
2,20
$ ap.cawk '{print $x + $y}' example.csv
11
22
```

```
$ ap.cawk 'NR == 2 {print HEADER} {print $x + $y}' q
x,y
11
22
33
```

#### 10.1.4 Source

deploy/scripts/cawk

### 10.2 Format

### 10.2.1 Synopsis

```
ap.format [-y]
```

runs clang-format for all C/C++ files found recursively from current directory.

**-y** 

Force 'yes' for all questions

### 10.2.2 Configuration

The configuration is based on Google code style with modifications.

.clang-format

#### 10.2.3 Source

deploy/scripts/format

### 10.3 Histogram

### 10.3.1 Synopsis

```
ap.hist [-densityl-cumulative] [-bins BINS] [-range L R] print histogram of STDIN as columns [center,density,left,right]
```

### 10.3.2 Examples

```
seq 10 | ap.hist --density
seq 10 | ap.hist --cumulative
```

#### 10.3.3 Source

deploy/scripts/hist

38 Chapter 10. Tools

**ELEVEN** 

#### **LIBRARY**

### 11.1 CSV IO

### 11.1.1 Synopsis

A library to read/write floating point data from CSV file

```
#include <csv.h>
```

```
enum { CSV_MAX_NF = 999 };
struct CSV {
    char* name[CSV_MAX_NF];
    double* data[CSV_MAX_NF];
    int nf, nr;
};

struct CSV* csv_ini(int);
struct CSV* csv_read(FILE*);
int csv_fin(struct CSV*);
double* csv_field(struct CSV*, const char*);
int csv_nf(struct CSV*);
int csv_nr(struct CSV*);
int csv_write(struct CSV*, FILE*);
int csv_write_space(struct CSV*, FILE*);
int csv_add(struct CSV*, const char*);
```

### 11.1.2 Description

#### 11.1.3 Source

deploy/lib/csv

#### 11.1.4 Examples

### 11.2 HDF5 IO wrapper

#### 11.2.1 Synopsis

A library to read/write scalar field on uniform grid.

```
#include <h5.h>
```

```
int h5_hdf(
    MPI_Comm, const char* path, const int size[3], const int start[3],
    const int extent[3], const double*);
```

```
#include <h5serial.h>
```

```
int h5_xmf(
   const char* path, const char* name, const double origin[3], double spacing,
   const int size[3]);
int h5_silence(void);
int h5_serial_hdf(const char* path, const int size[3], const double* data);
int h5_read_hdf(const char* path, /**/ int size[3], double**);
int h5_read_xmf(
   const char*, /**/ char* name, double origin[3], double spacing[3],
   int size[3]);
```

### 11.2.2 Description

A field is stored as two files: hdf5 file contains data and xmf file contains information.

h5\_serial\_hdf write scalar field of dimension size[3] to file path.h5.

h5\_hdf write path.h5 using MPI.

h5\_xmf writes xmf file.

h5\_read\_hdf reads scalar field from path.h5.

h5\_read\_xmf reads information about a field from path.xmf.

```
// Created by Sergey Litvinov on 24.12.2019
// Copyright 2019 ETH Zurich

#include <stdio.h>
#include <h5serial.h>

int main(int argc, char** argv) {
   enum { X, Y, Z };
   char name[999];
   double ori[3], spa;
   int siz[3];
   if (h5_read_xmf(argv[1], name, ori, &spa, siz) != 0) {
     fprintf(stderr, "fail to read '%s'\n", argv[1]);
     exit(2);
```

(continues on next page)

(continued from previous page)

```
}
printf("name: %s\n", name);
printf("ori: %g %g %g\n", ori[X], ori[Y], ori[Z]);
printf("spa: %g\n", spa);
printf("siz: %d %d %d\n", siz[X], siz[Y], siz[Z]);
}
```

#### 11.2.3 Source

deploy/lib/h5

### 11.2.4 Examples

Write a field in serial:

```
examples/003_h5_serial_write/main.c
```

Write a field using mpi:

examples/004\_h5\_mpi\_write/main.c

### 11.3 Marching cubes

### 11.3.1 Synopsis

Marching cubes.

#### 11.3.2 Description

Generates triangles of the isosurface for three-dimensional discrete field.

march\_cube generates triangles for one cell, u[8] are values of the field in the nodes. Returns ntri – the number of triangles, tri – vertices of the triangles in the form [x0 y0 z0 ... xn yn zn].

```
double cube[8] = {-1, 0, 0, 0, 0, 0, 0, 1};
double tri[3 * 3 * MARCH_NTRI];
int n;
march_cube(cube, &n, tri);
```

MARCH\_NTRI is a maximum number of triangles. MARCH\_0[8][3] are coordinates of the nodes.

march\_cube\_location in addition to the output of the march\_cube returns location of the vertex i relative the nodes. first[i], second[i] are indexes of the nodes. offset[i] is a relative distance from the node first[i].

```
// Created by Sergey Litvinov on 24.12.2019
// Copyright 2019 ETH Zurich
#undef NDEBUG
#include <assert.h>
#include <math.h>
#include <aphros/march/march.h>
int main() {
  enum { X, Y, Z };
  enum { N = 3 * 3 * MARCH_NTRI };
  double u[] = \{-1, 1, 1, 1, 1, 1, 1, -1\}, tri[N], offset[N], x, a, b;
  int first[N], second[N], i, n;
  i = 0;
 march_cube_location(u, &n, tri, first, second, offset);
  a = MARCH_O[first[i]][X];
  b = MARCH_O[second[i]][X];
  x = a + (b - a) * offset[i];
  assert(fabs(x - tri[3 * i + X]) < 1e-12);
```

#### 11.3.3 Source

deploy/lib/march

#### 11.3.4 Examples

Generate triangles for cube configurations given as arguments:

```
examples/001_march_cell/main.c
```

Generate a triangulated sphere:

examples/002\_march\_sphere/main.c

#### 11.4 VOF advection

#### 11.4.1 Synopsis

Volume-of-fluid advection solver with PLIC reconstruction.

#### 11.4.2 Parameters

```
struct VofPar {
 using Scal = typename M::Scal;
 using Vect = typename M::Vect;
 size_t dim = 3; // dimension (dim=2 assumes zero velocity in z)
 Scal clipth = 1e-10; // vf clipping threshold
 Scal filterth = 0; // orphan filtering threshold
 bool recolor = true; // run connected component labeling on every step
 bool recolor_unionfind = true; // use union-find algorithm
 bool recolor_reduce = true; // reduce set of colors to integers
 bool recolor_grid = true; // use grid heuristic
 Scal clfixed = -1; // if >= 0, value for color at point clfixed_x
 Vect clfixed_x = Vect(1e10);
 bool cloverride = false; // XXX adhoc if clear1<1, override color with 0
 bool sharpen = false;
 Scal sharpen_cfl = 0.5;
 size_t layers = 4;
 Scal avgnorm0 = 1; // original normal with sum(u) < avgnorm0</pre>
 Scal avgnorm1 = 1; // overriden normal with sum(u) >= acgnorm1
 Scal coalth = 1e10;
 int verb = 0;
 bool bcc_reflectpoly = true; // reflection for DumpPolyMarch
 Scal dumppolymarch_fill = -1; // fill cells outside
 bool vtkbin = true;
 bool vtkmerge = true;
 bool vtkpoly = true; // dump vtk polygins instead of lines
 Scal vtkiso = 0.5;
 enum class Scheme { plain, aulisa, weymouth };
 Scheme scheme = Scheme::weymouth;
 // Enables extrapolation to halo or cut cells,
 // required for the contact angle model.
 // Extrapolate volume fraction to excluded cells before computing normals
 // Extrapolate volume fraction, plane constant and normals to cut cells
 // after the advection step.
 // If embedded boundaries are enabled, supports only periodic condtitions.
 bool extrapolate_boundaries = false;
 Labeling<M>* labeling = nullptr; // Pointer to implementation of
                                   // connected component labeling.
                                   // Defaults to Recolor().
};
```

11.4. VOF advection 43

#### 11.4.3 Source

src/solver/vof.h src/solver/vof.cpp src/solver/vof.ipp

#### **11.4.4 Example**

examples/100\_advection/main.cpp

```
// Created by Petr Karnakov on 24.12.2019
// Copyright 2019 ETH Zurich
#undef NDEBUG
#include <cassert>
#include <iostream>
#include <memory>
#include <string>
#include <distr/distrbasic.h>
#include <solver/vof.h>
using M = MeshCartesian<double, 3>;
using Scal = typename M::Scal;
using Vect = typename M::Vect;
void Run(M& m, Vars&) {
 auto sem = m.GetSem();
 struct {
   std::unique_ptr<Vof<M>> as; // advection solver
   FieldCell<Scal> fc_src; // volume source
   FieldEmbed<Scal> fe_flux; // volume flux
   MapEmbed<BCondAdvection<Scal>> mf_cond; // face conditions
 } * ctx(sem);
 auto& as = ctx->as;
 const Scal tmax = 1.;
 const Vect vel(0.5, 0.3, 0.1);
 const Scal cfl = 0.5;
 if (sem("init")) {
   auto& fc_src = ctx->fc_src;
   auto& fe_flux = ctx->fe_flux;
   auto& mf_cond = ctx->mf_cond;
   fc_src.Reinit(m, 0);
   fe_flux.Reinit(m, 0);
   for (auto f : m.Faces()) {
     fe_flux[f] = vel.dot(m.GetSurface(f));
   FieldCell<Scal> fccl(m, 0); // initial color
   FieldCell<Scal> fcu(m, 0); // initial volume fraction
    for (auto c : m.Cells()) {
      fcu[c] = (m.GetCenter(c).dist(Vect(0.5, 0.5, 0.5)) < 0.2);
```

(continues on next page)

(continued from previous page)

```
const Scal dt = cfl * m.GetCellSize()[0] / vel.norm();
   typename Vof<M>::Par p;
   as.reset(
        new Vof<M>(m, m, fcu, fccl, mf_cond, &fe_flux, &fc_src, 0., dt, p));
  sem.LoopBegin();
  if (sem.Nested("start")) {
   as->StartStep();
  if (sem.Nested("iter")) {
  as->MakeIteration();
  if (sem.Nested("finish")) {
   as->FinishStep();
  if (sem("checkloop")) {
   if (as->GetTime() >= tmax) {
      sem.LoopBreak();
  if (sem("dump")) {
  m.Dump(&as->GetField(), "u");
 if (sem()) {
 }
 sem.LoopEnd();
int main(int argc, const char** argv) {
 std::string conf = R"EOF(
set int bx 1
set int by 1
set int bz 1
set int bsx 16
set int bsy 16
set int bsz 16
set int px 1
set int py 1
set int pz 1
) EOF";
 MpiWrapper mpi(&argc, &argv);
 return RunMpiBasicString<M> (mpi, Run, conf);
```

11.4. VOF advection 45

46 Chapter 11. Library

#### **TWELVE**

#### LOG

## 12.1 Surface tension as gradient

2018-08-30 22:08:47

Goal: zero integral of force

**What**: surface tension as  $\nabla(\kappa\alpha)$  on faces, curvature in cells copied from neighbour faces if nan.

Result: instability for test of single drop equilibrium,

Data: doc/sphinx/src/log/log01\_grad\_ka

- doc/sphinx/src/log/log01\_grad\_ka/grad\_ka.mp4: surface tension as  $\nabla(\kappa * \alpha)$
- doc/sphinx/src/log/log01\_grad\_ka/k\_grad\_a.mp4: surface tension as  $\kappa \nabla \alpha$
- doc/sphinx/src/log/log01\_grad\_ka/k\_grad\_a\_kmean.mp4: mean curvature on face if both cells contain interface

## 12.2 Particle normal displacement

2018-09-02 09:41:49

Goal: reduce spurious flow and deformation for single drop equilibrium

What: particle strings without normal displacement, position of central particle fixed at the interface line center

**Result**: deformation of the interface greatly reduced, probably due to stronger coupling or penalization of deformed interfaces

Data: doc/sphinx/src/log/log02\_dn

- doc/sphinx/src/log/log02\_dn/dn0.mp4: without normal displacement
- doc/sphinx/src/log/log02\_dn/dn1.mp4: with normal displacement

#### 12.3 march=native

2018-09-09 11:59:47

Goal: use automatic vectorization and specific optimizations

What: add -march=native to CMAKE\_C\_FLAGS and CMAKE\_CXX\_FLAGS

Result: slight improvement of performance (3.60 vs 3.76 s for confdiff: 01:assemble) with 64 cores on Euler

**Data**: doc/sphinx/src/log/log03\_native:

- out std: standard flags
- out\_native: -march=native

### 12.4 max\_iter

2018-09-12 14:03:27

Goal: choose optimal number of iterations max\_iter

What: Taylor-Green with bubbles (sim06) with max\_iter=1,2,3,4,5 and convsc=cd,quick.

#### Result

- qualitatively different trajectories for max\_iter=1,2;
- convergence at max\_iter=4
- no major difference between cd and quick,
- no difference between simpler=0 and 1

Data: doc/sphinx/src/log/log04\_maxit

- kedr.pdf: kinetic energy dissipation rate
- traj.pdf: x-component of trajectory of bubble 2

## 12.5 Number of particles and strings

Goal: check the influence of the part\_np and part\_ns in curvature estimator

What: Free-field coalescence of bubbles based on sim04 univel

#### Result

• slight differences in shapes comparing np=5, 0 and ns=2, 3

Data: doc/sphinx/src/log/log05\_coalnp

- gen1\_ns3\_np5: configuration
- nx064\_ns?\_np?.png: shapes at t=0.466 with nx=64
- nx128\_ns2\_np9.png: shapes at t=0.466 with nx=128

48 Chapter 12. Log

### 12.6 Number of iterations for coalescence

Goal: check the influence of the min\_iter and tol on bubble coalescence

What: Free-field coalescence of bubbles based on sim04\_univel/case/partstrcoal

#### Result

• negligible difference in trajectories between default and min\_iter=10

Data: doc/sphinx/src/log/log06\_coaliter

- nx\*iter\*: configuration, data, movie
- a.gnu: gnuplot script

### 12.7 Relaxation parameters

2019-03-21 22:48:56

Goal: check the influence of vrelax and prelax on bubble coalescence

What: Near-wall coalescence of bubbles with vrelax=0.8, prelax=0.8 and vrelax=0.9, prelax=1

#### Result

- spurious oscillations in the pressure field (wforce) with vrelax=0.9 after the bubble detachment
- no effect on x- and y-trajectories, slower rising in z after detachment
- changed default parameters for sim04 to prelax=0.8, vrelax=0.8 and min\_iter=4

Data: doc/sphinx/src/log/log07\_vrelax

- gen1: generator of parameters for sim04/gen
- wforce: force acting on z=0 and z=1
- out, stat.dat: log and statistics

## 12.8 Reduced usage of GetCenter

2019-04-27 01:19:03

Goal: Performance improvement.

What: Reduced usage of GetCenter and GetVectToCell. Test of the Taylor-Green vortex with bubbles.

**Result**: Speedup of 15%.

Data doc/sphinx/src/log/log08\_getcenter

- tg: setup
- tq0\_\*: timings before
- tg1\_\*: timings after

### 12.9 Debug linear solver with ConvertLsCompact

2019-08-15 10:04:39

**Goal**: Fix sim12\_ringgauss after reimplementing simple.ipp with ConvertLsCompact in 48fa3cf0. Iterations for pressure correction diverged.

What: Bisection between 1ffd55c5 from Jan 12 2019 and 9cb90989 from Aug 14 2019. Complication from another bug in InitVort () which attempted to use uninitialized fs\_ in hydro.h (fixed by patch).

**Result**: Found the problem by printing the coefficients of the linear system before and after ConvertLs() or ConvertLsCompact(). The problem appeared from changing the order of stencil cells. In sim12, the symmetric linear solver is called twice: for initialization of vorticity and for pressure correction. Then Hypre is apparently initialized only once and that instance is used for both cases which leads to the wrong order of coefficients.

Data: doc/sphinx/src/log/log09\_debug\_linear

- patch: fix for InitVort()
- r: tool to apply patch and rebuild
- simple\_{bad, good}.ipp: two versions of simple.ipp
- min: minimal simulation setup

### 12.10 Registered modules in Ubuntu

2020-06-03 11:34:54

Ubuntu has --as-needed by default (seen from gcc -dumpspecs) which makes the linker ignore unused libraries and, in particular, the implementations of modules (e.g. init\_contang.so).

## 12.11 VTK merge, comparison of floats with tolerance

2020-06-13 21:56:35

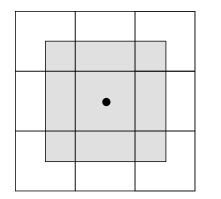
ConvertMerge in dump/vtk.h mapped each Vect to a hash and used the hash to merge closely located points together (up to tolerance tol). This effectively split the space of Vect to partitions. However, if two points are located close to the boundary between two partitions, they can be arbitrarily close but have different hash values.

The solution was to check compare against the hash of neighboring points (from vertices of a cube) when looking for an existing hash.

Minimal example that gave vertices of rank 1: doc/sphinx/src/log/log10\_vtkmerge.

The opposite problem: hash collisions of distant points. Example is in log10\_vtkmerge/hash\_collision. To fix, changed the map from hash->index to Vect->index (ensures exact comparison of points) and introduced canonical (x) to get a single point from the cell of size tol.

50 Chapter 12. Log





### 12.12 Explicit part of viscous stress

2021-06-11 15:32:27

The viscous stress tensor has the form  $\mu(\nabla \mathbf{u} + \nabla \mathbf{u}^T)$ . Parameter int explviscous controls whether the second term is included in the discretization. Setting explviscous=0 changes the approximated tensor to  $\mu\nabla\mathbf{u}$ . This omitted term  $\mu\nabla\mathbf{u}^T$  is significant if the dynamic viscosity is non-uniform.

The following test case of a rising bubble (based on http://basilisk.fr/src/test/rising.c) shows a small difference. See full example in examples/208\_rising.

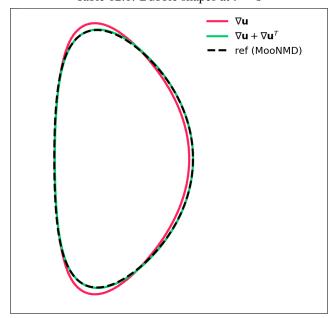


Table 12.1: Bubble shapes at t = 3

52 Chapter 12. Log

## **THIRTEEN**

## **CONTRIBUTING**

# 13.1 Style guide

Use Google C++ Style Guide.

Loop indices:

- i generic
- c IdxCell
- f IdxFace
- $\bullet$  w MIdx
- d direction
- d index 0 . . dim-1

#### **BIBLIOGRAPHY**

- [1] Gabriel D Weymouth and Dick K-P Yue. Conservative volume-of-fluid method for free-surface simulations on cartesian-grids. *Journal of Computational Physics*, 229(8):2853–2865, 2010.
- [2] Ann S Almgren, John B Bell, Phillip Colella, and Tyler Marthaler. A cartesian grid projection method for the incompressible euler equations in complex geometries. *SIAM Journal on Scientific Computing*, 18(5):1289–1309, 1997.
- [3] S Mohammad H Hashemi, Petr Karnakov, Pooria Hadikhani, Enrico Chinello, Sergey Litvinov, Christophe Moser, Petros Koumoutsakos, and Demetri Psaltis. A versatile and membrane-less electrochemical reactor for the electrolysis of water and brine. *Energy & Environmental Science*, 12(5):1592–1604, 2019.
- [4] Petr Karnakov, Fabian Wermelinger, Michail Chatzimanolakis, Sergey Litvinov, and Petros Koumoutsakos. A high performance computing framework for multiphase, turbulent flows on structured grids. In *Proceedings of the Platform for Advanced Scientific Computing Conference*, 1–9. 2019.
- [5] Petr Karnakov, Sergey Litvinov, and Petros Koumoutsakos. A hybrid particle volume-of-fluid method for curvature estimation in multiphase flows. *International Journal of Multiphase Flow*, 125:103209, 2020.
- [6] Zhong Yi Wan, Petr Karnakov, Petros Koumoutsakos, and Themistoklis P Sapsis. Bubbles in turbulent flows: data-driven, kinematic models with history terms. *International Journal of Multiphase Flow*, 129:103286, 2020.
- [7] Petr Karnakov, Sergey Litvinov, Jean M Favre, and Petros Koumoutsakos. Breaking waves: to foam or not to foam? *Physical Review Fluids*, 5(11):110503, 2020.
- [8] Petr Karnakov, Fabian Wermelinger, Sergey Litvinov, and Petros Koumoutsakos. Aphros: high performance software for multiphase flows with large scale bubble and drop clusters. In *Proceedings of the Platform for Advanced Scientific Computing Conference*, 1–10. 2020.
- [9] Petr Karnakov, Sergey Litvinov, and Petros Koumoutsakos. Computing foaming flows across scales: from breaking waves to microfluidics. *arXiv preprint arXiv:2103.01513*, 2021.