

**Problem 1.** Assume that PCA was performed on a dataset containing 4 features:  $x_1$ ,  $x_2$ ,  $x_3$ , and  $x_4$ . The resulting four principal components are:

- $pc1 = [0.478, -0.400, 0.180, 0.761]$
- $pc2 = [-0.731, -0.463, -0.395, 0.309]$
- $pc3 = [-0.480, 0.423, 0.678, 0.363]$
- $pc4 = [0.083, 0.669, -0.594, 0.440]$

The mean of each of the four original features is given by the array  $[3.58, 5.53, 7.98, 2.29]$

Two observations are transformed to new coordinates using the PCA decomposition. The transformed coordinates of these observations are given below. Convert each observation back into its original  $x_1$ ,  $x_2$ ,  $x_3$ , and  $x_4$  coordinates.

Round your final answers (but not your intermediate steps) to 2 decimal places. Box your final answers.

- $[3.63, -1.03, -0.31, -0.81]$

$$3.63 \cdot pc1 = [1.735, -1.452, 0.653, 2.762]$$

$$-1.03 \cdot pc2 = [0.753, 0.477, 0.407, -0.318]$$

$$-0.31 \cdot pc3 = [0.149, -0.131, -0.210, -0.113]$$

$$-0.81 \cdot pc4 = [-0.067, -0.542, 0.481, -0.356]$$

$$\mu = [3.58, 5.53, 7.98, 2.29]$$

$$\boxed{[6.15, 3.88, 9.31, 4.27]}$$

- ~~$[0.33, -1.54, -0.67, 2.13]$~~

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