

# COMPUTER AIDED DIAGNOSIS SYSTEM IN DIGITAL MAMMOGRAPHY

João Maria Patacho de Matos Rocha e Melo

Discussion of the Thesis to obtain the Master of Science Degree in

**Electrical and Computer Engineering**

Supervisors: Prof. Maria Margarida Campos da Silveira

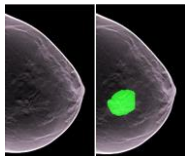
Prof. Nuno Miguel de Pinto Lobo e Matela

## Examination Committee

Chairperson: Prof. João Fernando Cardoso Silva Sequeira

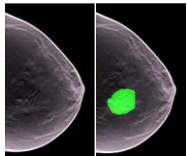
Supervisor: Prof. Maria Margarida Campos da Silveira

Members of the Committee: Prof. Jorge dos Santos Salvador Marques



# OUTLINE

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- Experimental Results
- Conclusions and Future Work



# 1.1 CANCER STATISTICS

- 14.1 million cases of cancer in 2012
- Breast cancer represents 25% of all cancer cases among the female population
- High survival rates if caught in early stages

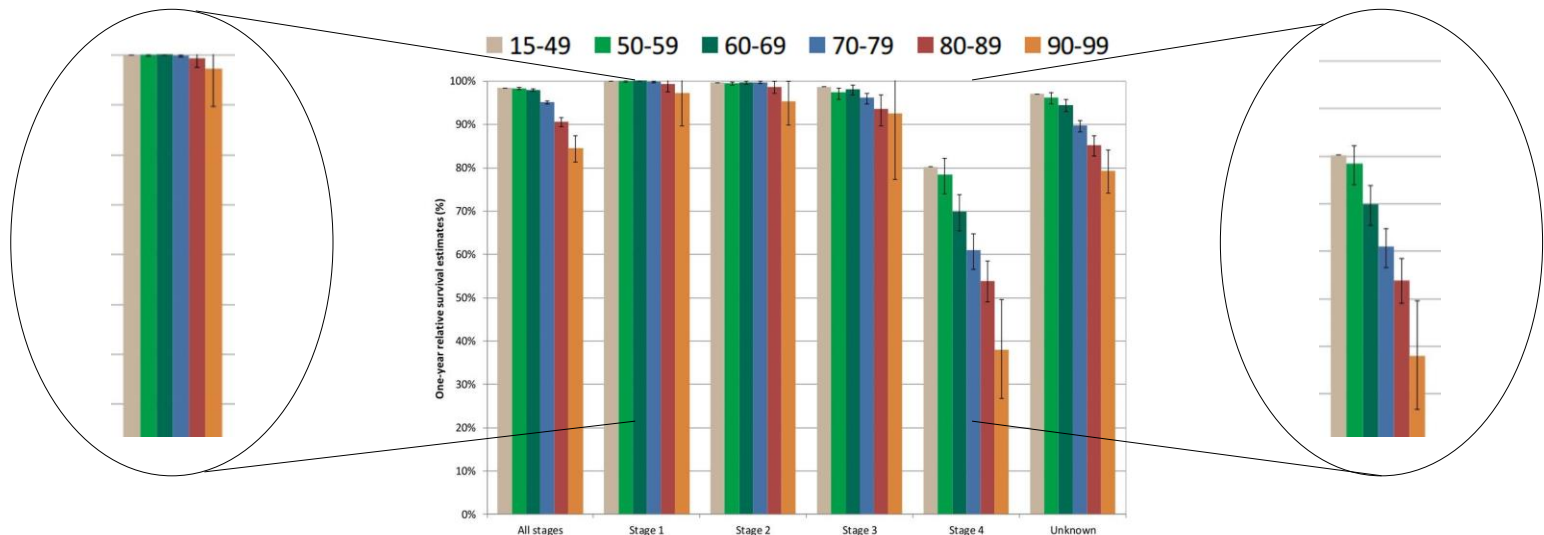
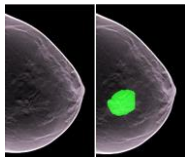


Figure 1 – Survival rate broke down by stage and age sector



## 1.3 BREAST IMAGING TECHNIQUES

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- Experimental Results
- Conclusions and Future Work

### MAMMOGRAPHY

- Most common breast imaging technique
- X-Ray based
- Standard Views:
  - Craniocaudal (Fig 2)
  - MedioLateral Oblique (Fig 3)

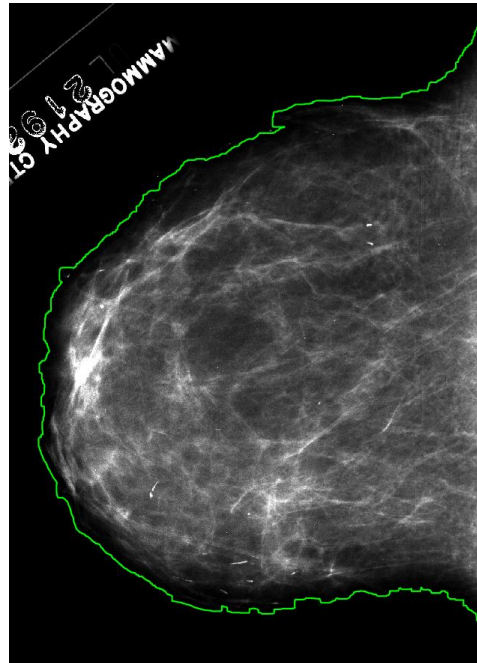


Figure 2 – Craniocaudal view of right breast

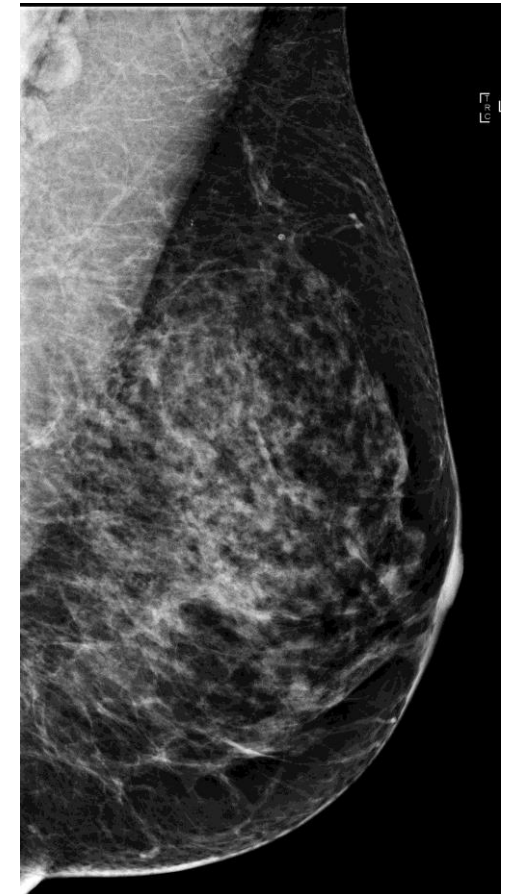
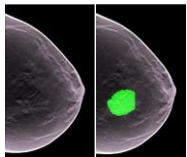


Figure 3 – MedioLateral Oblique view of left breast



# 1.4 COMPUTER AIDED DIAGNOSIS

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- Experimental Results
- Conclusions and Future Work

- Image Processing and Machine Learning based techniques
- Results to be reported to the doctor (not the patient)
- Aims to improve the accuracy of the whole diagnosis process

DOCTOR'S DIAGNOSIS



COMPUTER AIDED DIAGNOSIS

BI-RADS CLASSIFICATION LEVELS	BI-RADS 0
	BI-RADS 1
	BI-RADS 2
	BI-RADS 3
	BI-RADS 4
	BI-RADS 5
	BI-RADS 6

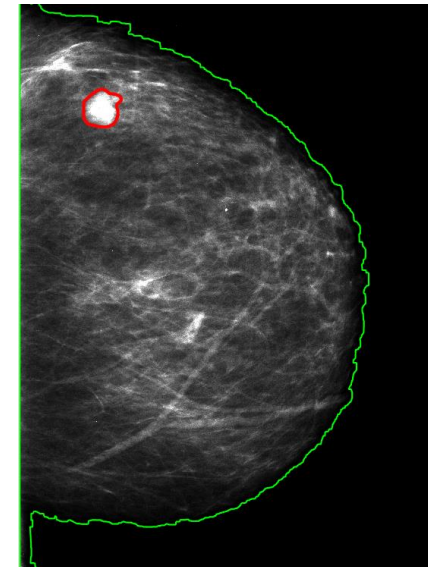


Figure 4 – Example of the application of CAD to a mammogram

# 1.5 THESIS OVERALL

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- Experimental Results
- Conclusions and Future Work

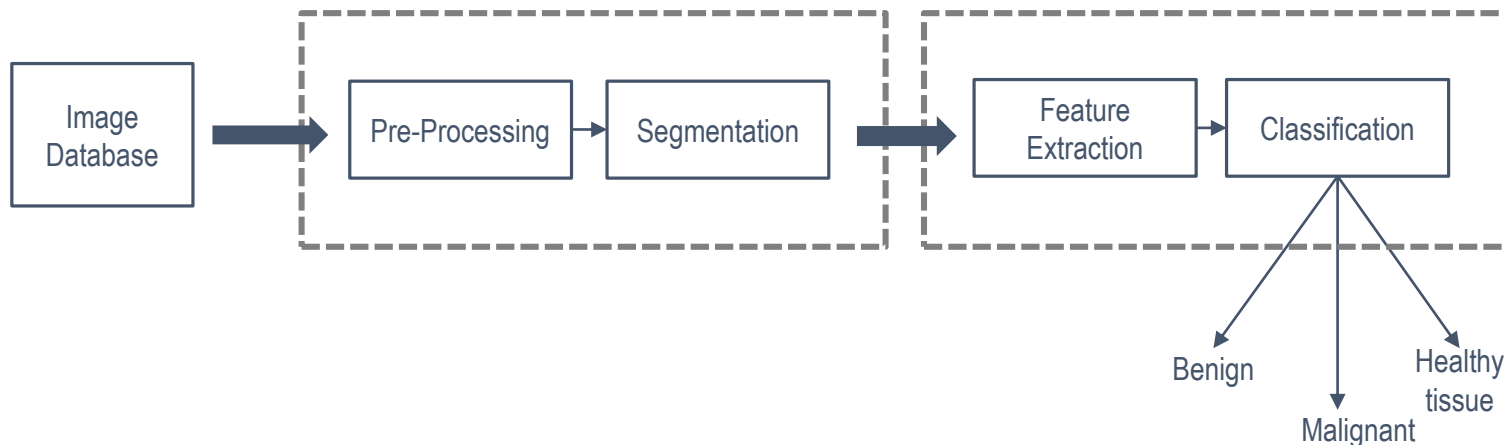
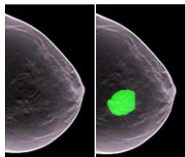


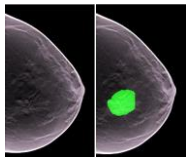
Figure 5 – Schema of the sequence of steps describing this work

PRE-PROCESSING	Bilateral Filter
SEGMENTATION	Sliding Band Filter
FEATURE EXTRACTION	Morphological, Intensity and Texture
CLASSIFICATION	Decision Tree and AdaBoost



# OUTLINE

- Context and Motivation
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## 2.1 BILATERAL FILTER

- Pixel-by-Pixel technique
- Reduces Noise
- Keeps the information of the edges
- Disregards irrelevant information (including noise)
- Reduces the number of false positives

[1] X. Qin, G. Lu, I. Sechopoulos, and B. Fei, "Breast tissue classification in digital tomosynthesis images based on global gradient minimization and texture features," in SPIE Medical Imaging. International Society for Optics and Photonics, 2014, pp. 90341V–90341V.

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- Experimental Results
- Conclusions and Future Work

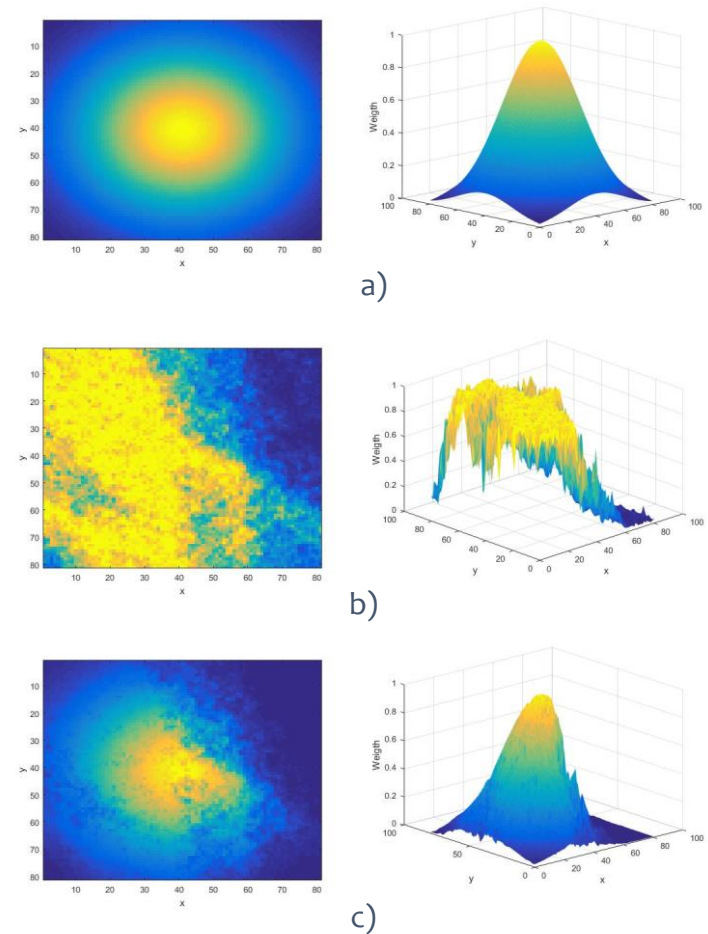
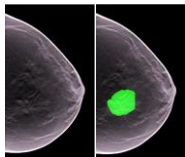


Figure 6 – 2D (on the left) and 3D (on the right) representations of a) spatial distance filter, b) intensity distance filter and c) bilateral filter.





## 2.2 SLIDING BAND FILTER

- Context and Motivation
- Pre-processing and Segmentation
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Gradient based technique

Finds the center and the border of the ROI

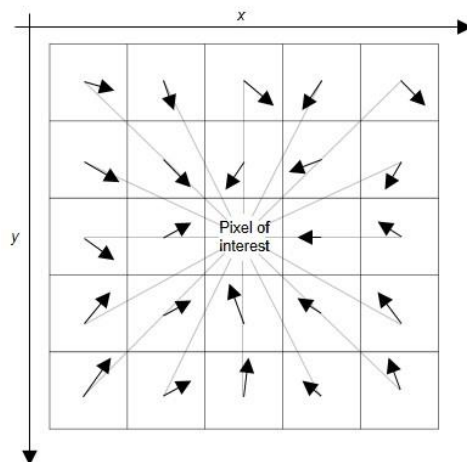


Figure 7 – Representation of the gradients of each pixel in the window of analysis of the pixel of interest -

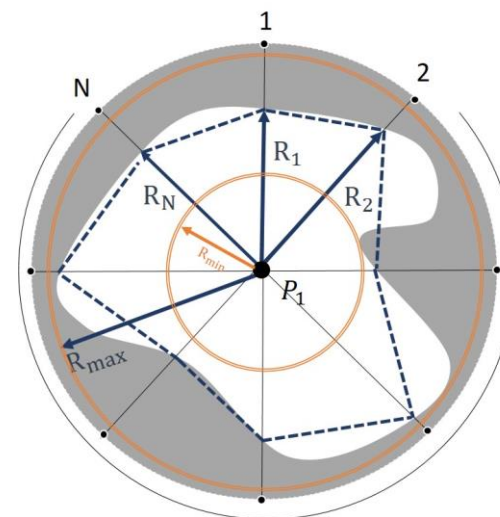
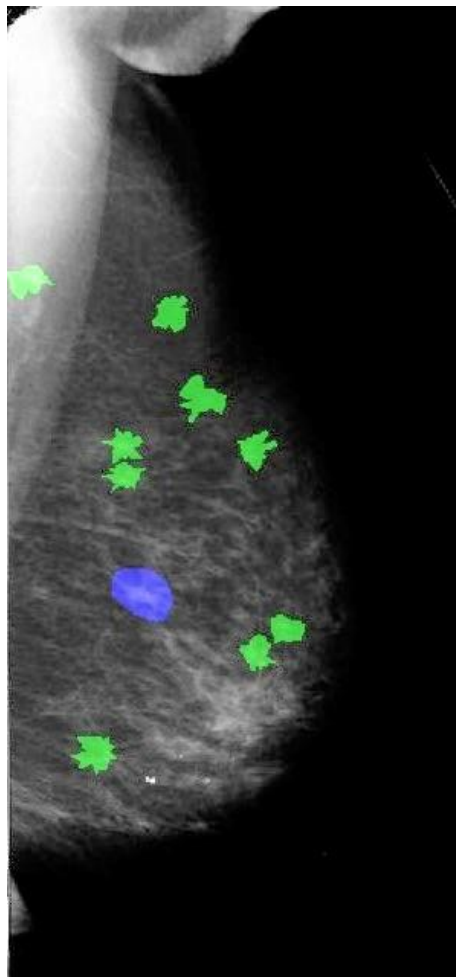


Figure 8 – Illustration of the border found by the Sliding band filter

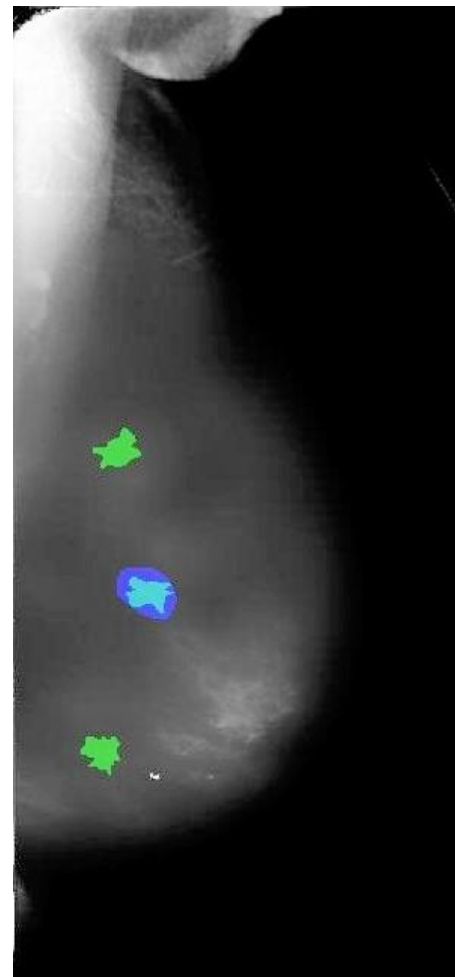
[2] T. Esteves, P. Quelhas, A. M. Mendonça, and A. Campilho, "Gradient convergence filters and a phase congruency approach for in vivo cell nuclei detection," Machine Vision and Applications, vol. 23, no. 4, pp. 623–638, 2012.

## 2.3 RESULTS

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- Experimental Results
- Conclusions and Future Work

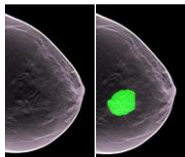


a)



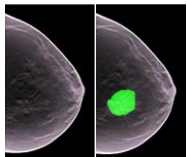
b)

Figure 9 – Mammogram of left breast a) not filtered and b) filtered



# OUTLINE

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
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- Conclusions and Future Work



## 3.1 FEATURE EXTRACTION

- Context and Motivation
- Pre-processing and Segmentation
- **Feature Extraction and Classification**
- Experimental Results
- Conclusions and Future Work

### MORPHOLOGICAL

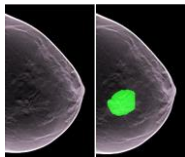
- X and Y coordinates of the location of the centre
- Maximum Radius
- Perimeter
- Area
- Surface Change

### INTENSITY

- Mean Intensity Value
- Maximum Intensity Value
- Minimum Intensity Value
- Standard Deviation of Intensity Values
- Skewness
- Kurtosis
- Contrast
- Energy
- 10 Intensity Histogram bins

### TEXTURE

- Entropy
- HOG Features



# 3.1 FEATURE EXTRACTION

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- Experimental Results
- Conclusions and Future Work

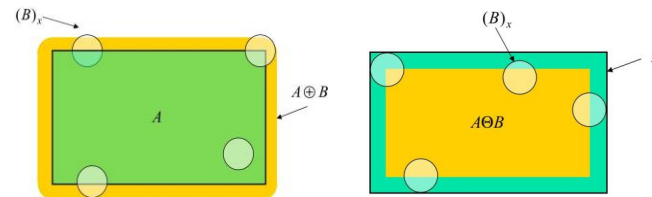


Figure 10 – Illustration of mathematical morphology operations. Dilation (on left) and Erosion (on right).

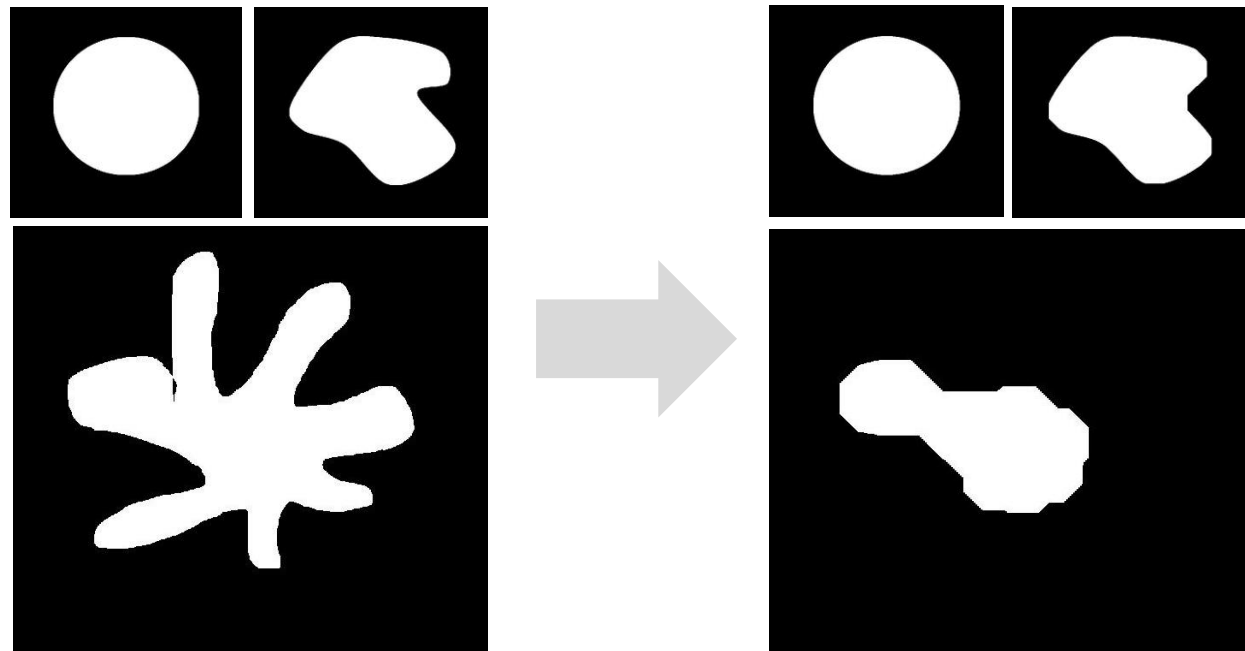
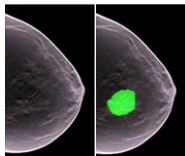


Figure 11 – Illustration of mathematical morphology opening applied to 3 different types of structures

[3] Q. Zheng, "Mathematical morphology - set-theoretic representation for binary shapes," Language and Media Processing Lab - Center for Automation Research, University of Maryland College Park.



# 3.1 FEATURE EXTRACTION

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- Experimental Results
- Conclusions and Future Work

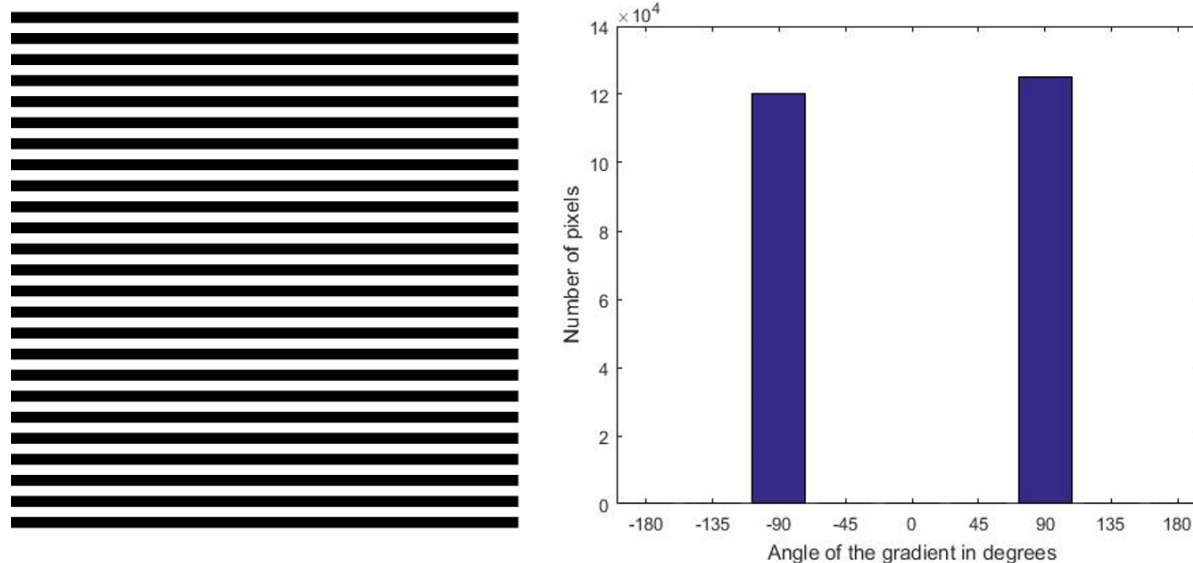


Figure 12 – Striped image (on top) and its HOG features (on the bottom).

[4] M. Davis and F. Sahin, “HOG feature human detection system,” in Systems, Man, and Cybernetics (SMC), 2016 IEEE International Conference on. IEEE, 2016, pp. 002878–002883.

## 3.2.1 SINGLE MODEL DECISION TREE

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- Experimental Results
- Conclusions and Future Work

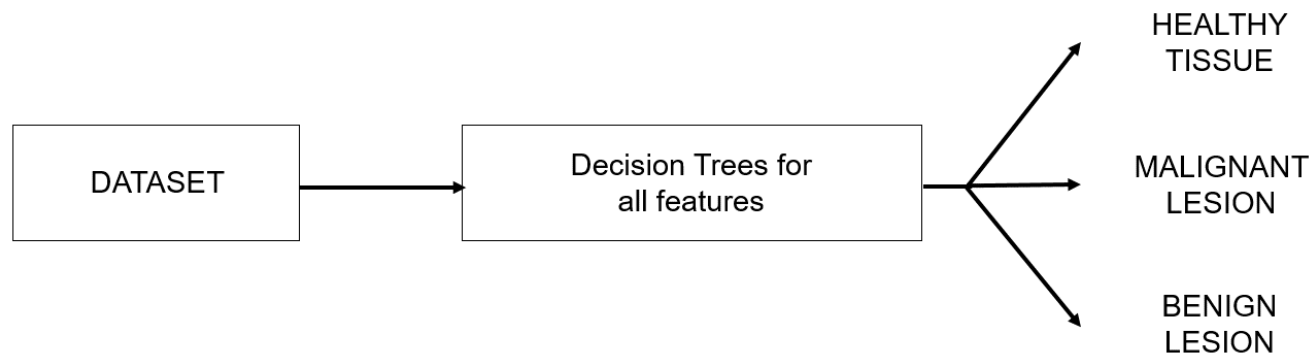
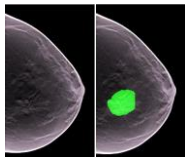


Figure 13 – Schematic representation of the classifier used in the Single Model Decision Tree experiment.



## 3.2.1 SINGLE MODEL DECISION TREE

- Cross Validation
- Pruned
- 100% of the dataset

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- Experimental Results
- Conclusions and Future Work

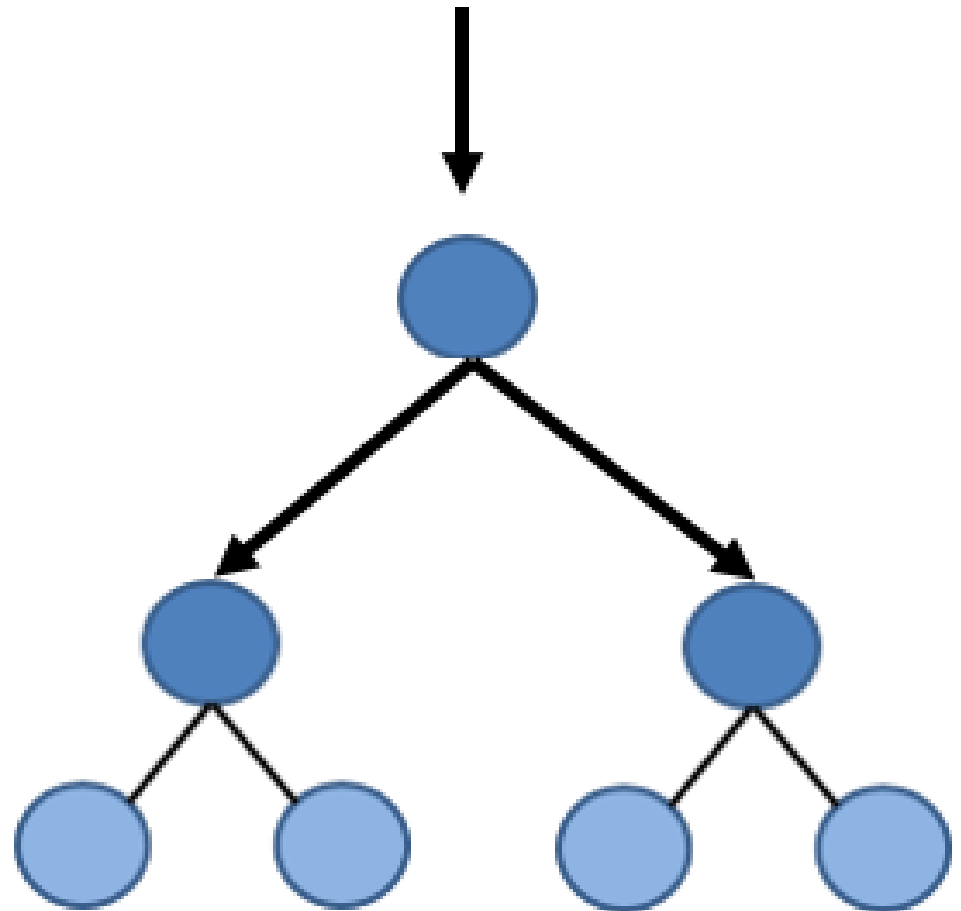
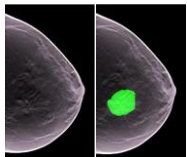


Figure 14 – Illustration of a Decision Tree.





## 3.2.2 DECISION TREE ENSEMBLE CLASSIFIER

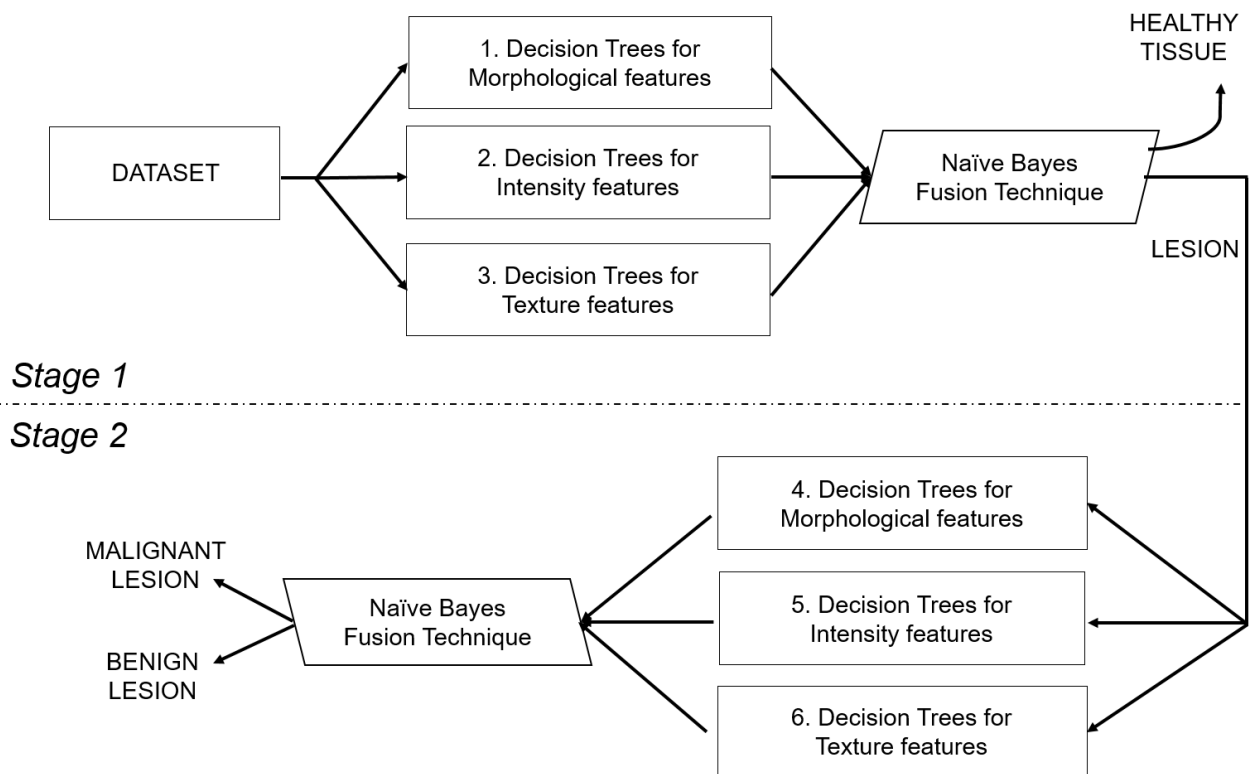
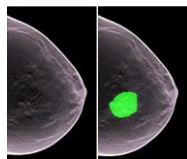


Figure 15 – Schematic representation of the classifier used in the Decision Tree Ensemble Classifier experiment.



## 3.2.3 ADABOOST

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- Experimental Results
- Conclusions

$$h(x, f, p, \theta) = \begin{cases} 1, & \text{if } pf(x) < p\theta \\ 0, & \text{otherwise} \end{cases}$$

$$\epsilon^t = \min_{f, \theta, p} \sum_{i=1}^N w_i^{(t)} |h^{(t)}(x_i, f, p, \theta, p) - d_i|$$

$$\beta^{(t)} = \frac{\epsilon^{(t)}}{1 - \epsilon^{(t)}}$$

$$w_i^{(t+1)} = w_i^{(t)} \beta^{(1 - |h_i^{(t)} - y_i|)}$$

$$\alpha^{(t)} = \frac{1}{\log(\beta^{(t)})}$$

$$C(Z_i) = \begin{cases} 1, & \text{if } \sum_T \alpha^{(t)} h^{(t)}(Z_i) > \frac{1}{2} \sum_T \alpha^{(t)} \\ 0, & \text{otherwise} \end{cases}$$

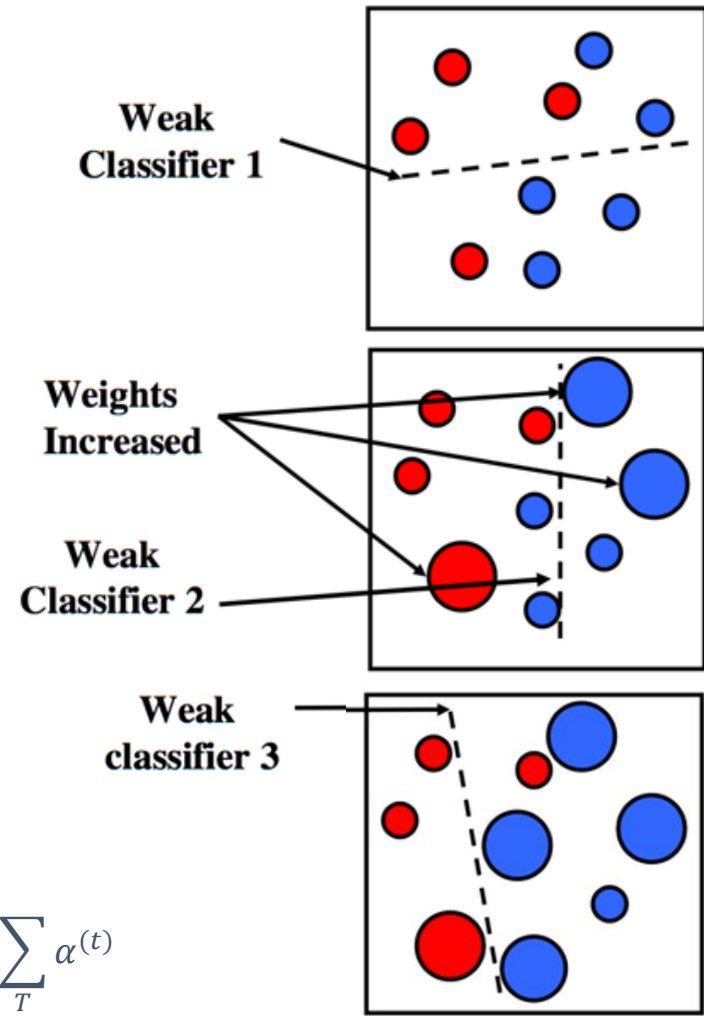


Figure 16 – Illustration of an AdaBoost Classifier.

## 3.2.3 ADABOOST

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- Experimental Results
- Conclusions and Future Work

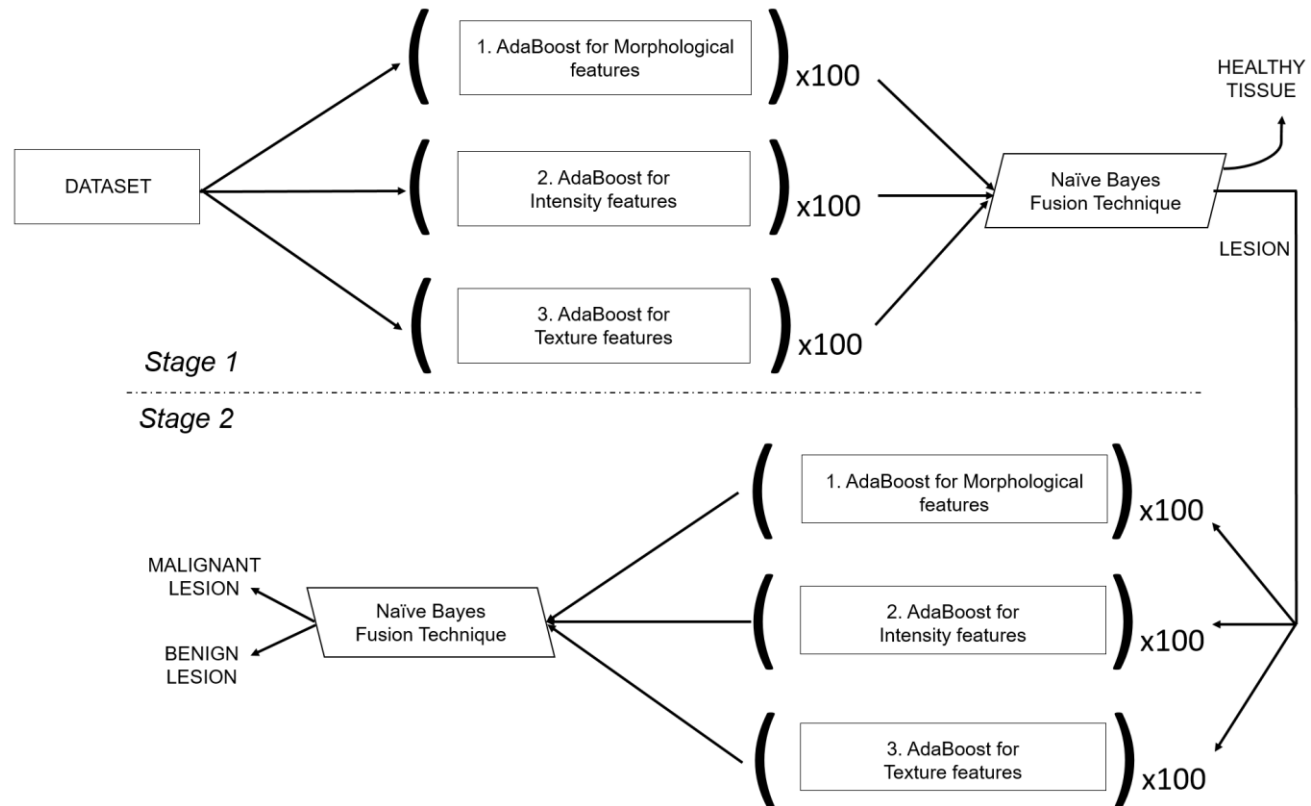
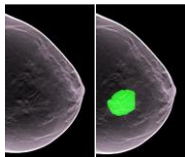


Figure 17 – Schematic representation of the classifier used in the AdaBoost experiment.



## 3.2.3 ADABOOST

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- Experimental Results
- Conclusions and Future Work

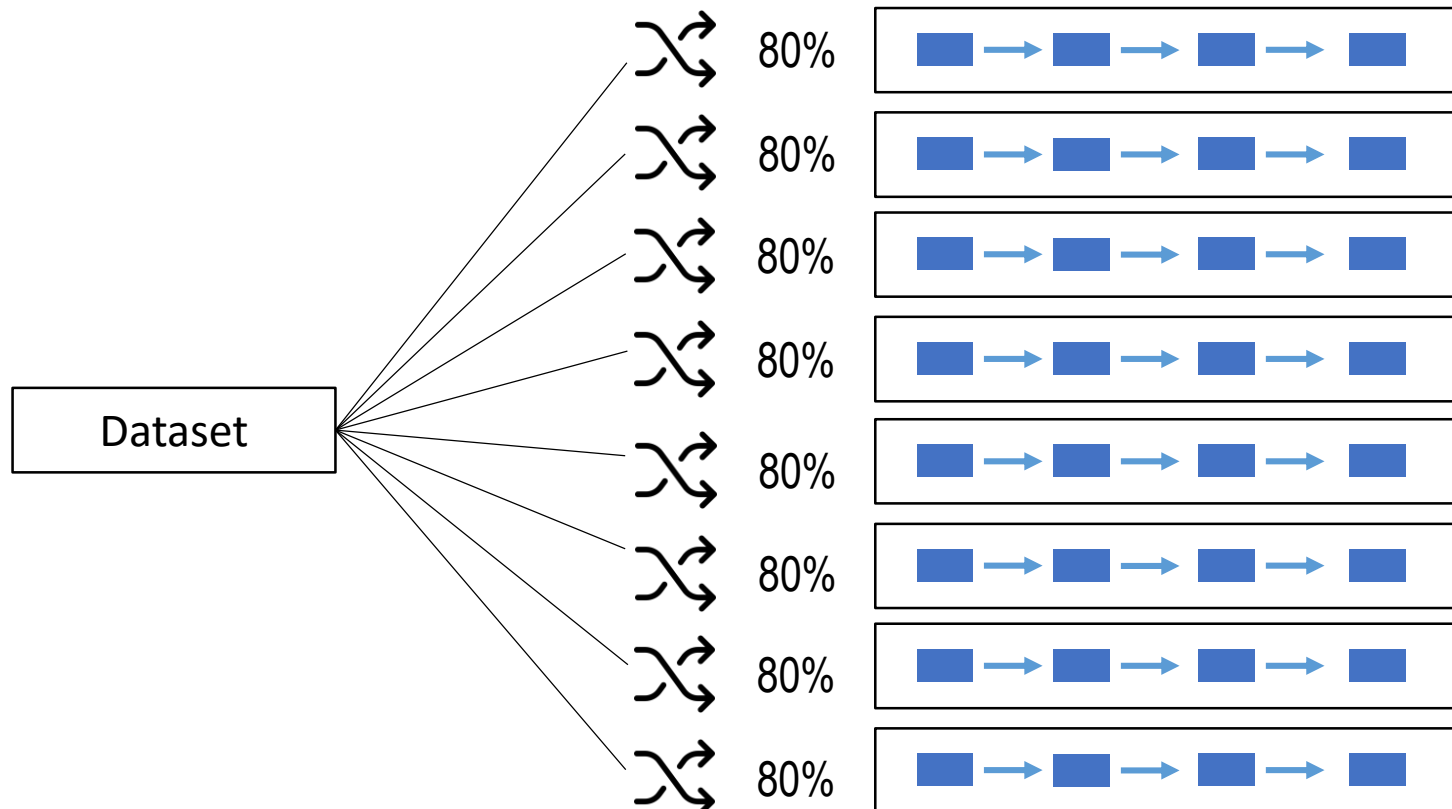


Figure 18 – Representation of bagging technique used in the AdaBoost experiment.

## 3.2.4 FUSION TECHNIQUES

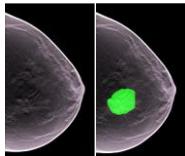
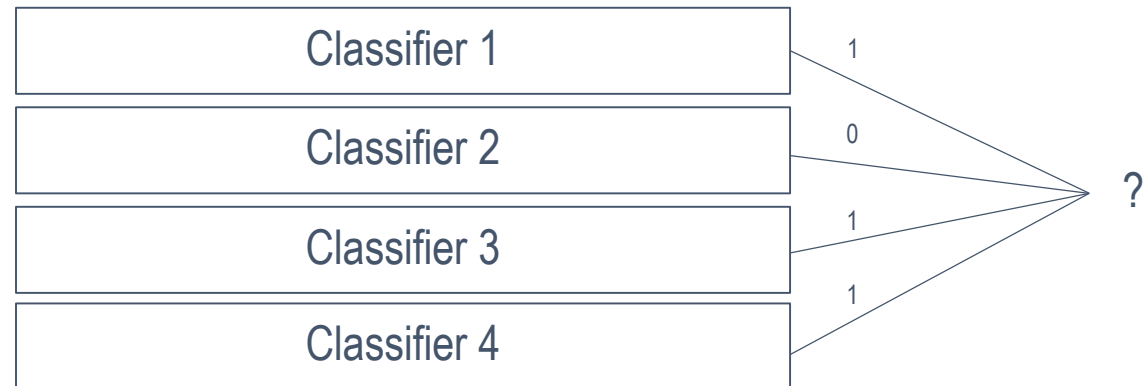
- Context and Motivation
- Pre-processing and Segmentation
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### NAÏVE BAYES TECHNIQUE

$$P(d_i = c | \mathbf{o}) = \frac{P(d_i = c)P(\mathbf{o}|d_i = c)}{P(\mathbf{o})} \propto \frac{1}{N_c^{K-1}} \prod_{k=1}^K cm_k(c, s)$$

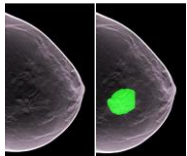
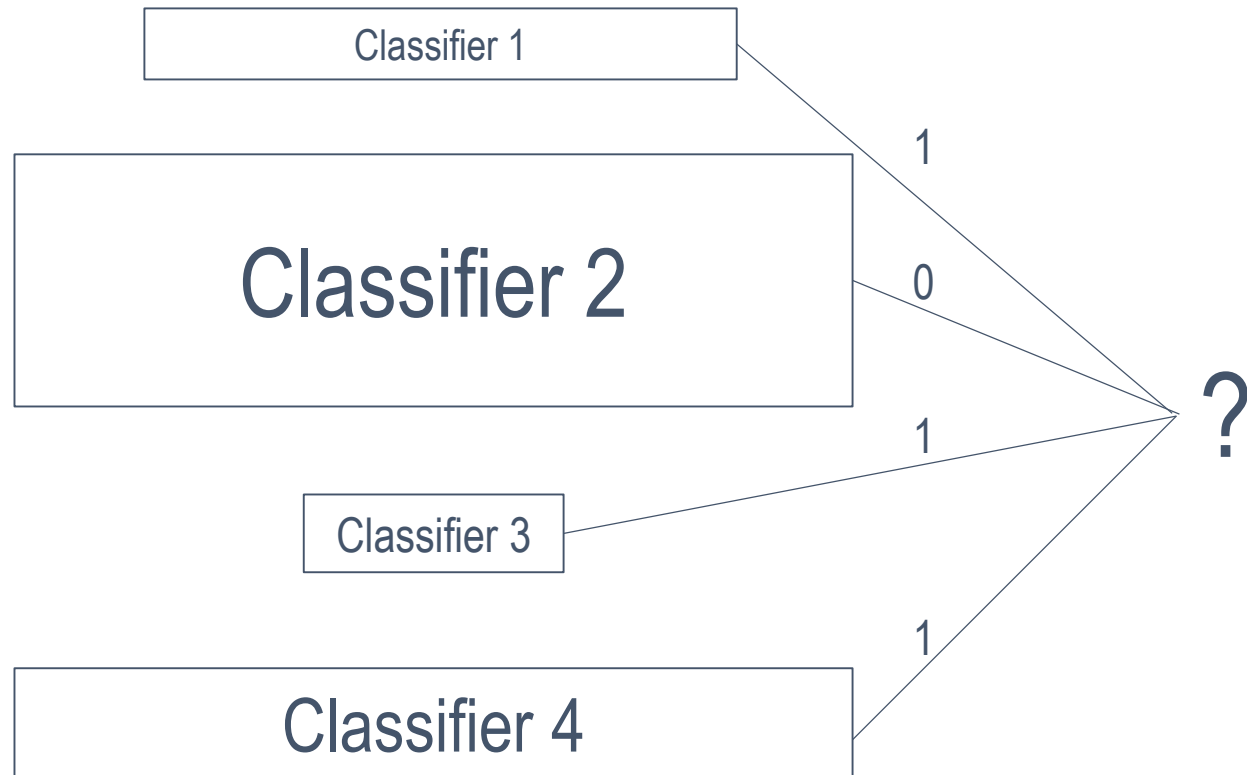
Assume the independence between the classifiers

$$P(\mathbf{o}|d_i = c) = P(o_1, o_2, \dots, o_K | d_i = c) = \prod_{k=1}^K P(o_k | d_i = c)$$



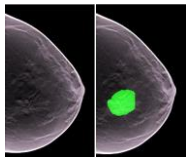
## 3.2.4 FUSION TECHNIQUES

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- Experimental Results
- Conclusions and Future Work



# OUTLINE

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- Experimental Results
- Conclusions and Future Work



## 4.1 DATABASE

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- **Experimental Results**
- Conclusions and Future Work

- 3 Experiments
  - Single Model Decision Tree
  - Decision Tree Ensemble
  - AdaBoost Ensemble
- 3185 images
  - 1950 Healthy Tissue
  - 846 Malignant Lesion
  - 399 Benign Lesions

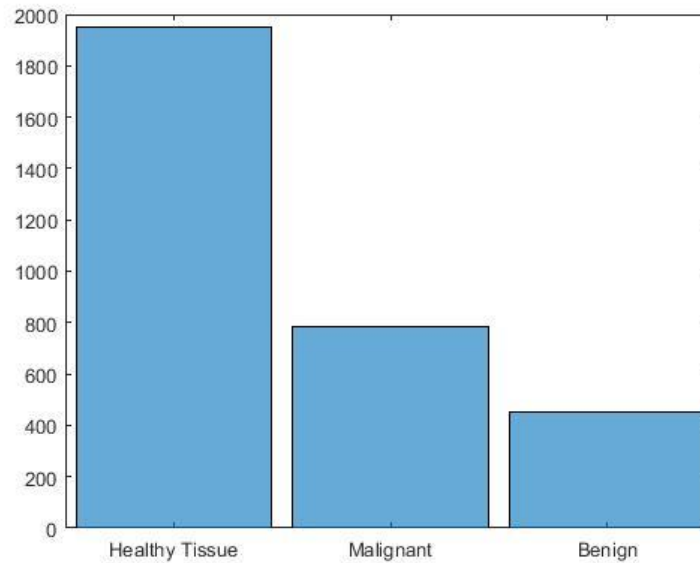
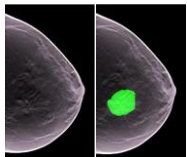


Figure 19 – Description of the database used in this work, broken down by class





## 4.2 EXPERIMENTAL RESULTS

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- **Experimental Results**
- Conclusions and Future Work

### SINGLE MODEL DECISION TREE

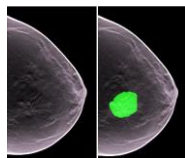
		Output Labels		
		Healthy Tissue	Benign Mass	Malignant Mass
Target Class	Healthy Tissue	1760	83	107
	Benign Mass	136	189	125
	Malignant Mass	134	56	595

### DECISION TREE ENSEMBLE CLASSIFIER

		Output Labels		
		Healthy Tissue	Benign Mass	Malignant Mass
Target Class	Healthy Tissue	1763	99	88
	Benign Mass	99	255	96
	Malignant Mass	105	80	600

### ADABOOST ENSEMBLE CLASSIFIER

		Output Labels		
		Healthy Tissue	Benign Mass	Malignant Mass
Target Class	Healthy Tissue	1863	59	28
	Benign Mass	113	269	68
	Malignant Mass	81	153	551



## 4.2 EXPERIMENTAL RESULTS

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- **Experimental Results**
- Conclusions and Future Work

### SINGLE MODEL DECISION TREE

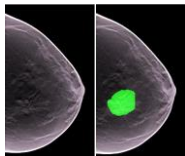
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- Context and Motivation
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- Feature Extraction and Classification
- **Experimental Results**
- Conclusions and Future Work

### SINGLE MODEL DECISION TREE

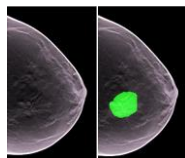
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## 4.2 EXPERIMENTAL RESULTS

- Context and Motivation
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- **Experimental Results**
- Conclusions and Future Work

### SINGLE MODEL DECISION TREE

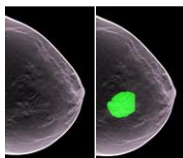
	Single Model Decision Tree
ACC General	0.82
ACC Malignant	0.80
ACC Benign	0.47
ACC Healthy Tissue	0.91

### DECISION TREE ENSEMBLE CLASSIFIER

	Morphological Feat.	Intensity Feat	Texture Feat	Classifier ensemble
ACC General	0.80	0.73	0.71	0.82
ACC Malignant	0.62	0.42	0.43	0.77
ACC Benign	0.41	0.45	0.18	0.57
ACC Healthy Tissue	0.97	0.92	0.94	0.90

### ADABOOST ENSEMBLE CLASSIFIER

	Morphological Feat.	Intensity Feat	Texture Feat	Classifier ensemble
ACC General	0.84	0.76	0.75	0.85
ACC Malignant	0.74	0.59	0.62	0.70
ACC Benign	0.46	0.27	0.20	0.60
ACC Healthy Tissue	0.97	0.94	0.92	0.96



## 4.2 EXPERIMENTAL RESULTS

- Context and Motivation
- Pre-processing and Segmentation
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- **Experimental Results**
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### SINGLE MODEL DECISION TREE

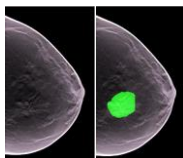
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## 4.2 EXPERIMENTAL RESULTS

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- **Experimental Results**
- Conclusions and Future Work

### SINGLE MODEL DECISION TREE

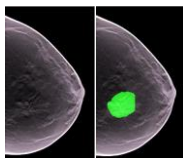
	Single Model Decision Tree
ACC General	0.82
ACC Malignant	0.80
ACC Benign	0.47
ACC Healthy Tissue	0.91

### DECISION TREE ENSEMBLE CLASSIFIER

	Morphological Feat.	Intensity Feat	Texture Feat	Classifier ensemble
ACC General	0.80	0.73	0.71	0.82
ACC Malignant	0.62	0.42	0.43	0.77
ACC Benign	0.41	0.45	0.18	0.57
ACC Healthy Tissue	0.97	0.92	0.94	0.90

### ADABOOST ENSEMBLE CLASSIFIER

	Morphological Feat.	Intensity Feat	Texture Feat	Classifier ensemble
ACC General	0.84	0.76	0.75	0.85
ACC Malignant	0.74	0.59	0.62	0.70
ACC Benign	0.46	0.27	0.20	0.60
ACC Healthy Tissue	0.97	0.94	0.92	0.96



## 4.2 EXPERIMENTAL RESULTS

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- **Experimental Results**
- Conclusions and Future Work

### SINGLE MODEL DECISION TREE

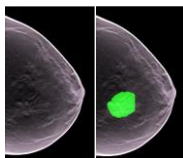
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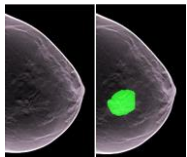
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# OUTLINE

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- Experimental Results
- Conclusions and Future Work





## 4.2 CONCLUSIONS AND FUTURE WORK

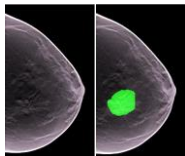
- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- Experimental Results
- Conclusions and Future Work

### SUMMARY OF CONCLUSIONS

- AdaBoost Ensemble Classifier increases the accuracy in 3%
- Separation of the classifiers into different models improves the accuracy for benign lesions only
- Morphological Features increase a model's accuracy in 8,25%

### FUTURE WORK

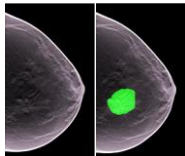
- Test the influence of all the parameters
- Distinguish the lesions using expert's knowledge
- Cost of classification between classes



# COMPUTER AIDED DIAGNOSIS SYSTEM IN DIGITAL MAMMOGRAPHY

THANK  
YOU

JOÃO ROCHA E MELO



# BREAST AND BREAST TUMORS

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- Experimental Results
- Conclusions and Future Work

- Breast breakdown into 4 density types:
  - I, II, III, IV
- Breast Tissue divided into:
  - Adipose Tissue
  - Glandular Tissue

	Malignant	Benign
Mass	●	●
Micro Calcifications	●	●

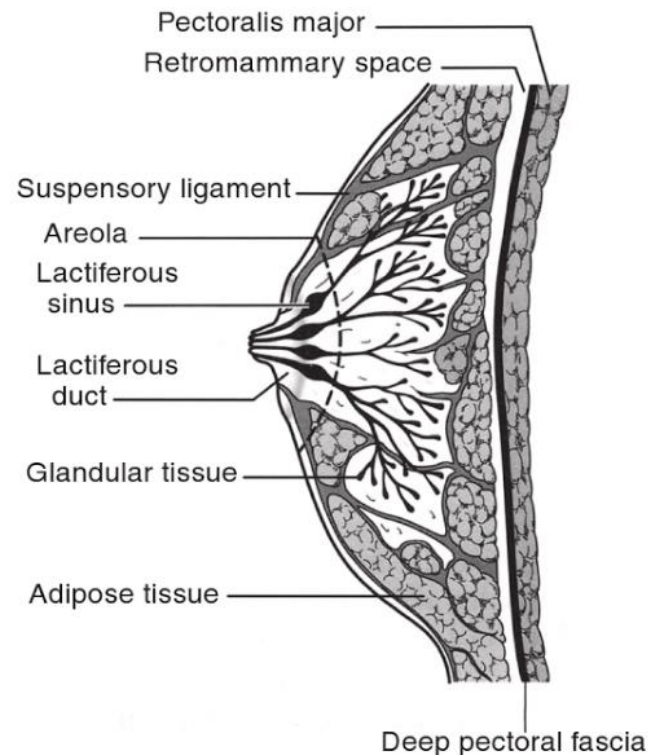
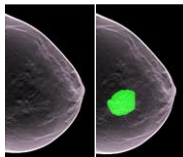


Figure 20 – Breast Illustration



# BILATERAL FILTER

- Pixel-by-Pixel technique
- Reduces Noise
- Keeps the information of the edges
- Disregards irrelevant information (including noise)
- Improves the accuracy of the segmentation stage by reducing the number of false positives

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- Experimental Results
- Conclusions and Future Work

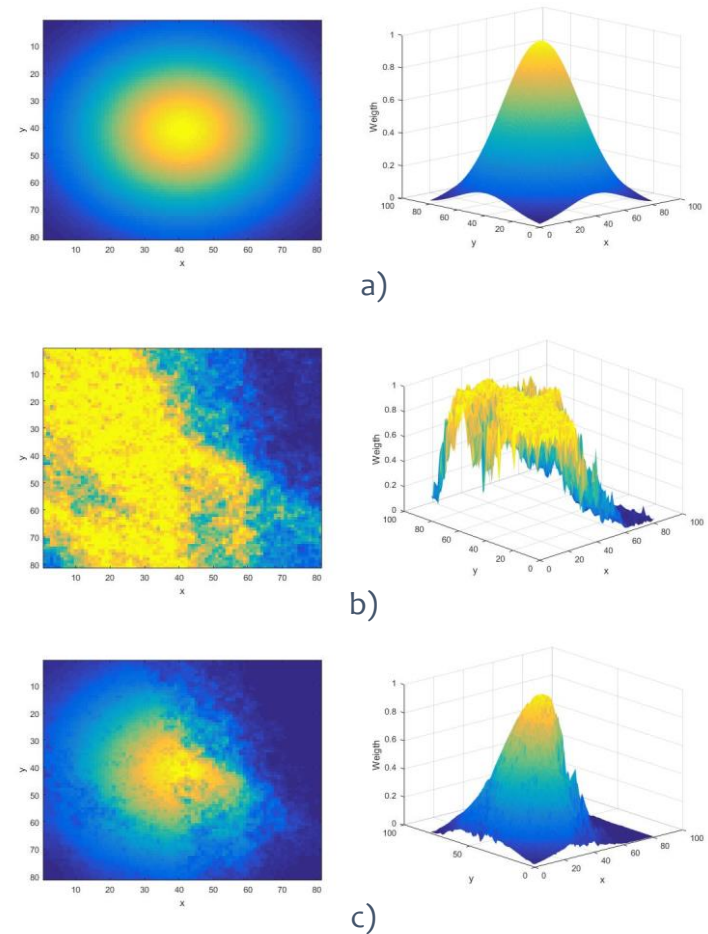
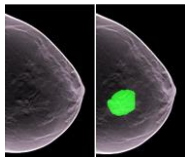


Figure 21 – 2D (on the left) and 3D (on the right) representations of a) spatial distance filter, b) intensity distance filter and c) bilateral filter



# BILATERAL FILTER

Spatial Distance Filter

$$f(c_x, c_y, x, y) = \frac{e^{-|(c_x, c_y) - (x, y)|}}{\sigma_s^2}$$

Intensity Based Filter

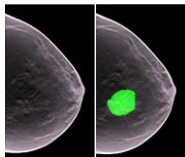
$$g(c_x, c_y, x, y) = \frac{e^{-(I(c_x, c_y) - I(x, y))}}{\sigma_I^2}$$

Bilateral filter

$$r(c_x, c_y) = \sum_{x \text{ in } \Omega} \sum_{y \text{ in } \Omega} f(c_x, c_y, x, y) \times g(c_x, c_y, x, y)$$

Filtered image

$$I_{BF}(c_x, c_y) = \sum_{x \text{ in } \Omega} \sum_{y \text{ in } \Omega} I(x, y) \times f \times g$$



# SLIDING BAND FILTER

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- Experimental Results
- Conclusions and Future Work

$$DC_{SBF}(P) = \frac{1}{N} \sum_{i=1}^N \max_{R_{min} < R < R_{max}} \left[ \frac{1}{R - R_{min}} \sum_{r=R_{min}}^R CI(x_i, y_i) \right]$$

Gradient based technique

Finds the center and the border of the ROI

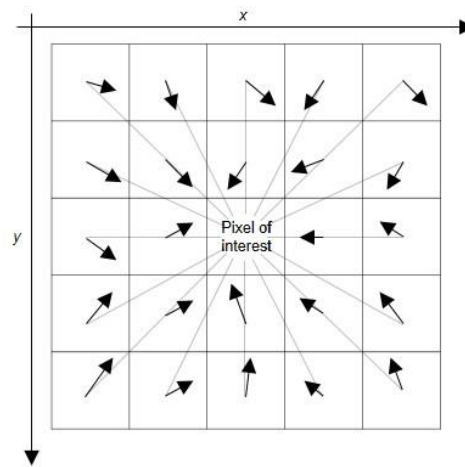


Figure 22 – Representation of the gradients of each pixel in the window of analysis of the pixel of interest -

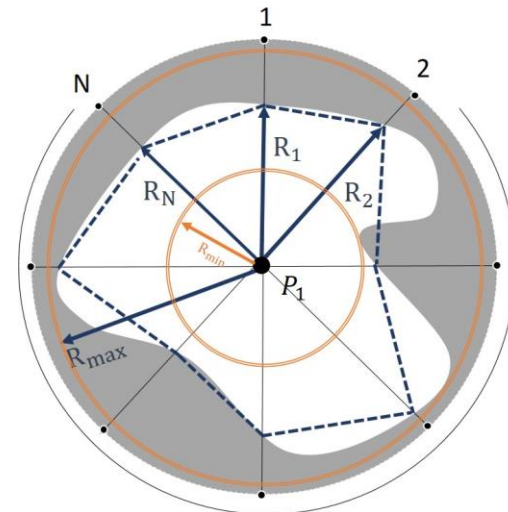
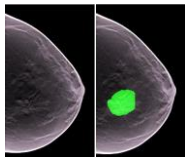


Figure 23 – Illustration of the border found by the Sliding band filter



# FEATURE EXTRACTION

## MORPHOLOGICAL

- X and Y coordinates of the location of the centre
- Maximum Radius
- Perimeter
- Area
- Surface Change

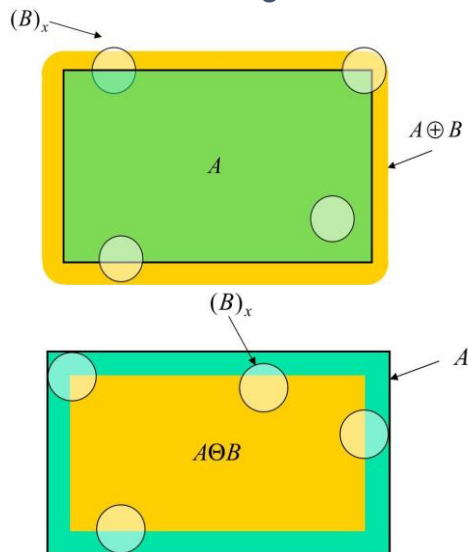


Figure 24 – Illustration of mathematical morphology operations. Dilation (on top) and Erosion (on bottom).

## INTENSITY

- Mean Intensity Value
- Maximum Intensity Value
- Minimum Intensity Value
- Standard Deviation of Intensity Values
- Skewness
- Kurtosis
- Contrast
- Energy
- 10 Intensity Histogram bins

## TEXTURE

- Entropy
- HOG Features

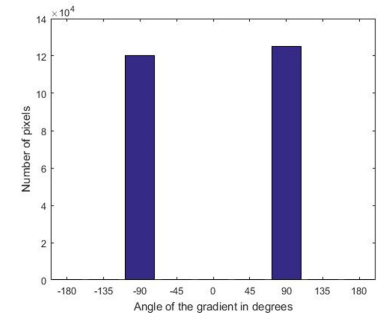
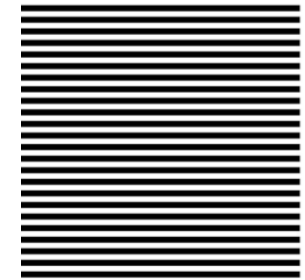


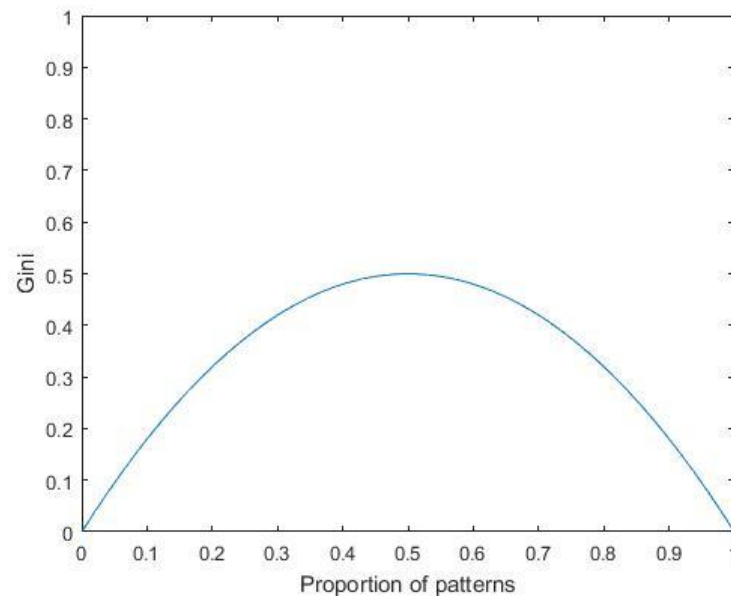
Figure 25 – Striped image (on top) and its HOG features (on the bottom).

# SINGLE MODEL DECISION TREE

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- Experimental Results
- Conclusions and Future Work

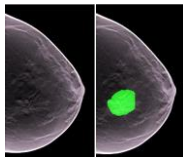
*Gini* Function

$$Gini(S) = 1 - \sum_{k=1}^C p_s(k)^2$$



*DROP*

$$Drop(S, A) = Gini(S) - \sum_{v \in values(A)} \frac{|S_v|}{|S|} Gini(S_v)$$





# ADABOOST

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- Experimental Results
- Conclusions

$$h(x, f, p, \theta) = \begin{cases} 1, & \text{if } pf(x) < p\theta \\ 0, & \text{otherwise} \end{cases}$$

$$\epsilon^t = \min_{f, \theta, p} \sum_{i=1}^N w_i^{(t)} |h^{(t)}(x_i, f, p, \theta, p) - d_i|$$

$$\beta^{(t)} = \frac{\epsilon^{(t)}}{1 - \epsilon^{(t)}}$$

$$w_i^{(t+1)} = w_i^{(t)} \beta^{(1 - |h_i^{(t)} - y_i|)}$$

$$\alpha^{(t)} = \frac{1}{\log(\beta^{(t)})}$$

$$C(Z_i) = \begin{cases} 1, & \text{if } \sum_T \alpha^{(t)} h^{(t)}(Z_i) > \frac{1}{2} \sum_T \alpha^{(t)} \\ 0, & \text{otherwise} \end{cases}$$

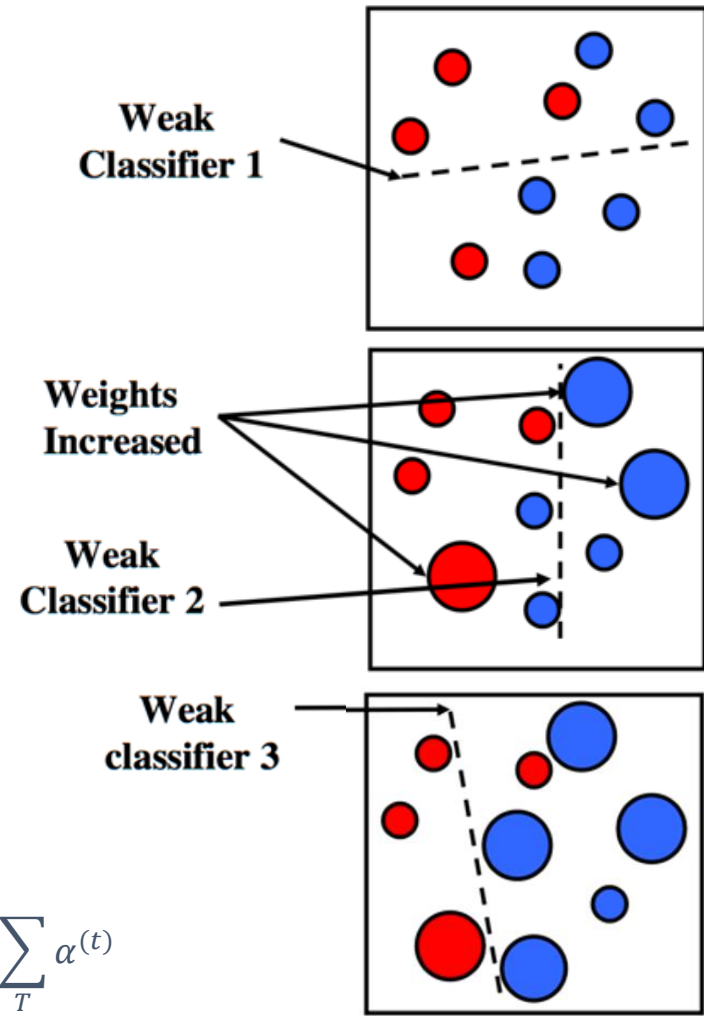


Figure 27 – Illustration of an AdaBoost Classifier

# FUSION TECHNIQUES

## NAÏVE BAYES TECHNIQUE

$$P(d_i = c | \mathbf{o}) = \frac{P(d_i = c)P(\mathbf{o}|d_i = c)}{P(\mathbf{o})}$$

1. Disregard  $P(\mathbf{o})$
2.  $P(d_i = c) = \frac{N_c}{N}$
3. Assume the independence between the classifiers

$$P(\mathbf{o}|d_i = c) = P(o_1, o_2, \dots, o_K|d_i = c) = \prod_{k=1}^K P(o_k|d_i = c)$$

4. This can be withdrawn from:

$$P(o_k|d_i = c) = \frac{cm_k(c, s)}{N_c}$$

5. Which means that:

$$P(d_i = c | \mathbf{o}) \propto \frac{1}{N_c^{K-1}} \prod_{k=1}^K cm_k(c, s)$$

- Context and Motivation
- Pre-processing and Segmentation
- Feature Extraction and Classification
- Experimental Results
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