

Neural Neural Networks

Part I

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CSS634: Deep Learning

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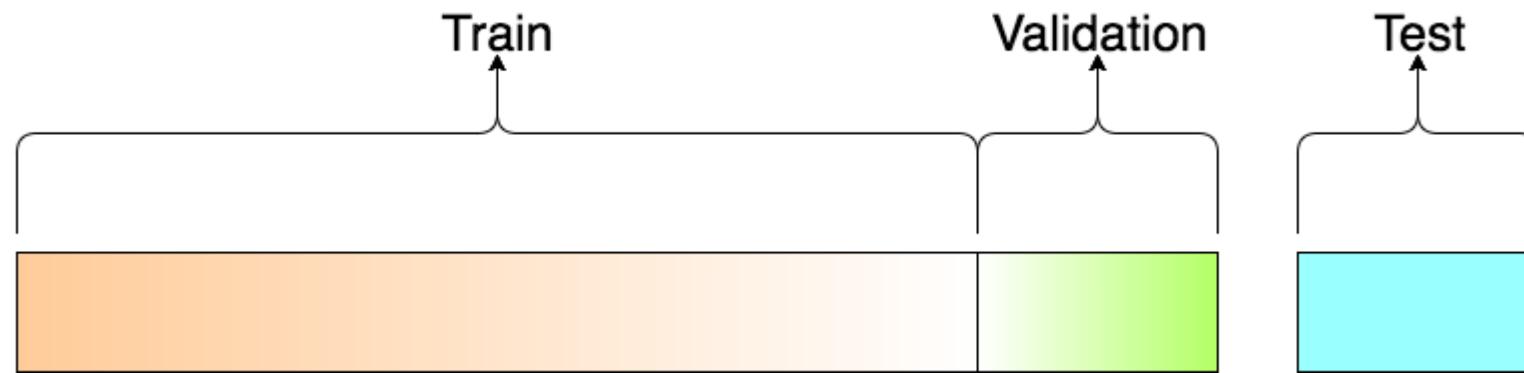
Part I

- Splitting dataset
- Bias/Variance
- Activation functions
- Normalizing Inputs
- Vanishing/Exploding gradients
- Weight initialization
- Batch normalization
- Babysitting the learning process
- Hyperparameter tuning

Splitting Dataset

Splitting Dataset

Train/validation(dev)/test sets



Traditional ML split example: 60/20/20

Deep learning split example: 98/1/1

K-fold cross validation is very expensive!

Mismatched train/test distribution

Training set:
cat pictures from webpages

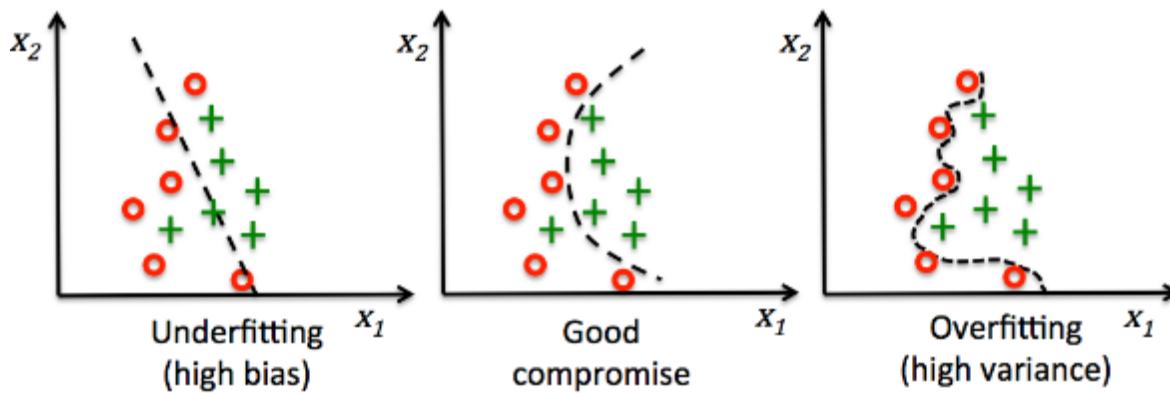
Dev/test sets:
cat pictures from users using your app

Make sure dev and test sets come from same distribution

Bias/Variance

Bias/Variance

- Easy to learn but difficult to master
- In DL there is less of discussion about bias/variance tradeoff



Bias/Variance

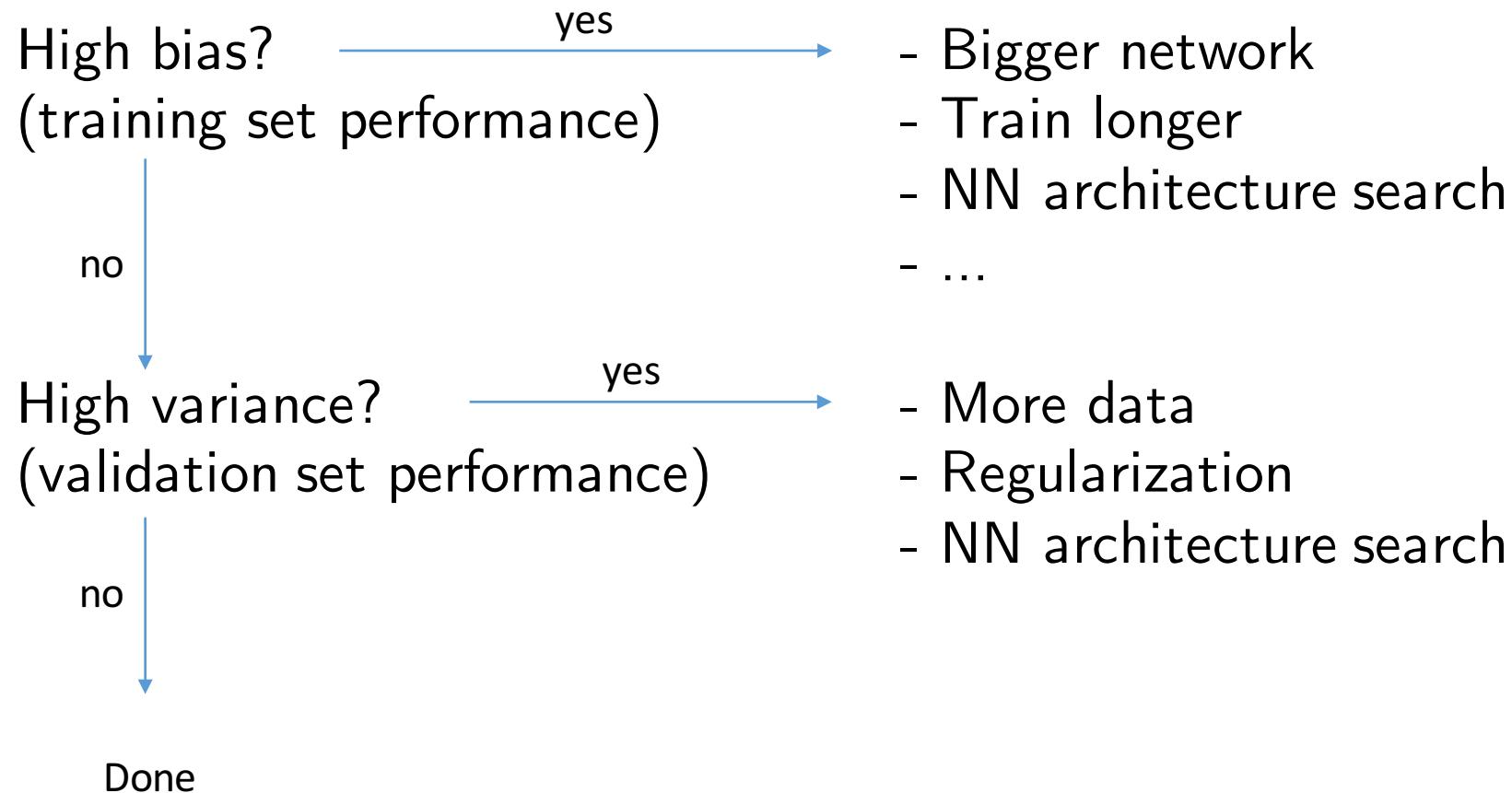
Cat classification



Train set error:	1%	15%	13%	0.5%
Dev set error:	11%	16%	30%	1%
	high variance	high bias	high bias & high variance	low bias & low variance

Bayes error (human): $\approx 0\%$

Basic Recipe

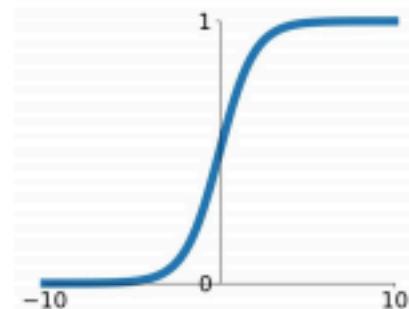


Activation Functions

Activation Functions

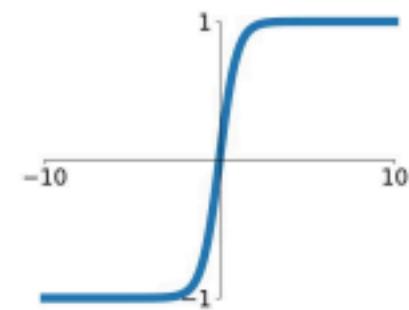
Sigmoid

$$\sigma(x) = \frac{1}{1+e^{-x}}$$



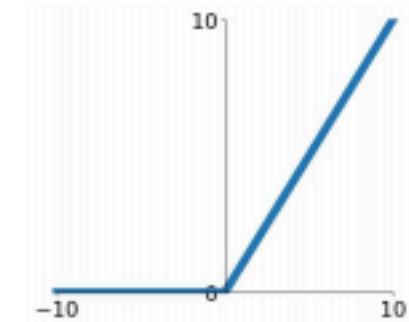
tanh

$$\tanh(x)$$



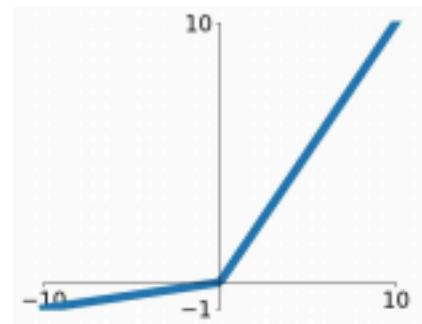
ReLU

$$\max(0, x)$$



Leaky ReLU

$$\max(0.1x, x)$$

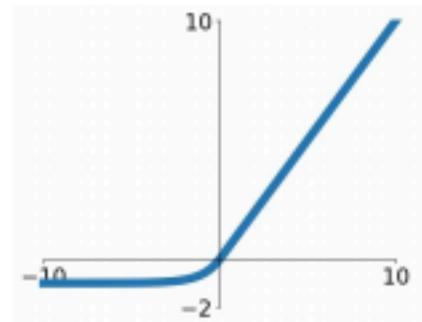


Maxout

$$\max(w_1^T x + b_1, w_2^T x + b_2)$$

ELU

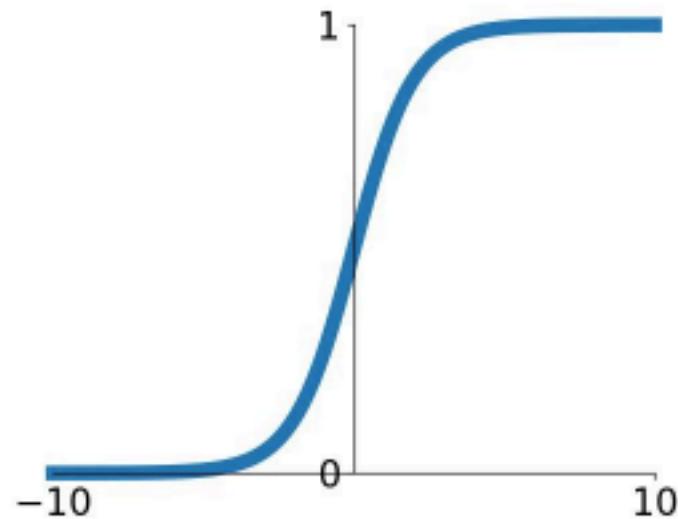
$$\begin{cases} x & x \geq 0 \\ \alpha(e^x - 1) & x < 0 \end{cases}$$



Activation Functions

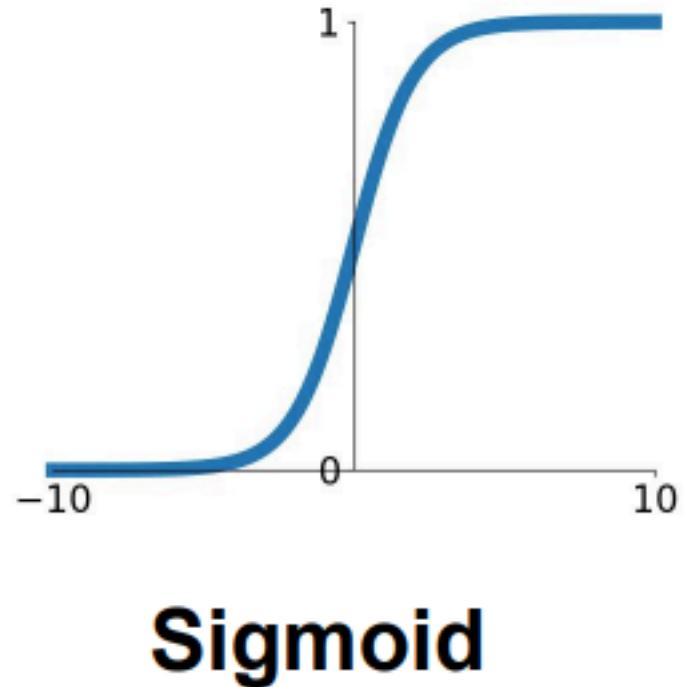
$$\sigma(x) = 1/(1 + e^{-x})$$

- Squashes numbers to range [0,1]
- Historically popular since they have nice interpretation as a saturating “firing rate” of a neuron



Sigmoid

Activation Functions

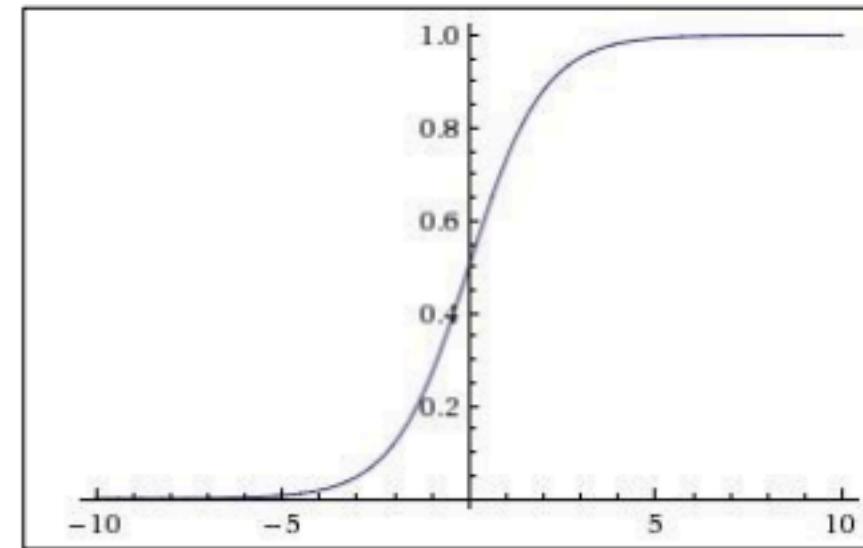
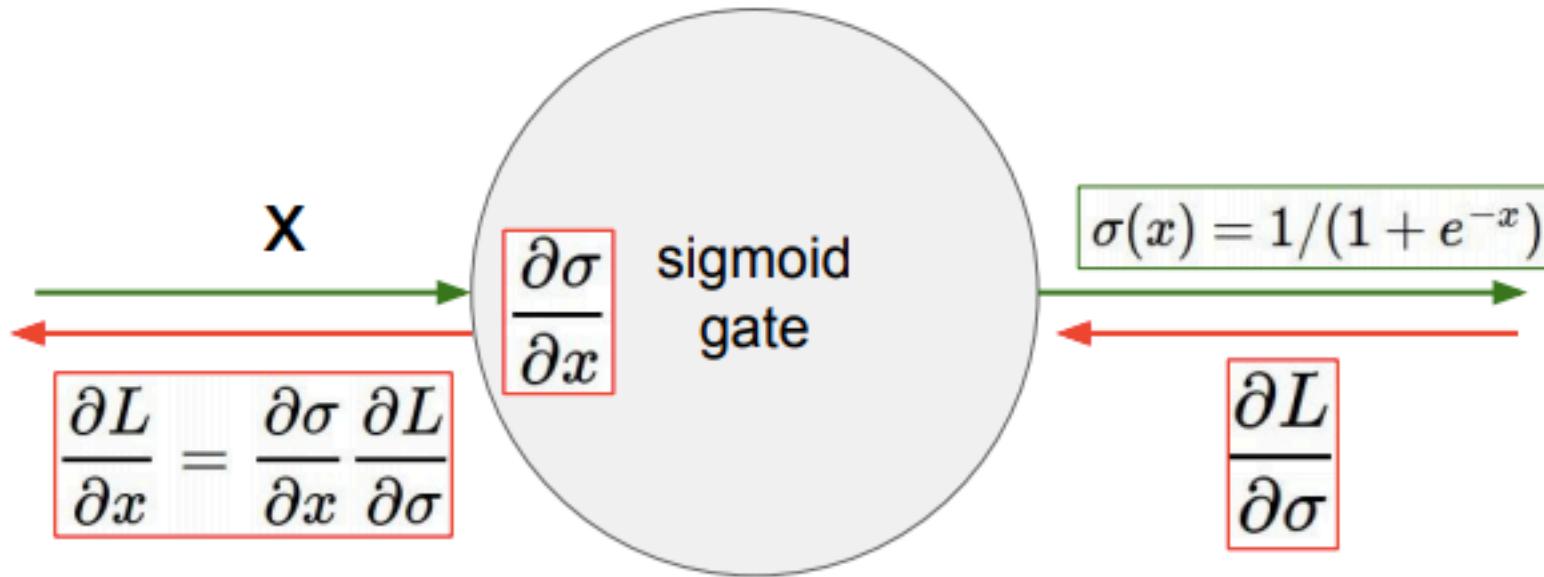


$$\sigma(x) = 1/(1 + e^{-x})$$

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3 problems:

1. Saturated neurons “kill” the gradients

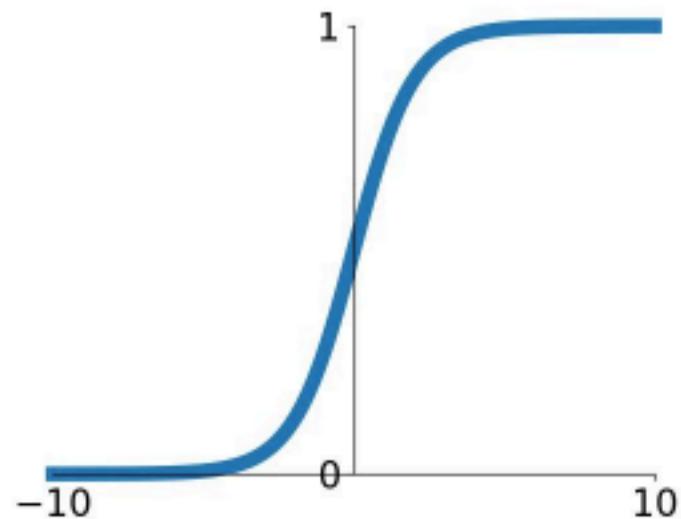


What happens when $x = -10$?

What happens when $x = 0$?

What happens when $x = 10$?

Activation Functions



Sigmoid

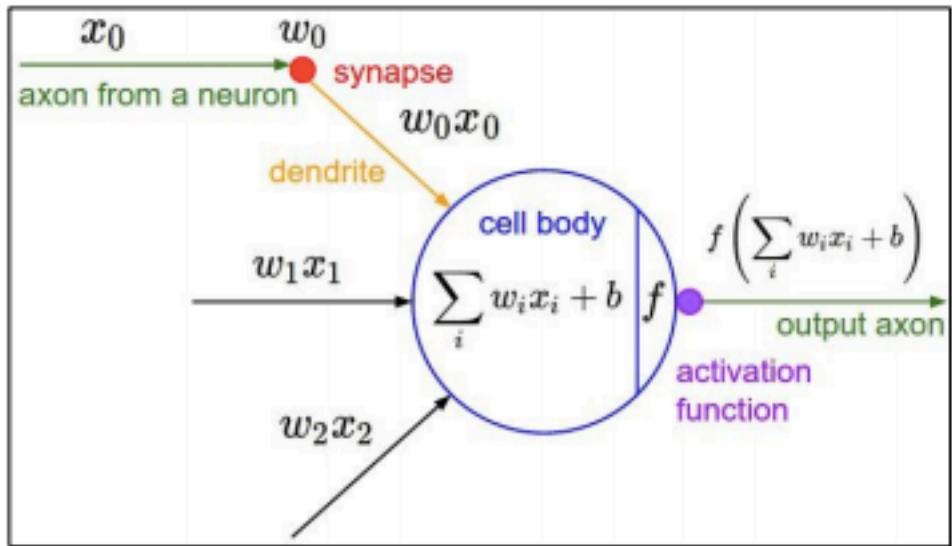
$$\sigma(x) = 1/(1 + e^{-x})$$

- Squashes numbers to range [0,1]
- Historically popular since they have nice interpretation as a saturating “firing rate” of a neuron

3 problems:

1. Saturated neurons “kill” the gradients
2. Sigmoid outputs are not zero-centered

Consider what happens when the input to a neuron (x) is always positive:

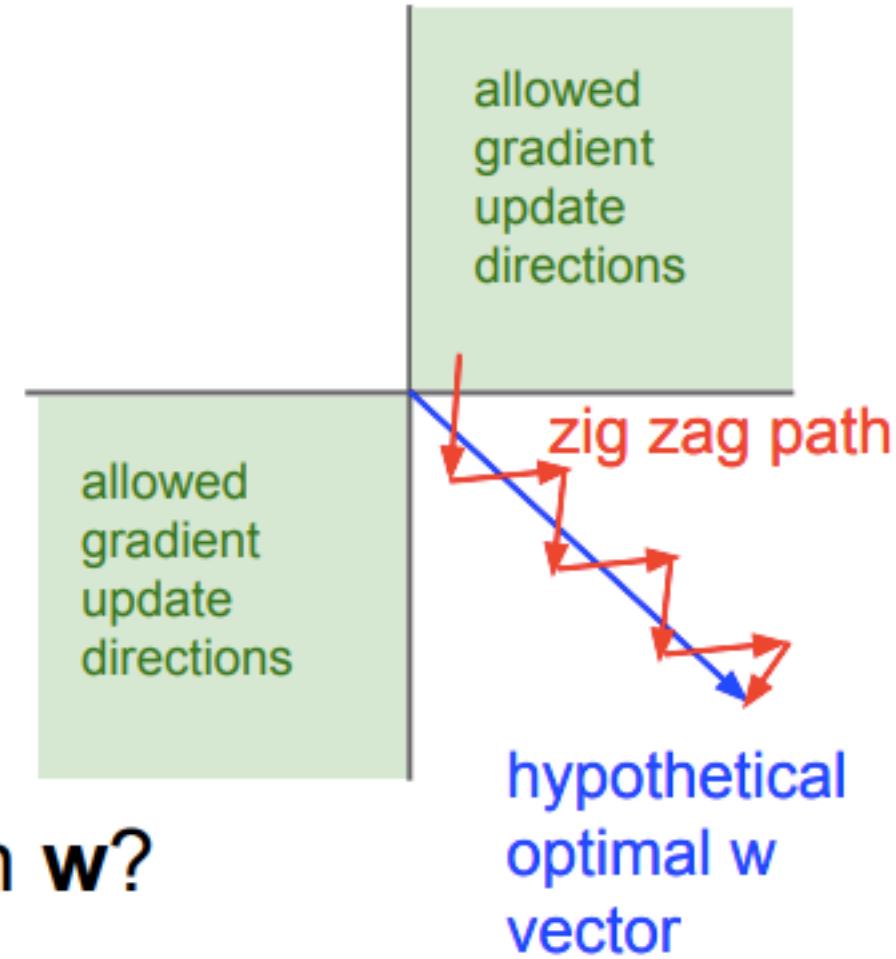


$$f \left(\sum_i w_i x_i + b \right)$$

What can we say about the gradients on w ?

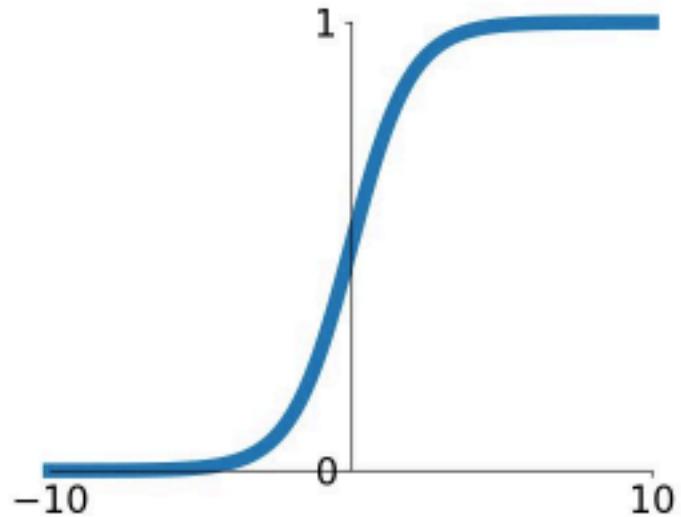
Consider what happens when the input to a neuron is always positive...

$$f \left(\sum_i w_i x_i + b \right)$$



What can we say about the gradients on w ?
Always all positive or all negative :(
(this is also why you want zero-mean data!)

Activation Functions



Sigmoid

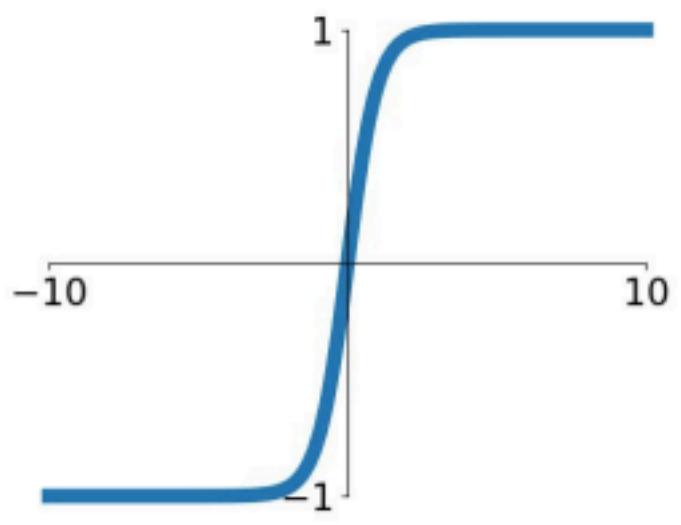
$$\sigma(x) = 1/(1 + e^{-x})$$

- Squashes numbers to range [0,1]
- Historically popular since they have nice interpretation as a saturating “firing rate” of a neuron

3 problems:

1. Saturated neurons “kill” the gradients
2. Sigmoid outputs are not zero-centered
3. $\exp()$ is a bit compute expensive

Activation Functions

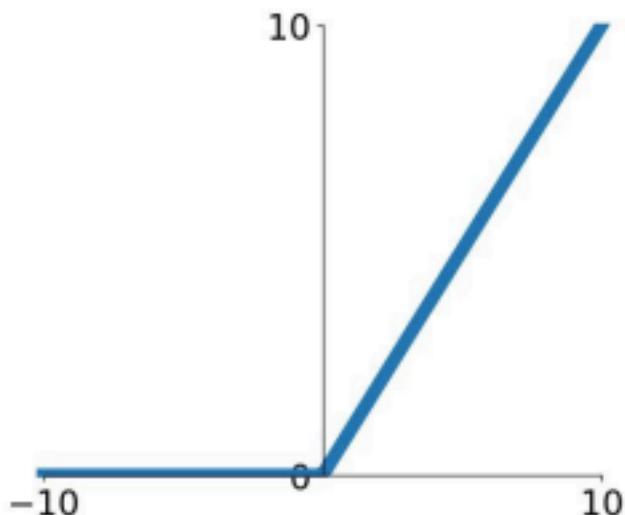


tanh(x)

- Squashes numbers to range [-1,1]
- zero centered (nice)
- still kills gradients when saturated :(

[LeCun et al., 1991]

Activation Functions

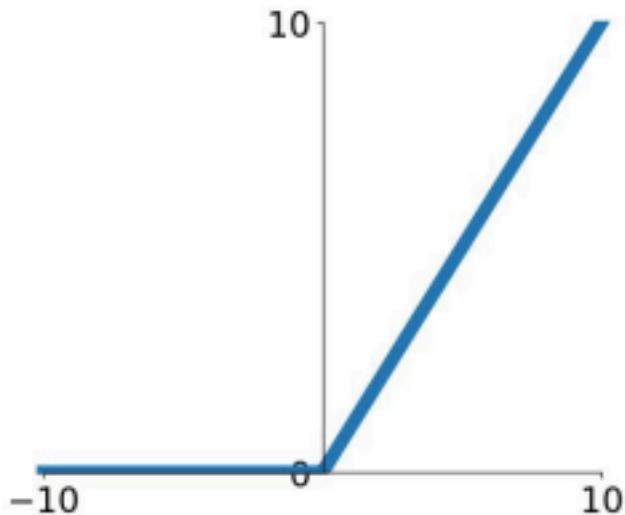


- Computes $f(x) = \max(0, x)$
- Does not saturate (in +region)
- Very computationally efficient
- Converges much faster than sigmoid/tanh in practice (e.g. 6x)
- Actually more biologically plausible than sigmoid

ReLU
(Rectified Linear Unit)

[Krizhevsky et al., 2012]

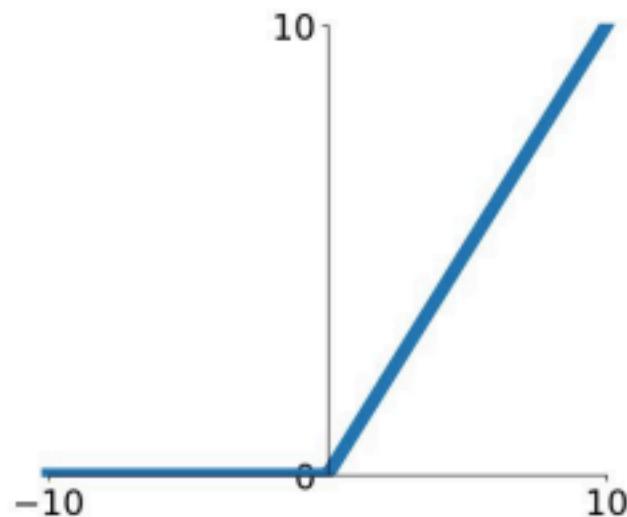
Activation Functions



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- Not zero-centered output

Activation Functions

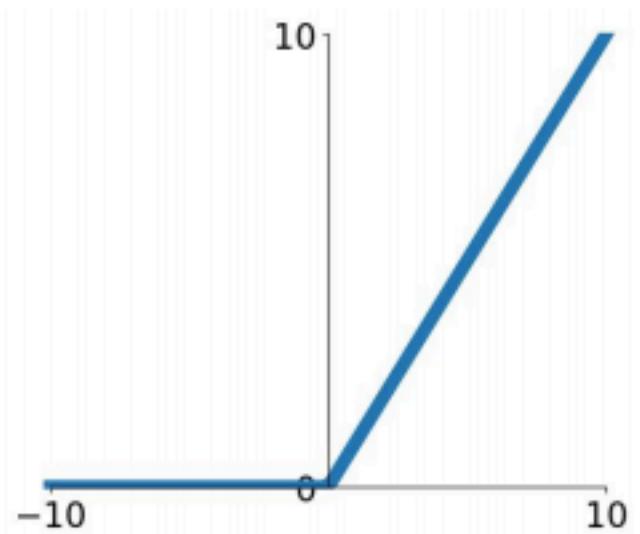
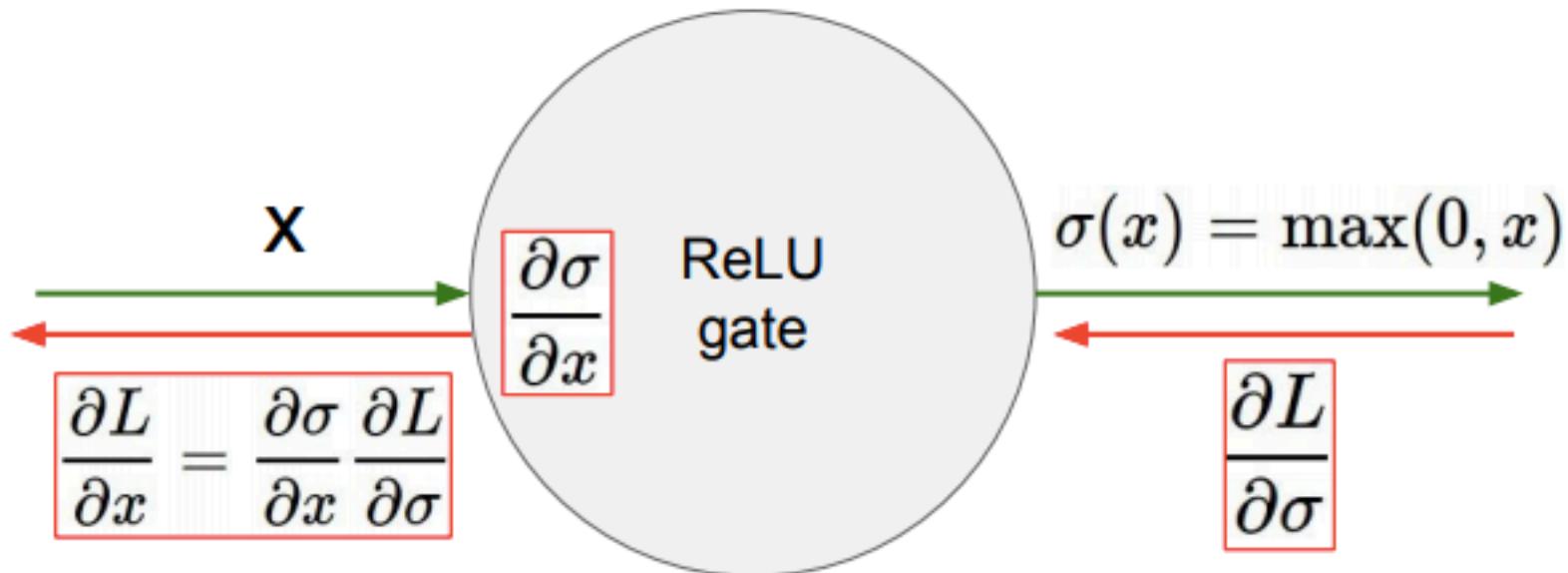


ReLU
(Rectified Linear Unit)

- Computes $f(x) = \max(0, x)$
- Does not saturate (in +region)
- Very computationally efficient
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- Actually more biologically plausible than sigmoid

- Not zero-centered output
- An annoyance:

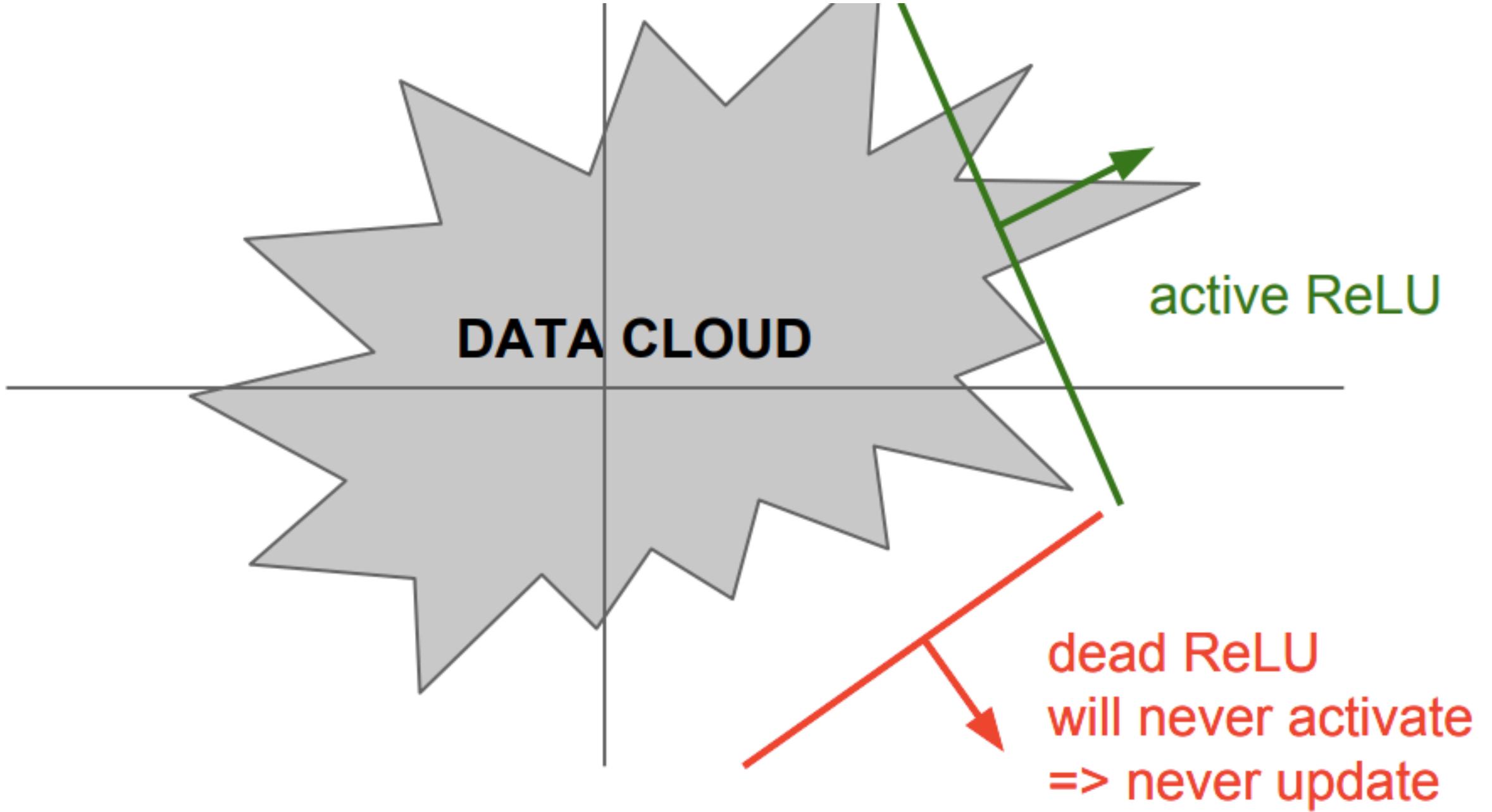
hint: what is the gradient when $x < 0$?



What happens when $x = -10$?

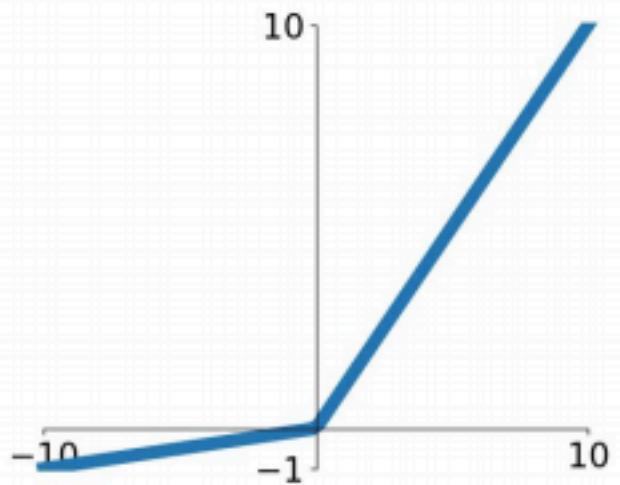
What happens when $x = 0$?

What happens when $x = 10$?



Activation Functions

[Mass et al., 2013]
[He et al., 2015]



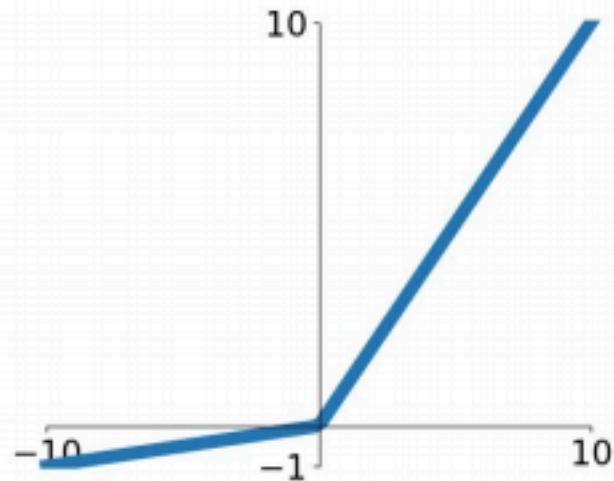
- Does not saturate
- Computationally efficient
- Converges much faster than sigmoid/tanh in practice! (e.g. 6x)
- **will not “die”.**

Leaky ReLU

$$f(x) = \max(0.01x, x)$$

Activation Functions

[Mass et al., 2013]
[He et al., 2015]



Leaky ReLU

$$f(x) = \max(0.01x, x)$$

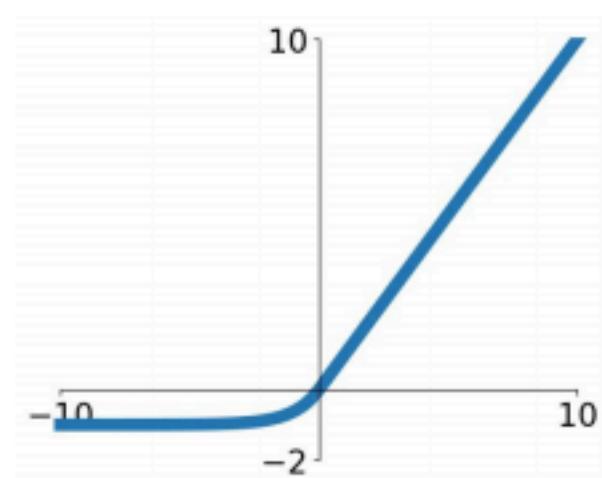
- Does not saturate
- Computationally efficient
- Converges much faster than sigmoid/tanh in practice! (e.g. 6x)
- **will not “die”.**

Parametric Rectifier (PReLU)

$$f(x) = \max(\alpha x, x)$$

backprop into α
(parameter)

Exponential Linear Units (ELU)



- All benefits of ReLU
- Closer to zero mean outputs
- Negative saturation regime compared with Leaky ReLU adds some robustness to noise

$$f(x) = \begin{cases} x & \text{if } x > 0 \\ \alpha (\exp(x) - 1) & \text{if } x \leq 0 \end{cases}$$

- Computation requires `exp()`

Maxout “Neuron”

[Goodfellow et al., 2013]

- Does not have the basic form of dot product -> nonlinearity
- Generalizes ReLU and Leaky ReLU
- Linear Regime! Does not saturate! Does not die!

$$\max(w_1^T x + b_1, w_2^T x + b_2)$$

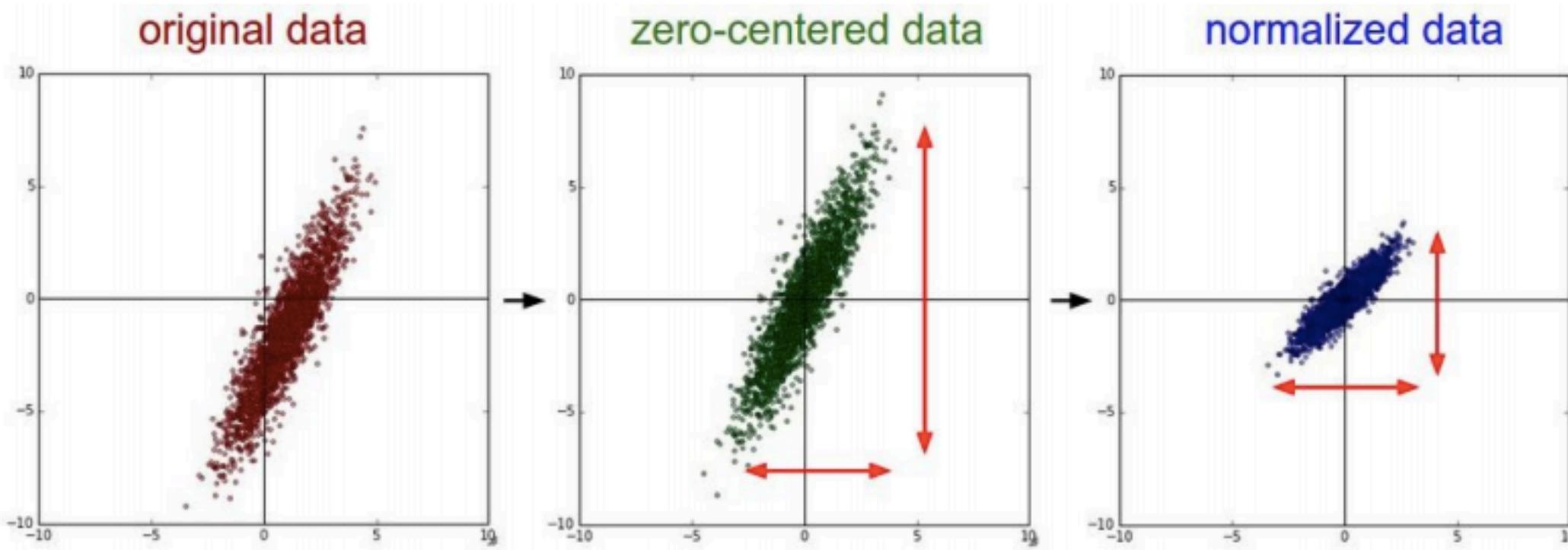
Problem: doubles the number of parameters/neuron :(

TLDR: In practice:

- Use ReLU. Be careful with your learning rates
- Try out Leaky ReLU / Maxout / ELU
- Try out tanh but don't expect much
- Don't use sigmoid

Normalizing Inputs

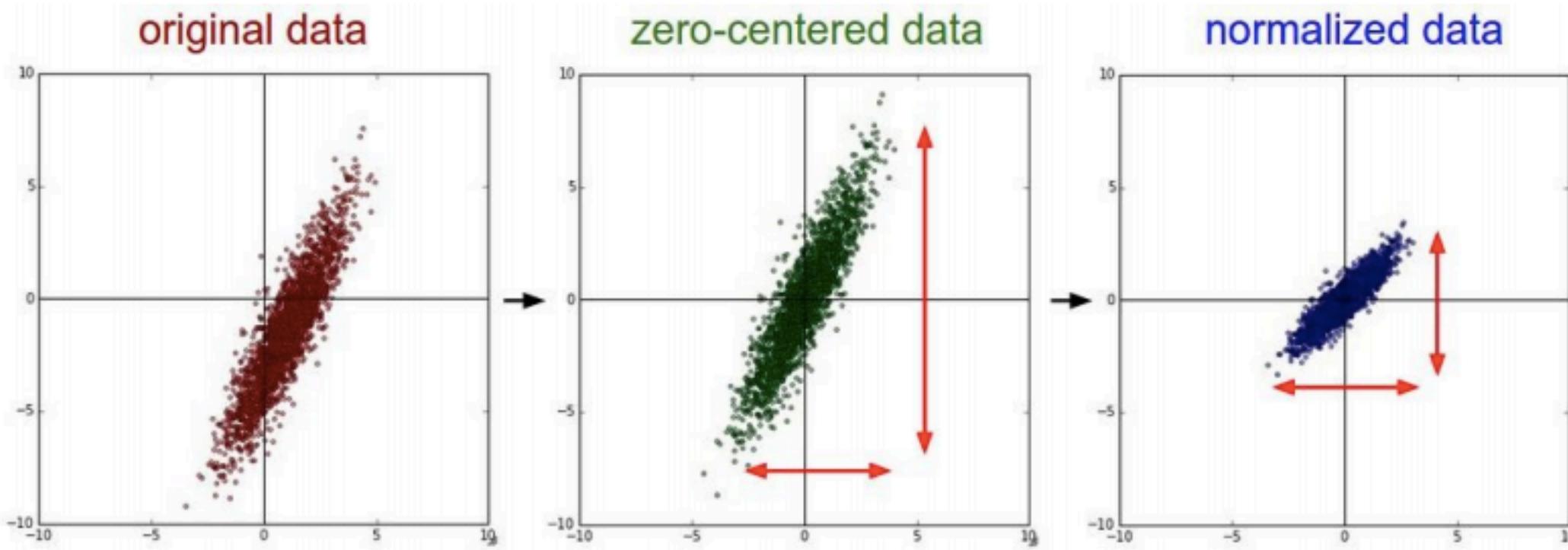
Normalizing Inputs



```
X -= np.mean(X, axis = 0)
```

```
X /= np.std(X, axis = 0)
```

Normalizing Inputs

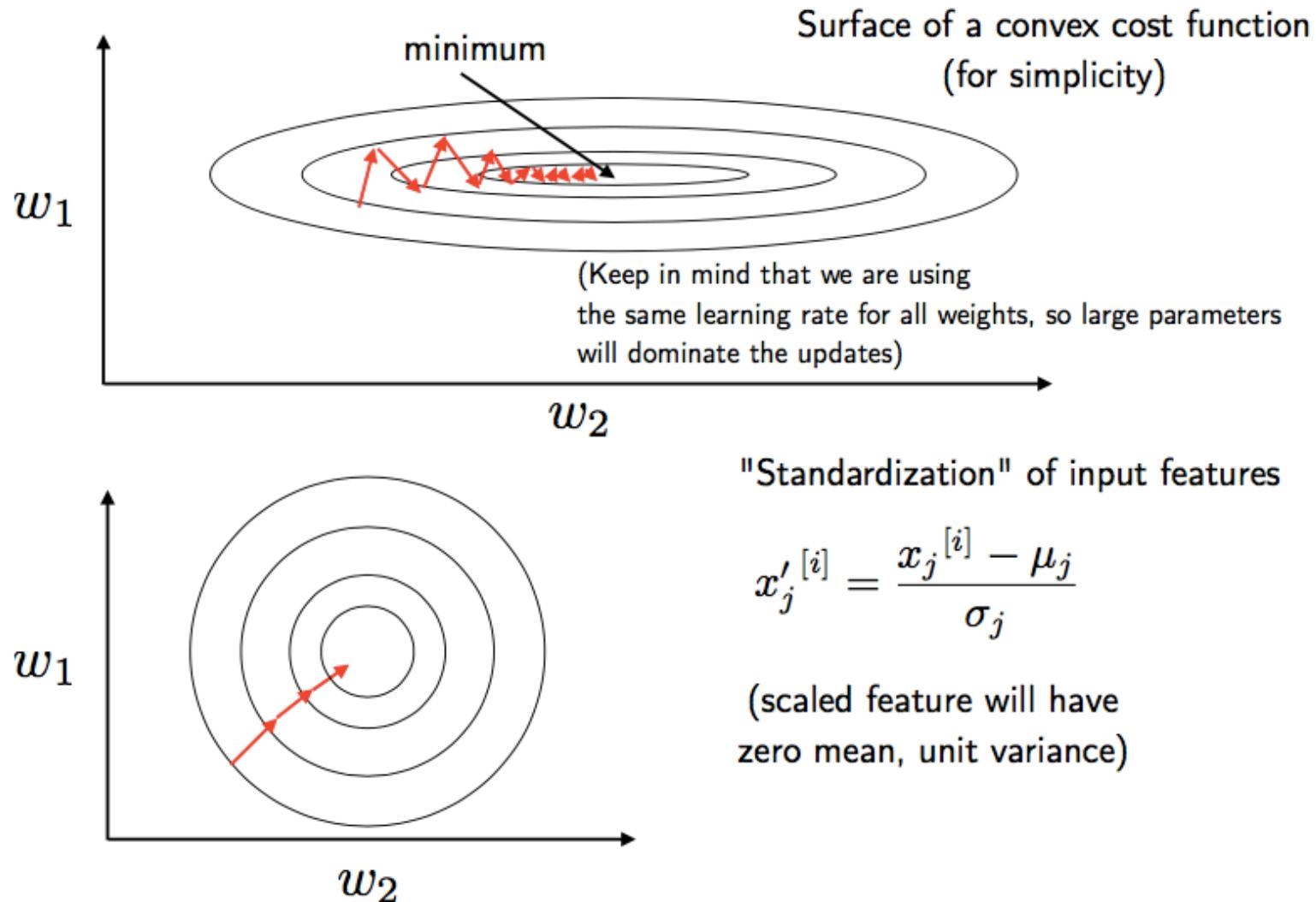


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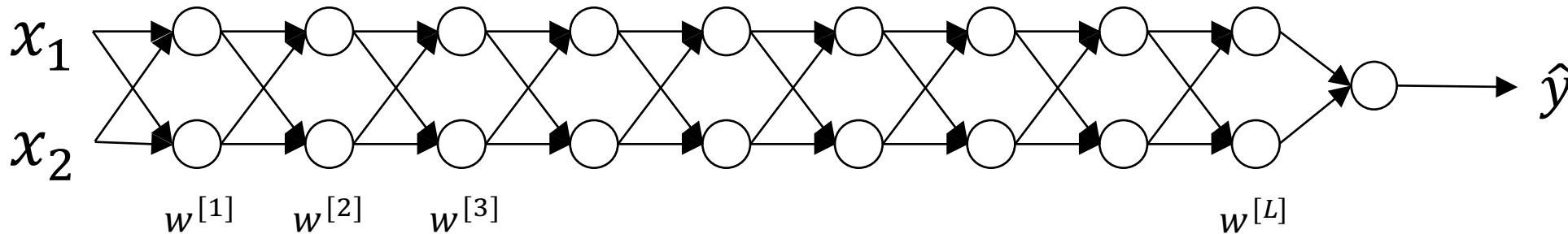
Use same μ, σ^2 to normalize test set

Normalizing Inputs



Vanishing/Exploding Gradients

Vanishing/Exploding Gradient Problems



Assume $g(z) = z$ (identity function), then

$$\hat{y} = w^{[L]}w^{[L-1]}w^{[L-2]} \dots w^{[1]}x$$

for $w^{[l]} > 1$ we will then have a problem of exploding gradients. E.g:

$$\begin{bmatrix} 1.5 \\ 1.5 \end{bmatrix} \Rightarrow 1.5^{L-1}$$

and for $w^{[l]} < 1$ we will then have a problem of vanishing gradients. E.g:

$$\begin{bmatrix} 0.9 \\ 0.9 \end{bmatrix} \Rightarrow 0.9^{L-1}$$

Weight Initialization

- First idea: **Small random numbers**
(gaussian with zero mean and 1e-2 standard deviation)

```
W = 0.01* np.random.randn(D,H)
```

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(gaussian with zero mean and 1e-2 standard deviation)

```
W = 0.01* np.random.randn(D,H)
```

Works ~okay for small networks, but problems with deeper networks.

Lets look at some activation statistics

E.g. 10-layer net with 500 neurons on each layer, using tanh non-linearities, and initializing as described in last slide.

```
# assume some unit gaussian 10-D input data
D = np.random.randn(1000, 500)
hidden_layer_sizes = [500]*10
nonlinearities = ['tanh']*len(hidden_layer_sizes)

act = {'relu':lambda x:np.maximum(0,x), 'tanh':lambda x:np.tanh(x)}
Hs = {}
for i in xrange(len(hidden_layer_sizes)):
    X = D if i == 0 else Hs[i-1] # input at this layer
    fan_in = X.shape[1]
    fan_out = hidden_layer_sizes[i]
    W = np.random.randn(fan_in, fan_out) * 0.01 # layer initialization

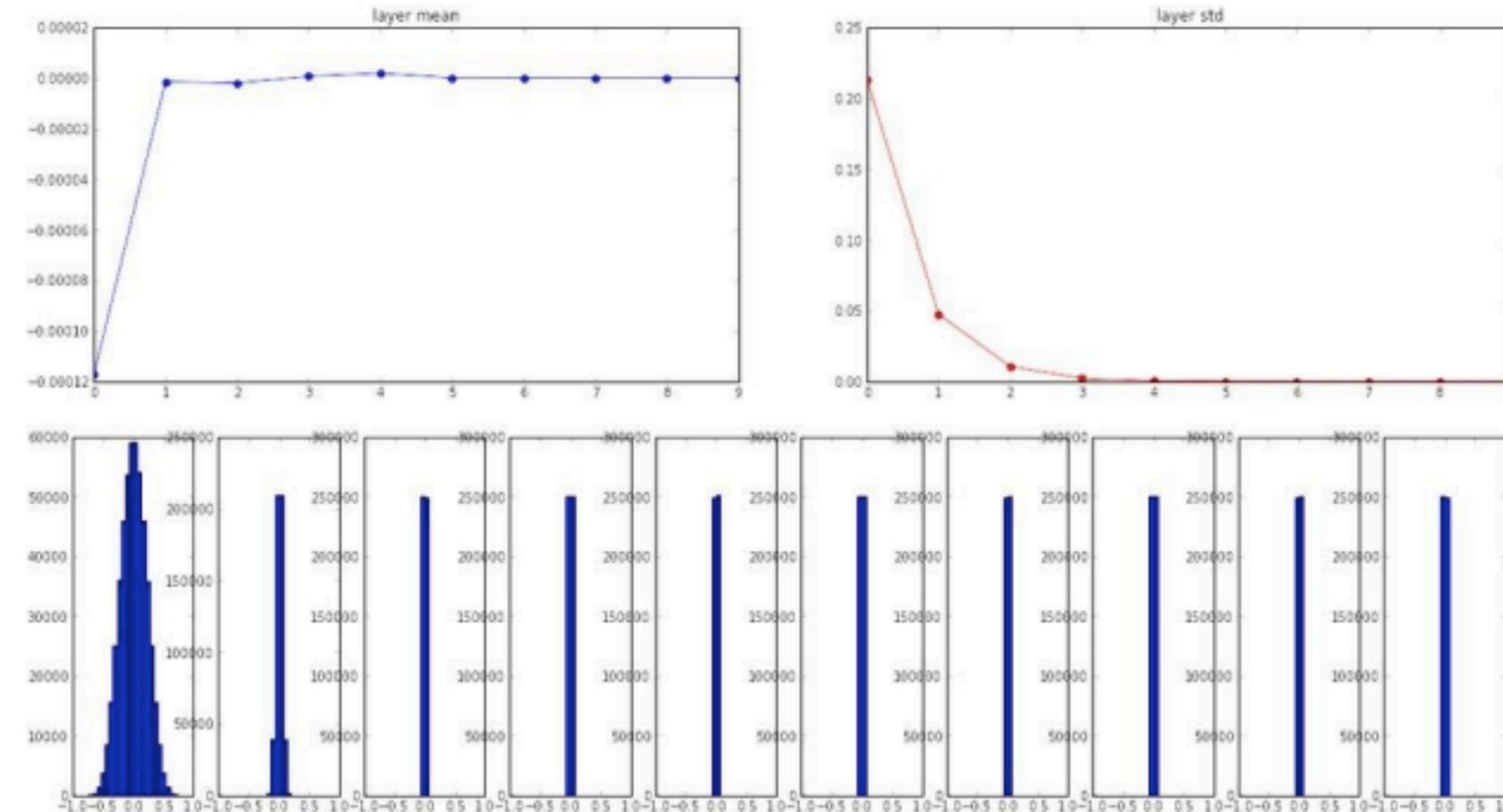
    H = np.dot(X, W) # matrix multiply
    H = act[nonlinearities[i]](H) # nonlinearity
    Hs[i] = H # cache result on this layer

# look at distributions at each layer
print 'input layer had mean %f and std %f' % (np.mean(D), np.std(D))
layer_means = [np.mean(H) for i,H in Hs.iteritems()]
layer_stds = [np.std(H) for i,H in Hs.iteritems()]
for i,H in Hs.iteritems():
    print 'hidden layer %d had mean %f and std %f' % (i+1, layer_means[i], layer_stds[i])

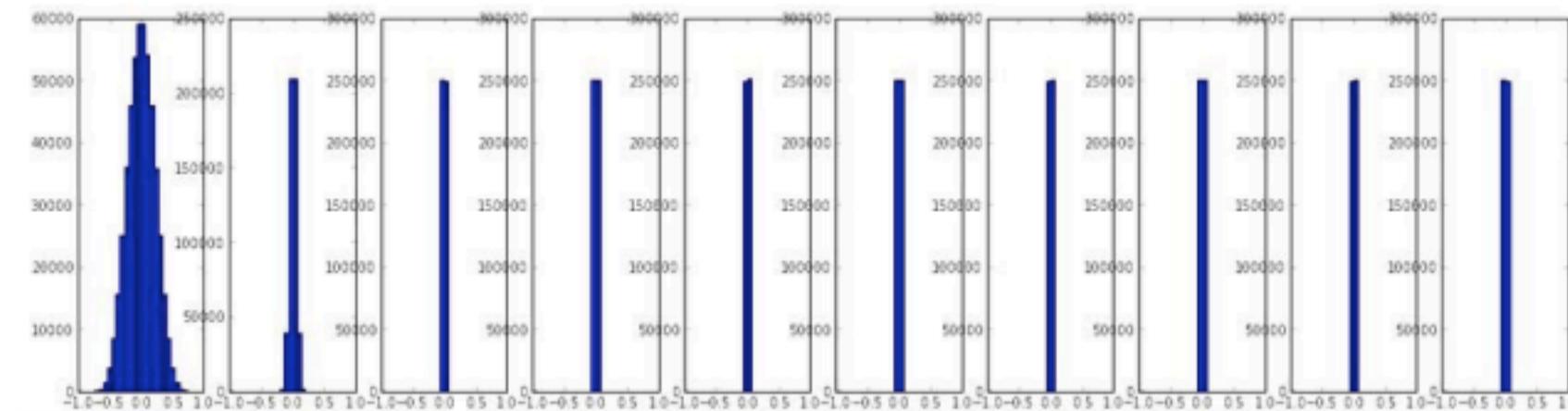
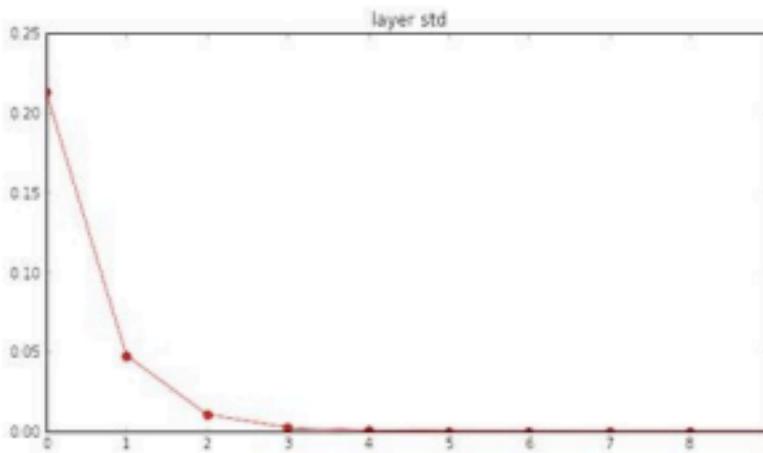
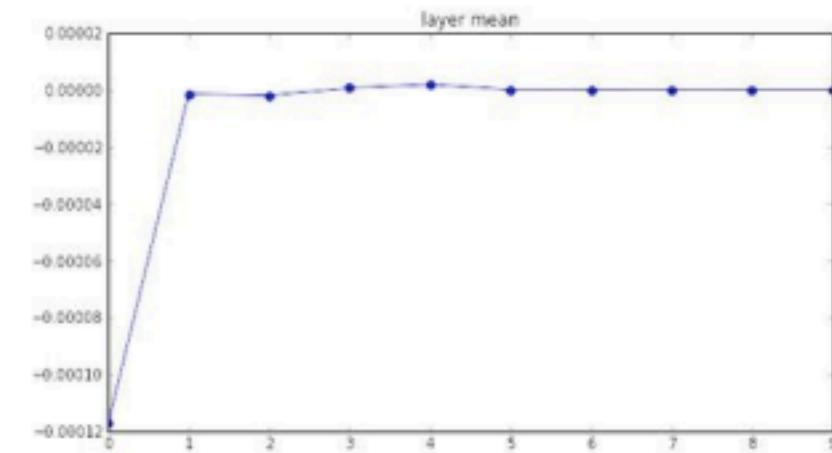
# plot the means and standard deviations
plt.figure()
plt.subplot(121)
plt.plot(Hs.keys(), layer_means, 'ob-')
plt.title('layer mean')
plt.subplot(122)
plt.plot(Hs.keys(), layer_stds, 'or-')
plt.title('layer std')

# plot the raw distributions
plt.figure()
for i,H in Hs.iteritems():
    plt.subplot(1,len(Hs),i+1)
    plt.hist(H.ravel(), 30, range=(-1,1))
```

```
input layer had mean 0.000927 and std 0.998388  
hidden layer 1 had mean -0.000117 and std 0.213081  
hidden layer 2 had mean -0.000001 and std 0.047551  
hidden layer 3 had mean -0.000002 and std 0.010630  
hidden layer 4 had mean 0.000001 and std 0.002378  
hidden layer 5 had mean 0.000002 and std 0.000532  
hidden layer 6 had mean -0.000000 and std 0.000119  
hidden layer 7 had mean 0.000000 and std 0.000026  
hidden layer 8 had mean -0.000000 and std 0.000006  
hidden layer 9 had mean 0.000000 and std 0.000001  
hidden layer 10 had mean -0.000000 and std 0.000000
```



```
input layer had mean 0.000927 and std 0.998388  
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hidden layer 4 had mean 0.000001 and std 0.002378  
hidden layer 5 had mean 0.000002 and std 0.000532  
hidden layer 6 had mean -0.000000 and std 0.000119  
hidden layer 7 had mean 0.000000 and std 0.000026  
hidden layer 8 had mean -0.000000 and std 0.000006  
hidden layer 9 had mean 0.000000 and std 0.000001  
hidden layer 10 had mean -0.000000 and std 0.000000
```



All activations become zero!

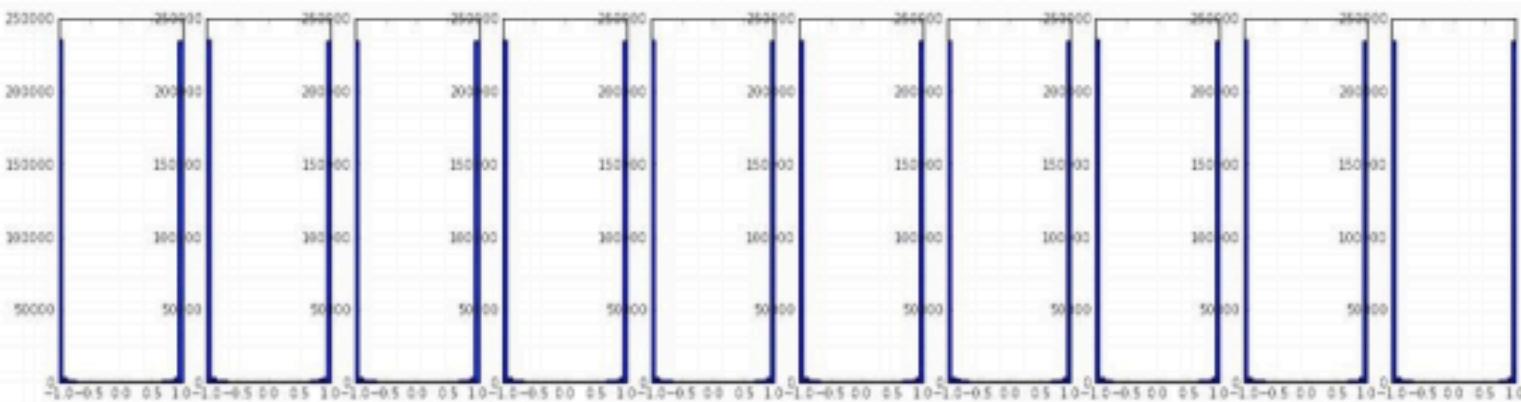
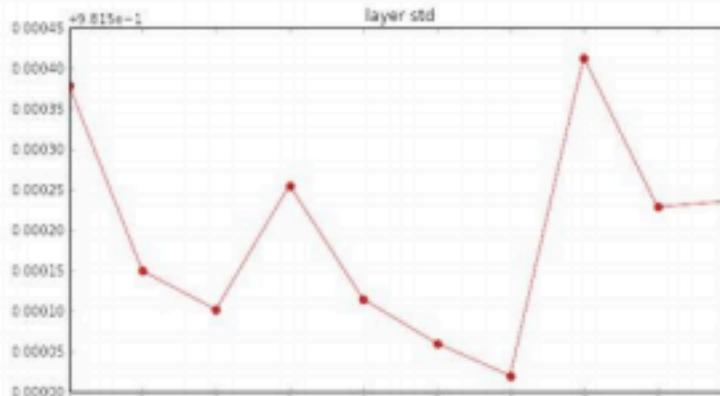
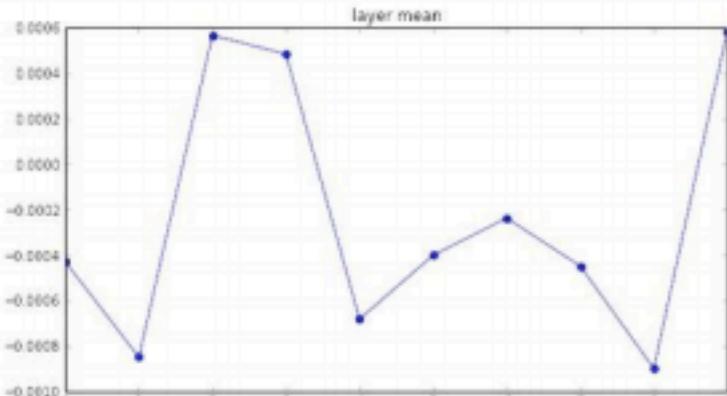
Q: think about the backward pass.
What do the gradients look like?

Hint: think about backward pass for a W^*X gate.

```
W = np.random.randn(fan_in, fan_out) * 1.0 # layer initialization
```

```
input layer had mean 0.001800 and std 1.001311  
hidden layer 1 had mean -0.000430 and std 0.981879  
hidden layer 2 had mean -0.000849 and std 0.981649  
hidden layer 3 had mean 0.000566 and std 0.981601  
hidden layer 4 had mean 0.000483 and std 0.981755  
hidden layer 5 had mean -0.000682 and std 0.981614  
hidden layer 6 had mean -0.000401 and std 0.981560  
hidden layer 7 had mean -0.000237 and std 0.981520  
hidden layer 8 had mean -0.000448 and std 0.981913  
hidden layer 9 had mean -0.000899 and std 0.981728  
hidden layer 10 had mean 0.000584 and std 0.981736
```

*1.0 instead of *0.01



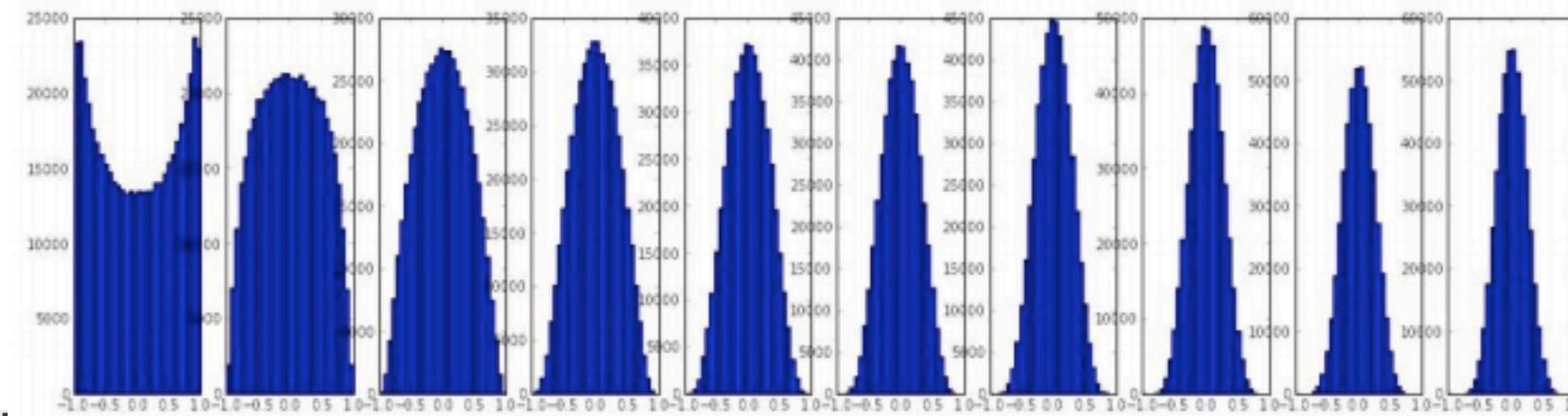
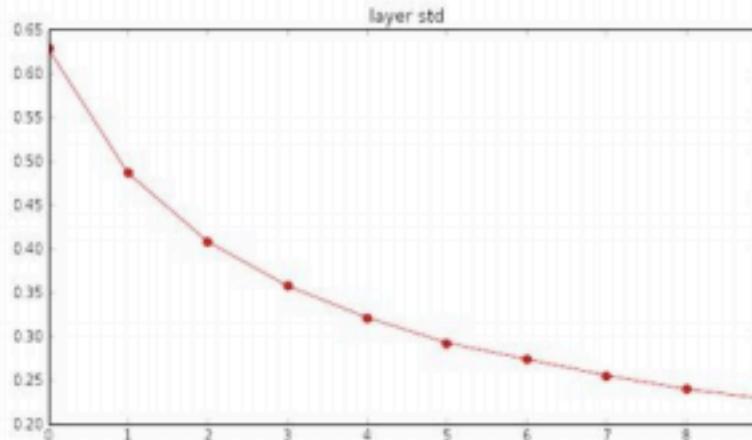
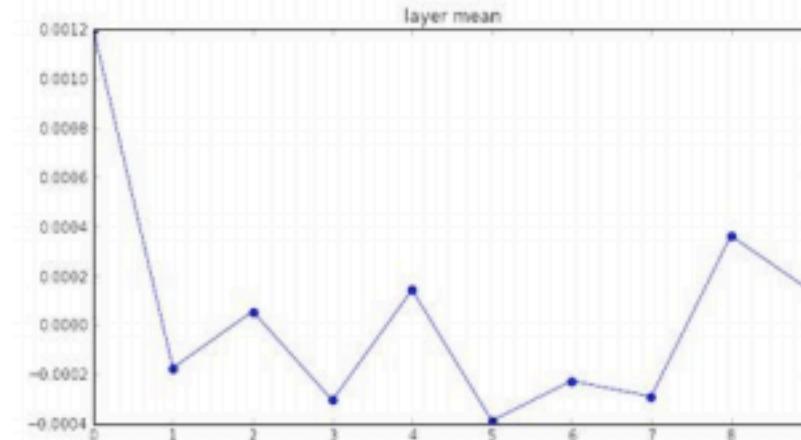
Almost all neurons completely saturated, either -1 and 1. Gradients will be all zero.

```
input layer had mean 0.001800 and std 1.001311  
hidden layer 1 had mean 0.001198 and std 0.627953  
hidden layer 2 had mean -0.000175 and std 0.486051  
hidden layer 3 had mean 0.000055 and std 0.407723  
hidden layer 4 had mean -0.000306 and std 0.357108  
hidden layer 5 had mean 0.000142 and std 0.320917  
hidden layer 6 had mean -0.000389 and std 0.292116  
hidden layer 7 had mean -0.000228 and std 0.273387  
hidden layer 8 had mean -0.000291 and std 0.254935  
hidden layer 9 had mean 0.000361 and std 0.239266  
hidden layer 10 had mean 0.000139 and std 0.228008
```

```
W = np.random.randn(fan_in, fan_out) / np.sqrt(fan_in) # layer initialization
```

“Xavier initialization”
[Glorot et al., 2010]

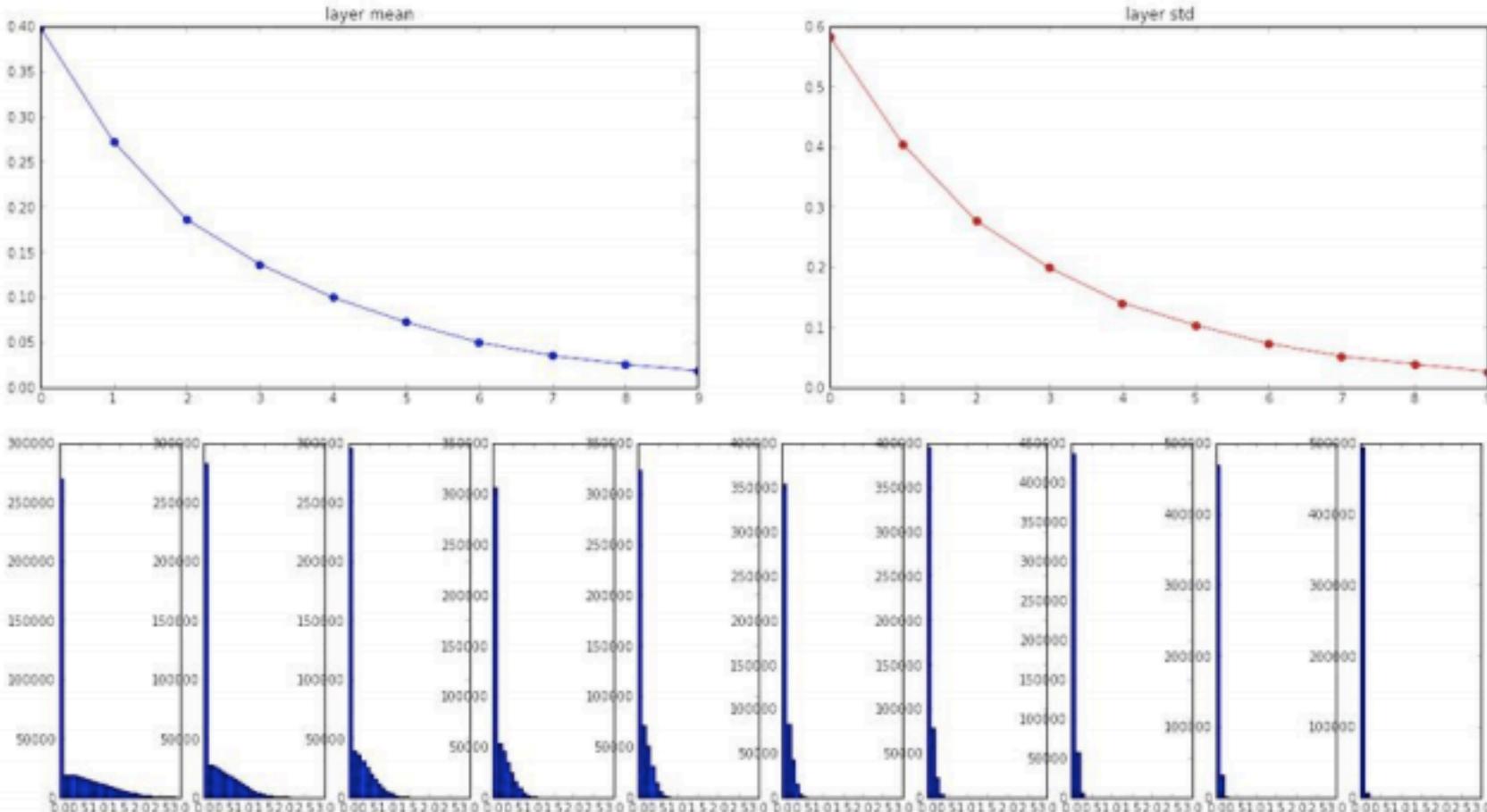
Reasonable initialization.
(Mathematical derivation
assumes linear activations)



```
input layer had mean 0.000501 and std 0.999444  
hidden layer 1 had mean 0.398623 and std 0.582273  
hidden layer 2 had mean 0.272352 and std 0.403795  
hidden layer 3 had mean 0.186076 and std 0.276912  
hidden layer 4 had mean 0.136442 and std 0.198685  
hidden layer 5 had mean 0.099568 and std 0.140299  
hidden layer 6 had mean 0.072234 and std 0.103280  
hidden layer 7 had mean 0.049775 and std 0.072748  
hidden layer 8 had mean 0.035138 and std 0.051572  
hidden layer 9 had mean 0.025404 and std 0.038583  
hidden layer 10 had mean 0.018408 and std 0.026076
```

```
W = np.random.randn(fan_in, fan_out) / np.sqrt(fan_in) # layer initialization
```

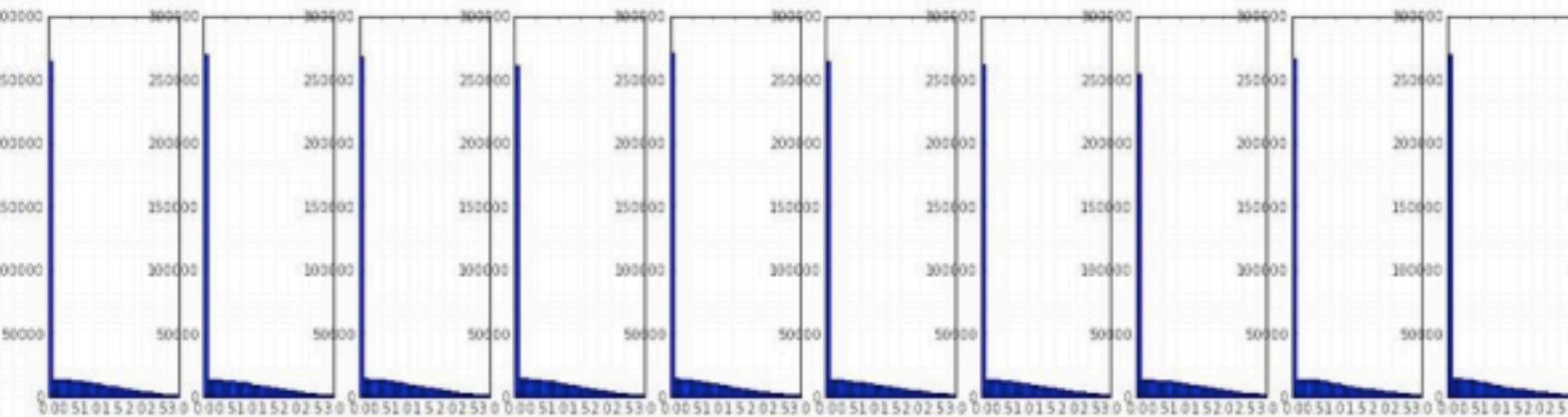
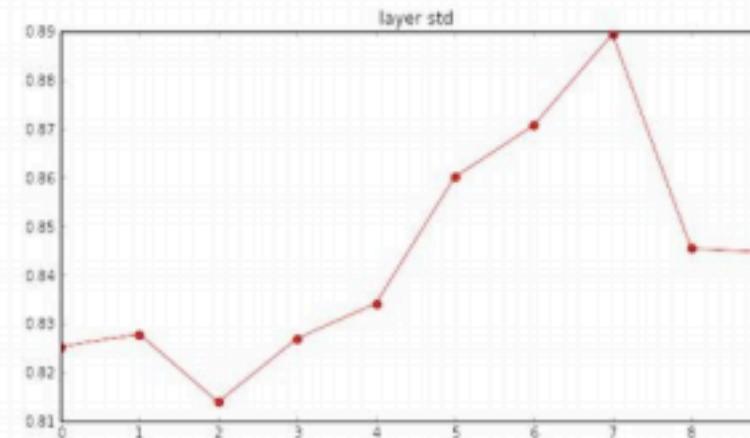
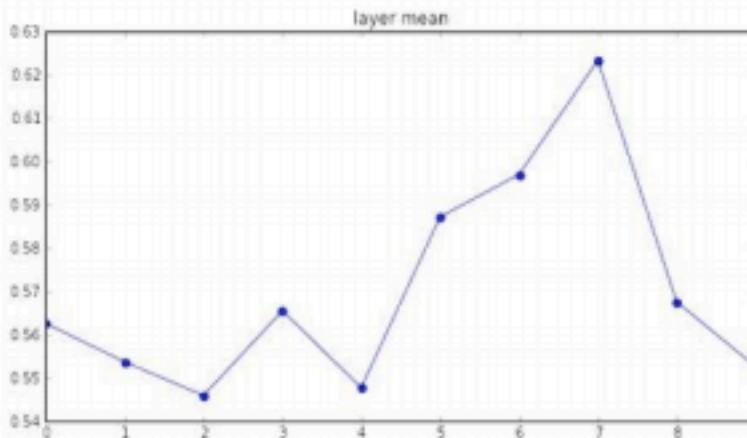
but when using the ReLU nonlinearity it breaks.



```
input layer had mean 0.000501 and std 0.999444  
hidden layer 1 had mean 0.562488 and std 0.825232  
hidden layer 2 had mean 0.553614 and std 0.827835  
hidden layer 3 had mean 0.545867 and std 0.813855  
hidden layer 4 had mean 0.565396 and std 0.826902  
hidden layer 5 had mean 0.547678 and std 0.834092  
hidden layer 6 had mean 0.587103 and std 0.860035  
hidden layer 7 had mean 0.596867 and std 0.870610  
hidden layer 8 had mean 0.623214 and std 0.889348  
hidden layer 9 had mean 0.567498 and std 0.845357  
hidden layer 10 had mean 0.552531 and std 0.844523
```

```
W = np.random.randn(fan_in, fan_out) / np.sqrt(2/fan_in) # layer initialization
```

He et al., 2015
(note additional 2/)



```

input layer had mean 0.000501 and std 0.999444
hidden layer 1 had mean 0.562488 and std 0.825232
hidden layer 2 had mean 0.553614 and std 0.827835
hidden layer 3 had mean 0.545867 and std 0.813855
hidden layer 4 had mean 0.565396 and std 0.826902
hidden layer 5 had mean 0.547678 and std 0.834092
hidden layer 6 had mean 0.587103 and std 0.860035
hidden layer 7 had mean 0.596867 and std 0.870610
hidden layer 8 had mean 0.623214 and std 0.889348
hidden layer 9 had mean 0.567498 and std 0.845357
hidden layer 10 had mean 0.552531 and std 0.844523

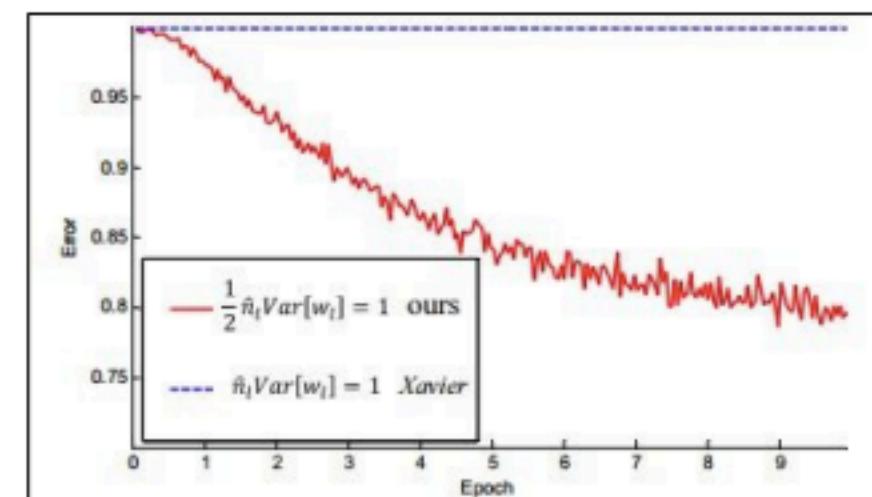
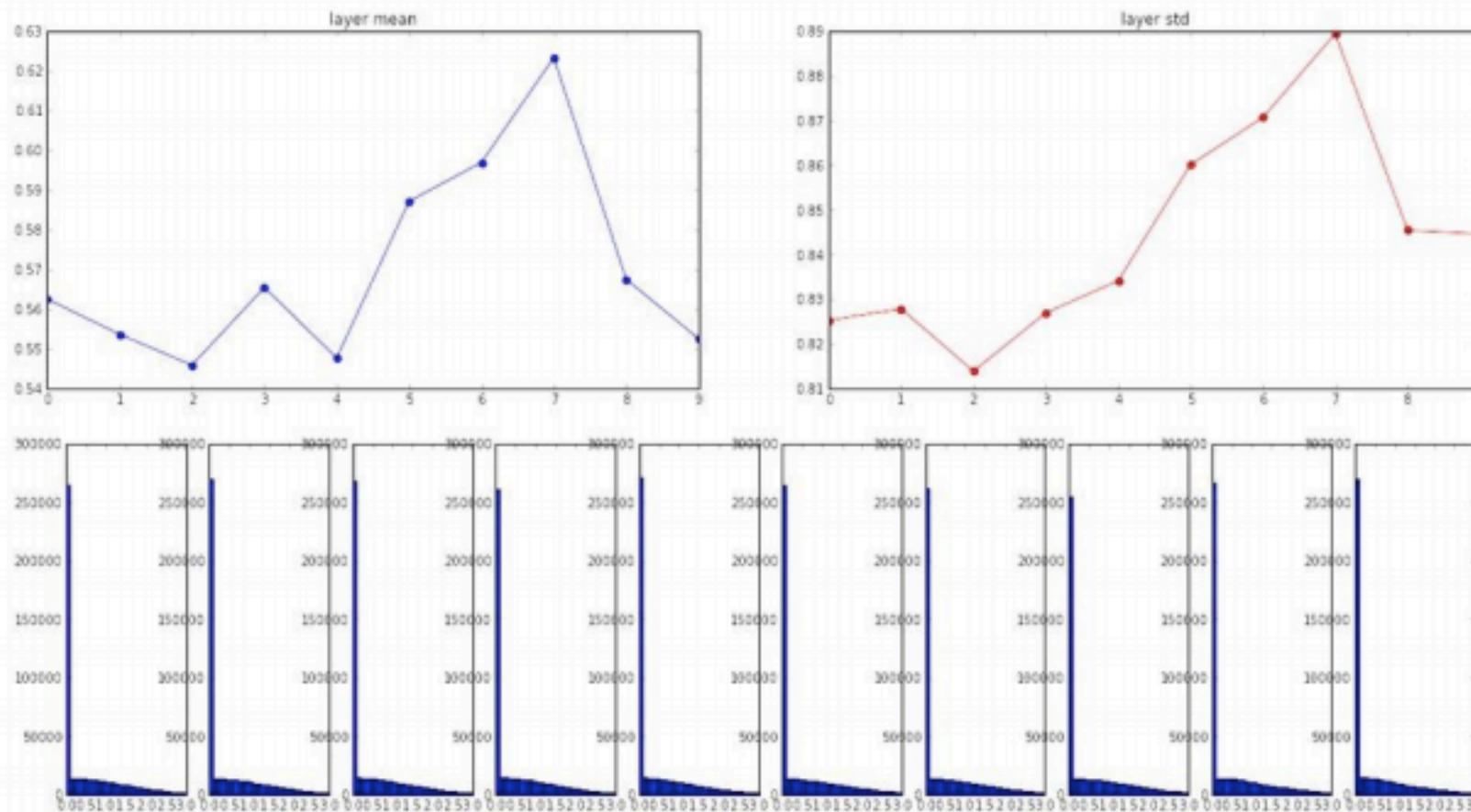
```

```

W = np.random.randn(fan_in, fan_out) / np.sqrt(2/fan_in) # layer initialization

```

He et al., 2015
(note additional 2/)



Custom Weight Initialization in PyTorch

```
class MLP(torch.nn.Module):

    def __init__(self, num_features, num_hidden, num_classes):
        super(MLP, self).__init__()

        self.num_classes = num_classes

        ### 1st hidden layer
        self.linear_1 = torch.nn.Linear(num_features, num_hidden)
        self.linear_1.weight.detach().normal_(0.0, 0.1)
        self.linear_1.bias.detach().zero_()

        ### Output layer
        self.linear_out = torch.nn.Linear(num_hidden, num_classes)
        self.linear_out.weight.detach().normal_(0.0, 0.1)
        self.linear_out.bias.detach().zero_()

    def forward(self, x):
        out = self.linear_1(x)
        out = torch.sigmoid(out)
        logits = self.linear_out(out)
        probas = torch.sigmoid(logits)
        return logits, probas
```

Note that if BatchNorm is used,
initial feature weight choice is less important anyway

Batch Normalization

Batch Normalization

- Normalization of inputs for hidden layers
- Helps with exploding/vanishing gradient problems
- Can increase training stability and convergence rate
- Can be understood as additional normalization layers (with additional parameters)

BatchNorm Step 1: Normalize Net Inputs

$$\mu_j = \frac{1}{n} \sum_i z_j^{[i]}$$

$$\sigma_j^2 = \frac{1}{n} \sum_i (z_j^{[i]} - \mu_j)^2$$

$$z'_j^{[i]} = \frac{z_j^{[i]} - \mu_j}{\sigma_j}$$

In practice:

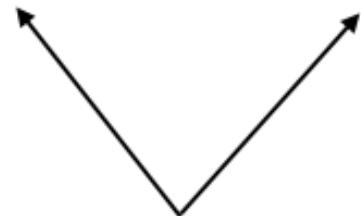
$$z'_j^{[i]} = \frac{z_j^{[i]} - \mu_j}{\sqrt{\sigma_j^2 + \epsilon}}$$

For numerical stability, where epsilon
is a small number like 1E-5

BatchNorm Step 2: Pre-Activation Scaling

$$z'_j^{[i]} = \frac{z_j^{[i]} - \mu_j}{\sqrt{\sigma_j^2 + \epsilon}}$$

$$a'_j^{[i]} = \gamma_j \cdot z'_j^{[i]} + \beta_j$$



These are learnable parameters

BatchNorm Step 2: Pre-Activation Scaling

$$z'_j^{[i]} = \frac{z_j^{[i]} - \mu_j}{\sigma_j}$$

$$a'_j^{[i]} = \gamma_j \cdot z'_j^{[i]} + \beta_j$$

Controls the spread or scale

Controls the mean

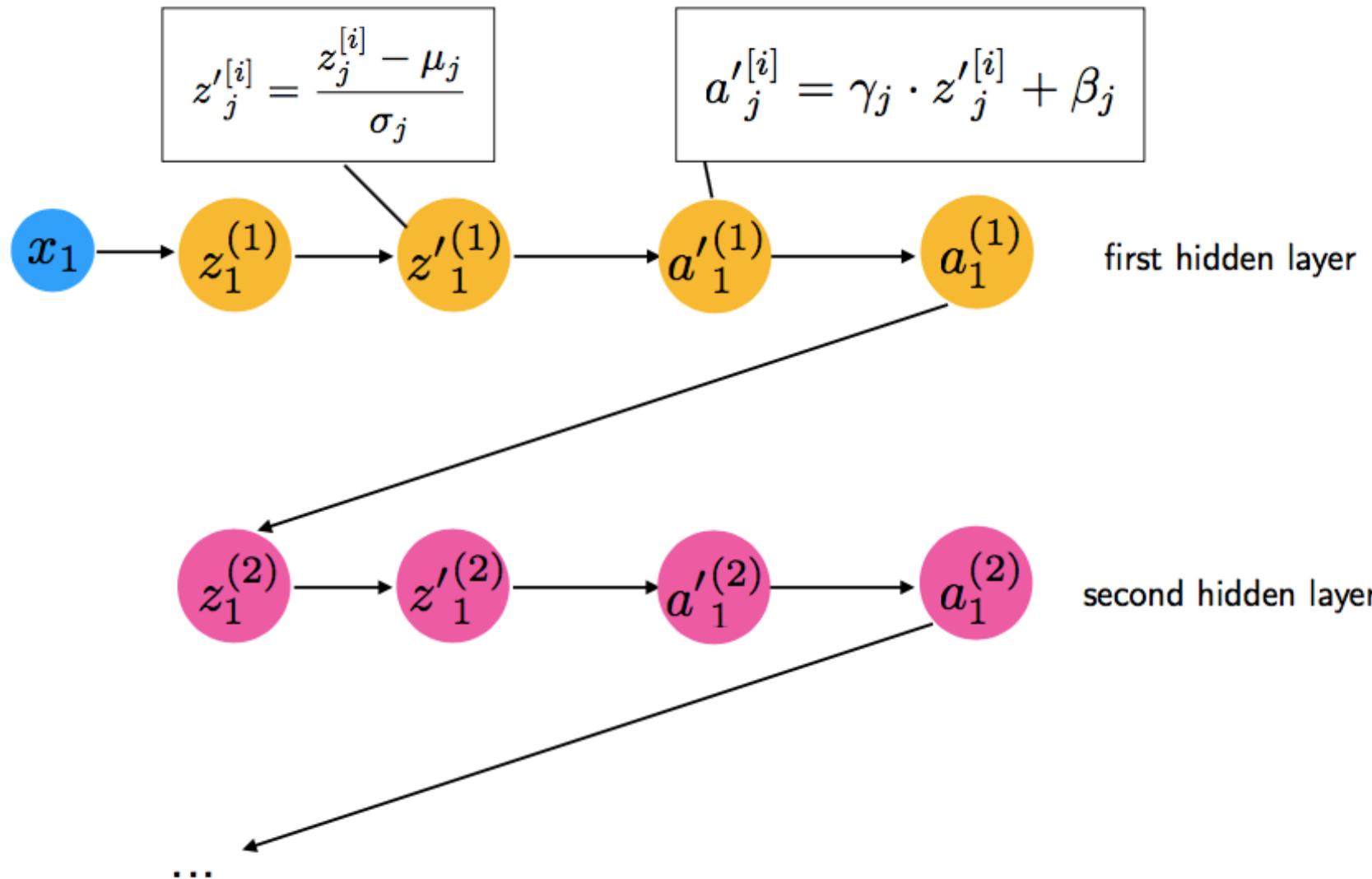
Note, the network can learn:

$$\gamma^{(k)} = \sqrt{\text{Var}[x^{(k)}]}$$

$$\beta^{(k)} = \text{E}[x^{(k)}]$$

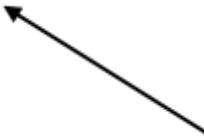
to recover the identity mapping.

BatchNorm Step 1&2 Summary



Working with Mini-Batches

$$a_j^{[i]} = \gamma_j \cdot z_j^{[i]} + \beta_j$$



This parameter makes the bias units redundant

Also, note that the batchnorm parameters are vectors with the same number of elements as the bias vector

BatchNorm in PyTorch

```
class MultilayerPerceptron(torch.nn.Module):

    def __init__(self, num_features, num_classes):
        super(MultilayerPerceptron, self).__init__()

        ### 1st hidden layer
        self.linear_1 = torch.nn.Linear(num_features, num_hidden_1)
        self.linear_1_bn = torch.nn.BatchNorm1d(num_hidden_1)

        ### 2nd hidden layer
        self.linear_2 = torch.nn.Linear(num_hidden_1, num_hidden_2)
        self.linear_2_bn = torch.nn.BatchNorm1d(num_hidden_2)

        ### Output layer
        self.linear_out = torch.nn.Linear(num_hidden_2, num_classes)

    def forward(self, x):
        out = self.linear_1(x)
        # note that batchnorm is in the classic
        # sense placed before the activation
        out = self.linear_1_bn(out)
        out = F.relu(out)

        out = self.linear_2(out)
        out = self.linear_2_bn(out)
        out = F.relu(out)

        logits = self.linear_out(out)
        probas = F.softmax(logits, dim=1)
        return logits, probas
```

BatchNorm in PyTorch

```
class MultilayerPerceptron(torch.nn.Module):

    def __init__(self, num_features, num_classes):
        super(MultilayerPerceptron, self).__init__()

        ### 1st hidden layer
        self.linear_1 = torch.nn.Linear(num_features, num_hidden_1)
        self.linear_1_bn = torch.nn.BatchNorm1d(num_hidden_1)

        ### 2nd hidden layer
        self.linear_2 = torch.nn.Linear(num_hidden_1, num_hidden_2)
        self.linear_2_bn = torch.nn.BatchNorm1d(num_hidden_2)

        ### Output layer
        self.linear_out = torch.nn.Linear(num_hidden_2, num_classes)

    def forward(self, x):
        out = self.linear_1(x)
        # note that batchnorm is in the classic
        # sense placed before the activation
        out = self.linear_1_bn(out)
        out = F.relu(out)

        out = self.linear_2(out)
        out = self.linear_2_bn(out)
        out = F.relu(out)

        logits = self.linear_out(out)
        probas = F.softmax(logits, dim=1)
        return logits, probas
```

don't forget `model.train()`
and `model.eval()`
in training and test loops

BatchNorm During Prediction (“Inference”)

Use exponentially weighted average (moving average) of mean and variance

```
running_mean = momentum * running_mean  
              + (1 - momentum) * sample_mean
```

(where momentum is typically ~0.1; and same for variance)

Alternatively, can also use global training set mean and variance

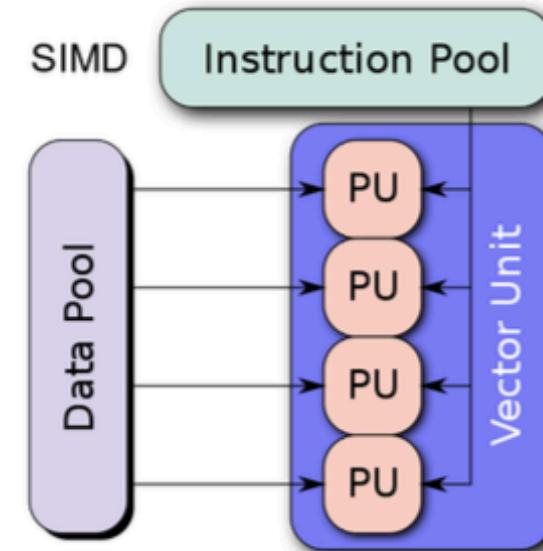
Why Minibatch Sizes as Powers of 2?

Related to SIMD - Single Instruction Multiple Data - paradigm used by CPUs/GPUs

Comes from mapping the computations (e.g., dot products) to physical processing cores on the GPU, where the number of processing cores is usually a power of 2

E.g., if we have 48 columns in a matrix, we can map 3 dot products to each processing core if we have 16 processing cores (GPUs usually have many, many more processing cores)

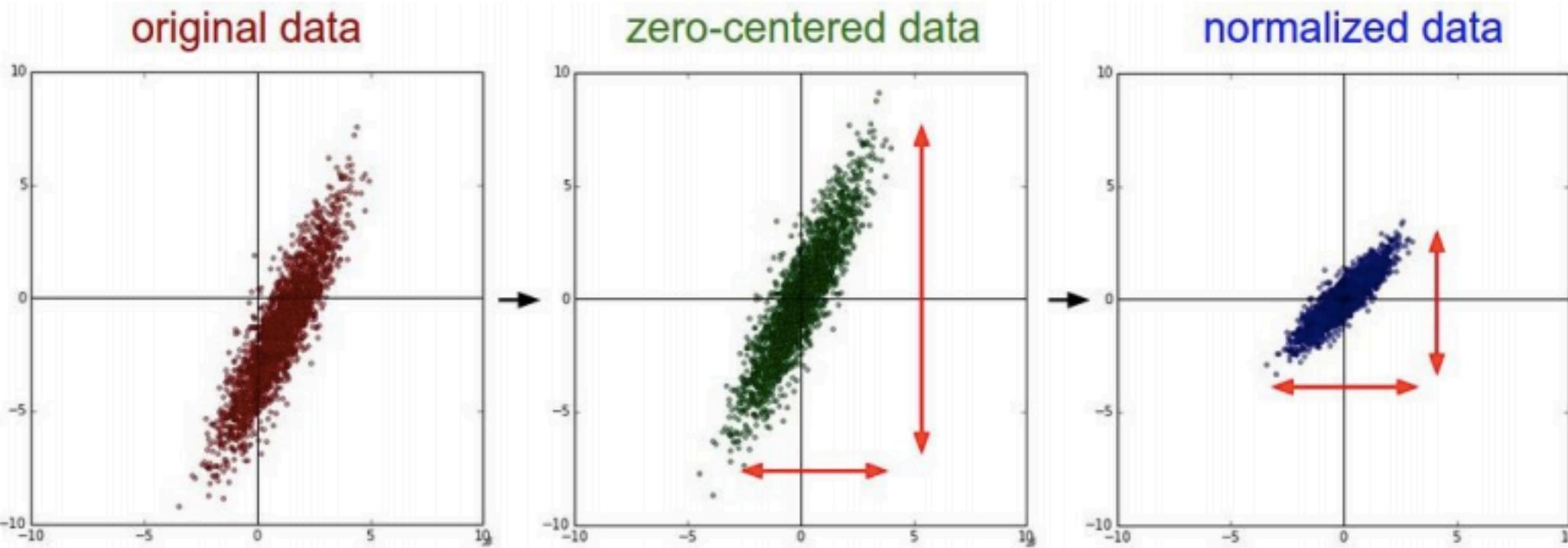
(It might be one of the archaic DL conventions/traditions, and I don't think this matters much anymore for modern frameworks)



Source: <https://upload.wikimedia.org/wikipedia/commons/thumb/c/ce/SIMD2.svg/440px-SIMD2.svg.png>

Babysitting the Learning Process

Step 1: Preprocess the data

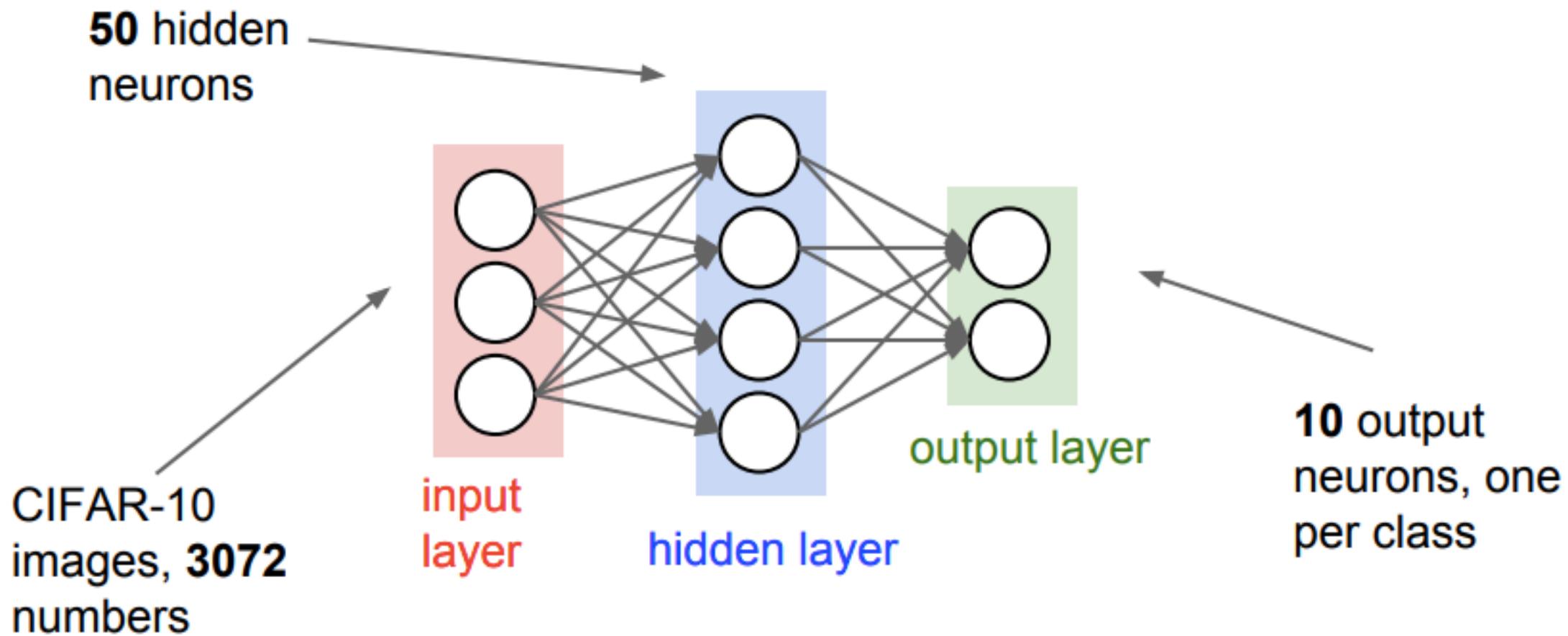


```
X -= np.mean(X, axis = 0)
```

```
X /= np.std(X, axis = 0)
```

(Assume $X [NxD]$ is data matrix,
each example in a row)

Step 2: Choose the architecture: say we start with one hidden layer of 50 neurons:



Double check that the loss is reasonable:

```
def init_two_layer_model(input_size, hidden_size, output_size):
    # initialize a model
    model = {}
    model['W1'] = 0.0001 * np.random.randn(input_size, hidden_size)
    model['b1'] = np.zeros(hidden_size)
    model['W2'] = 0.0001 * np.random.randn(hidden_size, output_size)
    model['b2'] = np.zeros(output_size)
    return model
```

```
model = init_two_layer_model(32*32*3, 50, 10) # input size, hidden size, number of classes
loss, grad = two_layer_net(X_train, model, y_train, 0.0) disable regularization
print loss
```

2.30261216167

loss ~2.3.
“correct” for
10 classes

returns the loss and the
gradient for all parameters

Double check that the loss is reasonable:

```
def init_two_layer_model(input_size, hidden_size, output_size):
    # initialize a model
    model = {}
    model['W1'] = 0.0001 * np.random.randn(input_size, hidden_size)
    model['b1'] = np.zeros(hidden_size)
    model['W2'] = 0.0001 * np.random.randn(hidden_size, output_size)
    model['b2'] = np.zeros(output_size)
    return model
```

```
model = init_two_layer_model(32*32*3, 50, 10) # input size, hidden size, number of classes
loss, grad = two_layer_net(X_train, model, y_train, 1e3)      crank up regularization
print loss
```

3.06859716482

loss went up, good. (sanity check)

Lets try to train now...

Tip: Make sure that you can overfit very small portion of the training data

```
model = init_two_layer_model(32*32*3, 50, 10) # input size, hidden size, number of classes
trainer = ClassifierTrainer()
X_tiny = X_train[:20] # take 20 examples
y_tiny = y_train[:20]
best_model, stats = trainer.train(X_tiny, y_tiny, X_tiny, y_tiny,
                                  model, two_layer_net,
                                  num_epochs=200, reg=0.0,
                                  update='sgd', learning_rate_decay=1,
                                  sample_batches = False,
                                  learning_rate=1e-3, verbose=True)
```

The above code:

- take the first 20 examples from CIFAR-10
- turn off regularization ($\text{reg} = 0.0$)
- use simple vanilla 'sgd'

Lets try to train now...

Tip: Make sure that you can overfit very small portion of the training data

Very small loss,
train accuracy 1.00,
nice!

```

model = init_two_layer_model(32*32*3, 50, 10) # input size, hidden size, number of classes
trainer = ClassifierTrainer()
X_tiny = X_train[:20] # take 20 examples
y_tiny = y_train[:20]
best_model, stats = trainer.train(X_tiny, y_tiny, X_tiny, y_tiny,
                                  model, two_layer_net,
                                  num_epochs=200, reg=0.0,
                                  update='sgd', learning_rate_decay=1,
                                  sample_batches = False,
                                  learning_rate=1e-3, verbose=True)

Finished epoch 1 / 200: cost 2.302603, train: 0.400000, val 0.400000, lr 1.000000e-03
Finished epoch 2 / 200: cost 2.302258, train: 0.450000, val 0.450000, lr 1.000000e-03
Finished epoch 3 / 200: cost 2.301849, train: 0.600000, val 0.600000, lr 1.000000e-03
Finished epoch 4 / 200: cost 2.301196, train: 0.650000, val 0.650000, lr 1.000000e-03
Finished epoch 5 / 200: cost 2.300044, train: 0.650000, val 0.650000, lr 1.000000e-03
Finished epoch 6 / 200: cost 2.297864, train: 0.550000, val 0.550000, lr 1.000000e-03
Finished epoch 7 / 200: cost 2.293595, train: 0.600000, val 0.600000, lr 1.000000e-03
Finished epoch 8 / 200: cost 2.285096, train: 0.550000, val 0.550000, lr 1.000000e-03
Finished epoch 9 / 200: cost 2.268094, train: 0.550000, val 0.550000, lr 1.000000e-03
Finished epoch 10 / 200: cost 2.234787, train: 0.500000, val 0.500000, lr 1.000000e-03
Finished epoch 11 / 200: cost 2.173187, train: 0.500000, val 0.500000, lr 1.000000e-03
Finished epoch 12 / 200: cost 2.076862, train: 0.500000, val 0.500000, lr 1.000000e-03
Finished epoch 13 / 200: cost 1.974090, train: 0.400000, val 0.400000, lr 1.000000e-03
Finished epoch 14 / 200: cost 1.895885, train: 0.400000, val 0.400000, lr 1.000000e-03
Finished epoch 15 / 200: cost 1.820876, train: 0.450000, val 0.450000, lr 1.000000e-03
Finished epoch 16 / 200: cost 1.737430, train: 0.450000, val 0.450000, lr 1.000000e-03
Finished epoch 17 / 200: cost 1.642356, train: 0.500000, val 0.500000, lr 1.000000e-03
Finished epoch 18 / 200: cost 1.535239, train: 0.600000, val 0.600000, lr 1.000000e-03
Finished epoch 19 / 200: cost 1.421527, train: 0.600000, val 0.600000, lr 1.000000e-03
Finished epoch 20 / 200: cost 1.307500, train: 0.550000, val 0.550000, lr 1.000000e-03
Finished epoch 195 / 200: cost 0.002694, train: 1.000000, val 1.000000, lr 1.000000e-03
Finished epoch 196 / 200: cost 0.002674, train: 1.000000, val 1.000000, lr 1.000000e-03
Finished epoch 197 / 200: cost 0.002655, train: 1.000000, val 1.000000, lr 1.000000e-03
Finished epoch 198 / 200: cost 0.002635, train: 1.000000, val 1.000000, lr 1.000000e-03
Finished epoch 199 / 200: cost 0.002617, train: 1.000000, val 1.000000, lr 1.000000e-03
Finished epoch 200 / 200: cost 0.002597, train: 1.000000, val 1.000000, lr 1.000000e-03
finished optimization. best validation accuracy: 1.000000

```



Lets try to train now...

Start with small regularization and find learning rate that makes the loss go down.

```
model = init_two_layer_model(32*32*3, 50, 10) # input size, hidden size, number of classes
trainer = ClassifierTrainer()
best_model, stats = trainer.train(X_train, y_train, X_val, y_val,
                                  model, two_layer_net,
                                  num_epochs=10, reg=0.000001,
                                  update='sgd', learning_rate_decay=1,
                                  sample_batches = True,
                                  learning_rate=1e-6, verbose=True)
```

Lets try to train now...

Start with small regularization and find learning rate that makes the loss go down.

```
model = init_two_layer_model(32*32*3, 50, 10) # input size, hidden size, number of classes
trainer = ClassifierTrainer()
best_model, stats = trainer.train(X_train, y_train, X_val, y_val,
                                  model, two_layer_net,
                                  num_epochs=10, reg=0.000001,
                                  update='sgd', learning_rate_decay=1,
                                  sample_batches=True,
                                  learning_rate=1e-6, verbose=True)
```

```
Finished epoch 1 / 10: cost 2.302576, train: 0.080000, val 0.103000, lr 1.000000e-06
Finished epoch 2 / 10: cost 2.302582, train: 0.121000, val 0.124000, lr 1.000000e-06
Finished epoch 3 / 10: cost 2.302558, train: 0.119000, val 0.138000, lr 1.000000e-06
Finished epoch 4 / 10: cost 2.302519, train: 0.127000, val 0.151000, lr 1.000000e-06
Finished epoch 5 / 10: cost 2.302517, train: 0.158000, val 0.171000, lr 1.000000e-06
Finished epoch 6 / 10: cost 2.302518, train: 0.179000, val 0.172000, lr 1.000000e-06
Finished epoch 7 / 10: cost 2.302466, train: 0.180000, val 0.176000, lr 1.000000e-06
Finished epoch 8 / 10: cost 2.302452, train: 0.175000, val 0.185000, lr 1.000000e-06
Finished epoch 9 / 10: cost 2.302459, train: 0.206000, val 0.192000, lr 1.000000e-06
Finished epoch 10 / 10: cost 2.302420, train: 0.190000, val 0.192000, lr 1.000000e-06
finished optimization. best validation accuracy: 0.192000
```

Loss barely changing

Lets try to train now...

Start with small regularization and find learning rate that makes the loss go down.

loss not going down:
learning rate too low

```
model = init_two_layer_model(32*32*3, 50, 10) # input size, hidden size, number of classes
trainer = ClassifierTrainer()
best_model, stats = trainer.train(X_train, y_train, X_val, y_val,
                                  model, two_layer_net,
                                  num_epochs=10, reg=0.000001,
                                  update='sgd', learning_rate_decay=1,
                                  sample_batches=True,
                                  learning_rate=1e-6, verbose=True)
```

```
Finished epoch 1 / 10: cost 2.302576, train: 0.080000, val 0.103000, lr 1.000000e-06
Finished epoch 2 / 10: cost 2.302582, train: 0.121000, val 0.124000, lr 1.000000e-06
Finished epoch 3 / 10: cost 2.302558, train: 0.119000, val 0.138000, lr 1.000000e-06
Finished epoch 4 / 10: cost 2.302519, train: 0.127000, val 0.151000, lr 1.000000e-06
Finished epoch 5 / 10: cost 2.302517, train: 0.158000, val 0.171000, lr 1.000000e-06
Finished epoch 6 / 10: cost 2.302518, train: 0.179000, val 0.172000, lr 1.000000e-06
Finished epoch 7 / 10: cost 2.302466, train: 0.180000, val 0.176000, lr 1.000000e-06
Finished epoch 8 / 10: cost 2.302452, train: 0.175000, val 0.185000, lr 1.000000e-06
Finished epoch 9 / 10: cost 2.302459, train: 0.206000, val 0.192000, lr 1.000000e-06
Finished epoch 10 / 10: cost 2.302420, train: 0.190000, val 0.192000, lr 1.000000e-06
finished optimization. best validation accuracy: 0.192000
```

Loss barely changing: Learning rate is probably too low

Lets try to train now...

Start with small regularization and find learning rate that makes the loss go down.

loss not going down:
learning rate too low

```
model = init_two_layer_model(32*32*3, 50, 10) # input size, hidden size, number of classes
trainer = ClassifierTrainer()
best_model, stats = trainer.train(X_train, y_train, X_val, y_val,
                                  model, two_layer_net,
                                  num_epochs=10, reg=0.000001,
                                  update='sgd', learning_rate_decay=1,
                                  sample_batches = True,
                                  learning_rate=1e-6, verbose=True)
```

```
Finished epoch 1 / 10: cost 2.302576, train: 0.080000, val 0.103000, lr 1.000000e-06
Finished epoch 2 / 10: cost 2.302582, train: 0.121000, val 0.124000, lr 1.000000e-06
Finished epoch 3 / 10: cost 2.302558, train: 0.119000, val 0.138000, lr 1.000000e-06
Finished epoch 4 / 10: cost 2.302519, train: 0.127000, val 0.151000, lr 1.000000e-06
Finished epoch 5 / 10: cost 2.302517, train: 0.158000, val 0.171000, lr 1.000000e-06
Finished epoch 6 / 10: cost 2.302518, train: 0.179000, val 0.172000, lr 1.000000e-06
Finished epoch 7 / 10: cost 2.302466, train: 0.180000, val 0.176000, lr 1.000000e-06
Finished epoch 8 / 10: cost 2.302452, train: 0.175000, val 0.185000, lr 1.000000e-06
Finished epoch 9 / 10: cost 2.302459, train: 0.206000, val 0.192000, lr 1.000000e-06
Finished epoch 10 / 10: cost 2.302420, train: 0.190000, val 0.192000, lr 1.000000e-06
finished optimization. best validation accuracy: 0.192000
```

Loss barely changing: Learning rate is probably too low

Notice train/val accuracy goes to 20% though, what's up with that? (remember this is softmax)

Lets try to train now...

Start with small regularization and find learning rate that makes the loss go down.

loss not going down:
learning rate too low

```
model = init_two_layer_model(32*32*3, 50, 10) # input size, hidden size, number of classes
trainer = ClassifierTrainer()
best_model, stats = trainer.train(X_train, y_train, X_val, y_val,
                                  model, two_layer_net,
                                  num_epochs=10, reg=0.000001,
                                  update='sgd', learning_rate_decay=1,
                                  sample_batches = True.
```

Now let's try learning rate 1e6.



Lets try to train now...

Start with small regularization and find learning rate that makes the loss go down.

loss not going down:
learning rate too low
loss exploding:
learning rate too high

```
model = init_two_layer_model(32*32*3, 50, 10) # input size, hidden size, number of classes
trainer = ClassifierTrainer()
best_model, stats = trainer.train(X_train, y_train, X_val, y_val,
                                    model, two_layer_net,
                                    num_epochs=10, reg=0.000001,
                                    update='sgd', learning_rate_decay=1,
                                    sample_batches = True,
                                    learning_rate=1e-6, verbose=True)

/home/karpathy/cs231n/code/cs231n/classifiers/neural_net.py:50: RuntimeWarning: divide by zero encountered in log
    data_loss = -np.sum(np.log(probs[range(N), y])) / N
/home/karpathy/cs231n/code/cs231n/classifiers/neural_net.py:48: RuntimeWarning: invalid value encountered in subtract
    probs = np.exp(scores - np.max(scores, axis=1, keepdims=True))
Finished epoch 1 / 10: cost nan, train: 0.091000, val 0.087000, lr 1.000000e+06
Finished epoch 2 / 10: cost nan, train: 0.095000, val 0.087000, lr 1.000000e+06
Finished epoch 3 / 10: cost nan, train: 0.100000, val 0.087000, lr 1.000000e+06
```

cost: NaN almost always means high learning rate...

Lets try to train now...

Start with small regularization and find learning rate that makes the loss go down.

loss not going down:
learning rate too low
loss exploding:
learning rate too high

```
model = init_two_layer_model(32*32*3, 50, 10) # input size, hidden size, number of classes
trainer = ClassifierTrainer()
best_model, stats = trainer.train(X_train, y_train, X_val, y_val,
                                   model, two_layer_net,
                                   num_epochs=10, reg=0.000001,
                                   update='sgd', learning_rate_decay=1,
                                   sample_batches = True,
                                   learning_rate=3e-3, verbose=True)
```

```
Finished epoch 1 / 10: cost 2.186654, train: 0.308000, val 0.306000, lr 3.000000e-03
Finished epoch 2 / 10: cost 2.176230, train: 0.330000, val 0.350000, lr 3.000000e-03
Finished epoch 3 / 10: cost 1.942257, train: 0.376000, val 0.352000, lr 3.000000e-03
Finished epoch 4 / 10: cost 1.827868, train: 0.329000, val 0.310000, lr 3.000000e-03
Finished epoch 5 / 10: cost inf, train: 0.128000, val 0.128000, lr 3.000000e-03
Finished epoch 6 / 10: cost inf, train: 0.144000, val 0.147000, lr 3.000000e-03
```

3e-3 is still too high. Cost explodes....

=> Rough range for learning rate we should be cross-validating is somewhere [1e-3 ... 1e-5]

Hyperparameter Optimization

Cross-validation strategy

coarse -> fine cross-validation in stages

First stage: only a few epochs to get rough idea of what params work

Second stage: longer running time, finer search
... (repeat as necessary)

Tip for detecting explosions in the solver:

If the cost is ever $> 3 * \text{original cost}$, break out early

For example: run coarse search for 5 epochs

```
max_count = 100
for count in xrange(max_count):
    reg = 10**uniform(-5, 5)
    lr = 10**uniform(-3, -6) ←

    trainer = ClassifierTrainer()
    model = init_two_layer_model(32*32*3, 50, 10) # input size, hidden size, number of classes
    trainer = ClassifierTrainer()
    best_model_local, stats = trainer.train(X_train, y_train, X_val, y_val,
                                              model, two_layer_net,
                                              num_epochs=5, reg=reg,
                                              update='momentum', learning_rate_decay=0.9,
                                              sample_batches = True, batch_size = 100,
                                              learning_rate=lr, verbose=False)
```

note it's best to optimize
in log space!

```
val_acc: 0.412000, lr: 1.405206e-04, reg: 4.793564e-01, (1 / 100)
val_acc: 0.214000, lr: 7.231888e-06, reg: 2.321281e-04, (2 / 100)
val_acc: 0.208000, lr: 2.119571e-06, reg: 8.011857e+01, (3 / 100)
val_acc: 0.196000, lr: 1.551131e-05, reg: 4.374936e-05, (4 / 100)
val_acc: 0.079000, lr: 1.753300e-05, reg: 1.200424e+03, (5 / 100)
val_acc: 0.223000, lr: 4.215128e-05, reg: 4.196174e+01, (6 / 100)
val_acc: 0.441000, lr: 1.750259e-04, reg: 2.110807e-04, (7 / 100)
val_acc: 0.241000, lr: 6.749231e-05, reg: 4.226413e+01, (8 / 100)
val_acc: 0.482000, lr: 4.296863e-04, reg: 6.642555e-01, (9 / 100)
val_acc: 0.079000, lr: 5.401602e-06, reg: 1.599828e+04, (10 / 100)
val_acc: 0.154000, lr: 1.618508e-06, reg: 4.925252e-01, (11 / 100)
```

→ nice

Now run finer search...

```
max_count = 100
for count in xrange(max_count):
    reg = 10**uniform(-5, 5)
    lr = 10**uniform(-3, -6)
```

adjust range

```
max_count = 100
for count in xrange(max_count):
    reg = 10**uniform(-4, 0)
    lr = 10**uniform(-3, -4)
```

```
val_acc: 0.527000, lr: 5.340517e-04, reg: 4.097824e-01, (0 / 100)
val_acc: 0.492000, lr: 2.279484e-04, reg: 9.991345e-04, (1 / 100)
val_acc: 0.512000, lr: 8.680827e-04, reg: 1.349727e-02, (2 / 100)
val_acc: 0.461000, lr: 1.028377e-04, reg: 1.220193e-02, (3 / 100)
val_acc: 0.460000, lr: 1.113730e-04, reg: 5.244309e-02, (4 / 100)
val_acc: 0.498000, lr: 9.477776e-04, reg: 2.001293e-03, (5 / 100)
val_acc: 0.469000, lr: 1.484369e-04, reg: 4.328313e-01, (6 / 100)
val_acc: 0.522000, lr: 5.586261e-04, reg: 2.312685e-04, (7 / 100)
val_acc: 0.530000, lr: 5.808183e-04, reg: 8.259964e-02, (8 / 100)
val_acc: 0.489000, lr: 1.979168e-04, reg: 1.010889e-04, (9 / 100)
val_acc: 0.490000, lr: 2.036031e-04, reg: 2.406271e-03, (10 / 100)
val_acc: 0.475000, lr: 2.021162e-04, reg: 2.287807e-01, (11 / 100)
val_acc: 0.460000, lr: 1.135527e-04, reg: 3.905040e-02, (12 / 100)
val_acc: 0.515000, lr: 6.947668e-04, reg: 1.562808e-02, (13 / 100)
val_acc: 0.531000, lr: 9.471549e-04, reg: 1.433895e-03, (14 / 100)
val_acc: 0.509000, lr: 3.140888e-04, reg: 2.857518e-01, (15 / 100)
val_acc: 0.514000, lr: 6.438349e-04, reg: 3.033781e-01, (16 / 100)
val_acc: 0.502000, lr: 3.921784e-04, reg: 2.707126e-04, (17 / 100)
val_acc: 0.509000, lr: 9.752279e-04, reg: 2.850865e-03, (18 / 100)
val_acc: 0.500000, lr: 2.412048e-04, reg: 4.997821e-04, (19 / 100)
val_acc: 0.466000, lr: 1.319314e-04, reg: 1.189915e-02, (20 / 100)
val_acc: 0.516000, lr: 8.039527e-04, reg: 1.528291e-02, (21 / 100)
```

53% - relatively good
for a 2-layer neural net
with 50 hidden neurons.

Now run finer search...

```
max_count = 100
for count in xrange(max_count):
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```

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val_acc: 0.527000, lr: 5.340517e-04, reg: 4.097824e-01, (0 / 100)
val_acc: 0.492000, lr: 2.279484e-04, reg: 9.991345e-04, (1 / 100)
val_acc: 0.512000, lr: 8.680827e-04, reg: 1.349727e-02, (2 / 100)
val_acc: 0.461000, lr: 1.028377e-04, reg: 1.220193e-02, (3 / 100)
val_acc: 0.460000, lr: 1.113730e-04, reg: 5.244309e-02, (4 / 100)
val_acc: 0.498000, lr: 9.477776e-04, reg: 2.001293e-03, (5 / 100)
val_acc: 0.469000, lr: 1.484369e-04, reg: 4.328313e-01, (6 / 100)
val_acc: 0.522000, lr: 5.586261e-04, reg: 2.312685e-04, (7 / 100)
val_acc: 0.530000, lr: 5.808183e-04, reg: 8.259964e-02, (8 / 100)
val_acc: 0.489000, lr: 1.979168e-04, reg: 1.010889e-04, (9 / 100)
val_acc: 0.490000, lr: 2.036031e-04, reg: 2.406271e-03, (10 / 100)
val_acc: 0.475000, lr: 2.021162e-04, reg: 2.287807e-01, (11 / 100)
val_acc: 0.460000, lr: 1.135527e-04, reg: 3.905040e-02, (12 / 100)
val_acc: 0.515000, lr: 6.947668e-04, reg: 1.562808e-02, (13 / 100)
val_acc: 0.531000, lr: 9.471549e-04, reg: 1.433895e-03, (14 / 100)
val_acc: 0.509000, lr: 3.140888e-04, reg: 2.857518e-01, (15 / 100)
val_acc: 0.514000, lr: 6.438349e-04, reg: 3.033781e-01, (16 / 100)
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val_acc: 0.466000, lr: 1.319314e-04, reg: 1.189915e-02, (20 / 100)
val_acc: 0.516000, lr: 8.039527e-04, reg: 1.528291e-02, (21 / 100)
```

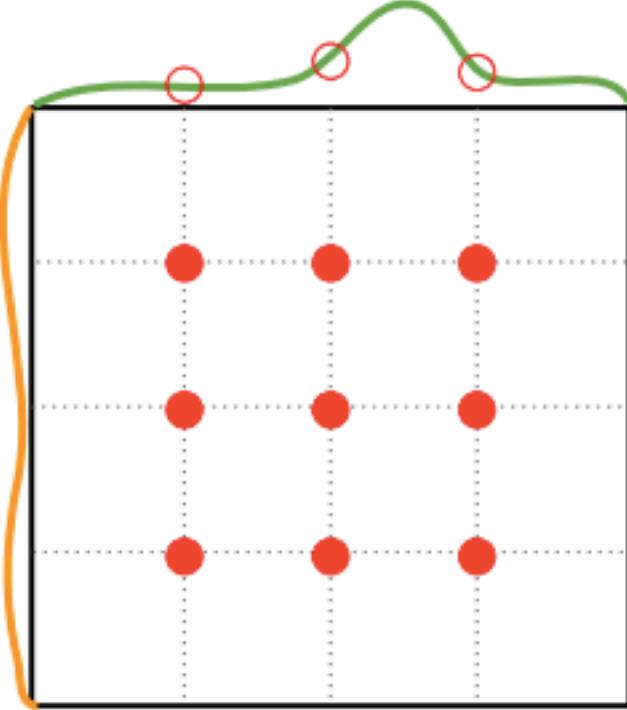
53% - relatively good
for a 2-layer neural net
with 50 hidden neurons.

But this best
cross-validation result is
worrying. Why?

Random Search vs. Grid Search

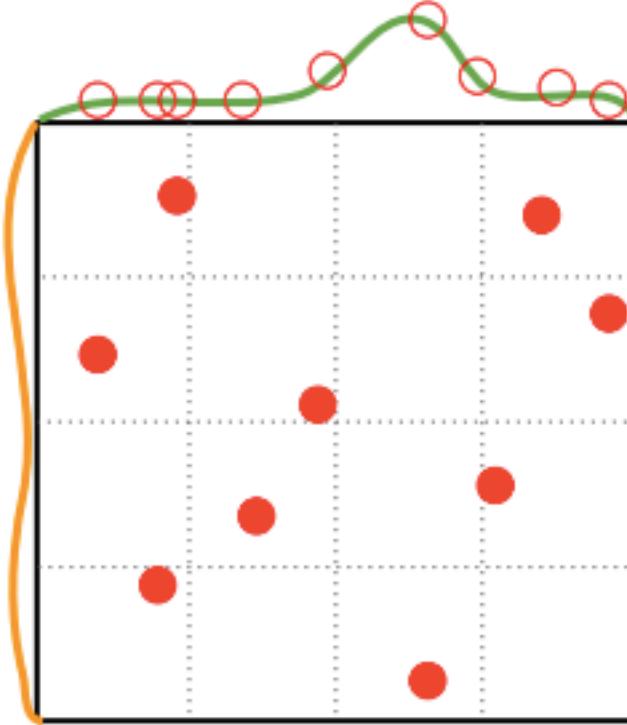
*Random Search for
Hyper-Parameter Optimization
Bergstra and Bengio, 2012*

Grid Layout



Important Parameter

Random Layout

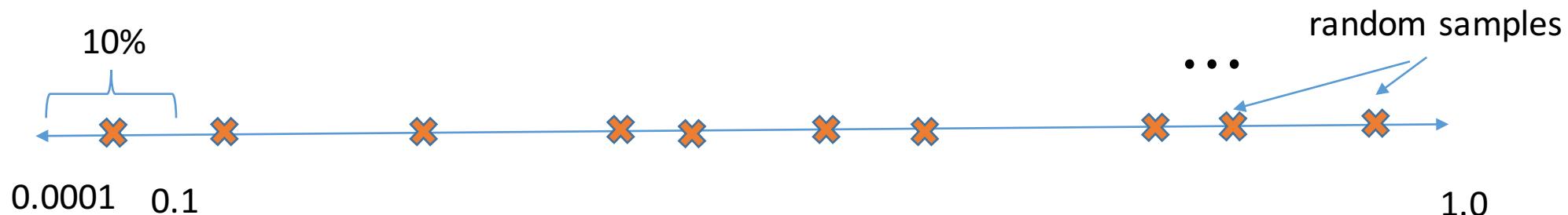


Important Parameter

Illustration of Bergstra et al., 2012 by Shayne
Longpre, copyright CS231n 2017

Why Searching in Log Space?

Appropriate scale for hyperparameters
 $\alpha = 0.0001, \dots, 1$



About 90% of the resources will be used to search between 0.1 and 1.0 which is not efficient. Instead it would be more efficient to search in log space:



```
alpha = 10**uniform (-4, 0)
```

Hyperparameter for Exponentially Weighted Averages

$$\beta = 0.9, \dots, 0.999$$

we can search for $1 - \beta$ instead:

$$1 - \beta = 0.1, \dots, 0.001$$

Some Best Practices

When NNs Don't Work, You Have Many Choices

Your choices: (from Andrew Ng's talk at Bay Learn'17)

- Fetch more data
- Add more layers to Neural Network
- Try some new approach in Neural Network
- Train longer (increase the number of iterations)
- Change batch size
- Try Regularization
- Use more GPUs for faster computation
- ...

Abstraction of Hyperparameter Tuning

Your input : Hyper parameters

- Architecture (#layers, #kernels, stride, kernel size)
- Learning rate, optimizer (momentum)
- Regularizations (weight decay rate, dropout probability)
- Batchnorm / no batchnorm

Your output: Some diagnostic statistics:

- Loss curves
- Accuracy / Visual output (generative models)
- Performance on training vs validation set
- Other abnormal behaviors

Architecture

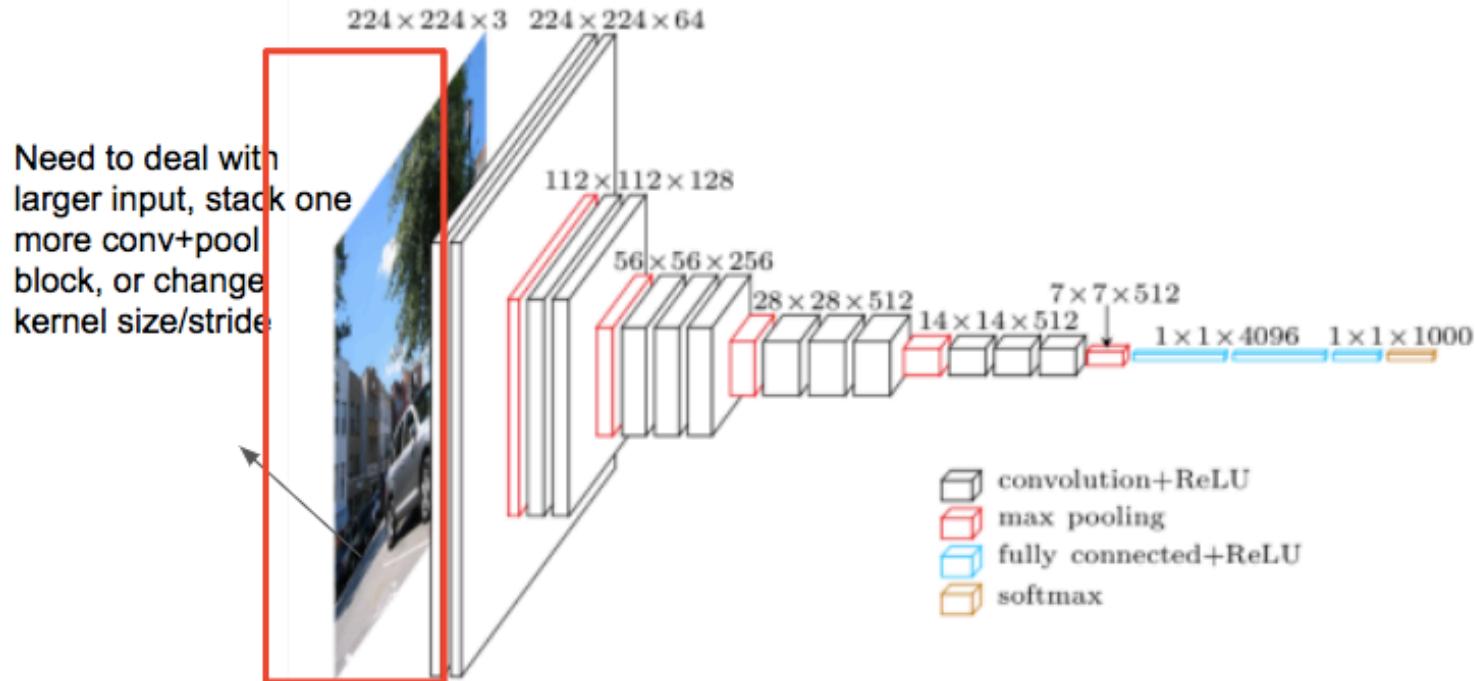
Using or adapt from established networks

- Classification: AlexNet, VGG, ResNet, DenseNet, ...
- Segmentation: FCN, Dilated Convolution, Mask RCNN
- Detection: Faster-RCNN, YOLO, SSD
- Image Generation: UNet, Dilated Convolution, DCGAN, WGAN
- ...

How to adapt:

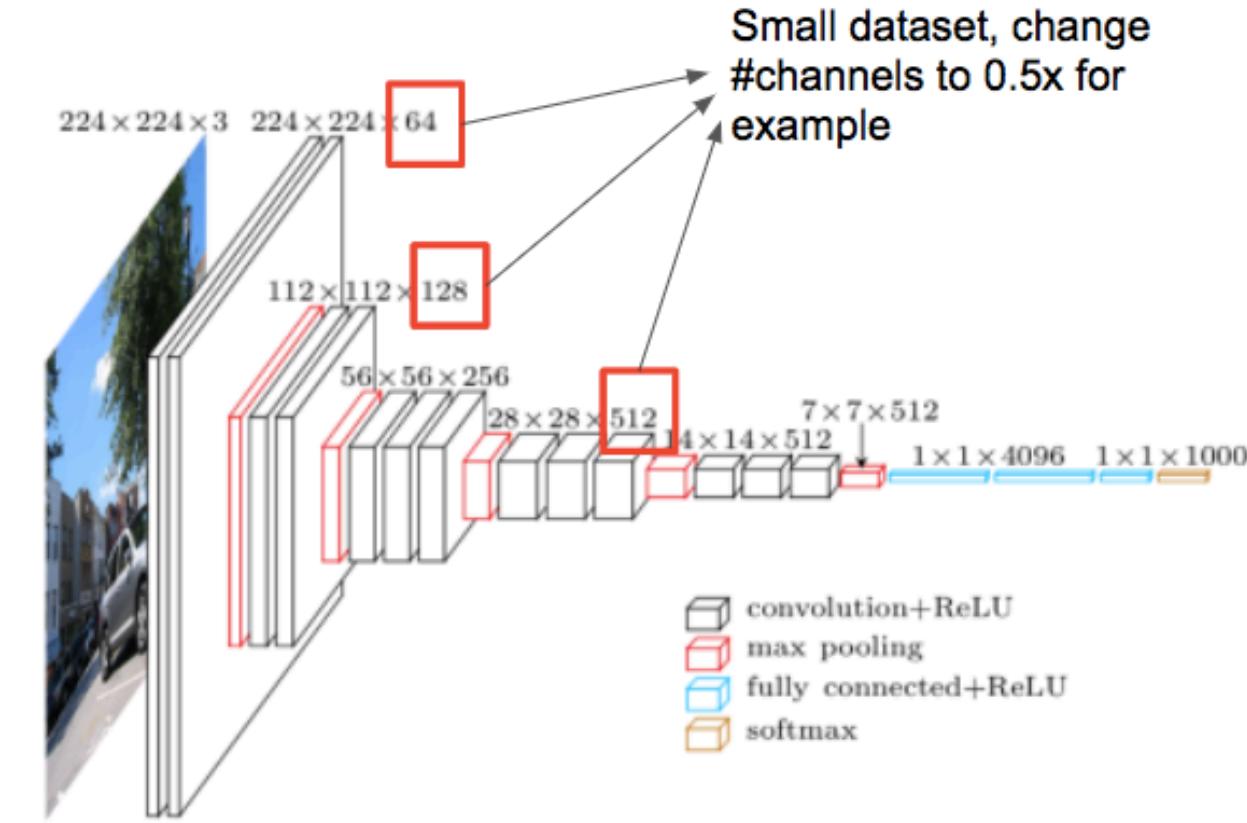
- Change number of kernels to ideal numbers
- Remove / add layers
- Change the structure of last few layers for your task

Architecture: Adapt to Different Input



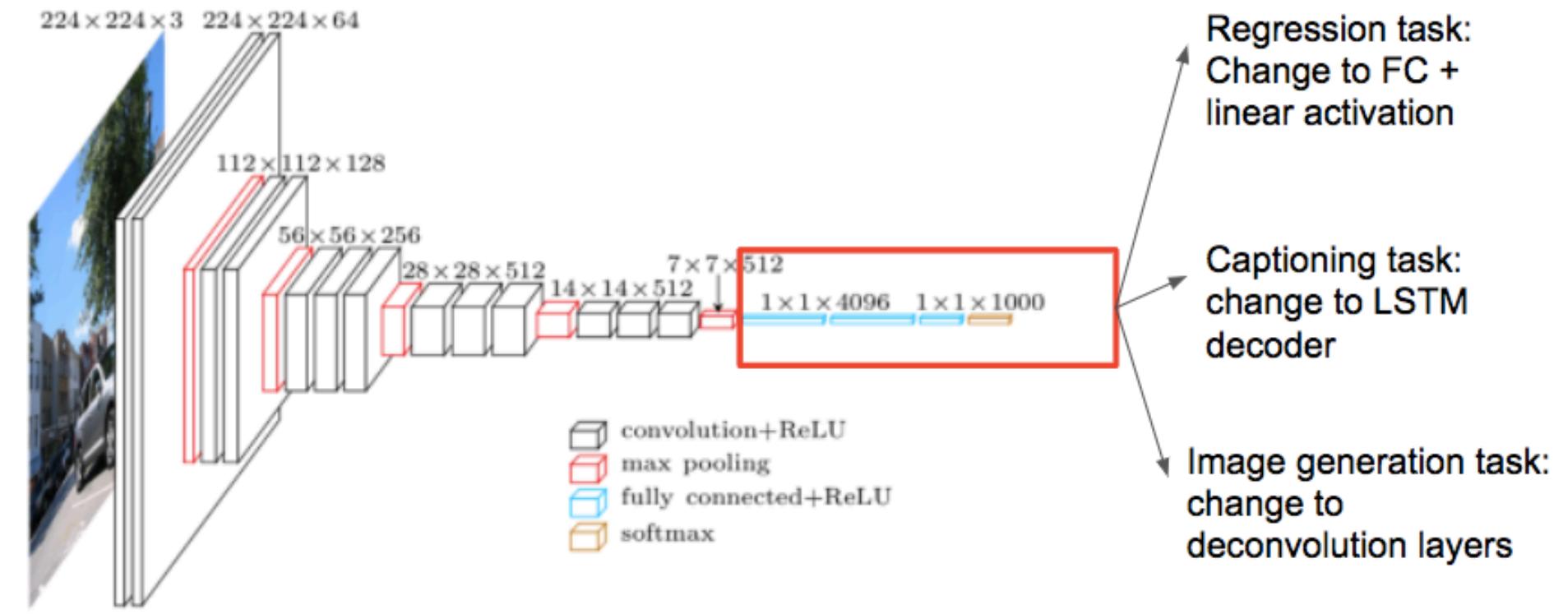
Let's say you saw this awesome network on some related work, but the input is not the same.

Architecture: for Different Size of Dataset



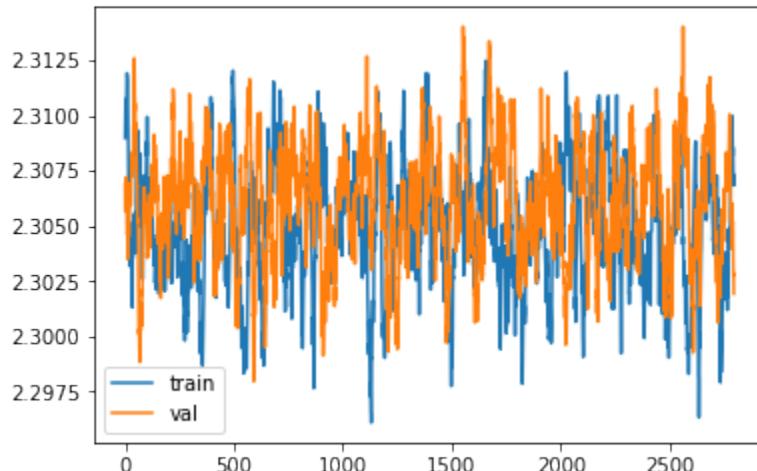
Let's say you saw this awesome network on some related work, but the dataset you have is much smaller

Architecture: for Tasks

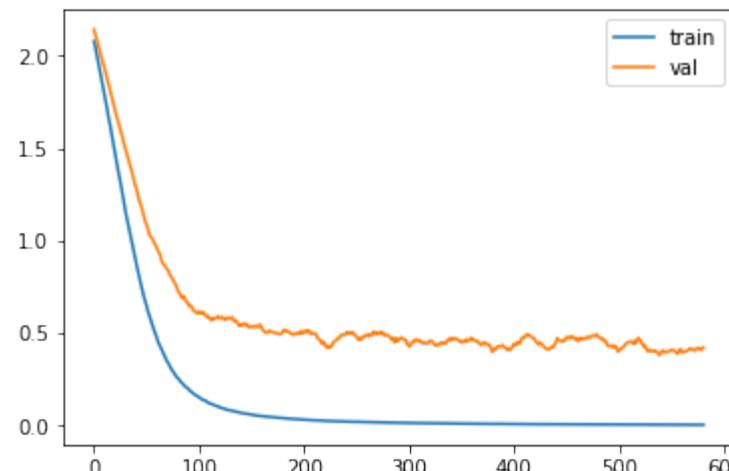


Let's say you saw this awesome network on some related work, but the task is not the same.

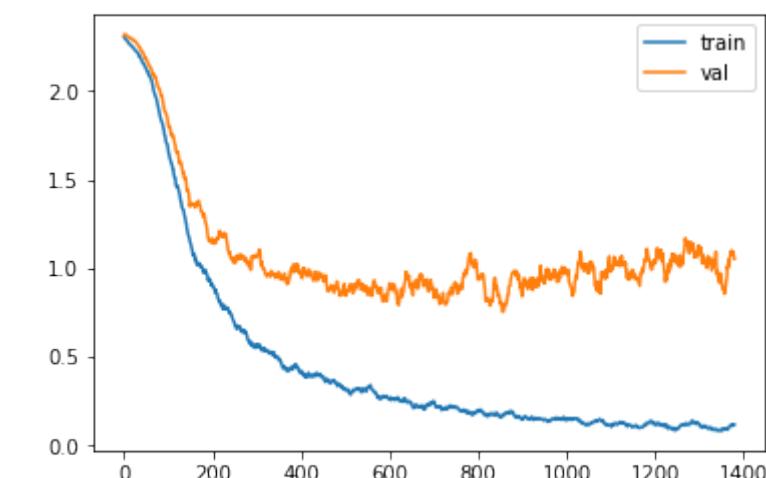
Loss Curves: What are the Problems?



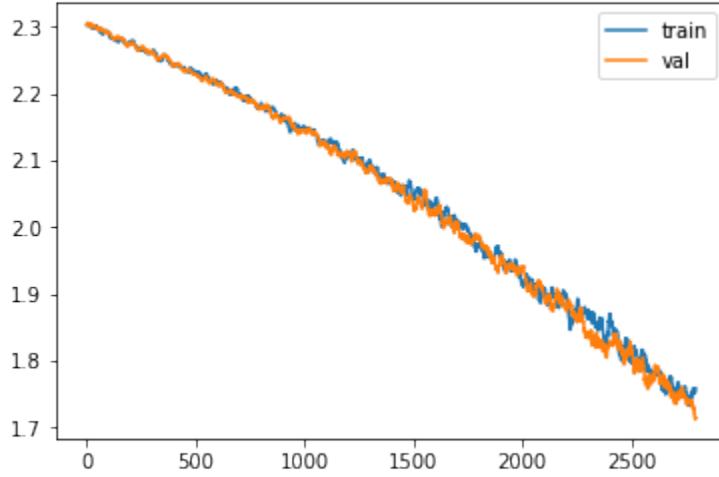
Not learning: gradients not applied to weights



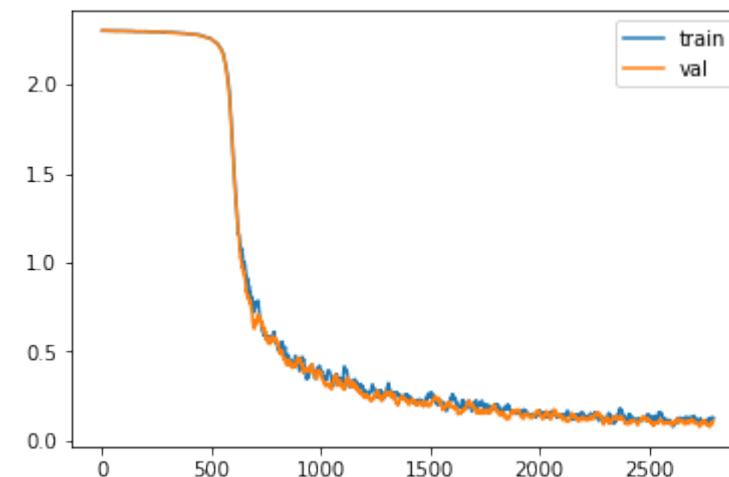
Overfit: model too large/dataset too small



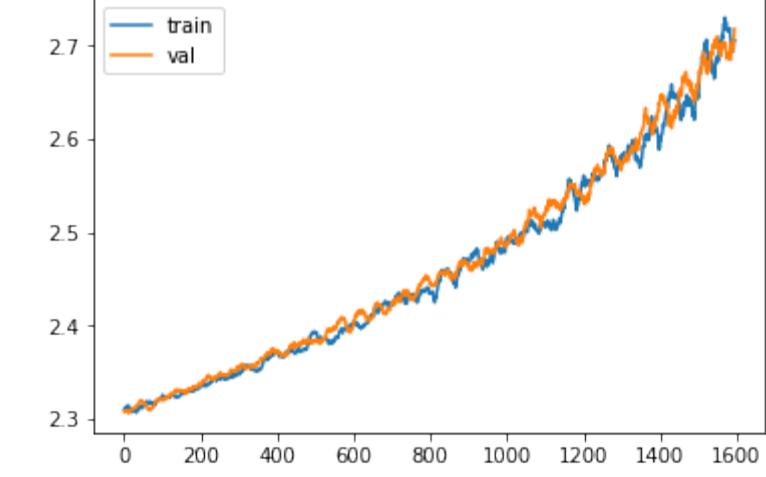
More extreme case of overfitting



Not converged yet: need longer training

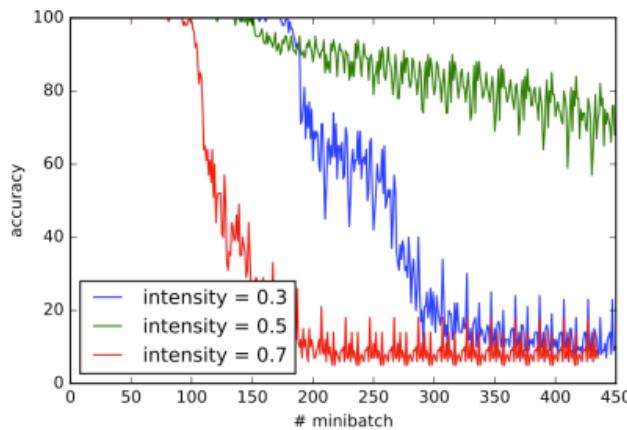


Slow start: initialization weights too small

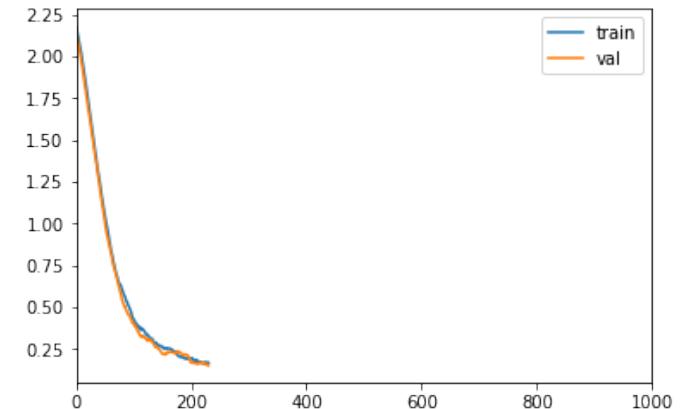
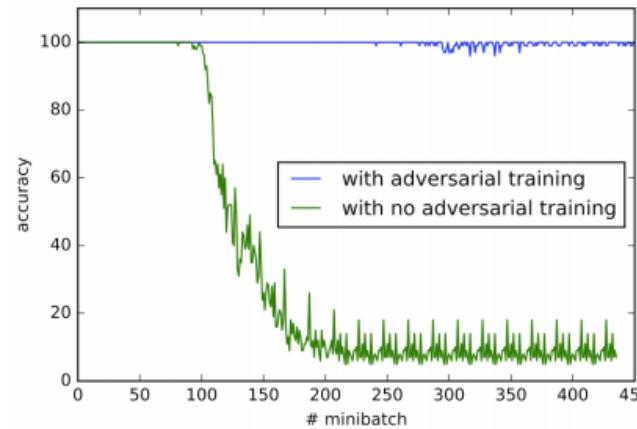


Applied the negative of gradients

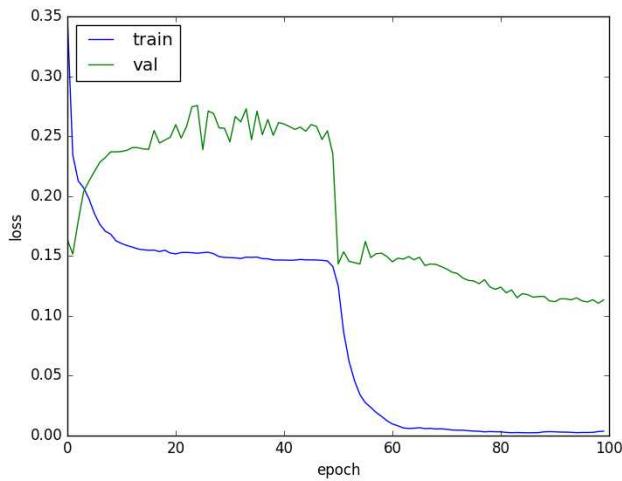
Loss Curves: What are the Problems?



Problem: Not shuffling data, periodical patterns in loss curve

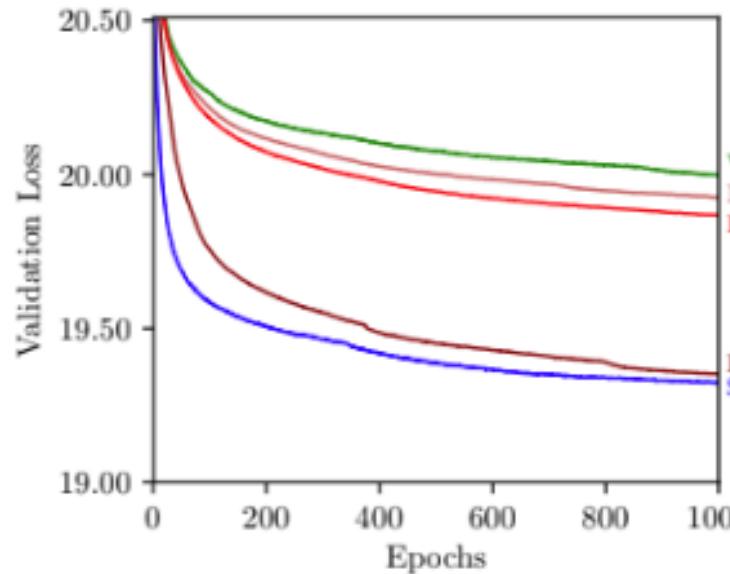


Get nans in the loss after a number of iterations: caused by numerical instability in models

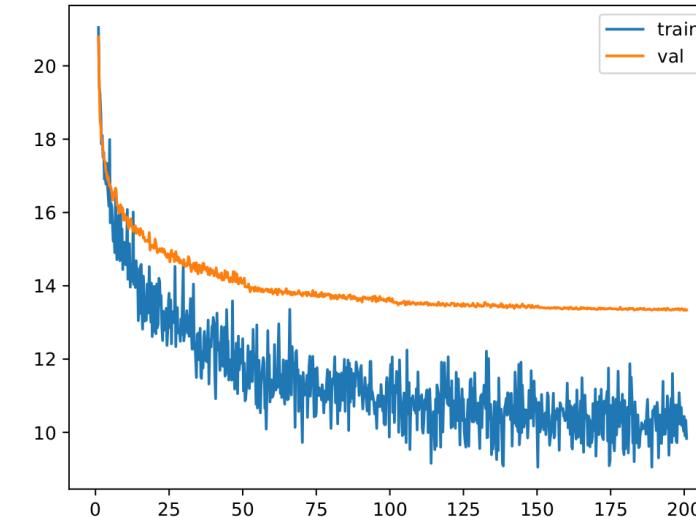


Problem: val set too small, statistics not meaningful

Loss Curves: What are the Problems?



Problem: applied nonlinear activation before softmax



Make sure to optimize correct loss

$$\sigma(\mathbf{z})_j = \frac{e^{z_j}}{\sum_{k=1}^k e^{z_k}} \text{ for } j = 1, \dots, k$$

Loss: Summary

- Loss curve is one powerful indicator when debugging NNs
- Abnormal loss curves can be caused by
 - Wrong implementation of data loading
 - Wrong implementation/choice of losses
 - Optimizer problems
 - Suboptimal hyper-parameters
- Some back of the envelope calculation can help:
 - What do you expect the loss to start at?
 - What do you expect the loss to converge to?
 - Any ideas of how many iterations are required?

Resources Used

- Deeplearning.ai; Improving Deep Neural Networks: Hyperparameter Tuning; Andrew Ng
- CS231n Convolutional Neural Networks for Visual Recognition by Fei-Fei Li, Justin Johnson, Seran Yeung
- STAT 479: Deep Learning by Sebastian Raschka