

TALLER 11

$$\nabla^2 u = \frac{1}{r^2} \frac{\partial^2 u}{\partial t^2} \rightarrow \text{ec. onda.}$$

cilíndricas $u(r, \theta, t)$

$\nabla^2 u \rightarrow$ esféricas \rightarrow Pol. de Legendre

$\nabla^2 u \rightarrow$ cilíndricas \rightarrow Ecs. de Bessel.

S.V.

$$u = S(r, \theta) T(t)$$

$$T(t) = e^{\pm i\omega t}$$

$$k^2 = \frac{\omega^2}{v^2}$$

\uparrow
const.

1ra separación.

$$\nabla^2 S + k^2 S = 0, \quad S(r, \theta) = R(r) \Theta(\theta)$$

S.V. (m^2 const. 2da separación).

$$\frac{r^2}{R} \frac{d^2 R}{dr^2} + \frac{r}{R} \frac{dR}{dr} + \frac{1}{\Theta} \frac{d\Theta}{d\theta} + r^2 k^2 = 0$$

$\hookrightarrow \omega^2/v^2$

$$\frac{1}{\Theta} \frac{d^2 \Theta}{d\theta^2} = -m^2 \rightarrow \frac{d^2 \Theta}{d\theta^2} + m^2 \Theta = 0$$

$$\hookrightarrow \Theta = e^{\frac{r}{m} \theta}$$

Parte radial

$$r^2 \frac{d^3 R}{dr^3} + r \frac{dR}{dr} + (k^2 r^2 - m^2) R = 0 \rightarrow \text{ec. de Bessel}$$

$$R(r) = J_m(kr)$$

$$u_m(r, \theta, t) = R(r) \Theta(\theta) T(t)$$

Cond. de Frontière.

$$R(r=r') = 0 \rightarrow J_m(kr') = 0$$

$$\mu_n^m \Rightarrow k_{mn} = \frac{\mu_n^m}{r'}$$

↑

raíces.

F.B.E. Series

$$j_n(x) = J_{n+\frac{1}{2}}(x)$$

$$y_n(x) = Y_{n+\frac{1}{2}}(x)$$

→ Artien

→ Chow