

Anexos

$$\begin{aligned}
\vec{E} &= \frac{1}{4\pi\epsilon_0} \int \frac{(r-r')\rho(r')}{|r-r'|^3} dV, & Q &= \int_C \lambda dl, & \vec{F} &= Q\vec{E}, & \nabla \times \vec{E} &= 0 \\
\oint_S \vec{E} \cdot \vec{n} da &= \frac{Q_{enc}}{\epsilon_0}, & \vec{F} &= \frac{q}{4\pi\epsilon_0} \int \frac{(r-r')\rho(r')}{|r-r'|^3} dV, & \varphi &= - \int \vec{E} \cdot d\vec{l}, & \sigma &= -\epsilon_0 \frac{\partial \varphi}{\partial n} \\
\vec{E} &= -\nabla \varphi, & \int_S (\nabla \times \vec{F}) \cdot \hat{n} da &= \oint_C \vec{F} \cdot d\vec{l}, & W &= \int_a^b \vec{F} \cdot d\vec{l}, & \nabla \cdot \vec{E} &= \frac{\rho}{\epsilon_0} \\
\int_V (\nabla \cdot \vec{F}) dV &= \oint_S \vec{F} \cdot \hat{n} da, & W &= \frac{\epsilon_0}{2} \int_V E^2 dV, & \nabla^2 \varphi &= -\frac{\rho}{\epsilon_0}, & \varphi(r) &= \frac{1}{4\pi\epsilon_0} \frac{q}{r} \\
\vec{P} &= \chi \vec{E}, & \vec{D} &= \epsilon \vec{E}, & \epsilon &= \epsilon_0 + \chi, & K &= \epsilon/\epsilon_0 \\
\sigma_p &= \vec{n} \cdot \vec{P}, & \vec{D} &= \epsilon_0 \vec{E} + \vec{P}, & \vec{P} &= \Delta \vec{p} / \Delta V, & \rho_P &= -\nabla \cdot \vec{P} \\
\vec{p}_m &= \alpha \vec{E}_m & \varphi &= \frac{1}{4\pi\epsilon_0} \frac{\vec{p} \cdot \hat{r}}{r^2}, & \vec{J} &= g \vec{E} & R &= \frac{l}{gA} = \frac{l\eta}{A} \\
U &= \frac{1}{2} Q \Delta \varphi & C &= \frac{\epsilon A}{d} & F_x &= - \left(\frac{\partial U}{\partial x} \right)_Q & F_x &= + \left(\frac{\partial U}{\partial x} \right)_\varphi \\
\vec{J} &= \sum N_i q_i \vec{v}_i & U &= \frac{1}{2} \int \rho(r) \varphi(r) dv + \frac{1}{2} \int \sigma(r) \varphi(r) da & \nabla \cdot \vec{J} &+ \frac{\partial \rho}{\partial t} &= 0
\end{aligned}$$

$$\vec{E}_{dip} = \frac{1}{4\pi\epsilon_0} \left[\frac{3(r-r') \cdot \vec{p}(r-r')}{(r-r')^5} - \frac{\vec{p}}{(r-r')^3} \right]$$

Grad, Div, Curl and the Laplacian

	Cartesian Coordinates	Cylindrical Coordinates	Spherical Coordinates
Conversion to Cartesian Coordinates		$x = \rho \cos \varphi \quad y = \rho \sin \varphi \quad z = z$	$x = r \cos \varphi \sin \theta \quad y = r \sin \varphi \sin \theta \quad z = r \cos \theta$
Vector A	$A_x \hat{i} + A_y \hat{j} + A_z \hat{k}$	$A_\rho \hat{\rho} + A_\varphi \hat{\varphi} + A_z \hat{z}$	$A_r \hat{r} + A_\theta \hat{\theta} + A_\varphi \hat{\varphi}$
Gradient $\nabla \phi$	$\frac{\partial \phi}{\partial x} \hat{i} + \frac{\partial \phi}{\partial y} \hat{j} + \frac{\partial \phi}{\partial z} \hat{k}$	$\frac{\partial \phi}{\partial \rho} \hat{\rho} + \frac{1}{\rho} \frac{\partial \phi}{\partial \varphi} \hat{\varphi} + \frac{\partial \phi}{\partial z} \hat{z}$	$\frac{\partial \phi}{\partial r} \hat{r} + \frac{1}{r} \frac{\partial \phi}{\partial \theta} \hat{\theta} + \frac{1}{r \sin \theta} \frac{\partial \phi}{\partial \varphi} \hat{\varphi}$
Divergence $\nabla \cdot A$	$\frac{\partial A_x}{\partial x} + \frac{\partial A_y}{\partial y} + \frac{\partial A_z}{\partial z}$	$\frac{1}{\rho} \frac{\partial(\rho A_\rho)}{\partial \rho} + \frac{1}{\rho} \frac{\partial A_\varphi}{\partial \varphi} + \frac{\partial A_z}{\partial z}$	$\frac{1}{r^2} \frac{\partial(r^2 A_r)}{\partial r} + \frac{1}{r \sin \theta} \frac{\partial A_\theta \sin \theta}{\partial \theta} + \frac{1}{r \sin \theta} \frac{\partial A_\varphi}{\partial \varphi}$
Curl $\nabla \times A$	$\begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ A_x & A_y & A_z \end{vmatrix}$	$\begin{vmatrix} \frac{1}{\rho} \hat{\rho} & \hat{\varphi} & \frac{1}{\rho} \hat{z} \\ \frac{\partial}{\partial \rho} & \frac{\partial}{\partial \varphi} & \frac{\partial}{\partial z} \\ A_\rho & \rho A_\varphi & A_z \end{vmatrix}$	$\begin{vmatrix} \frac{1}{r^2 \sin \theta} \hat{r} & \frac{1}{r \sin \theta} \hat{\theta} & \frac{1}{r} \hat{\varphi} \\ \frac{\partial}{\partial r} & \frac{\partial}{\partial \theta} & \frac{\partial}{\partial \varphi} \\ A_r & r A_\theta & r A_\varphi \sin \theta \end{vmatrix}$
Laplacian $\nabla^2 \phi$	$\frac{\partial^2 \phi}{\partial x^2} + \frac{\partial^2 \phi}{\partial y^2} + \frac{\partial^2 \phi}{\partial z^2}$	$\frac{1}{\rho} \frac{\partial}{\partial \rho} \left(\rho \frac{\partial \phi}{\partial \rho} \right) + \frac{1}{\rho^2} \frac{\partial^2 \phi}{\partial \varphi^2} + \frac{\partial^2 \phi}{\partial z^2}$	$\frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial \phi}{\partial r} \right) + \frac{1}{r^2 \sin \theta} \frac{\partial}{\partial \theta} \left(\sin \theta \frac{\partial \phi}{\partial \theta} \right) + \frac{1}{r^2 \sin^2 \theta} \frac{\partial^2 \phi}{\partial \varphi^2}$