

SOUND WAVE IMPLEMENTATION IN THE VORTICITY

The parallel thermal velocity is included in the parallel component of the Vorticity definition:

$$U = \frac{1}{\rho} \frac{\partial}{\partial \rho} \left[\rho_m \rho \sqrt{g} \left(g_{\rho\rho} v^\rho + g_{\theta\theta} v^\theta + g_{\theta\zeta} v^\zeta + g_{\theta\zeta} v_{th,\parallel}^\zeta \right) \right] - \frac{1}{\rho} \frac{\partial}{\partial \theta} \left[\rho_m \sqrt{g} \left(g_{\rho\rho} v^\rho + g_{\rho\theta} v^\theta + g_{\rho\zeta} v^\zeta + g_{\theta\zeta} v_{th,\parallel}^\zeta \right) \right]$$

new terms added:

$$U = \dots + \frac{1}{\varepsilon} \frac{1}{\rho} \frac{\partial}{\partial \rho} \left[\rho_m \rho \sqrt{g} g_{\theta\zeta} \right] v_{th,\parallel}^\zeta + \frac{\rho_m}{\varepsilon} \sqrt{g} g_{\theta\zeta} \frac{\partial v_{th,\parallel}^\zeta}{\partial \rho} - \frac{1}{\varepsilon} \frac{1}{\rho} \frac{\partial}{\partial \theta} \left[\rho_m \sqrt{g} g_{\rho\zeta} \right] v_{th,\parallel}^\zeta + \frac{\rho_m}{\varepsilon} \sqrt{g} g_{\rho\zeta} \frac{1}{\rho} \frac{\partial v_{th,\parallel}^\zeta}{\partial \theta}$$

Implementation:

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do l=1,lmax
    wk7(:,l)=r*denseq*wk5(:,l)/eps
end do
call dbydr(wk8,wk7,0.0_IDP,1.0_IDP,2)
do l=1,lmax
    wk7(:,l)=denseq*wk4(:,l)/eps
end do
call dbydth(wk9,wk7,-1,0.0_IDP,1.0_IDP,0)
do l=1,lmax
    wk7(:,l)=rinv*wk8(:,l)-wk9(:,l)
end do
call mult(ss,wk7,1,vthprlf,-1,1.0_IDP,1.0_IDP)

do l=1,lmax
    wk7(:,l)=denseq*wk5(:,l)/eps
end do
call dbydr(wk8,vthprlf,0.0_IDP,1.0_IDP,0)
call mult(ss,wk8,-1,wk7,1,1.0_IDP,1.0_IDP)
do l=1,lmax
    wk7(:,l)=-denseq*wk4(:,l)/eps
end do
call dbydth(wk8,vthprlf,-1,0.0_IDP,1.0_IDP,0)
call mult(ss,wk8,1,wk7,-1,1.0_IDP,1.0_IDP)

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