

GOVERNMENT COLLEGE OF ENGINEERING, AMRAVATI
(An autonomous institute of Govt. of Maharashtra)

CT-1 [Direct-IInd year] W- 2015

SHU301, SHU303, SHU304. ENGG. MATHS-III [CIVIL/ MECH/ ELPO/ EXTC/ CS/ IT/ IN]

MARKS-15 TIME-1 HOUR

Q.1 Using the method of variation of parameters Solve

$$\left(1 + \frac{1}{e^x}\right)^2 \left[(D^2 - 1)y\right] = 1$$

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Q.2 Solve $y = \log x \frac{\sin(\log x) + 1}{x} - x^2 \frac{d^2 y}{dx^2} + 3x \frac{dy}{dx}$

3

Q.3 ATTEMPT ANY THREE

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(A) Solve $(D^3 + 1)y = \cos^2\left(\frac{x}{2}\right) + e^{-x}$

(B) Solve $\frac{1}{e^x} \left(\frac{d^2 y}{dx^2} - 2 \frac{dy}{dx} + 2y \right) - \tan x = 0$

(C) Solve the method of variation of parameter $\frac{d^2 y}{dx^2} + y = \tan x$

(D) Solve $(1+x)^2 \frac{d^2 y}{dx^2} + (1+x) \frac{dy}{dx} + y = 2 \sin \log(1+x)$

1. Find the elastic curve of a uniform cantilever beam of length l , having a constant weight w pound per foot by using the differential equation $EI \frac{d^2y}{dx^2} = \frac{w}{2}(l-x)^2$ under the conditions $\frac{dy}{dx} = y = 0$.

Also determine the deflection of the free end. (4)

2. Solve the equation by method of variation of parameters

$$\frac{d^2y}{dx^2} - 4y = e^{2x}. \quad (2)$$

Que: ATTEMPT ANY THREE :

(9)

3. Solve $\frac{d^2y}{dx^2} - 4\frac{dy}{dx} + 4y = e^{2x} + x^3 + \cos 2x$.

4. Solve $(3x+2)^2 \frac{d^2y}{dx^2} + 3(3x+2) \frac{dy}{dx} - 36y = 3x^2 + 4x + 1$.

5. Solve $x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} + y = \sin(\log x^2)$.

6. Solve $\frac{d^3y}{dx^3} + 3\frac{dy}{dx} = \cosh 2x \sinh 3x$.