

GOVERNMENT COLLEGE OF ENGINEERING.
(An autonomous institute of Govt. of Maharashtra)

CT-I W-2017 SHU-301 ENGG. MATHS-III
TIME-1 HOUR

MARKS-15
Date-03/08/2017

(3)

Q.1 The differential equation satisfied by a beam uniformly loaded (w kg/m) with one end fixed and second end subjected to tensile force P is given by E.I. $\frac{d^2 y}{dx^2} = Py - \frac{1}{2} Wx^2$ show that the elastic curve for the beam with condition $y=0=\frac{dy}{dx}$ at $x=0$ given by $y = \frac{w}{Pn^2} (1 - \cos hnx) + \frac{wx^2}{2P}$ where $n^2 = \frac{P}{EI}$

Q.2 Attempt any four :-

(12)

- a) Solve the differential equation $\frac{d^2 x}{dt^2} + \frac{g}{l} x = \frac{g}{l} L$ where g, l, L are constants subject to the condition $x=a, \frac{dx}{dt} = 0$, at $t = 0$
- b) Solve $(D^2 + 5D + 6)y = e^{-2x} \sin 2x + 4x^2 e^x$
- c) Using the method of variation of parameters solve $\frac{d^2 y}{dx^2} - y = (1 + \frac{1}{e^x})^{-2}$
- d) Solve $x^2 \frac{d^2 y}{dx^2} - x \frac{dy}{dx} + 4y = \cos(\log x) + x \sin(\log x)$
- e) Solve $(2x - 1)^2 y'' - 6(2x - 1)y' + 16y = 8(2x - 1)^2$

GOVERNMENT COLLEGE OF ENGINEERING.
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CT-1 W-2013 SHU-301 ENGG. MATHS-III [Civil/Mech] MARKS-15 TIME-1 HOUR

Q.1 Solve the differential equation $\frac{d^2x}{dt^2} + \frac{g}{l}x = \frac{g}{l}L$ where g, l, L are constant subject to the conditions $x = a, \frac{dx}{dt} = 0$, at $t = 0$. 3

Q.2 A body executes damped forced vibrations given by the equation $\frac{d^2x}{dt^2} + 2k \frac{dx}{dt} + b^2x = e^{-kt} \sin \omega t$. Solve the differential equation for both the cases when $\omega^2 \neq b^2 - k^2$ and when $\omega^2 = b^2 - k^2$ 3

Q.3 ATTEMPT ANY THREE 9

(A) Solve $(D^3 + 1)y = \cos^2\left(\frac{x}{2}\right) + e^{-x}$

(B) Solve $(D^2 + 5D + 6)y = e^{-2x} \sec^2 x (1 + 2 \tan x)$

(C) Solve the method of variation of parameter $(D^2 - 1)y = \left(1 + \frac{1}{e^x}\right)^{-2}$

(D) Solve $(3x + 2)^2 \frac{d^2y}{dx^2} + 3(3x + 2) \frac{dy}{dx} - 36y = 3x^2 + 4x + 1$

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Q.1 The differential equation satisfied by a beam uniformly loaded (w kg/m) with one end fixed and second end subjected to tensile force P is given by E.I. $\frac{d^2x}{dt^2} = Py - \frac{1}{2}Wx^2$ show that the elastic curve for the beam with condition $y=0=\frac{dy}{dx}$ at $x=0$ given by $y = \frac{w}{Pn^2}(1 - \cos hnx) + \frac{wx^2}{2P}$ where $n^2 = \frac{P}{EI}$ (3)

Q.2 Attempt any four :-

a) Solve the differential equation $\frac{d^2x}{dt^2} + \frac{g}{l}x = \frac{g}{l}L$ where g, l, L are constants subject to the condition $x=a, \frac{dx}{dt} = 0$, at $t = 0$ (12)

b) Solve $(D^2 + 5D + 6)y = e^{-2x} \sin 2x + 4x^2 e^x$

c) Using the method of variation of parameters solve $\frac{d^2y}{dx^2} - y = (1 + \frac{1}{e^x})^{-2}$

d) Solve $x^2 \frac{d^2y}{dx^2} - x \frac{dy}{dx} + 4y = \cos(\log x) + x \sin(\log x)$

e) Solve $(2x - 1)^2 y'' - 6(2x - 1)y' + 16y = 8(2x - 1)^2$

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SHU-301 ENGG. MATHS-III

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(3)

Q.1 The differential equation satisfied by a beam uniformly loaded (w kg/m) with one end fixed and second end subjected to tensile force P is given by E.I. $\frac{d^2y}{dx^2} = Py - \frac{1}{2}Wx^2$ show that the elastic curve for the beam with condition $y=0=\frac{dy}{dx}$ at $x=0$ given by $y = \frac{w}{Pn^2}(1 - \cos hnx) + \frac{wx^2}{2P}$ where $n^2 = \frac{P}{EI}$

Q.2 Attempt any four :-

(12)

- a) Solve the differential equation $\frac{d^2x}{dt^2} + \frac{g}{l}x = \frac{g}{l}L$ where g, l, L are constants subject to the condition $x=a, \frac{dx}{dt} = 0$, at $t = 0$
- b) Solve $(D^2 + 5D + 6)y = e^{-2x} \sin 2x + 4x^2 e^x$
- c) Using the method of variation of parameters solve $\frac{d^2y}{dx^2} - y = (1 + \frac{1}{e^x})^{-2}$
- d) Solve $x^2 \frac{d^2y}{dx^2} - x \frac{dy}{dx} + 4y = \cos(\log x) + x \sin(\log x)$
- e) Solve $(2x - 1)^2 y'' - 6(2x - 1)y' + 16y = 8(2x - 1)^2$

GOVERNMENT COLLEGE OF ENGINEERING, AMRAVATI
(An autonomous institute of Govt. of Maharashtra)

CT-1 W- 2015 SHU301 [CIVIL/MECH] ENGG.MATHS-III MARKS-15 TIME-1 HOUR

- Q.1** The differential equation satisfied by a beam, uniformly loaded with one end fixed and second subjected to a tensile force P is given by $EI \frac{d^2 y}{dx^2} - Py = -\frac{w}{2} x^2$ find the Elastic curve for the beam under conditions $y = 0, \frac{dy}{dx} = 0$, where $x = 0$. 3

Q.2 Solve $x^2 \frac{d^2 y}{dx^2} - 3x \frac{dy}{dx} + y = \log x \frac{\sin(\log x) + 1}{x}$. 3

Q.3 ATTEMPT ANY THREE 9

(A) Solve $\frac{1}{8x^2} \left(\frac{d^2 y}{dx^2} - 4 \frac{dy}{dx} + 4y \right) = e^{2x} \sin 2x$

(B) Solve $(D^2 + 5D + 6)y = e^{-2x} \sec^2 x (1 + 2 \tan x) \cdot e^{-x} e^{2x}$

(C) Solve the method of variation of parameter $(D^3 + D)y = \tan x$

(D) Solve $[(3x+2)D^2 + 3D]y = \frac{3x^2 + 4x + 36y + 1}{(3x+2)}$

16
4
-2

GOVERNMENT COLLEGE OF ENGINEERING, AMRAVATI
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CT-1 [Direct-IInd year] W- 2015

MARKS-15 TIME-1 HOUR

SHU301, SHU303, SHU304. ENGG. MATHS-III [CIVIL/ MECH/ELPO/EXTC/CS/IT/IN]

Q.1 Using the method of variation of parameters Solve

$$\left(1 + \frac{1}{e^x}\right)^2 [(D^2 - 1)y] = 1$$

3

Q.2 Solve $y = \log x \frac{\sin(\log x) + 1}{x} - x^2 \frac{d^2 y}{dx^2} + 3x \frac{dy}{dx}$

3

Q.3 ATTEMPT ANY THREE

9

(A) Solve $(D^3 + 1)y = \cos^2\left(\frac{x}{2}\right) + e^{-x}$

(B) Solve $\frac{1}{e^x} \left(\frac{d^2 y}{dx^2} - 2 \frac{dy}{dx} + 2y \right) - \tan x = 0$

(C) Solve the method of variation of parameter $\frac{d^2 y}{dx^2} + y = \tan x$

(D) Solve $(1+x)^2 \frac{d^2 y}{dx^2} + (1+x) \frac{dy}{dx} + y = 2 \sin \log(1+x)$

Government College of Engineering, Amravati
(An Autonomous Institute of Government of Maharashtra)
B. TECH II (CIVIL/MECH) CT1 Winter 2016
SHU301 Engineering Mathematics III

Dt: 4/08/2016 Time 1 Hour

1. Find the elastic curve of a uniform cantilever beam of length l , having a constant weight w pound per foot by using the differential equation $EI \frac{d^2y}{dx^2} = \frac{w}{2}(l-x)^2$ under the conditions $\frac{dy}{dx} = y = 0$.

Also determine the deflection of the free end.

(4)

2. Solve the equation by method of variation of parameters

$$\frac{d^2y}{dx^2} - 4y = e^{2x}.$$

(2)

Que: ATTEMPT ANY THREE :

(9)

3. Solve $\frac{d^2y}{dx^2} - 4\frac{dy}{dx} + 4y = e^{2x} + x^3 + \cos 2x$.

4. Solve $(3x+2)^2 \frac{d^2y}{dx^2} + 3(3x+2) \frac{dy}{dx} - 36y = 3x^2 + 4x + 1$.

5. Solve $x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} + y = \sin(\log x^2)$.

6. Solve $\frac{d^3y}{dx^3} + 3\frac{dy}{dx} = \cosh 2x \sinh 3x$.

for $\log x^2$
 $z = \log x^2$