

**Government College of Engineering, Amravati**  
(An Autonomous Institute of Government of Maharashtra)

**Third Semester B. Tech. (CS / IT)**

**Winter – 2014**

**Course Code: CSU303**

**Course Name: Discrete Mathematics and Graph Theory**

**Time: 2 hr. 30min.**

**Max. Marks: 60**

**Instructions to Candidate**

- 1) All questions are compulsory.
- 2) Assume suitable data wherever necessary and clearly state the assumptions made.
- 3) Diagrams/sketches should be given wherever necessary.
- 4) Use of logarithmic table, drawing instruments and non-programmable calculators is permitted.
- 5) Figures to the right indicate full marks.

**1. Solve.**

(a) Obtain Principal Conjunctive & Disjunctive Normal Form of  $(\neg P \rightarrow R) \wedge (Q \leftrightarrow P)$ . **6**

(b) Show the following equivalence without using truth table. **6**

(i)  $\neg (P \wedge Q) \rightarrow (\neg P \vee (\neg P \vee Q)) \Leftrightarrow (\neg P \vee Q)$

(ii)  $(P \rightarrow C) \wedge (Q \rightarrow C) \Leftrightarrow (P \vee Q) \rightarrow C$



## 2. Solve.

- (a) Let  $R = \{ \langle 1, 2 \rangle, \langle 3, 4 \rangle, \langle 2, 2 \rangle \}$  and  $S = \{ \langle 4, 2 \rangle, \langle 2, 5 \rangle, \langle 3, 1 \rangle, \langle 1, 3 \rangle \}$ . Find  $R \circ S, S \circ R, R \circ (S \circ R), (R \circ S) \circ R, R \circ R, S \circ S$  and  $R \circ R \circ R$  6
- (b) Let  $f: R \rightarrow R$  and  $g: R \rightarrow R$ , where  $R$  is the set of real Numbers. find  $f \circ g$  and  $g \circ f$ , where  $f(x) = x^2 - 2$  and  $g(x) = x + 4$ . state whether these functions are one to one, into and onto. 6

OR

- (c) Write down the composition table for  $\langle Z_7, +_7 \rangle$  and  $\langle Z_7^*, \times_7 \rangle$  where  $Z_7^* = Z_7 - \{ [0] \}$  6

## 3. Solve.

- (a) Find the complement of every element of the Lattice  $\langle S_n, D \rangle$  for  $n = 75$ . 6

OR

- (b) Simplify the following Boolean expressions: 6
- (i)  $(a * b' * c) \oplus (a * b' * c) \oplus (a * b' * c')$ .
- (ii)  $(a * c) \oplus c \oplus [(b \oplus b') * c]$ .
- (c) Expand the following functions into their canonical sum-of-product form. 6
- (i)  $f(a, b, c, d) = xy + yw'z$
- (ii)  $f(a, b, c, d) = w + y'z + x'y$

## 4. Solve.

- (a) The language  $L(G) = \{ a^n b^m c^n \mid n, m \geq 1 \}$  is generated by the grammar  $G = \langle \{S, A, B, C\}, \{a, b\}, S, \emptyset \rangle$  where  $\emptyset$  consist of 6



productions

$S \rightarrow aS$

$S \rightarrow aB$

$B \rightarrow bC$

$C \rightarrow aC$

$C \rightarrow a$

Find the derivation for  $a^3 b a^4$

- (b) Explain the following terms with example  
(i) degree of node (ii) Acyclic graph  
(iii) complete graph (iv) isomorphic graph

6

OR

- (c) Show that in complete binary tree the total number of edges is given by  $2(n_t - 1)$ , where  $n_t$  is the number of terminal nodes.

6

**Solve.**

- (a) Explain finite state machine with suitable example.
- (b) Consider the finite state machine whose state transition table is

6

6

	0	1
$S_0$	$S_0$	$S_1$
$S_1$	$S_1$	$S_2$
$S_2$	$S_2$	$S_3$
$S_3$	$S_3$	$S_0$

- (i) List the values of the transition function for  $w=011001$
- (ii) List the values of the transition function for  $w=1110$



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**Time: 2 Hrs. 30 Min.**

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- 1) All questions are compulsory.
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**1**      Solve:

(a) Obtain the DNF and CNF: **6m**  
 $(\sim P \rightarrow R) \wedge (Q \rightarrow P) \wedge (P \rightarrow Q)$

(b) Show that  $S \vee R$  is tautologically implied by **6m**  
 $(P \vee Q) \wedge (P \rightarrow R) \wedge (Q \rightarrow S)$ , by validity using  
(i) truth table and (ii) rules of inference

**2**      Solve any two:

(a) Let  $A = \{2, 3\}$ ,  $B = \{4, 6, 9\}$  and  $R$  be a relation **6m**  
such that  $a R b$ , if and only if  $a$  is divisor of  $b$ .  
Find domain, range, inverse, compliment, matrix  
and digraph of  $R$  along with the list of degrees.

(b) In a survey of 260 computer science students, the following data were obtained: 94 like to work in USA, 64 like to work in UK, 58 like to work in UAE, 28 like UK and UAE, 26 USA and UK, 22 USA and UAE, and 14 like all the three places. Find how many students like none of the three countries and how many like only USA? 6m

(c) Let  $X=Y=Z=R$  and let  $f: X \rightarrow Y$  and  $g: Y \rightarrow Z$  are defined by  $f(x) = x+1$  and  $g(y) = y^2+2$ . Find  $(g \circ f)$ ,  $(f \circ f)$ ,  $(g \circ g)$  and  $(f \circ g)$  6m

3 Solve:

(a) Obtain SOP & POS form of the given expression in 3 variables:  $x_1 * (x_2' + x_3)$ . 6m

(b) Minimize the given expression using K-Map and design logical diagram for it: 6m

(i)  $F(a,b,c,d) = \sum_m (0,4,5,7,8,12)$

(ii)  $F(w,x,y,z) = \sum_m (0,1,2,4,5,6,8,9,12,13)$

4 Solve any two:

(a) Write short note on: Isomorphic graph, bipartite graph and complete graph 6m

(b) Draw tree for the algebraic expression:  $((a - b) * (c / d)) + e$  and find its infix, prefix and postfix polish expressions along with their values if  $a = 9$ ,  $b = 4$ ,  $c = 6$ ,  $d = 2$  and  $e = 5$ . 6m

(c) What is minimal spanning tree? Explain any one algorithm of it with a proper example. 6m

5 Solve any two:

(a) Design a Finite state acceptor that will accept the set of natural numbers which are divisible by 5. 6m



(b) Consider a grammar: 6m  
 $G = \langle \{E, T\}, \{a, b, c, +, *\}, E, \Phi \rangle$  with productions  
 $E \rightarrow aTb \mid abEb \mid ab \mid a, T \rightarrow bE \mid aTTb$ ;  
Prove that the  $G$  is ambiguous and derive the  
string "ababab"

(c) What is a Turing machine? Elaborate its working 6m  
with a suitable example