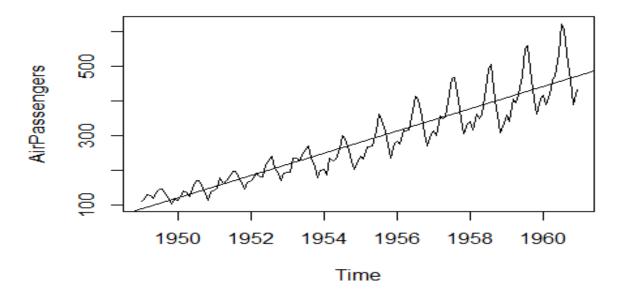
Third Lab Assignment

assignment3.R

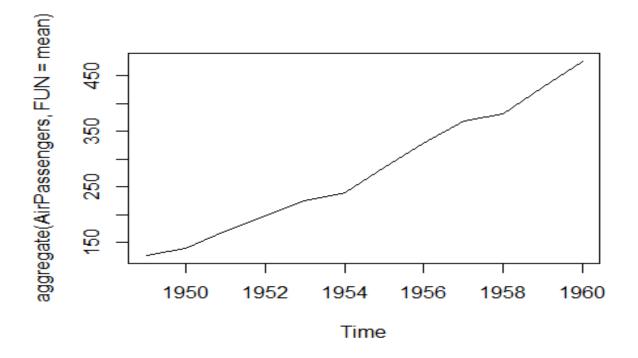
Suraj Durgesht (16EC06)

Fri Apr 26 14:26:26 2019

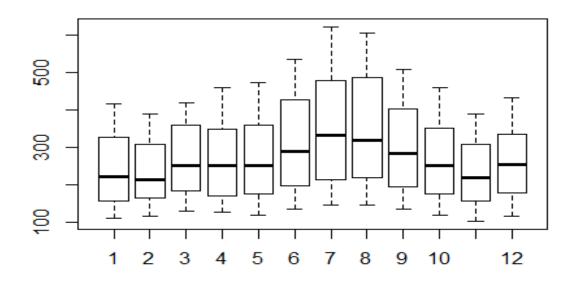
```
# Airpassengers dataset
library(forecast)
library(timeSeries)
data("AirPassengers")
View(AirPassengers)
plot(AirPassengers)
class(AirPassengers)
## [1] "ts"
start(AirPassengers)
## [1] 1949
               1
end(AirPassengers)
## [1] 1960
              12
frequency(AirPassengers)
## [1] 12
summary(AirPassengers)
##
      Min. 1st Qu. Median
                             Mean 3rd Qu.
                                              Max.
##
     104.0
             180.0
                     265.5
                             280.3 360.5
                                             622.0
plot(AirPassengers)
abline(reg=lm(AirPassengers~time(AirPassengers)))
```



```
cycle(AirPassengers)
##
         Jan Feb Mar Apr May Jun Jul Aug Sep Oct Nov Dec
## 1949
           1
                2
                    3
                                  6
                                           8
                                                   10
                                                       11
                                                            12
## 1950
           1
                2
                    3
                             5
                                  6
                                      7
                                           8
                                               9
                                                   10
                                                       11
                                                            12
## 1951
                             5
                                      7
                                           8
                                               9
                2
                    3
                                  6
                                                   10
                                                       11
                                                            12
           1
## 1952
                2
                             5
                                      7
                                           8
                                               9
                                                   10
                                                       11
                                                            12
                    3
                                  6
           1
## 1953
           1
               2
                    3
                             5
                                  6
                                      7
                                           8
                                               9
                                                   10
                                                       11
                                                            12
                                      7
## 1954
           1
               2
                    3
                             5
                                  6
                                           8
                                               9
                                                   10
                                                       11
                                                            12
## 1955
               2
                    3
                             5
                                  6
                                      7
                                           8
                                               9
                                                   10
                                                       11
                                                            12
           1
                        4
                                      7
## 1956
           1
               2
                    3
                             5
                                  6
                                           8
                                               9
                                                   10
                                                       11
                                                            12
                             5
                                      7
                                           8
                                               9
## 1957
               2
                    3
                                  6
                                                   10
           1
                                                       11
                                                            12
                                      7
                                           8
                                               9
               2
## 1958
           1
                                  6
                                                   10
                                                       11
                                                            12
## 1959
                2
                             5
                                  6
                                      7
                                           8
                                               9
                                                            12
           1
                    3
                         4
                                                   10
                                                       11
                             5
                                      7
## 1960
                2
                    3
                                  6
                                           8
                                               9
           1
                                                   10
                                                       11
                                                            12
plot(aggregate(AirPassengers,FUN=mean))
```

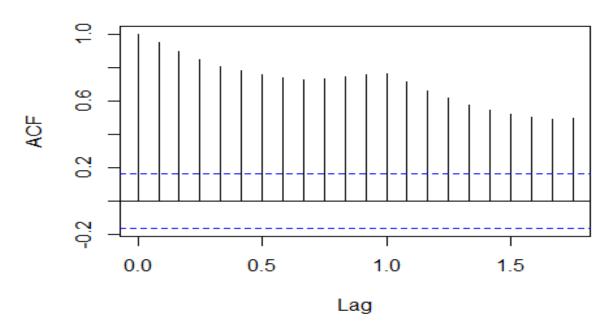


boxplot(AirPassengers~cycle(AirPassengers))



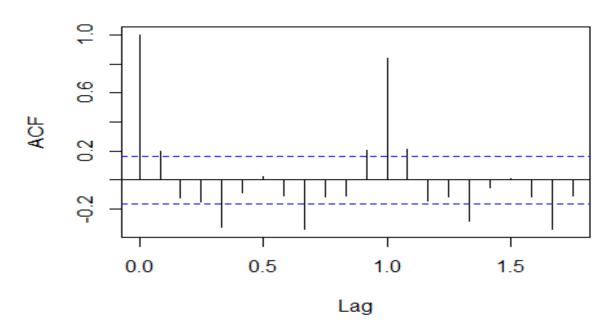
acf(log(AirPassengers))

Series log(AirPassengers)



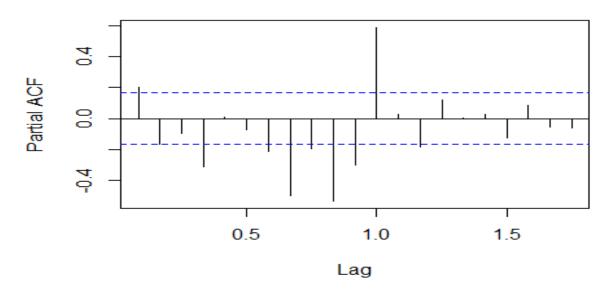
acf(diff(log(AirPassengers)))

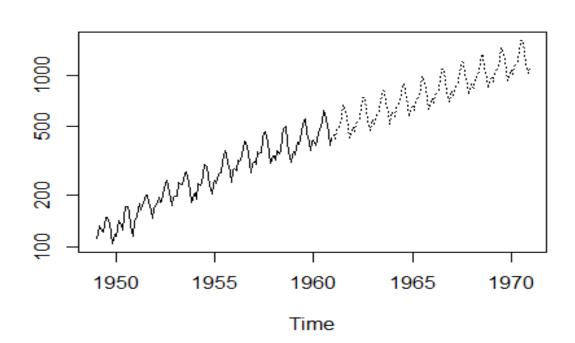
Series diff(log(AirPassengers))



pacf(diff(log(AirPassengers)))

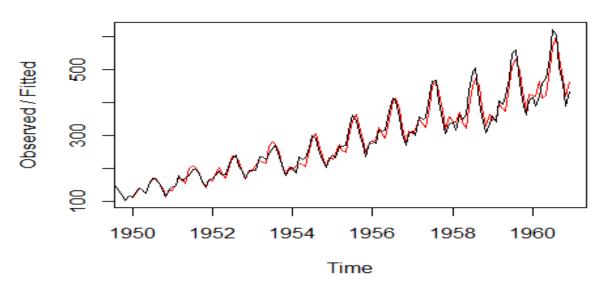
Series diff(log(AirPassengers))



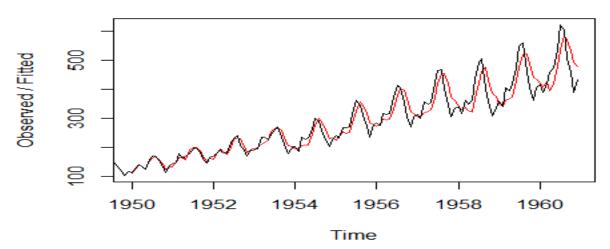


h1 <- HoltWinters(AirPassengers, alpha="0.5", beta=0.3, gamma=0.2, seasonal =
"multiplicative")
plot(h1)</pre>

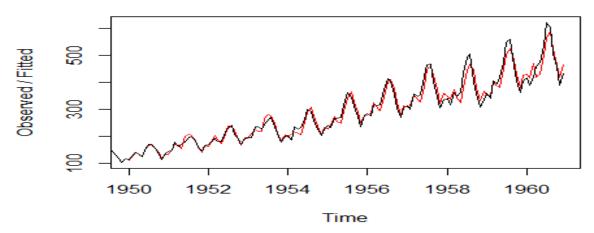
Holt-Winters filtering



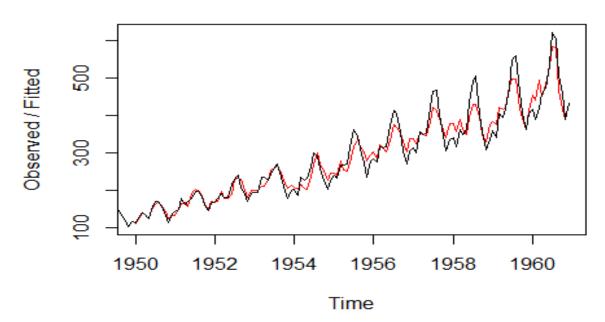
h2 <- HoltWinters(AirPassengers, alpha="0.5", beta=0.3, gamma=0.2, seasonal =
"additive")
plot(h2)</pre>



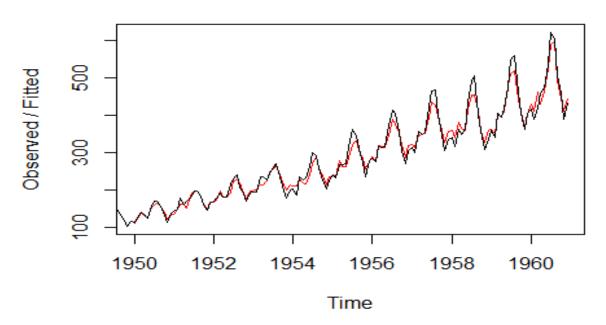
h3 <- HoltWinters(AirPassengers, alpha="0.5", beta=0.3, gamma=NULL, seasonal
= "multiplicative")
plot(h3)</pre>



h3 <- HoltWinters(AirPassengers, alpha="0.5", beta=0.3, gamma=NULL, seasonal
= "additive")
plot(h3)</pre>



h4 <- HoltWinters(AirPassengers, alpha="0.5", beta=NULL, gamma=NULL, seasonal
= "additive")
plot(h4)</pre>

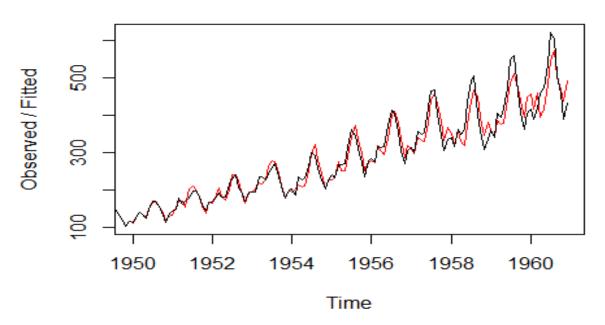


```
predict(h4)
##
             Jan
## 1961 455.7067
predict(h4, n.ahead = 12)
             Jan
                      Feb
                               Mar
                                        Apr
                                                  May
                                                           Jun
## 1961 455.7067 439.3487 488.9996 516.4954 524.6679 582.4770 652.6906
                      Sep
                               0ct
                                        Nov
             Aug
## 1961 631.9450 527.6073 473.0967 412.6361 460.1758
predict(h1, n.ahead = 12)
##
                      Feb
                               Mar
                                        Apr
                                                  May
             Jan
                                                           Jun
## 1961 454.0631 448.3313 517.3658 506.3646 491.2708 543.5584 586.9933
             Aug
                      Sep
                               0ct
                                        Nov
## 1961 566.7703 485.9691 429.5541 376.6006 426.5524
predict(h1, n.ahead = 120)
                               Mar
             Jan
                      Feb
                                        Apr
                                                  May
                                                           Jun
## 1961 454.0631 448.3313 517.3658 506.3646 491.2708 543.5584 586.9933
## 1962 435.7003 430.1390 496.3010 485.6775 471.1318 521.1996 562.7647
## 1963 417.3375 411.9467 475.2362 464.9904 450.9928 498.8407 538.5362
## 1964 398.9747 393.7544 454.1714 444.3033 430.8538 476.4819 514.3076
## 1965 380.6119 375.5621 433.1066 423.6163 410.7148 454.1230 490.0791
## 1966 362.2491 357.3698 412.0417 402.9292 390.5758 431.7642 465.8505
```

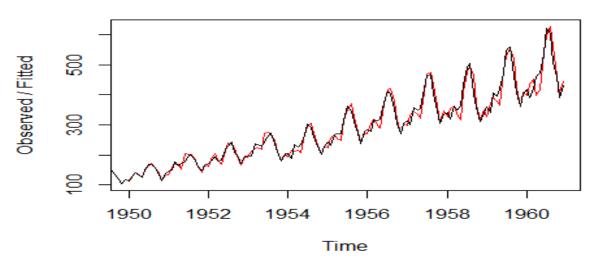
```
## 1967 343.8863 339.1775 390.9769 382.2421 370.4368 409.4053 441.6220
## 1968 325.5235 320.9851 369.9121 361.5550 350.2978 387.0465 417.3934
## 1969 307.1607 302.7928 348.8473 340.8679 330.1588 364.6877 393.1649
## 1970 288.7979 284.6005 327.7825 320.1809 310.0198 342.3288 368.9363
##
             Aug
                      Sep
                               0ct
                                        Nov
                                                 Dec
## 1961 566.7703 485.9691 429.5541 376.6006 426.5524
## 1962 543.2957 465.7714 411.6391 360.8393 408.6381
## 1963 519.8211 445.5737 393.7241 345.0780 390.7237
## 1964 496.3465 425.3761 375.8091 329.3167 372.8094
## 1965 472.8720 405.1784 357.8941 313.5554 354.8951
## 1966 449.3974 384.9808 339.9790 297.7941 336.9807
## 1967 425.9228 364.7831 322.0640 282.0328 319.0664
## 1968 402.4482 344.5855 304.1490 266.2715 301.1520
## 1969 378,9736 324,3878 286,2340 250,5102 283,2377
## 1970 355.4991 304.1902 268.3190 234.7489 265.3234
p1 <- predict(h1, n.ahead = 12)
plot(p1)
```



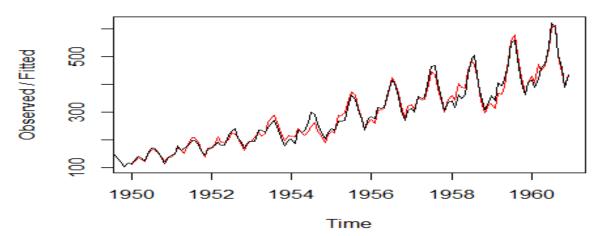
h5 <- HoltWinters(AirPassengers, alpha=0.5, beta=0.5, gamma=0.5, seasonal =
"multiplicative")
plot(h5)</pre>



h5 <- HoltWinters(AirPassengers, alpha=0.75, beta=0.2, gamma=0.1, seasonal =
"multiplicative")
plot(h5)</pre>



h6 <- HoltWinters(AirPassengers, alpha=0.1, beta=0.5, gamma=0.8, seasonal =
"multiplicative")
plot(h6)</pre>



```
m1 <- auto.arima(AirPassengers)
confint(m1)

## 2.5 % 97.5 %

## ar1 0.42190083 0.7700606

## ar2 0.04186402 0.3866851

## ma1 -1.03911157 -0.9246429

tsdiag(m1)
```

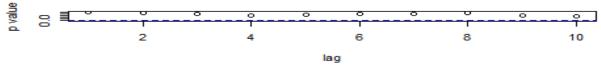
Standardized Residuals



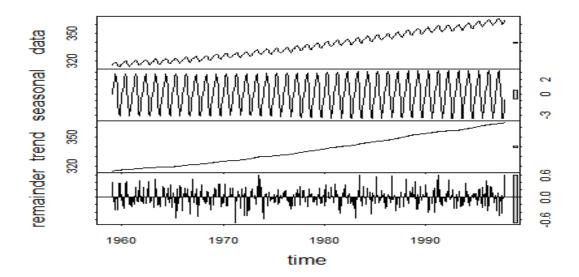
ACF of Residuals



p values for Ljung-Box statistic



```
data("CO2")
m <- stl(co2, s.window = 12)
plot(m)</pre>
```



```
m2 <- auto.arima(co2)
confint(m2)

## 2.5 % 97.5 %

## ar1 -0.01864467 0.5324457

## ma1 -0.82060727 -0.3488421

## sar1 -1.70122774 0.6033431

## sma1 -1.37931560 0.8552593

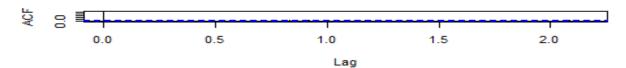
## sma2 -1.45673544 0.4321064

tsdiag(m2)
```

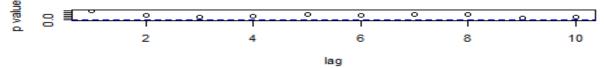
Standardized Residuals



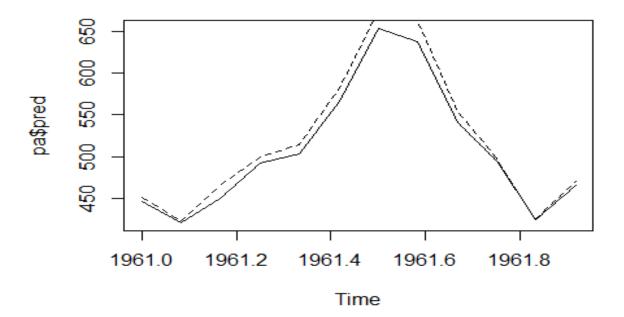
ACF of Residuals



p values for Ljung-Box statistic

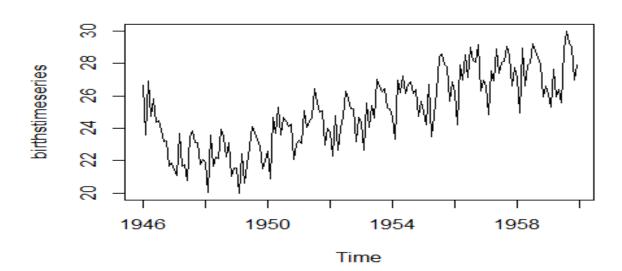


```
# comparing two models, HoltWinters and ARIMA
ph <- predict(h6, n.ahead = 12)
pa <- predict(m1, n.ahead = 12)
plot(pa$pred)
lines(ph, lty="dashed")</pre>
```



```
# time series of the number of births per month in New York city is seasonal
#with a peak every summer and trough every winter
births <- scan("http://robjhyndman.com/tsdldata/data/nybirths.dat")</pre>
View(births)
# To make time series dataset
birthstimeseries <- ts(births, frequency=12, start=c(1946,1))</pre>
start(birthstimeseries)
## [1] 1946
             1
end(birthstimeseries)
## [1] 1959
            12
frequency(birthstimeseries)
## [1] 12
class(birthstimeseries)
```

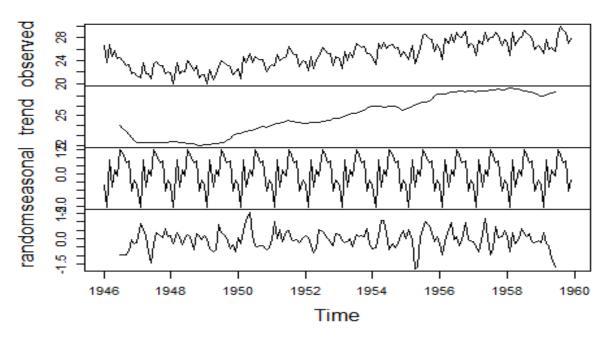
```
## [1] "ts"
cycle(birthstimeseries)
##
         Jan Feb Mar Apr May Jun Jul Aug Sep Oct Nov Dec
                               5
## 1946
            1
                 2
                      3
                          4
                                    6
                                         7
                                              8
                                                   9
                                                       10
                                                            11
                                                                 12
## 1947
            1
                 2
                      3
                               5
                                         7
                                              8
                                                   9
                          4
                                    6
                                                       10
                                                            11
                                                                 12
                                         7
## 1948
                 2
                      3
                               5
                                                   9
                                                                 12
            1
                          4
                                    6
                                              8
                                                       10
                                                            11
## 1949
                 2
                      3
                               5
                                         7
                                                   9
            1
                          4
                                    6
                                              8
                                                       10
                                                            11
                                                                12
## 1950
                 2
                               5
                                         7
                                                   9
                                                                12
            1
                      3
                          4
                                    6
                                              8
                                                       10
                                                            11
                               5
                                         7
                                                   9
## 1951
            1
                 2
                      3
                          4
                                    6
                                              8
                                                       10
                                                            11
                                                                 12
## 1952
                 2
                      3
                               5
                                         7
                                              8
                                                   9
                                                                 12
            1
                          4
                                    6
                                                       10
                                                            11
                                         7
                 2
                               5
                                                   9
## 1953
            1
                      3
                          4
                                    6
                                              8
                                                       10
                                                            11
                                                                 12
                               5
                                         7
                                              8
                                                   9
## 1954
            1
                 2
                      3
                                    6
                                                       10
                                                            11
                                                                12
## 1955
                 2
                               5
                                         7
                                              8
                                                   9
            1
                      3
                                    6
                                                       10
                                                            11
                                                                 12
## 1956
            1
                 2
                      3
                               5
                                    6
                                         7
                                              8
                                                   9
                                                       10
                                                            11
                                                                 12
                 2
                                         7
## 1957
            1
                      3
                          4
                               5
                                    6
                                              8
                                                   9
                                                       10
                                                            11
                                                                 12
                                         7
                 2
                      3
                               5
                                              8
                                                   9
## 1958
            1
                           4
                                    6
                                                       10
                                                            11
                                                                12
                                         7
                                                   9
## 1959
            1
                 2
                      3
                          4
                               5
                                    6
                                              8
                                                       10
                                                            11
                                                                12
plot(birthstimeseries)
```



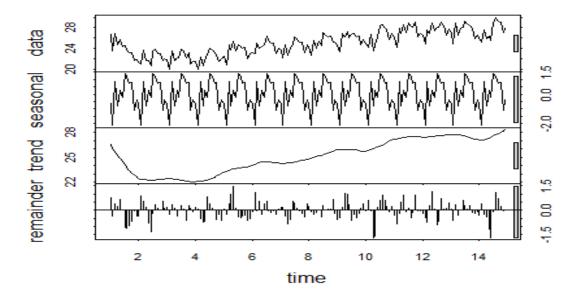
```
# decompose() function
birthstimeseriescomponents <- decompose(birthstimeseries)</pre>
birthstimeseriescomponents$seasonal
##
               Jan
                           Feb
                                      Mar
                                                 Apr
                                                            May
                                                                        Jun
## 1946 -0.6771947 -2.0829607
                                0.8625232 -0.8016787
                                                       0.2516514 -0.1532556
## 1947 -0.6771947 -2.0829607
                                0.8625232 -0.8016787
                                                      0.2516514 -0.1532556
## 1948 -0.6771947 -2.0829607
                                0.8625232 -0.8016787
                                                      0.2516514 -0.1532556
## 1949 -0.6771947 -2.0829607 0.8625232 -0.8016787
                                                      0.2516514 -0.1532556
```

```
## 1950 -0.6771947 -2.0829607
                                0.8625232 -0.8016787
                                                       0.2516514 -0.1532556
## 1951 -0.6771947 -2.0829607
                                0.8625232 -0.8016787
                                                       0.2516514 -0.1532556
  1952 -0.6771947 -2.0829607
                                0.8625232 -0.8016787
                                                       0.2516514 -0.1532556
  1953 -0.6771947 -2.0829607
                                0.8625232 -0.8016787
                                                       0.2516514 -0.1532556
  1954 -0.6771947 -2.0829607
                                0.8625232 -0.8016787
                                                       0.2516514 -0.1532556
  1955 -0.6771947 -2.0829607
                                0.8625232 -0.8016787
                                                       0.2516514 -0.1532556
   1956 -0.6771947 -2.0829607
                                0.8625232 -0.8016787
                                                       0.2516514 -0.1532556
  1957 -0.6771947 -2.0829607
                                0.8625232 -0.8016787
                                                       0.2516514 -0.1532556
## 1958 -0.6771947 -2.0829607
                                0.8625232 -0.8016787
                                                       0.2516514 -0.1532556
## 1959 -0.6771947 -2.0829607
                                0.8625232 -0.8016787
                                                       0.2516514 -0.1532556
##
               Jul
                                      Sep
                                                  0ct
                                                             Nov
                                                                         Dec
                           Aug
                                0.6916162
## 1946
                                           0.7752444 -1.1097652 -0.3768197
         1.4560457
                    1.1645938
## 1947
         1.4560457
                    1.1645938
                                0.6916162
                                           0.7752444 -1.1097652 -0.3768197
## 1948
         1.4560457
                    1.1645938
                                0.6916162
                                           0.7752444 -1.1097652 -0.3768197
## 1949
         1.4560457
                    1.1645938
                                0.6916162
                                           0.7752444 -1.1097652 -0.3768197
## 1950
         1.4560457
                    1.1645938
                                0.6916162
                                           0.7752444 -1.1097652 -0.3768197
## 1951
         1.4560457
                    1.1645938
                                0.6916162
                                           0.7752444 -1.1097652 -0.3768197
## 1952
                                           0.7752444 -1.1097652 -0.3768197
         1.4560457
                    1.1645938
                                0.6916162
## 1953
         1.4560457
                    1.1645938
                                0.6916162
                                           0.7752444 -1.1097652 -0.3768197
## 1954
         1.4560457
                    1.1645938
                                0.6916162
                                           0.7752444 -1.1097652 -0.3768197
## 1955
                                0.6916162
                                           0.7752444 -1.1097652 -0.3768197
         1.4560457
                    1.1645938
## 1956
         1.4560457
                    1.1645938
                                0.6916162
                                           0.7752444 -1.1097652 -0.3768197
## 1957
         1.4560457
                    1.1645938
                                0.6916162
                                           0.7752444 -1.1097652 -0.3768197
## 1958
         1.4560457
                    1.1645938
                                0.6916162
                                           0.7752444 -1.1097652 -0.3768197
## 1959
         1.4560457
                    1.1645938
                                0.6916162
                                           0.7752444 -1.1097652 -0.3768197
plot(birthstimeseriescomponents)
```

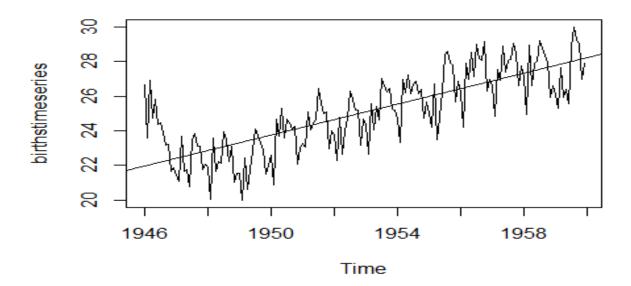
Decomposition of additive time series



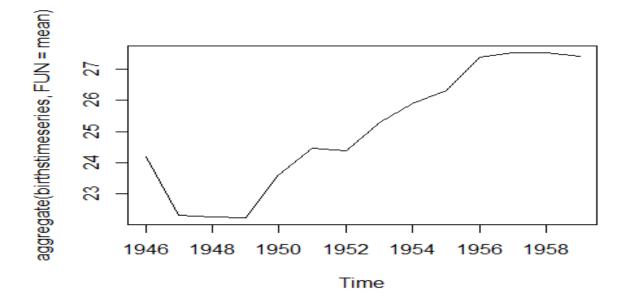
```
# stl function
ts_beer = ts(birthstimeseries, frequency = 12)
stl_beer = stl(ts_beer, "periodic")
plot(stl_beer)
```



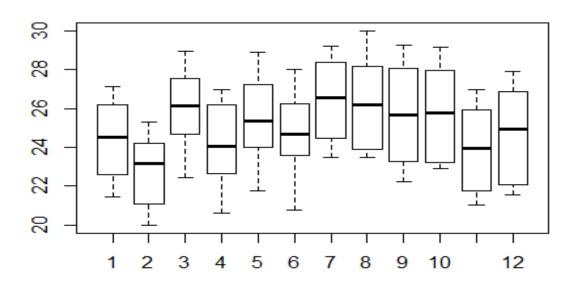
```
# regression line linear model
plot(birthstimeseries)
abline(reg = lm(birthstimeseries~time(birthstimeseries)))
```



plot(aggregate(birthstimeseries, FUN = mean))

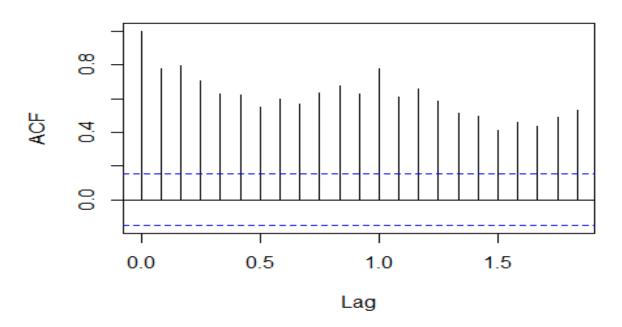


monthly boxplot
boxplot(birthstimeseries~cycle(birthstimeseries))



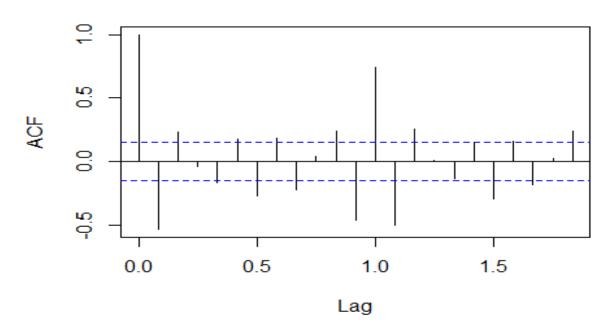
auto corelation function, partial corelation function
acf(log(birthstimeseries))

Series log(birthstimeseries)



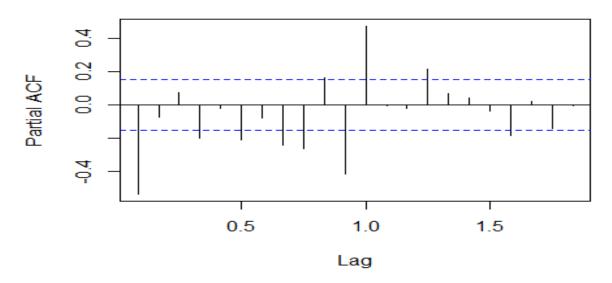
acf(diff(log(birthstimeseries)))

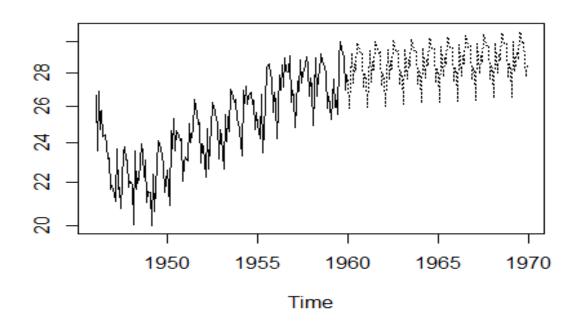
Series diff(log(birthstimeseries))



pacf(diff(log(birthstimeseries)))

Series diff(log(birthstimeseries))



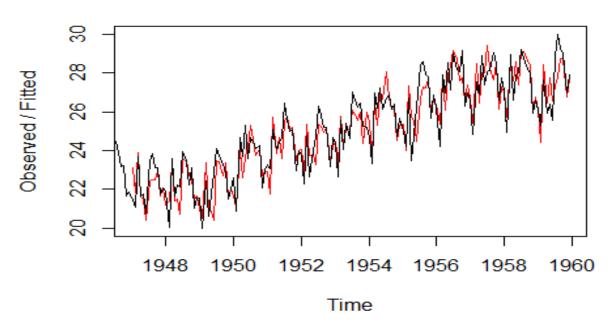


```
birthstimeseriesforecasts <- HoltWinters(birthstimeseries)</pre>
birthstimeseriesforecasts
## Holt-Winters exponential smoothing with trend and additive seasonal
component.
##
## Call:
## HoltWinters(x = birthstimeseries)
##
## Smoothing parameters:
## alpha: 0.4823655
## beta: 0.02988495
## gamma: 0.563186
##
## Coefficients:
##
              [,1]
## a
       28.04366357
## b
       0.04199921
## s1 -0.78546221
      -2.19944507
## s2
## s3
        0.87813012
## s4
      -0.65164728
## s5
       0.63427267
## s6
        0.21182821
## s7
        2.23177191
## s8
        2.17167733
## s9
        1.52077678
## s10
       1.16900861
## s11 -0.97500043
## s12 -0.18636055
birthstimeseriesforecasts$fitted
##
                xhat
                        level
                                      trend
                                                 season
## Jan 1947 23.13579 23.81055 -0.1567618007 -0.51798958
## Feb 1947 21.83089 22.83531 -0.1812218860 -0.82319792
## Mar 1947 23.90724 22.29623 -0.1919165635 1.80292708
## Apr 1947 21.58463 22.00869 -0.1947742244 -0.22928125
## May 1947 21.51602 21.85461 -0.1935580066 -0.14503125
## Jun 1947 20.43661 21.77488 -0.1901562399 -1.14811458
## Jul 1947 22.44490 21.74120 -0.1854799895 0.88917708
## Aug 1947 22.51935 22.05453 -0.1705728887
                                             0.63538542
## Sep 1947 22.50969 22.51328 -0.1517657072 0.14817708
## Oct 1947 22.96787 22.64867 -0.1431840736 0.46238542
## Nov 1947 21.63717 22.57404 -0.1411352421 -0.79573958
## Dec 1947 22.07360 22.49168 -0.1393790022 -0.27869792
## Jan 1948 21.19997 22.35201 -0.1393876391 -1.01264664
## Feb 1948 21.39990 22.56814 -0.1287630591 -1.03947671
## Mar 1948 23.37769 21.78099 -0.1484386874 1.74513652
## Apr 1948 21.38490 21.73497 -0.1453781694 -0.20468564
```

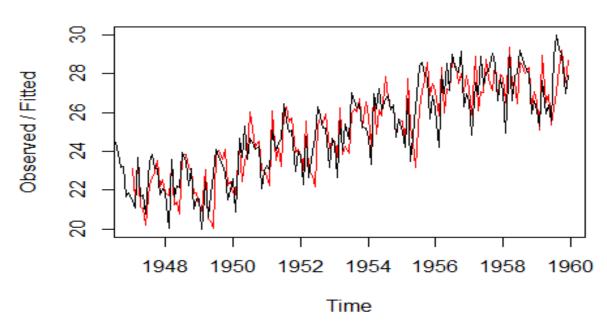
```
## May 1948 21.51060 21.72807 -0.1412395136 -0.07623722
## Jun 1948 20.74546 21.92999 -0.1309843042 -1.05354663
## Jul 1948 23.54300 22.46348 -0.1111264103 1.19064384
## Aug 1948 23.45914 22.54868 -0.1052593374 1.01572363
## Sep 1948 22.68217 22.46506 -0.1046127180 0.32172372
## Oct 1948 22.53900 22.14619 -0.1110156146 0.50381900
## Nov 1948 21.46350 22.32605 -0.1023230358 -0.76022309
## Dec 1948 21.64158 22.02861 -0.1081540864 -0.27887258
## Jan 1949 20.98044 21.88737 -0.1091426894 -0.79778543
## Feb 1949 20.51366 22.05200 -0.1009610948 -1.43737755
## Mar 1949 23.40193 21.70327 -0.1083657450 1.80702947
## Apr 1949 20.87973 21.12318 -0.1224630574 -0.12098948
## May 1949 20.87790 20.87302 -0.1262792355 0.13115420
## Jun 1949 20.40721 21.17272 -0.1135488865 -0.65195982
## Jul 1949 23.48037 22.24907 -0.0779889821
                                            1.30929384
## Aug 1949 23.43170 22.47189 -0.0689990677 1.02880023
## Sep 1949 22.68327 22.55547 -0.0644393843 0.19223775
## Oct 1949 23.39370 22.77019 -0.0560966877
## Nov 1949 21.53807 22.47933 -0.0631127424 -0.87814461
## Dec 1949 22.04476 22.40701 -0.0633876120 -0.29886513
## Jan 1950 21.63809 22.33409 -0.0636724899 -0.63232879
## Feb 1950 21.09947 22.73634 -0.0497484903 -1.58712202
## Mar 1950 24.05671 22.58748 -0.0527104614 1.52193909
## Apr 1950 22.59204 22.83398 -0.0437686872 -0.19816416
## May 1950 23.67204 23.31162 -0.0281862050 0.38860044
## Jun 1950 24.14110 24.07836 -0.0044300653 0.06716922
## Jul 1950 25.28334 23.80472 -0.0124752973
                                            1.49109716
## Aug 1950 24.59658 23.49687 -0.0213025088
                                            1.12101085
## Sep 1950 23.74439 23.40679 -0.0233578809
                                             0.36095236
## Oct 1950 24.08539 23.56558 -0.0179144329
                                             0.53772340
## Nov 1950 22.72882 23.62803 -0.0155126980 -0.88370330
## Dec 1950 22.97205 23.30148 -0.0248080600 -0.30462622
## Jan 1951 22.91054 23.28582 -0.0245348767 -0.35074332
## Feb 1951 21.77674 23.44287 -0.0191080068 -1.64702205
## Mar 1951 25.73946 24.03746 -0.0007678348
                                            1.70276886
## Apr 1951 23.82329 23.71666 -0.0103319146
                                            0.11696086
## May 1951 24.67119 23.80942 -0.0072511778
                                            0.86902159
## Jun 1951 23.57957 23.68582 -0.0107279825 -0.09552975
## Jul 1951 25.51717 24.19964 0.0049478806 1.31258419
## Aug 1951 25.75289 24.65503
                             0.0184094962
                                            1.07944500
## Sep 1951 25.09588 24.60838 0.0164650350
                                            0.47103538
## Oct 1951 25.18693 24.58535
                              0.0152847303
                                             0.58629375
## Nov 1951 23.50602 24.56353
                              0.0141758088 -1.07168370
## Dec 1951 24.02351 24.31625
                              0.0063623670 -0.29910163
## Jan 1952 24.06686 24.30211
                              0.0057495433 -0.24099556
## Feb 1952 22.90391 24.17817
                              0.0018737848 -1.27612819
## Mar 1952 25.37635 23.87426 -0.0072643681
                                            1.50935418
## Apr 1952 23.74026 23.57693 -0.0159331572 0.17926269
## May 1952 23.80016 23.03316 -0.0317073795 0.79871006
## Jun 1952 23.28454 23.09206 -0.0289996476 0.22148371
```

```
## Jul 1952 25.34043 23.76368 -0.0080618116
                                             1.58481886
## Aug 1952 25.25245 24.20690
                              0.0054248405
                                             1.04012210
## Sep 1952 24.94488 24.48416
                               0.0135487385
                                             0.44716604
## Oct 1952 25.20684 24.62560
                               0.0173706022
                                             0.56386800
                               0.0172576413 -1.22969517
## Nov 1952 23.42675 24.63919
## Dec 1952 24.23069 24.52874
                               0.0134411353 -0.31149478
## Jan 1953 24.47287 24.77194
                               0.0203074314 -0.31937515
## Feb 1953 23.29754 24.73973
                               0.0187380145 -1.46092934
## Mar 1953 25.78659 24.44322
                               0.0093169443 1.33404499
## Apr 1953 24.21204 24.34566
                               0.0061226848 -0.13973989
## May 1953 25.13683 24.27940
                               0.0039598150
                                             0.85346860
## Jun 1953 25.07837 24.42526
                               0.0082003678
                                             0.64491022
## Jul 1953 26.07896 24.21959
                               0.0018089646
                                             1.85755984
## Aug 1953 25.88965 24.67002
                               0.0152158893
                                             1.20441194
## Sep 1953 25.58078 25.03078
                               0.0255424312
                                             0.52445571
## Oct 1953 25.98485 25.38781
                               0.0354490591
                                             0.56158359
## Nov 1953 24.38888 25.65343
                               0.0423274418 -1.30687649
## Dec 1953 25.99125 26.10920
                               0.0546832789 -0.17263746
## Jan 1954 25.46444 25.77257
                               0.0429887904 -0.35111351
## Feb 1954 23.80597 25.42607
                               0.0313491415 -1.65145193
## Mar 1954 26.50885 25.21529
                               0.0241130038
                                             1.26944738
## Apr 1954 25.31509 25.46763
                               0.0309336920 -0.18347968
## May 1954 26.90784 25.92494
                               0.0436757055
                                             0.93922543
## Jun 1954 26.67805 26.11436
                               0.0480315233
                                             0.51565667
## Jul 1954 28.06288 25.89418
                               0.0400157587
                                             2.12868849
## Aug 1954 26.71338 25.27968
                               0.0204556986
                                             1.41324592
## Sep 1954 26.12717 25.37954
                               0.0228287611
                                             0.72479775
## Oct 1954 26.13822 25.41435
                               0.0231867253
                                             0.70068534
## Nov 1954 24.52333 25.55368
                               0.0266576761 -1.05700401
## Dec 1954 25.29159 25.67134
                               0.0293774065 -0.40913547
## Jan 1955 25.34053 25.89194
                               0.0350919130 -0.58650249
## Feb 1955 23.99020 25.75795
                               0.0300389027 -1.79778857
## Mar 1955 27.34901 25.90800
                               0.0336255059
                                             1.40738237
## Apr 1955 25.73747 25.63870
                               0.0245724784
                                             0.07420246
## May 1955 25.59120 24.57193 -0.0080421066
                                             1.02731327
## Jun 1955 24.49995 24.16632 -0.0199233622
                                             0.35355362
## Jul 1955 26.71359 24.97561
                               0.0048575211
                                             1.73312479
## Aug 1955 27.26496 25.77512
                               0.0286057075
                                             1.46123643
## Sep 1955 27.22709 26.44722
                               0.0478365034
                                             0.73203687
## Oct 1955 27.65501 26.82640
                               0.0577385980
                                             0.77087848
## Nov 1955 26.00395 26.94635
                               0.0595980033 -1.00200282
## Dec 1955 26.61751 26.85596
                               0.0551155314 -0.29357082
## Jan 1956 26.40840 27.03818
                               0.0589139317 -0.68868968
## Feb 1956 25.33566 27.00477
                               0.0561547942 -1.72525658
## Mar 1956 27.78614 26.52180
                               0.0400431456
                                            1.22430271
## Apr 1956 26.08004 26.62351
                               0.0418862542 -0.58536330
## May 1956 27.93893 27.09710
                               0.0547875612
                                             0.78703827
## Jun 1956 28.35352 27.43555
                               0.0632649298
                                             0.85469819
## Jul 1956 29.17212 26.91298
                               0.0457570914
                                             2.21338510
## Aug 1956 28.76019 26.86703 0.0430164218 1.85014141
```

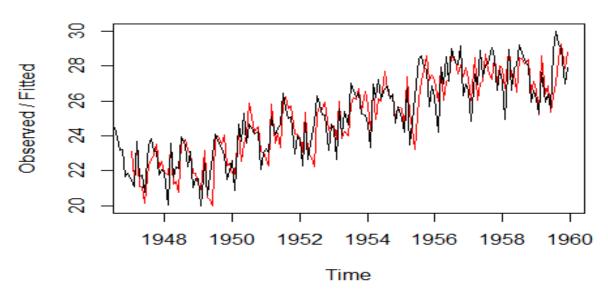
```
## Sep 1956 27.59166 26.62488 0.0344942058
                                             0.93228724
## Oct 1956 27.73302 26.88335 0.0411879146
                                             0.80848129
## Nov 1956 26.57005 27.60129 0.0614124953 -1.09265199
## Dec 1956 27.36873 27.52810
                              0.0573898623 -0.21675566
                              0.0518870166 -0.74448780
## Jan 1957 26.70875 27.40135
## Feb 1957 25.39455 27.39548
                              0.0501607281 -2.05108295
## Mar 1957 28.48586 27.18200
                              0.0422819008 1.26157596
## Apr 1957 26.47371 26.76948
                              0.0286901907 -0.32445977
## May 1957 27.99512 27.00187
                               0.0347777126 0.95847636
## Jun 1957 28.01066 27.46252
                               0.0475048213
                                             0.50063663
## Jul 1957 29.40715 27.21064
                              0.0385577620
                                            2.15796045
## Aug 1957 28.29879 26.60179
                              0.0192099671
                                            1.67779637
## Sep 1957 27.62947 26.54488
                              0.0169353277
                                             1.06765432
## Oct 1957 28.50093 27.24607
                               0.0373840821
                                            1.21748361
## Nov 1957 26.13842 27.27528
                               0.0371399679 -1.17400182
## Dec 1957 27.26772 27.55147
                               0.0442839832 -0.32803988
## Jan 1958 27.09278 27.82116
                              0.0510200910 -0.77939858
## Feb 1958 25.73227 27.89110
                              0.0515854734 -2.21041672
                              0.0399339466 0.98671039
## Mar 1958 28.57945 27.55280
## Apr 1958 27.62186 27.77775
                              0.0454630421 -0.20135163
## May 1958 28.57143 27.32500
                                            1.21585707
                              0.0305738671
## Jun 1958 27.38769 27.04665
                              0.0213418113
                                             0.31969997
## Jul 1958 29.16468 27.36769
                              0.0302982619
                                            1.76668940
## Aug 1958 29.09204 27.42901
                               0.0312255063
                                             1.63179627
## Sep 1958 28.80721 27.29959
                              0.0264246263
                                             1.48119011
## Oct 1958 28.36518 27.13201
                              0.0206265839
                                            1.21254688
                              0.0145694775 -1.02952818
## Nov 1958 25.93499 26.94995
## Dec 1958 26.77585 26.95343
                              0.0142379999 -0.19181536
## Jan 1959 26.13602 26.89201
                              0.0119768814 -0.76796484
## Feb 1959 24.44010 26.87503
                              0.0111116615 -2.44604591
## Mar 1959 28.41601 27.29418
                             0.0233057207
                                            1.09852546
## Apr 1959 26.46276 26.95281 0.0124074859 -0.50245588
## May 1959 27.75255 26.71836 0.0050301842
                                            1.02915692
## Jun 1959 26.55633 26.07000 -0.0144962780
                                            0.50082655
## Jul 1959 27.33398 25.57732 -0.0287868334
                                            1.78544109
## Aug 1959 27.81504 26.28705 -0.0067164116
                                            1.53470793
## Sep 1959 28.72300 27.33428 0.0247808156 1.36393612
## Oct 1959 28.74117 27.61858
                             0.0325363622 1.09005383
## Nov 1959 26.78196 27.78175 0.0364405634 -1.03623166
## Dec 1959 27.72144 27.91951 0.0394683600 -0.23754203
plot(birthstimeseriesforecasts)
```



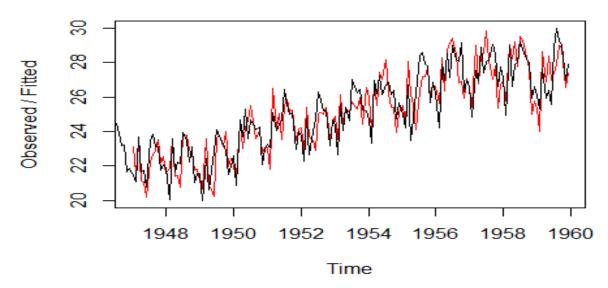
h1 <- HoltWinters(birthstimeseries, alpha="0.5", beta=0.3, gamma=0.2,
seasonal = "multiplicative")
plot(h1)</pre>



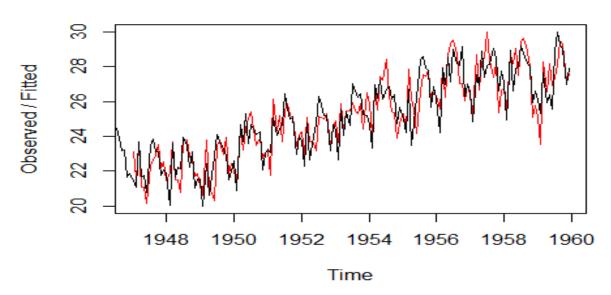
```
h2 <- HoltWinters(birthstimeseries, alpha="0.5", beta=0.3, gamma=0.2,
seasonal = "additive")
plot(h2)</pre>
```



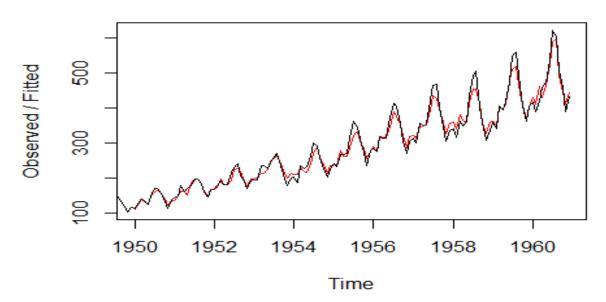
h3 <- HoltWinters(birthstimeseries, alpha="0.5", beta=0.3, gamma=NULL,
seasonal = "multiplicative")
plot(h3)</pre>



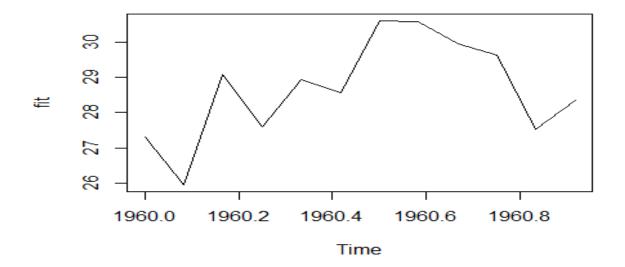
```
h3 <- HoltWinters(birthstimeseries, alpha="0.5", beta=0.3, gamma=NULL,
seasonal = "additive")
plot(h3)</pre>
```



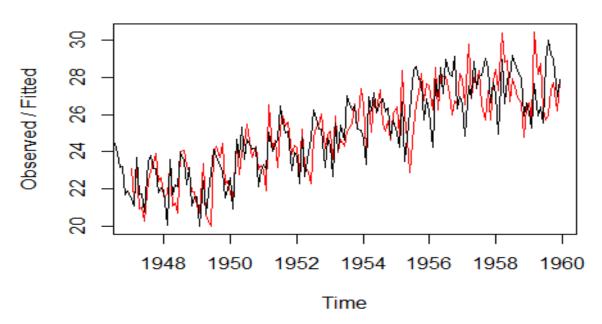
h1 <- HoltWinters(birthstimeseries, alpha="0.5", beta=NULL, gamma=NULL,
seasonal = "additive")
plot(h4)</pre>



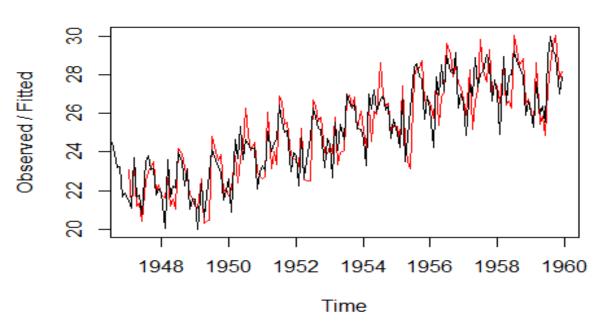
```
predict(h4)
##
             Jan
## 1961 455.7067
predict(h4, n.ahead = 12)
                      Feb
##
             Jan
                               Mar
                                        Apr
                                                  May
                                                           Jun
                                                                    Jul
## 1961 455.7067 439.3487 488.9996 516.4954 524.6679 582.4770 652.6906
                      Sep
                               0ct
                                        Nov
                                                  Dec
             Aug
## 1961 631.9450 527.6073 473.0967 412.6361 460.1758
predict(h1, n.ahead = 12)
                      Feb
##
             Jan
                               Mar
                                        Apr
                                                  May
                                                           Jun
                                                                    Jul
## 1960 27.30973 25.94509 29.07503 27.59975 28.93623 28.55882 30.61298
                      Sep
                               0ct
                                        Nov
                                                  Dec
             Aug
## 1960 30.57737 29.95399 29.63707 27.53124 28.36080
predict(h1, n.ahead = 120)
##
             Jan
                      Feb
                               Mar
                                        Apr
                                                  May
                                                           Jun
                                                                    Jul
## 1960 27.30973 25.94509 29.07503 27.59975 28.93623 28.55882 30.61298
## 1961 27.80938 26.44473 29.57468 28.09939 29.43587 29.05847 31.11262
## 1962 28.30902 26.94438 30.07432 28.59904 29.93552 29.55811 31.61226
## 1963 28.80866 27.44402 30.57397 29.09868 30.43516 30.05776 32.11191
## 1964 29.30831 27.94367 31.07361 29.59833 30.93481 30.55740 32.61155
## 1965 29.80795 28.44331 31.57325 30.09797 31.43445 31.05704 33.11120
## 1966 30.30760 28.94295 32.07290 30.59761 31.93409 31.55669 33.61084
## 1967 30.80724 29.44260 32.57254 31.09726 32.43374 32.05633 34.11048
## 1968 31.30688 29.94224 33.07218 31.59690 32.93338 32.55597 34.61013
## 1969 31.80653 30.44188 33.57183 32.09655 33.43303 33.05562 35.10977
                               0ct
##
             Aug
                      Sep
                                        Nov
                                                  Dec
## 1960 30.57737 29.95399 29.63707 27.53124 28.36080
## 1961 31.07702 30.45364 30.13671 28.03089 28.86045
## 1962 31.57666 30.95328 30.63636 28.53053 29.36009
## 1963 32.07630 31.45292 31.13600 29.03017 29.85974
## 1964 32.57595 31.95257 31.63565 29.52982 30.35938
## 1965 33.07559 32.45221 32.13529 30.02946 30.85902
## 1966 33.57523 32.95186 32.63493 30.52910 31.35867
## 1967 34.07488 33.45150 33.13458 31.02875 31.85831
## 1968 34.57452 33.95114 33.63422 31.52839 32.35796
## 1969 35.07417 34.45079 34.13386 32.02804 32.85760
p1 <- predict(h1, n.ahead = 12)
plot(p1)
```



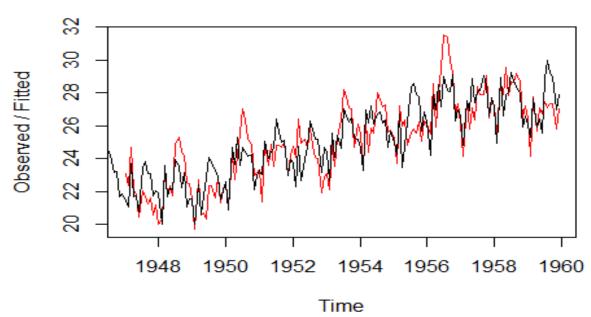
h5 <- HoltWinters(birthstimeseries, alpha=0.5, beta=0.5, gamma=0.5, seasonal
= "multiplicative")
plot(h5)</pre>



h5 <- HoltWinters(birthstimeseries, alpha=0.75, beta=0.2, gamma=0.1, seasonal
= "multiplicative")
plot(h5)</pre>

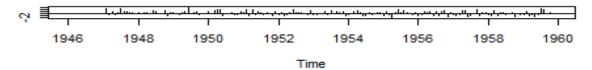


h6 <- HoltWinters(birthstimeseries, alpha=0.1, beta=0.5, gamma=0.8, seasonal
= "multiplicative")
plot(h6)</pre>



```
m1 <- auto.arima(birthstimeseries)</pre>
confint(m1)
##
              2.5 %
                         97.5 %
## ar1
         0.06514048
                    1.24260156
## ar2
       -0.93009076
                     0.02204818
       -1.35815024 -0.09294612
## ma1
## ma2 -0.31106945 0.81745702
## sar1 -0.43580962 -0.04963254
## sma1 -1.04013427 -0.65012924
tsdiag(m1)
```

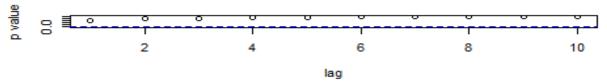
Standardized Residuals



ACF of Residuals



p values for Ljung-Box statistic



```
# comparing two models, HoltWinters and ARIMA
ph <- predict(h6, n.ahead = 12)
pa <- predict(m1, n.ahead = 12)
plot(pa$pred)
lines(ph, lty="dashed")</pre>
```

