

# Lab 4

```
M = {{a}, {b, b}, {a, a, a}, {a, a, b}, {a, b, b},  
      {a, a, a, b}, {a, a, b, a}, {a, a, b, a, b}, {a, a, b, b, b}};
```

```
Prefixes[M_] := Module[{list, i, aux},  
  módulo  
  list = {{}}; aux = M;  
  For[i = 1, i ≤ Length[aux], i++,  
    para cada longitud  
    While[Length[aux[[i]]] > 0, AppendTo[list, aux[[i]]];  
      mientras longitud añade al final  
      aux[[i]] = Drop[aux[[i]], -1];];  
    elimina  
  Return[Union[list]]];  
  retorna unión
```

## Exercise 1 - Longest suffix of u contained in M

```
LongestSuffix[u_, M_] := Module[{i, word},  
  módulo  
  word = u;  
  While[Length[word] > 0 && ! MemberQ[M, word], word = Rest[word];];  
  mientras longitud ¿contenido en? todos excepto el prin  
  If[MemberQ[M, word], Return[word], Return[False]];  
  si ¿contenido en? retorna retorna falso  
];
```

```
LongestSuffix[{}, M]
```

```
False
```

## Exercise 2 - Generate a dictionary automaton for M

```
DictionaryAutomaton[M_] := Module[{A, s, i, j},
  (*Automaton: {Q, Σ, δ, q₀, F}*)
  A = {Prefixes[M], Union[Flatten[M]], {}, {}, M};
  (*Generate list of transitions: for all states try to add each letter*)
  For[i = 1, i ≤ Length[A[[1]]], i++,
    For[j = 1, j ≤ Length[A[[2]]], j++,
      AppendTo[A[[3]],
        {A[[1, i]], A[[2, j]], LongestSuffix[Append[A[[1, i]], A[[2, j]]], A[[1]]}]
    ];
  ];
  (*Add to F any state of Q whose suffix is included in F*)
  If[i > 1 && ! LongestSuffix[Rest[A[[1, i]]], A[[5]]] ≠ False,
    (*TRUE*), (*FALSE*), (*SCHRÖDINGER*) AppendTo[A[[5]], A[[1, i]]];
  ];
  A[[5]] = Union[A[[5]]];
  Return[A];
];
```

DictionaryAutomaton[M]

```
{{ {}, {a}, {b}, {a, a}, {a, b}, {b, b}, {a, a, a}, {a, a, b}, {a, b, b},
  {a, a, a, b}, {a, a, b, a}, {a, a, b, b}, {a, a, b, a, b}, {a, a, b, b, b}, {a, b},
  {{ {}, a, {a}}, {{ }, b, {b}}, {{a}, a, {a, a}}, {{a}, b, {a, b}}, {{b}, a, {a}},
  {{b}, b, {b, b}}, {{a, a}, a, {a, a, a}}, {{a, a}, b, {a, a, b}}, {{a, b}, a, {a}},
  {{a, b}, b, {a, b, b}}, {{b, b}, a, {a}}, {{b, b}, b, {b, b}}, {{a, a, a}, a, {a, a, a}},
  {{a, a, a}, b, {a, a, a, b}}, {{a, a, b}, a, {a, a, b, a}}, {{a, a, b}, b, {a, a, b, b}},
  {{a, b, b}, a, {a}}, {{a, b, b}, b, {b, b}}, {{a, a, a, b}, a, {a, a, b, a}},
  {{a, a, a, b}, b, {a, a, b, b}}, {{a, a, b, a}, a, {a, a}}, {{a, a, b, a}, b, {a, a, b, a, b}},
  {{a, a, b, b}, a, {a}}, {{a, a, b, b}, b, {a, a, b, b, b}}, {{a, a, b, a, b}, a, {a}},
  {{a, a, b, a, b}, b, {a, b, b}}, {{a, a, b, b, b}, a, {a}}, {{a, a, b, b, b}, b, {b, b}},
  {}, {{a}, {a, a}, {b, b}, {a, a, a}, {a, a, b}, {a, b, b}, {a, a, a, b},
  {a, a, b, a}, {a, a, b, b}, {a, a, b, a, b}, {a, a, b, b, b}}}
```

## Exercise 3 - Analyze a word using a dictionary automaton

```

ScanWordDictionary[A_, x_] := Module[{state, i, curr, pos, s},
    (*módulo*)

    state = A[[4]];
    pos = {};
    For[i = 1, i ≤ Length[x], i++,
        (*para cada longitud*)
        state = Cases[A[[3]], {state, x[[i]], _}][[1, 3]];
        (*casos*)
        If[MemberQ[A[[5]], state],
            (*si ¿contenido en?*)
            (*AppendTo[pos, i - Length[state] + 1]; *)
            (*añade al final longitud*)
            For[s = state,
                (*para cada*)
                Length[s] ≥ Length[A[[5, 1]]], s = LongestSuffix[Rest[s], A[[5]]],
                (*longitud longitud todos excepto el primero*)
                If[s, (*TRUE*), Break; AppendTo[pos, i - Length[s] + 1];]
                (*si finaliza i añade al final longitud*)
            ];
        ];
    ];
    Return[Sort[pos]];
    (*retorna ordena*)
];

```

```
ScanWordDictionary[DictionaryAutomaton[M], {a, a, b, a, a, a}]
```

```
{ {1, {a}}, {1, {a, a}}, {1, {a, a, b}}, {1, {a, a, b, a}}, {2, {a}},
  {4, {a}}, {4, {a, a}}, {4, {a, a, a}}, {5, {a}}, {5, {a, a}}, {6, {a}} }
```

```

ScanWordDictionaryPro[M_, x_] := Module[{A, state, i, curr, pos, s},
    A = DictionaryAutomaton[M];
    state = A[[4]];
    pos = {};
    For[i = 1, i ≤ Length[x], i++,
        state = Cases[A[[3]], {state, x[[i]], _}][[1, 3]];
        If[MemberQ[A[[5]], state],
            For[s = state, Length[s] ≥ Length[A[[5, 1]]], s = LongestSuffix[Rest[s], M],
                If[MemberQ[M, s],
                    AppendTo[pos, {i - Length[s] + 1, s, i}];
                    AppendTo[err, {s, False}]; Break;
                    AppendTo[err, {s, "Other"}]; Break;
                ];
            ];
        ];
    Return[pos];

ScanWordDictionaryPro[M, {a, a, b, a, a, a}]
{{1, {a}, 1}, {2, {a}, 2}, {1, {a, a, b}, 3}, {1, {a, a, b, a}, 4},
{4, {a}, 4}, {5, {a}, 5}, {4, {a, a, a}, 6}, {6, {a}, 6}}

```

## Testing

```

err = {}
{}

err
{{{a, a}, False}, {{a, a}, False}}

state = {a, a}; A = DictionaryAutomaton[M]; pos = {};

s = state
{a, a}

Length[s] ≥ Length[A[[5, 1]]]
True

```

**s**

{a, a}

**If[s, , False, AppendTo[pos, i - Length[s] + 1]]**

si falso añade al final longitud

{0}

**s = LongestSuffix[s, A[[5]]]**

{a, a}

**M**

{ {a}, {b, b}, {a, a, a}, {a, a, b}, {a, b, b},  
{a, a, a, b}, {a, a, b, a}, {a, a, b, a, b}, {a, a, b, b, b} }

**A = DictionaryAutomaton[M]; x = {a, a}; state = A[[4]]**

{}

**i = 1;**

**i ≤ Length[x]**

longitud

True

**state = Cases[A[[3]], {{a, a, b, a}, a, \_}][[1, 3]]**

casos

{a, a}

**MemberQ[A[[5]], state]**

¿contenido en?

False

**state**

{{ {}, a, {a} }}

**state[[1]]**

{{ }, a, {a} }

**! {a, a} ≠ False**

falso

**For[i = 1, ! {a} ≠ False && i < 10, i++, Plot[i]]**

para cada falso representaci