

Algorithm 1 *ikj lu decomposition (delayed row dense algorithm)*

$$l = I_n$$

$$u = O_n$$

$$u_{11:n} = a_{1,1:n}$$

for $i=2:n$

 for $k=1:i-1$

$$l_{ik} = a_{ik}/a_{kk}$$

 for $j=k+1:n$

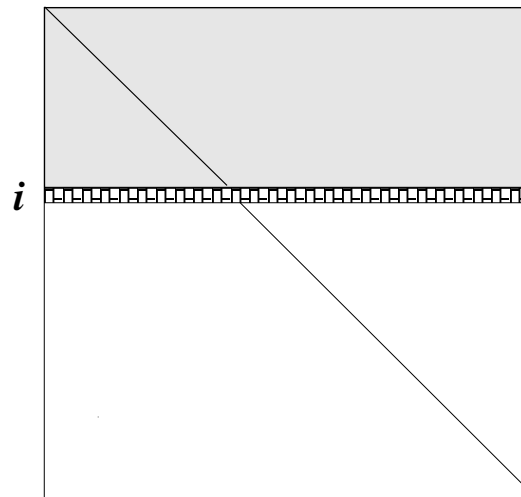
$$a_{ij} = a_{ij} - l_{ik} * a_{kj}$$

 end

end

$$u_{ii:n} = a_{ii:n}$$

end



Algorithm 2 ijk lu decomposition (dot product - based row dense algorithm)

$l = I_n, u = O_n, u_{11:n} = a_{11:n}$

for $i=2:n$

 for $j=2:i$

$l_{ij-1} = a_{ij-1} / a_{j-1j-1}$

 for $k=1:j-1$

$a_{ij} = a_{ij} - l_{ik} * a_{kj}$

 end

 end

 for $j=i+1:n$

 for $k=1:i-1$

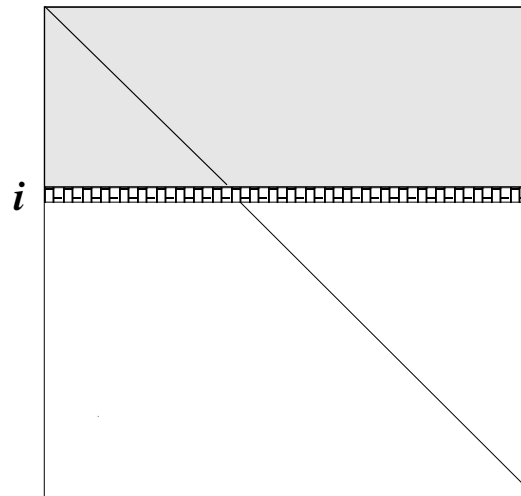
$a_{ij} = a_{ij} - l_{ik} * a_{kj}$

 end

 end

$u_{i,i:n} = a_{i,i:n}$

end

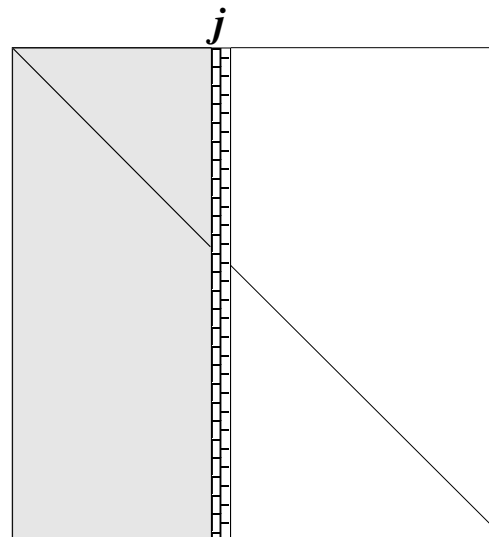


Algorithm 3 jki *lu decomposition (delayed column dense algorithm)*

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 $l = I_n, u = O_n, u_{11} = a_{11}$ 
for  $j=2:n$ 
  for  $s=j:n$ 
     $l_{sj-1} = a_{sj-1}/a_{j-1j-1}$ 
  end
  for  $k=1:j-1$ 
    for  $i=k+1:n$ 
       $a_{ij} = a_{ij} - l_{ik} * a_{kj}$ 
    end
  end
end
 $u_{1:jj} = a_{1:jj}$ 
end

```

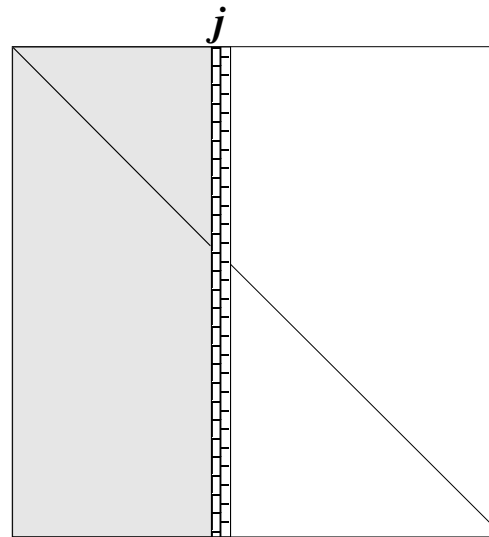


Algorithm 4 jik *lu decomposition (dot product - based column dense algorithm)*

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 $l = I_n, u_{11} = a_{11}$ 
for  $j=2:n$ 
  for  $s=j:n$ 
     $l_{sj-1} = a_{sj-1}/a_{j-1j-1}$ 
  end
  for  $i=2:j$ 
    for  $k=1:i-1$ 
       $a_{ij} = a_{ij} - l_{ik} * a_{kj}$ 
    end
  end
  for  $i=j+1:n$ 
    for  $k=1:j-1$ 
       $a_{ij} = a_{ij} - l_{ik} * a_{kj}$ 
    end
  end
   $u_{1:jj} = a_{1:jj}$ 
end

```

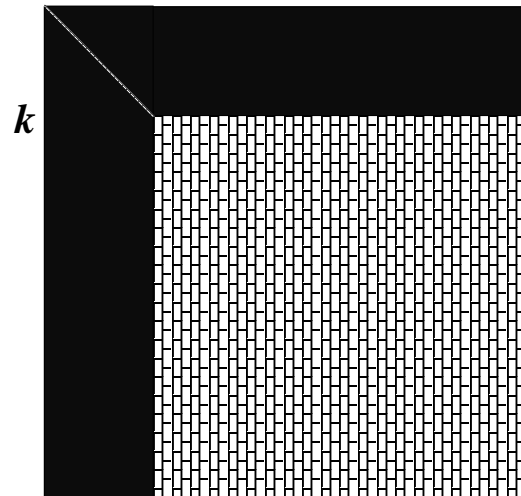


Algorithm 5 *kij* lu decomposition (row oriented submatrix dense algorithm)

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 $l = I_n$ 
 $u = O_n$ 
for  $k=1:n-1$ 
  for  $i=k+1:n$ 
     $l_{ik} = a_{ik}/a_{kk}$ 
    for  $j=k+1:n$ 
       $a_{ij} = a_{ij} - l_{ik} * a_{kj}$ 
    end
  end
end
 $u_{kk:n} = a_{kk:n}$ 
end
 $u_{nn} = a_{nn}$ 

```



Algorithm 6 kji *lu decomposition (column oriented submatrix dense algorithm)*

$l = I_n, u = O_n$

for $k=1:n-1$

for $s=k+1:n$

$l_{sk} = a_{s,k}/a_{k,k}$

end

for $j=k+1:n$

for $i=k+1:n$

$a_{ij} = a_{ij} - l_{ik} * a_{kj}$

end

end

$u_{kk:n} = a_{kk:n}$

end

$u_{nn} = a_{nn}$

