

# Guidelines for the stochastic production model in continuous time (SPiCT)

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This is a living document, be sure to check for the latest update ([link](#)). The SPiCT package is actively developed, check for the most recent package version and report problems at ([link](#)).

Document version	SPiCT version	Comments
v 1.0	v 1.2.7	Initial version (2019-09-23)
v 1.1	v 1.2.8	Management section added
v 1.2	v 1.3.0	Adjusted to package update
v 1.2	v 1.3.4	Adjusted after WKMSYSPiCT and WKLIFEX

This document provides specific guidelines for the use of the stochastic production model in continuous time (SPiCT, Pedersen and Berg 2017) and is divided into three parts, containing: (i) the main assumptions and data requirements of SPiCT, (ii) a checklist for the acceptance of a SPiCT assessment, (iii) options for assessment tuning, and (iv) harvest control rules for SPiCT.

Accompanying sample code that assumes that

- input data is contained in a list called `inp`,
- the results are contained in a list called `fit` after fitting SPiCT to the input data with `fit <- fit.spict(inp)`, and
- calculating the one-step-ahead residuals with `fit <- calc.osa.resid(fit)`.

## Main assumptions and input data for SPiCT

- Catch data should be representative of both landings and bycatch. It is also possible to use landings only, but then the interpretation of the results changes. If available, seasonal catches should be used as input. Catches are assumed to be taken over a time interval (e.g. years or quarters), thus the associated time vector in SPiCT `inp$timeC` should reflect the beginning of each catch interval (e.g. 2002.25 and 2002.75 for the second and fourth quarter catches, respectively). Additionally, the vector `inp$dtc` should reflect the length of each time interval (e.g. 1 for annual and 0.25 for quarterly catches, respectively).
- Stock size indices should be in terms of biomass (not numbers) and representative of the part of the stock vulnerable to the commercial fleets, the so called exploitable stock biomass (ESB). In many cases, the gear selectivity of the commercial and scientific fleets do not coincide and thus the stock size indices have to be corrected to exclude individuals that are not represented in the commercial fleets.
- Biomass indices are assumed to be snapshots at given points in time. Therefore, the timing of survey indices `inp$timeI` has to be given as decimal years reflecting the timing of the survey (e.g. 1995.5 for the middle of the year). The timing of the survey will be matched to the closest model time which

is dependent on `inp$dteuler` (see below). Commercial CPUE indices should be associated with the midpoint of the interval of the corresponding catches, i.e. middle of the year if they are based on yearly aggregated catches and effort.

- If input data spans long periods and there is ecological evidence for potential changes in productivity, it is possible to fit productivity regime shifts or long-term gradual changes in productivity with SPiCT (Mildenberger et al. 2019).
- The Euler discretisation has to be finer than the data, i.e. for yearly data the Euler time step `inp$dteuler` has to be smaller than 1. A value of 1 changes the model to a discrete time production model with different model assumptions. The default value is 1/16 year, which is sufficient in most cases.

## Checklist for the acceptance of a SPiCT assessment

ICES category 3 stocks can be managed using the official advice rule 3.1.1 and 3.1.2 in ICES (2017), which requires an accepted SPiCT assessment. Following points should be considered for the acceptance of a SPiCT assessment.

1. The assessment **converged** (`fit$opt$convergence` equals 0).
2. All **variance parameters** of the model parameters are **finite** (`all(is.finite(fit$sd))` should be TRUE).
3. **No violation of model assumptions** based on one-step-ahead residuals (bias, auto-correlation, normality). This means, that p-values are insignificant ( $> 0.05$ ), indicated by green titles in the graphs of `plotspict.diagnostic(fit)`. Slight violations of these assumptions do not necessarily invalidate model results.
4. **Consistent patterns in the retrospective analysis** (`fit <- retro(fit)`). This means that there is no tendency of consistent under- or overestimation of the relative fishing mortality ( $\frac{F}{F_{MSY}}$ ) and relative biomass ( $\frac{B}{B_{MSY}}$ ) in successive assessment. The retrospective trajectories of those two quantities should be inside the credible intervals of the base run.
5. **Realistic production curve**. The shape of the production curve should not be too skewed ( $\frac{B_{MSY}}{K}$  should be between 0.1 and 0.9). Low values of  $\frac{B_{MSY}}{K}$  allow for an infinite population growth rate (`calc.bmsyk(fit)`).
6. **High assessment uncertainty** can indicate a lack of contrast in the input data or violation of the ecological model assumptions. The main variance parameters (`logsdb`, `logsdc`, `logsdi`, `logsdf`) should not be unrealistically high. Credible intervals for  $\frac{B}{B_{MSY}}$  and  $\frac{F}{F_{MSY}}$  should not span more than 1 order of magnitude (`calc.om(fit)`).
7. **Initial values do not influence the parameter estimates** (`fit <- check.ini(fit)`). The estimates should be the same for all initial values (`fit$check.ini$resmat`). Runs which did not converge should not be considered in this regard.

## Optional model and assessment tuning

**Disclaimer:** An uncertain assessment is okay; the model should not be tweaked and parameters should not be fixed unless there is sufficient information and evidence to make such assumptions. Rather than avoiding uncertainty, it should be accounted for by means of stochastic harvest control rules (ICES 2019).

- Increase **iterations of optimisation**. The special error code `false convergence` (8) could indicate that the optimisation exceeded the maximum number of iterations `max.iter`. `inp$optimiser.control = list(iter.max = 1e5, eval.max = 1e5)`

- If the catch time series is longer than the survey(s), **shortening the catch time series** to cover only the period where there is an available biomass index may help model convergence. `inp = shorten.inp(inp, 2005, 2018)`
- **Adjust** the prior for the parameter `logn` determining the **shape of the production curve**.
  - Alternative priors for `logn` could be based on meta studies, e.g. for all species pooled based on Thorson et al. (2012): `inp$priors$logn <- c(log(1.478), 0.6, 1)`
  - Tighter Schaefer prior for `logn` (or any other prior e.g. from meta studies): `inp$priors$logn <- c(log(2), 0.5, 1)`
  - Fixing `n` to resemble the Schaefer production model (or the meta study, alternatively): `inp$ini$logn <- log(2); inp$phases$logn <- -1`

Be aware that these modifications might cause smaller credible bands.

- Use a **prior for the initial depletion level** based on available information, FOR EXAMPLE:
  - If evidence or expert knowledge allows to infer that there was **low or no** exploitation before the beginning of the available data: initial depletion level could be assumed to be close to the carrying capacity (e.g. `inp$priors$logbkfrac <- c(log(0.8), 0.5, 1)`)
  - If evidence or expert knowledge allows to infer that there was **high** exploitation before the beginning of the available data: initial depletion level could be assumed to be a certain fraction of the carrying capacity (e.g. `inp$priors$logbkfrac <- c(log(0.2), 0.5, 1)`)
- If information on the level of uncertainty in the biomass index and/or the uncertainty of the catch is available prior distribution could be used for the observation error term of the indices `logsdi` and `logsdc`, respectively. This requires to remove the priors for the ratios of process to observation errors `logalpha` and `logbeta`.

## Management based on an accepted SPiCT assessment

SPiCT estimates MSY based reference levels, which can be used to calculate quantities relevant for fisheries management, such as the Total Allowable Catch (TAC). The TAC can be calculated based on fishing at  $F_{MSY}$  or based more elaborate harvest control rules (HCR) which include additional components, e.g. a linearly reduction in  $F$  if the biomass is below a certain reference level (e.g.  $B_{trigger}$ ) as the hockey-stick MSY rule recommended by ICES (2017). Three ICES workshops emphasise the importance of the quantification and consideration of assessment uncertainty in HCRs (ICES 2018a, 2018b, 2019). They introduce two modifications of the hockey-stick MSY rule that account for assessment uncertainty by (i) using a percentile lower than 50 (i.e. median) for relative biomass  $\frac{B}{B_{MSY}}$  and catch  $C_{y+1}$  and higher than 50 for relative fishing mortality  $\frac{F}{F_{MSY}}$  (ICES 2018a), (ii) adjusting  $F$  to meet the condition that the predicted biomass at the end of the advice year is equal or smaller than a specified risk level (e.g. 5%, ICES 2018b). After comprehensive simulation testing, ICES (2019) recommends to use the MSY hockey-stick rule with 35th percentiles for all three quantities:

$$C_{y+1} = q_C(p)$$

$$F_{y+1} = F_y \frac{\min(1, q_B(p))}{q_F(100 - p)}$$

where the advised catch ( $C$ ) for advice year  $y+1$  corresponds to the predicted catch given the fishing mortality trajectory in the advice year, and where  $F_y$  and  $F_{y+1}$  are the fishing mortalities at the beginning and the end of the advice year, respectively. Other components of the equations are defined as follows:

Components	Definition and purpose
$q_C$	Function that takes a percentile and returns the corresponding predicted catch $C_{y+1}$ given the fishing mortality trajectory during the advice year $y+1$ , i.e. $q_C = \Phi_{C_{pred} F=F_y \dots F_{y+1}}^{-1}$
$q_B$	Function that takes a percentile and returns the corresponding predicted $\frac{B_{y+1}}{MSY B_{trigger}}$ at the beginning of the advice year and $MSY B_{trigger} = \frac{B_{MSY}}{2}$ , i.e. $q_B = \Phi_{\frac{B_{y+1}}{MSY B_{trigger}}}^{-1}$
$q_F$	Function that takes a percentile and returns the corresponding predicted $\frac{F_y}{F_{MSY}}$ at the beginning of the advice year $y+1$ , i.e. $q_F = \Phi_{\frac{F_y}{F_{MSY}}}^{-1}$
$p$	Specific percentile of the respective distributions, e.g. 35 (WKLIFE IX, ICES 2019).

Theoretically, any percentiles could be considered for the three quantities  $(C_{y+1}, \frac{B_{y+1}}{B_{MSY} B_{trigger}}, \frac{F_y}{F_{MSY}})$ . In the simulation testing done during WKLIFE IX, the same percentile ( $p$ ) was used for biomass and catch; for fishing mortality the percentile was equal to  $100 - p$ . The results show that across all tested scenarios and harvest control rules, management with the MSY-35 rule leads to high levels of relative yield while retaining the risks at low levels. Higher percentiles than 35th show higher levels of risk while achieving similar levels of relative yield, while lower percentiles show a decrease in yield with small change in risk (ICES 2019). It is important to mention that informative priors (lower standard deviations) potentially affect parameter estimates and credible intervals of SPiCT assessments, and therefore affecting the calculated TAC.

TAC based on a SPiCT assessment can be calculated using the `get.TAC()` function within the `spict` package in R, where the function arguments allow to use any of the above described HCRs or combinations thereof. The hockey-stick MSY rule with the 35th percentile as recommended by ICES (2019) is included as scenario 8 (or ‘ices’) in the `manage` function, but can also be applied independently of the `manage` function by `get.TAC(rep, fractiles = list(catch=0.35, bbmsy=0.35, ffmsy=0.35), breakpointB=0.5)`.

## Category 1 stocks

During WKMSYSPiCT (held online 15–19 February 2021), SPiCT was considered as the assessment model for several stocks. Stocks with accepted SPiCT assessments were raised to category 1. In accordance with basis for ICES advice (**ices?**) stocks and the recommendations from WKLIFEX (ICES 2019), the recommended management HCR includes a hockey-stick with  $B_{trigger} = B_{MSY}/2$  and  $B_{lim} = B_{MSY}/3$ . The TAC advice is the 35th percentile of the short term forecast of the catch distribution. This is achieved in `spict` using:

```
rep <- add.man.scenario(rep, "ICES MSY", fractiles = list(catch = 0.35), breakpointB =
c(1/3, 1/2))
```

## References

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