SPiCT

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Basic functionality

Getting started

This vignette explains basic and more advanced functions of the spict package. The package is installed from gihtub using the devtools package:

```
devtools::install_github("mawp/spict/spict")
```

installs the stable version of spict. When loading the package the user is greeted and the the installed version is shown:

```
library(spict)
  Loading required package: TMB
  Welcome to spict_v1.2.1@cec74e0d64908e3a676b856a64f90d6fb191fa53
```

The printed version follows the format ver@SHA, where *ver* is the manually defined version number and *SHA* refers to a unique github commit on github. The content of this vignette pertains to the version printed above that can be found here.

A specific verision of spict can be installed using the first few digits of the SHA:

```
devtools::install_github("mawp/spict/spict", ref = "cec74e0d")
```

Loading built-in example data

The package contains the catch and index data analysed in Polacheck, Hilborn, and Punt (1993) that can be loaded using

```
data(pol)
```

Data on three stocks are contained in this dataset: South Atlantic albacore, northern Namibian hake, and New Zealand rock lobster. Here focus will be on the South Atlantic albacore data. This dataset contains the following

```
$timeI
[1] 1967 1968 1969 1970 1971 1972 1973 1974 1975 1976 1977 1978 1979 1980
[15] 1981 1982 1983 1984 1985 1986 1987 1988 1989
```

Note that data are structured as a list containing the entries obsC (catch observations), timeC (time of catch observations), obsI (index observations), and timeI (time of index observations). If times are not specified it is assumed that the first observation is observed at time 1 and then sequentially onward with a time step of one year. It is therefore recommended to always specify observation times.

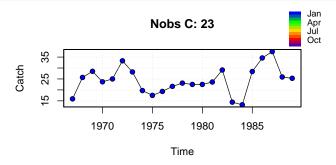
Each catch observation relates to a time interval. This is specified using dtc. If dtc is left unspecified (as is the case here) each catch observation is assumed to cover the time interval until the next catch observation. For this example with annual catches dtc therefore is

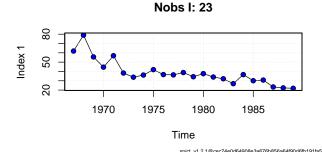
It is important to specify dtc if the default assumption is not fulfilled.

Plotting data

The data can be plotted using the command

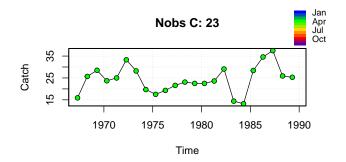
plotspict.data(pol\$albacore)

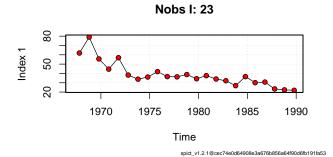




Note that the number of catch and index observations are given in the respective plot headers. Furthermore, the color of individual points shows when the observation was made and the corresponding colors are shown in the color legend in the top right corner. For illustrative purposes let's try shifting the data a bit

```
inpshift <- pol$albacore
inpshift$timeC <- inpshift$timeC + 0.3
inpshift$timeI <- inpshift$timeI + 0.8
plotspict.data(inpshift)</pre>
```



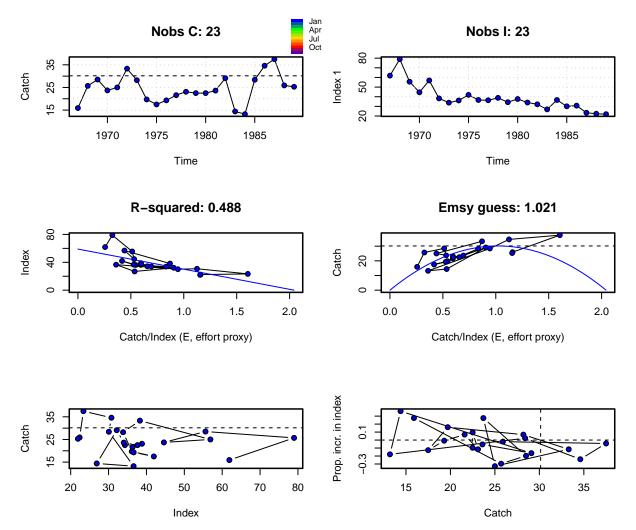


Now the colours show that catches are observed in spring and index in autumn.

Advanced data plotting

There is also a more advanced function for plotting data, which at the same time does some basic model fitting (linear regression) and shows the results

plotspict.ci(pol\$albacore)



The two top plots come from plotspict.data, with the dashed horizontal line representing a guess of MSY. This guess comes from a linear regression between the index and the catch divided by the index (middle row, left). This regression is expected to have a negative slope. A similar plot can be made showing catch versus catch/index (middle row, right) to approximately find the optimal effort (or effort proxy). The proportional increase in the index as a function of catch (bottom row, right) should show primarily positive increases in index at low catches and vice versa. Positive increases in index at large catches could indicate model violations. In the current plot these are not seen.

Fitting the model

The model is fitted to data by running

```
res <- fit.spict(pol$albacore)</pre>
```

Here the call to fit.spict is wrapped in the system.time command to check the time spent on the calculations. This is obviously not required, but done here to show that fitting the model only takes a few seconds. The result of the model fit is stored in res, which can either be plotted using plot or summarised using summary.

The results are returned as a list that contains output as well as input. The content of this list is

```
[4] "par.fixed" "cov.fixed" "pdHess"
[7] "gradient.fixed" "par.random" "diag.cov.random"
[10] "env" "inp" "obj"
[13] "opt" "pl" "Cp"
[16] "report" "computing.time"
```

Many of these variables are generated by TMB::sdreport(). In addition to these spict includes the list of input values (inp), the object used for fitting (obj), the result from the optimiser (opt), the time spent on fitting the model (computing.time), and more less useful variables.

Interpreting summary of results

The results are summarised using

```
capture.output(summary(res))
   [1] "Convergence: 0 MSG: relative convergence (4)"
   [2] "Objective function at optimum: 2.0654958"
   [3] "Euler time step (years): 1/16 or 0.0625"
   [4] "Nobs C: 23, Nobs I1: 23"
   [5] ""
   [6] "Priors"
   [7] "
            logn ~ dnorm[log(2), 2^2]"
   [8] " logalpha ~ dnorm[log(1), 2^2]"
   [9] " logbeta ~ dnorm[log(1), 2^2]"
  [10] ""
  [11] "Model parameter estimates w 95% CI "
  [12] "
                 estimate
                                cilow
                                           ciupp
                                                   log.est
  [13] " alpha
                 8.5380751
                          1.2232673 59.5934543 2.1445356
  [14] " beta
                0.1212598 0.0180690
                                       0.8137639 -2.1098202
  [15] " r
                 0.2556011 0.1010590
                                       0.6464730 -1.3641371
  [16] " rc
                 0.7435385 0.1445713
                                       3.8240616 -0.2963348
  [17] " rold
                0.8179927
                          0.0019101 350.3057009 -0.2009019
  [18] " m
                22.5827819 17.0681833 29.8791049 3.1171878
  [19] " K
               201.4753810 138.1193692 293.8930970 5.3056672
  [20] " q
                [21] " n
                 [22] " sdb
                 0.0128136 0.0018407
                                       0.0892017 -4.3572451
  [23] " sdf
                 0.3673758
                          0.2673605
                                       0.5048052 -1.0013700
  [24] " sdi
                 0.1094038
                           0.0808973
                                       0.1479555 -2.2127095
  [25] " sdc
                 0.0445479
                          0.0073370
                                       0.2704792 -3.1111902
  [26] " "
  [27] "Deterministic reference points (Drp)"
  [28] "
                estimate
                             cilow
                                       ciupp
                                             log.est
  [29] " Bmsyd 60.7440848 15.4030051 239.553503 4.106670
  [30] "Fmsyd 0.3717692 0.0722856
                                   1.912031 -0.989482 "
  [31] " MSYd 22.5827819 17.0681833 29.879105 3.117188 "
  [32] "Stochastic reference points (Srp)"
                estimate
                             cilow
                                               log.est rel.diff.Drp "
                                       ciupp
  [34] "Bmsys 60.7364344 15.4031639 239.490698 4.1065438 -1.259605e-04
  [35] " Fmsys 0.3717814 0.0722787
                                   1.912339 -0.9894493 3.272178e-05
  [36] "MSYs 22.5806762 17.0626482 29.883224 3.1170945 -9.325286e-05
  [37] ""
  [38] "States w 95% CI (inp$msytype: s)"
```

```
[39]
                                       cilow
                         estimate
                                                    ciupp
                                                             log.est
[40] " B_1989.00
                      59.1916639 31.0255656 112.9279356
                                                           4.0807807
[41] " F 1989.00
                        0.4160746
                                   0.2048129
                                                0.8452495 -0.8768908
[42] " B 1989.00/Bmsv
                       0.9745660
                                   0.3430172
                                                2.7688961 -0.0257630
[43] " F_1989.00/Fmsy
                       1.1191377
                                   0.2899257
                                                4.3199659
                                                           0.1125585
[44]
[45] "Predictions w 95% CI (inp$msytype: s)"
[46] "
                      prediction
                                       cilow
                                                    ciupp
                                                             log.est
[47] " B 1990.00
                      56.5242290 30.0511471 106.3183528
                                                           4.0346694
[48] " F 1990.00
                        0.4464502
                                   0.2098833
                                               0.9496597 -0.8064275
[49] " B 1990.00/Bmsy
                       0.9306478
                                   0.2932020
                                                2.9539540 -0.0718744
[50] " F 1990.00/Fmsy
                       1.2008405
                                   0.2832190
                                                5.0915295
[51] " Catch 1990.00
                      24.7359923 15.3328343
                                               39.9058192
                                                           3.2082594
[52] " E(B_inf)
                      49.9856610
                                          NA
                                                           3.9117362
```

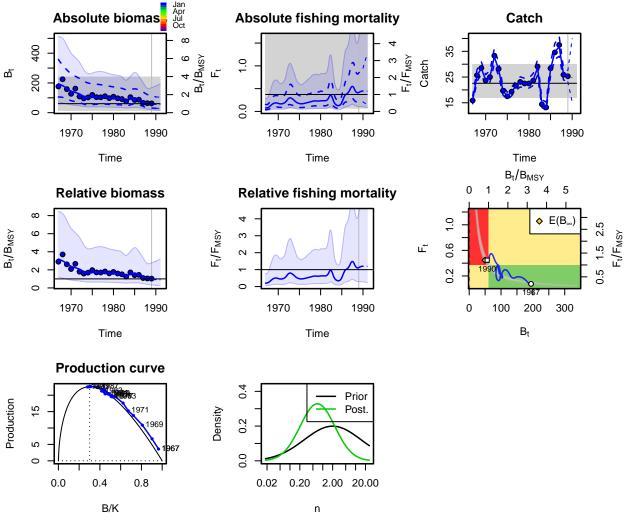
Here the capture.output() is only used to provide line numbers for easier reference, but the summary() command works without this.

- Line 1: Convergence of the model fit, which has code 0 if the fit was successful. If this is not the case convergence was not obtained and reported results should not be used. In case of non-convergence results will still be reported to aid diagnosis of the problem.
- Line 2: Objective function value at the optimum. The objective function is the likelihood function if priors are not used and the posterior density function if priors are used.
- Line 3: The Euler time step used in the calculation.
- Line 4: Number of observations for the time series used.
- Line 6-9: Summary of the priors used in the fit. The priors shown here are the default priors that are applied when priors are unspecified. These are relatively uninformative and are applied because most data-limited situations do not allow simultaneous estimation of all noise parameters and logn. The default priors can be disabled (see the section on priors).
- Line 11-25: Summary of the parameter estimates and their 95% CIs. These can be extracted as a data frame with sumspict.parest(res).
- Line 27-31: Estimates of deterministic reference points with 95% CIs. These are the reference points one would derive if stochasticity were ignored. Can be extracted with sumspict.drefpoints(res).
- Line 32-36: Estimates of stochastic reference points with 95% CIs. These are the reference points of the stochastic model. The column 'rel.diff.Drp' shows the relative difference when compared to the deterministic reference points. The information can be extracted with sumspict.srefpoints(res).
- Line 38-43: State estimates in the final year where data were available. The states of the model are biomass (B) and fishing mortality (F) with the year of the estimates appended. The year is shown as a decimal number as estimates within year are possible. Both absolute (B and F) and relative estimates (B/Bmsy and F/Fmsy) are shown. The relative estimates are calculated using the type of reference points given by msytype (line 38), where s is stochastic and d is deterministic. Here msytype is 's'. This information can be extracted using sumspict.states(res).
- Line 45-52: Predictions of absolute and relative biomass and fishing mortality at the time indicated by inp\$timepredi, here 1990 (line 47-50). In addition, predicted catch at the time indicated by inp\$timepredc (line 51). Finally, the equilibrium biomass, indicated by E(B_inf), if current conditions remain constant. There predictions or forecasts are calculated under the fishing scenario given by inp\$ffac. See the section on forecasting for more information. The prediction summary can be extracted using sumspict.predictions(res).

Interpreting plots of results

spict comes with several plotting abilities. The basic plotting of the results is done using the generic function plot that produces a multipanel plot with the most important outputs.

plot(res)



spict_v1.2.1@cec74e0d64908e3a676b856a64f90d6fb191fa53

Some general comments can be made regarding the style and colours of these plots:

- Estimates (biomass, fishing mortality, catch, production) are shown using blue lines.
- 95% CIs of absolute quantities are shown using dashed blue lines.
- 95% CIs of relative biomass and fishing mortality are shown using shaded blue regions.
- Estimates of reference points (B_{MSY}, F_{MSY}, MSY) are shown using black lines.
- 95% CIs of reference points are shown using grey shaded regions.
- The end of the data range is shown using a vertical grey line.
- Predictions beyond the data range are shown using dotted blue lines.
- Data are shown using points colored by season. Different index series use different point characters (not shown here).

The individual plots can be plotted separately using the plotspict.* family of plotting functions; all functions are summarised in Table 1 and their common arguments that control their look in Table 2:

Table 1: Available plotting functions.

Function Plot		
	Function	Plot

Data

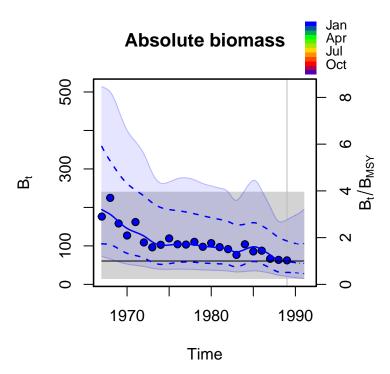
Function	Plot	
plotspict.ci	Basic data plotting (see section)	
plotspict.data	Advanced data plotting (see section)	
Estimates		
plotspict.bbmsy	Relative biomass B/B_{MSY} estimates with uncertainty	
plotspict.biomass	Absolute (and relative) biomass estimates with uncertainty	
plotspict.btrend	Expected biomass trend	
plotspict.catch	Catch data and estimates	
plotspict.f	Absolute (and relative) fishing mortality F	
plotspict.fb	Kobe plot of relative fishing mortality over biomass estimates	
plotspict.ffmsy	Relative fishing mortality F/F_{MSY}	
plotspict.priors	Prior-posterior distribution of all parameters that are estimated using priors	
plotspict.production	Production over B/K	
plotspict.season	Seasonal pattern of fishing mortality F	
Diagnostics & extras		
plotspict.diagnostic	OSA residual analysis to evaluate the fit	
plotspict.osar	One-step-ahead residual plots, one for data time-series	
plotspict.likprof	Profile likelihood of one or two parameters	
plotspict.retro	Retrospective analysis	
plotspict.infl	Influence statistics of observations	
plotspict.inflsum	Summary of influence of observations	
plotspict.tc	Time to B_{MSY} under different scenarios about F	

Table 2: Common arguments in the plotspict.* family of funtions

Argument	Value	Result
logax	logical	If TRUE, the y-axis is in log scale
main	string	The title of the plot
ylim	numeric vector	The limits of the y-axis
plot.obs	logical	If TRUE (default) the observations are shown
qlegend	logical	If TRUE (default) the color legend is shown
xlab, ylab	string	The x and y axes labels
stamp	string	Adds a "stamp" at the bottom right corner of the plotting area
		Default is the version and SHA hash of spict.
		An empty string removes the stamp.

We will now look at them one at a time. The top left is the plot of absolute biomass

plotspict.biomass(res)

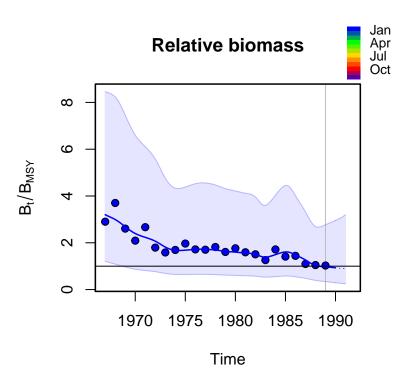


spict_v1.2.1@cec74e0d64908e3a676b856a64f90d6fb191fa53

Note that this plot has a y-axis on the right side related to the relative biomass (B_t/B_{MSY}) . The shaded 95% CI region relates to this axis, while the dashed blue lines relate to the left y-axis indicating absolute levels. The dashed lines and the shaded region are shown on the same plot to make it easier to assess whether the relative or absolute levels are most accurately estimated. Here, the absolute are more accurate than the relative. Later, we will see examples of the opposite. The horizontal black line is the estimate of B_{MSY} with 95% CI shown as a grey region.

The plot of the relative biomass is produced using

plotspict.bbmsy(res)



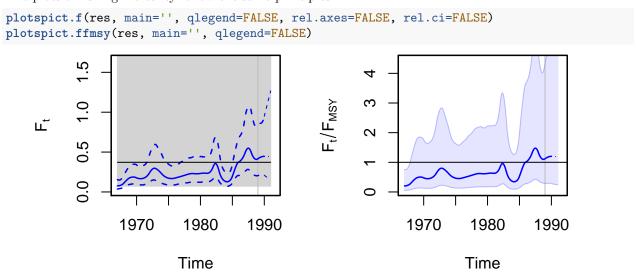
spict_v1.2.1@cec74e0d64908e3a676b856a64f90d6fb191fa53

spict_v1.2.1@cec74e0d64908e3a676b856a64f90d6fb191fa53

This plot contains much of the same information as given by plotspict.biomass, but without the information about absolute biomass and without the 95% CI around the B_{MSY} reference point.

The plots of fishing mortality follow the same principles

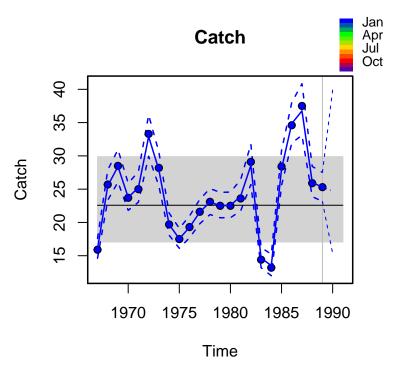
spict_v1.2.1@cec74e0d64908e3a676b856a64f90d6fb191fa53



The estimate of F_{MSY} is shown with a horizontal black line with 95% CI shown as a grey region (left plot). The 95% CI of F_{MSY} is very wide in this case. As shown here it is quite straightforward to remove the information about relative levels from the plot of absolute fishing mortality. Furthermore, the argument main='' removes the heading and qlegend=FALSE removes the colour legend for data points.

The plot of the catch is produced using

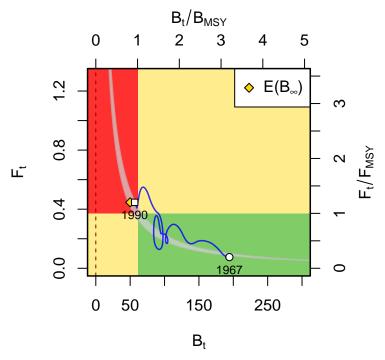
```
plotspict.catch(res)
```



spict_v1.2.1@cec74e0d64908e3a676b856a64f90d6fb191fa53

This plot shows estimated catches (blue line) versus observed catches (points) with the estimate of MSY plotted as a horizontal black line with its 95% CI given by the grey region.

A phase plot (or kobe plot) of fishing mortality versus biomass is plotted using



spict_v1.2.1@cec74e0d64908e3a676b856a64f90d6fb191fa53

The plot shows the development of biomass and fishing mortality since the initial year (here 1967) indicated

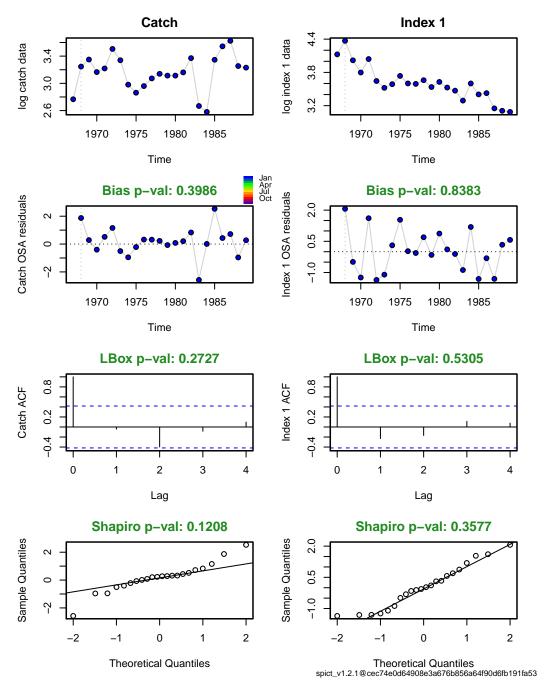
with a circle until the terminal year (here 1990) indicated with a square. The yellow diamond indicates the mean biomass over a long period if the current (1990) fishing pressure remains. This point can be interpreted as the fished equilibrium and is denoted $E(B_{\infty})$ in the legend as a statistical way of expressing the expectation of the biomass as $t \to \infty$. As the current fishing mortality is close to F_{MSY} the expected long term biomass is close to B_{MSY} .

A vertical dashed red line at $B_t = 0$ indicates the biomass level below which the stock has crashed. The grey shaded banana-shaped area indicates the 95% confidence region of the pair F_{MSY} , B_{MSY} . This region is important to visualise jointly as the two reference points are highly (negatively) correlated.

Residuals and diagnostics

Before proceeding with the results for an actual assessment it is very important that the model residuals are checked and possible model deficiencies identified. Residuals can be calculated using calc.osa.resid(). OSA stands for one-step-ahead, which are the proper residuals for state-space models. More information about OSA residuals is contained in Pedersen and Berg (2016). To calculate and plot residuals and diagnostics do

```
res <- calc.osa.resid(res)
plotspict.diagnostic(res)</pre>
```



The first column of the plot contains information related to catch data and the second column contains information related to the index data. The rows contain

- 1. Log of the input data series.
- 2. OSA residuals with the p-value of a test for bias (i.e. that the mean of the residuals is different from zero) in the plot header. If the header is green the test was not significant, otherwise the header would be red.
- 3. Empirical autocorrelation of the residuals. Two tests for significant autocorrelation is performed. A Ljung-Box simultaneous test of multiple lags (here 4) with p-value shown in the header, and tests for individual lags shown by dashed horizontal lines in the plot. Here no violation is identified.
- 4. Tests for normality of the residuals both as a QQ-plot and with a Shapiro test with p-value shown in the plot header.

This data did not have any significant violations of the assumptions, which increases confidence in the results. For a discussion of possible violations and remedies the reader is referred to Pedersen and Berg (2016).

Extracting parameter estimates

To extract an estimated quantity, here logBmsy use

```
get.par('logBmsy', res)

11 est ul sd cv
logBmsy 2.734573 4.106544 5.478515 0.6999851 0.170456
```

This returns a vector with 11 being the lower 95% limit of the CI, est being the estimated value, u1 being the upper 95% limit of the CI, sd being the standard deviation of the estimate, and cv being the coefficient of variation of the estimate. The estimated quantity can also be returned on the natural scale (as opposed to log scale) by running

```
get.par('logBmsy', res, exp=TRUE)

ll est ul sd cv
logBmsy 15.40316 60.73643 239.4907 0.6999851 0.7951617
```

This essentially takes the exponential of 11, est and u1 of the values in log, while sd is unchanged as it is the standard deviation of the quantity on the scale that it is estimated (here log). When transforming using exp=TRUE the $CV = \sqrt{e^{\sigma^2} - 1}$. Most parameters are log-transformed under estimation and should therefore be extracted using exp=TRUE.

For a standard fit (not using robust observation error, seasonality etc.), the quantities that can be extracted using this method are

```
list.quantities(res)
    [1] "Bmsv"
                                "Bmsy2"
                                                       "Bmsvd"
    [4] "Bmsys"
                                "Cp"
                                                       "Emsy"
    [7] "Emsy2"
                                "Fmsy"
                                                       "Fmsyd"
                                "gamma"
                                                       "isdb2"
   [10] "Fmsys"
   [13] "isdc2"
                                "isde2"
                                                       "isdf2"
   [16] "isdi2"
                                                       "logalpha"
   [19] "logB"
                                "logBBmsy"
                                                       "logbeta"
   [22] "logbkfrac"
                                "logBl"
                                                       "logBlBmsy"
   [25] "logBlK"
                                "logBmsy"
                                                       "logBmsyd"
                               "logBmsys"
   [28] "logBmsyPluslogFmsy"
                                                       "logBp"
                                "logBpK"
   [31] "logBpBmsy"
                                                       "logCp"
   [34] "logCpred"
                                "logEmsv"
                                                       "logEmsv2"
   [37] "logEp"
                                "logF"
                                                       "logFFmsy"
   [40] "logFFmsynotS"
                                "logFl"
                                                       "logFlFmsv"
   [43] "logFmsy"
                                "logFmsyd"
                                                       "logFmsys"
   [46] "logFnotS"
                                "logFp"
                                                       "logFpFmsy"
   [49] "logFs"
                                "logIp"
                                                       "logIpred"
   [52] "logK"
                                "logm"
                                                       "logMSY"
   [55] "logMSYd"
                                "logMSYs"
                                                       "logn"
   [58] "logq"
                                "logq2"
                                                       "logr"
                                "logrold"
                                                       "logsdb"
   [61] "logrc"
   [64] "logsdc"
                                "logsdf"
                                                       "logsdi"
                                "MSY"
                                                       "MSYd"
   [67] "m"
   [70] "MSYs"
                                "p"
                                                       "q"
   [73] "r"
                                "rc"
                                                       "rold"
   [76] "sdb"
                                "sdc"
                                                       "sde"
```

```
[79] "sdf" "seasonsplinefine"
```

These should be relatively self-explanatory when knowing that reference points ending with **s** are stochastic and those ending with **d** are deterministic, quantities ending with **p** are predictions and quantities ending with **1** are estimates in the final year. If a quantity is available both on natural and log scale, it is preferred to transform the quantity from log as most quantities are estimated on the log scale.

Extracting correlation between parameter estimates

The covariance between the model parameters (fixed effects) can be extracted from the results list

```
res$cov.fixed
                  logm
                              logK
                                                       logn
                                                                  logsdb
  logm
          0.0204040309 -0.005706714 0.026834550 -0.156740736
                                                             0.032240101
  logK
         -0.0057067141 0.037105155 -0.038074890 -0.011343169 -0.021784062
  logq
          0.0268345497 -0.038074890 0.091311212 -0.227633741
                                                             0.040958405
         -0.1567407356 -0.011343169 -0.227633741
                                                1.473743316 -0.190011585
  logn
  logsdb 0.0322401007 -0.021784062 0.040958405 -0.190011585
                                                             0.980089717
         0.0014253353 -0.002407435 0.003270276 -0.006648026 -0.002144227
  logsdi -0.0007603784 -0.002521057 0.002848540 0.007158237
                                                             0.010535579
  logsdc
          0.001997817
                                                             0.137920102
                logsdf
                             logsdi
                                          logsdc
          0.0014253353 -0.0007603784
   logm
                                     0.001553577
         -0.0024074352 -0.0025210569
                                     0.001300308
   logK
   logq
          0.0032702760 0.0028485396 -0.008392545
   logn
         -0.0066480259 0.0071582373 0.001997817
   logsdb -0.0021442270 0.0105355795 0.137920102
   logsdf 0.0262881975 -0.0002784384 -0.035159455
   logsdi -0.0002784384
                       0.0237200085
                                     0.005885858
  logsdc -0.0351594555 0.0058858584 0.846803905
```

It is however easier to interpret the correlation rather than covariance. The correlation matrix can be calculated using

```
cov2cor(res$cov.fixed)
                                                        logsdb
              logm
                         logK
                                    logq
                                               logn
  logm
         0.22798459
  logK
        -0.20740108 1.000000000 -0.65412309 -0.048507216 -0.11423227
  logq
         0.62169056 -0.654123089
                               1.00000000 -0.620531251
                                                    0.13691407
  logn
        -0.90388456 -0.048507216 -0.62053125
                                        1.000000000 -0.15810159
  logsdb 0.22798459 -0.114232274 0.13691407 -0.158101591
         0.06154300 -0.077082727
                              0.06674857 -0.033775468 -0.01335849
  logsdi -0.03456323 -0.084978313 0.06120724 0.038285802
                                                    0.06909842
  logsdc
         0.001788353
                                                    0.15139210
            logsdf
                       logsdi
                                  logsdc
         0.06154300 -0.03456323 0.011819075
  logm
  logK
        -0.07708273 -0.08497831 0.007335635
         logq
                             0.001788353
  logn
        -0.03377547 0.03828580
  logsdb -0.01335849
                   0.06909842
                              0.151392105
  logsdf 1.00000000 -0.01115042 -0.235651555
  logsdi -0.01115042 1.00000000 0.041529907
  logsdc -0.23565155 0.04152991 1.000000000
```

For this data most parameters are well separated, i.e. relatively low correlation, perhaps with the exception of logm and logn, which have a correlation of -0.9. Note that logr is absent from the covariance matrix. This is because the model is parameterised in terms of logm, logK, and logn from which logr can be derived. The estimate of logr is reported using TMB's sdreport() function and can be extracted using get.par().

The covariance between random effects (biomass and fishing mortality) is not reported automatically, but can be obtained by setting inp\$getJointPrecision to TRUE (this entails longer computation time and memory requirement).

The covariance between sdported values (i.e. the values reported in res\$value) are given in res\$cov. As this matrix is typically large, the function get.cov() can be used to extract the covariance between two scalar quantities

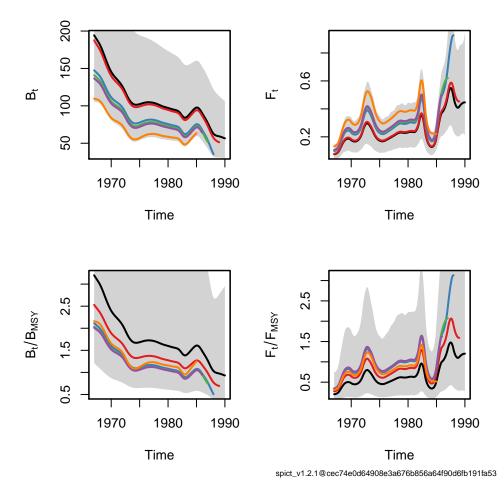
This reveals that for this data set the estimates of log Fmsy and log Bmsy are highly correlated. This is often the case and the reason why the model is reparameterised.

Advanced functionality

Retrospective plots

Retrospecitive plots are sometimes used to evaluate the robustness of the model fit to the introduction of new data, i.e. to check whether the fit changes substantially when new data becomes available. Such calculations and plotting thereof can be crudely performed using retro() as shown here

```
rep <- fit.spict(pol$albacore)
rep <- retro(rep)
plotspict.retro(rep)</pre>
```



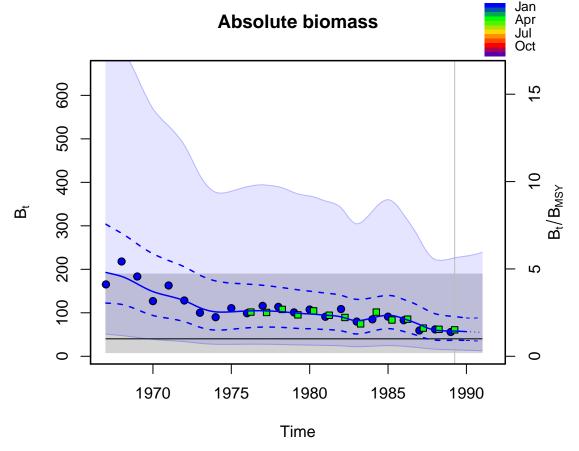
By default retro creates 5 scenarios with catch and index time series which are shortened by the 1 to 5 last observations. The number of scenarios and thus observations which are removed can be changed with the argument nretroyear in the function retro. The graphs show the different scenarios with different colors. For the albacore data, there is a high consistency between the scenarios except for the fishing mortalites of the second scenario (in red), which indicate a large increase in F.

Estimation using two or more biomass indices

The estimation can be done using more than one biomass index, for example when scientific surveys are performed more than once every year or when there are both commercial and survey CPUE time-series available. The following example emulates a situation where a long but noisy first quarter index series and a shorter and less noisy second quarter index series are available with different catchabilities

```
inp <- list(timeC=pol$albacore$timeC, obsC=pol$albacore$obsC)</pre>
inp$timeI <- list(pol$albacore$timeI, pol$albacore$timeI[10:23]+0.25)
inp$obsI <- list()</pre>
inp$obsI[[1]] <- pol$albacore$obsI * exp(rnorm(23, sd=0.1)) # Index 1
inp$obsI[[2]] <- 10*pol$albacore$obsI[10:23] # Index 2
res <- fit.spict(inp)</pre>
sumspict.parest(res)
               estimate
                                cilow
                                                      log.est
                                             ciupp
   alpha1
            5.54953258
                          0.94904897
                                       32.4507090
                                                    1.7137137
   alpha2
            3.45424294
                          0.58223835
                                       20.4929721
                                                    1.2396033
```

```
beta
            0.12057029
                          0.01912936
                                        0.7599414 -2.1155224
            0.18601586
                          0.08915985
                                        0.3880884 -1.6819234
   r
            1.20960496
                          0.19387714
                                        7.5467597
                                                   0.1902938
   rc
            0.26864003
                          0.05296983
                                        1.3624259 -1.3143830
   rold
           24.30176051
                         17.98198095
                                       32.8426309
                                                   3.1905488
   m
   K
          220.56429948 148.87722997 326.7699850
                                                   5.3961893
            0.35403669
                          0.22557139
                                        0.5556644 -1.0383547
   q1
            3.60405911
                          2.32437461
                                        5.5882739
                                                   1.2820607
   q2
            0.30756464
                          0.03135788
                                        3.0166586 -1.1790700
   n
            0.02006319
                          0.00372273
                                        0.1081282 -3.9088686
   sdb
   sdf
            0.36879354
                          0.26948768
                                        0.5046935 -0.9975183
   sdi1
            0.11134131
                          0.08158779
                                        0.1519454 -2.1951549
   sdi2
            0.06930312
                          0.04587566
                                        0.1046944 -2.6692653
   sdc
            0.04446554
                          0.00764489
                                        0.2586282 -3.1130407
plotspict.biomass(res)
```



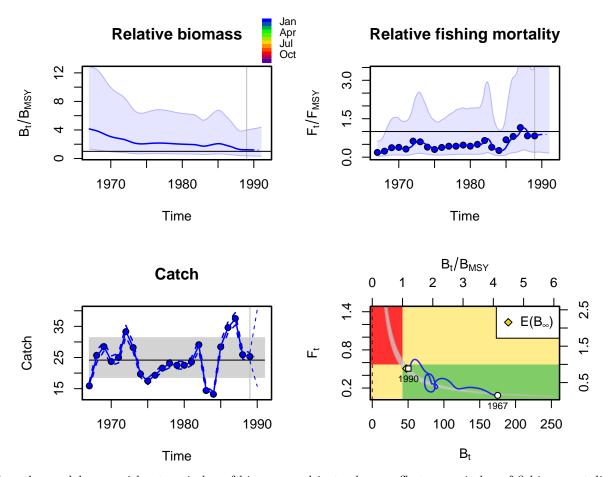
spict_v1.2.1@cec74e0d64908e3a676b856a64f90d6fb191fa53

The model estimates seperate observation noises and finds that the first index (sdi1) is more noisy than the second (sdi2). It is furthermore estimated that the catchabilities are different by a factor 10 (q1 versus q2). The biomass plot shows both indices, with circles indicating the first index and squares indicating the second index (the two series can also be distringuished by their colours).

Using effort data instead of commercial CPUE

It is possible to use effort data directly in the model instead of calculating commercial CPUE and inputting this as an index. It is beyond the scope of this vignette to discuss all problems associated with indices based on commercial CPUEs, however it is intuitively clear that using the same information twice (catch as catch and catch in catch/effort) induces a correlation, which the model does not account for. These problems are easily avoided by putting catch and effort seperately

```
inpeff <- list(timeC=pol$albacore$timeC, obsC=pol$albacore$obsC,</pre>
              timeE=pol$albacore$timeC, obsE=pol$albacore$obsC/pol$albacore$obsI)
repeff <- fit.spict(inpeff)</pre>
sumspict.parest(repeff)
             estimate
                            cilow
                                         ciupp
                                                 log.est
  beta
           0.07385347
                       0.01464722
                                    0.37238016 -2.6056723
           0.23822939
                       0.10656855
                                    0.53255150 -1.4345212
  r
           1.14399163
                       0.21452271
                                    6.10059827 0.1345236
  rc
  rold
           0.40826820
                       0.03851360
                                    4.32789751 -0.8958310
          24.16376129 18.62117900 31.35608974 3.1848540
  m
         189.53177432 132.49527141 271.12132451 5.2445567
  K
           0.41117179
                       qf
           0.41648800
                       0.04180192
                                  4.14962367 -0.8758976
  n
   sdb
           0.01430671
                       0.37625013
                       0.27938787
                                    0.50669403 -0.9775011
   sdf
  sde
           0.09820098
                       0.06985342
                                   0.13805240 -2.3207391
           0.02778738
   sdc
                       0.00568262
                                    0.13587724 -3.5831734
par(mfrow=c(2, 2))
plotspict.bbmsy(repeff)
plotspict.ffmsy(repeff, qlegend=FALSE)
plotspict.catch(repeff, qlegend=FALSE)
plotspict.fb(repeff)
```



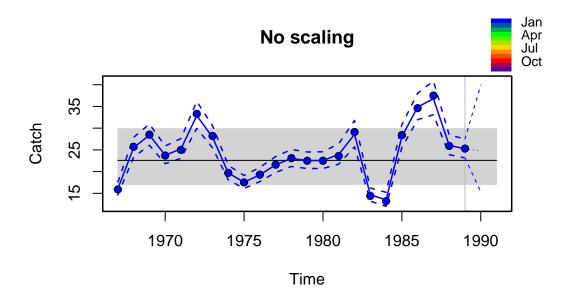
Here the model runs without an index of biomass and instead uses effort as an index of fishing mortality. Note that index observations are missing from the biomass plot, but effort observations are present in the plot of fishing mortality. Note also that **q** is missing from the summary of parameter estimates and instead **qf** is present, which is the commercial catchability.

Overall for this data set the results in terms of stock status etc. do not change much, and this will probably often be the case, however using effort data directly instead of commercial CPUE is cleaner and avoids inputting the same data twice.

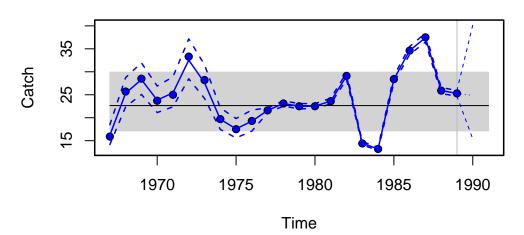
Scaling the uncertainty of individual data points

It is not always appropriate to assume that the observation noise of a data series is constant in time. Knowledge that certain data points are more uncertain than others can be implemented using stdevfacC, stdevfacI, and stdevfacE, which are vectors containing factors that are multiplied onto the standard deviation of the data points of the corresponding observation vectors. An example where the first 10 years of the biomass index are considered uncertain relative to the remaining time series and therefore are scaled by a factor 5.

```
inp <- pol$albacore
res1 <- fit.spict(inp)
inp$stdevfacC <- rep(1, length(inp$obsC))
inp$stdevfacC[1:10] <- 5
res2 <- fit.spict(inp)
par(mfrow=c(2, 1))
plotspict.catch(res1, main='No scaling')
plotspict.catch(res2, main='With scaling', qlegend=FALSE)</pre>
```



With scaling



From the plot it is noted that the scaling factor widens the 95% CIs of the initial ten years of catch data, while narrowing the 95% CIs of the remaining years.

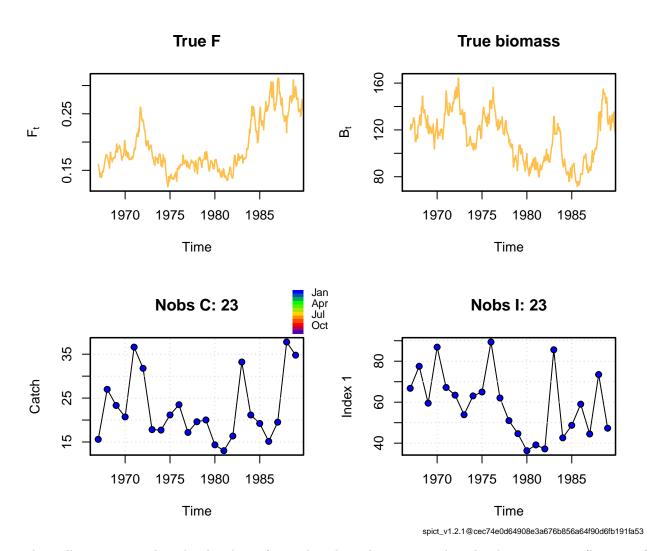
Simulating data

The package has built-in functionality for simulating data, which is useful for testing.

Annual data

Data are simulated using an input list, e.g. inp, containing parameter values specified in inp\$ini. To simulate data using default parameters run

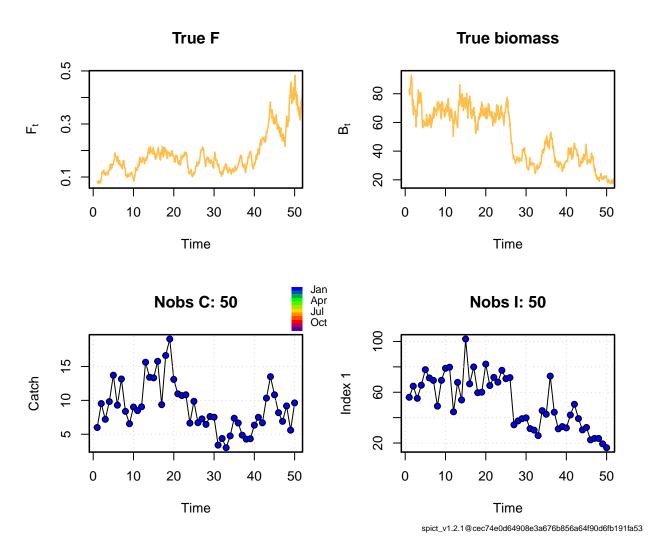
```
inp <- check.inp(pol$albacore)
sim <- sim.spict(inp)
plotspict.data(sim)</pre>
```



This will generate catch and index data of same length as the input catch and index time series (here 23 of each) at the time points of the input data. Note when plotting simulated data, the true biomass and fishing mortality are also included in the plot.

Another simple example is

```
inp <- list(ini=list(logK=log(100), logm=log(10), logq=log(1)))
sim <- sim.spict(inp, nobs=50)
plotspict.data(sim)</pre>
```

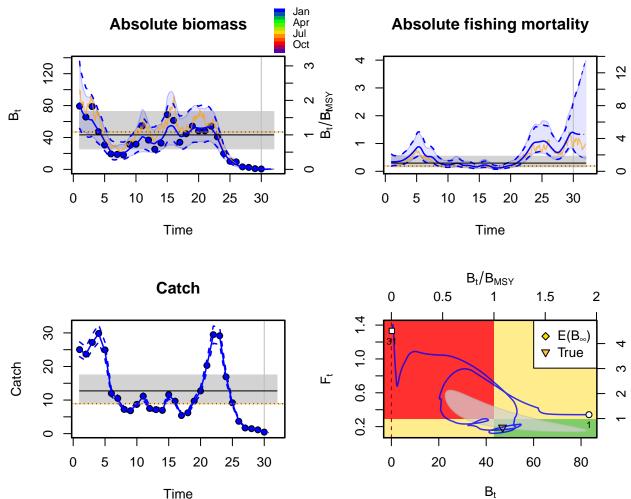


Here the required parameters are specified (the rest use default values), and the number of observations is specified as an argument to sim.spict().

A more customised example including model fitting is

```
set.seed(31415926)
inp <- list(ini=list(logK=log(100), logm=log(10), logq=log(1),
                      logbkfrac=log(1), logF0=log(0.3), logsdc=log(0.1),
                      logsdf = log(0.3)))
sim <- sim.spict(inp, nobs=30)</pre>
res <- fit.spict(sim)
sumspict.parest(res)
              estimate
                                    cilow
                                                 ciupp true.in.ci
                                                                        log.est
                        true
   alpha
            1.04607711
                        -9.0
                               0.31604357
                                             3.4624255
                                                                -9
                                                                    0.04504709
   beta
           0.13191757
                        -9.0
                               0.02269878
                                             0.7666599
                                                                -9 -2.02557801
                        -9.0
   r
            1.07672251
                               0.35061486
                                             3.3065666
                                                                -9
                                                                    0.07392172
                        -9.0
                               0.34468261
                                                                -9
           0.63474118
                                             1.1688909
                                                                   -0.45453795
   rc
           0.45001540
                        -9.0
                               0.22252978
                                             0.9100528
                                                                   -0.79847347
   rold
          14.48076844
                        10.0 10.46872828
                                            20.0303847
                                                                    2.67282145
   \mathbf{m}
   K
          76.02606890 100.0 46.11318791 125.3429532
                                                                    4.33107629
                         1.0
                               0.85013702
                                             1.6830688
           1.19617687
                                                                    0.17913053
   q
                         2.0
                                             8.4492032
   n
           3.39263481
                               1.36225519
                                                                    1.22160685
           0.19525936
                         0.2
                               0.08857955
                                             0.4304178
                                                                 1 -1.63342656
   sdb
```

```
sdf
           0.34363008
                         0.3
                              0.25198736
                                            0.4686014
                                                                1 -1.06818954
   sdi
           0.20425635
                              0.12166919
                                            0.3429024
                                                                1 -1.58837948
   sdc
           0.04533085
                              0.00814469
                                            0.2522975
                                                                1 -3.09376755
par(mfrow=c(2, 2))
plotspict.biomass(res)
plotspict.f(res, qlegend=FALSE)
plotspict.catch(res, qlegend=FALSE)
plotspict.fb(res)
```



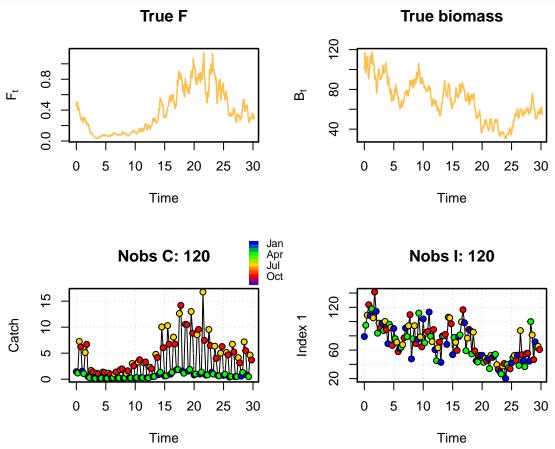
Here the ratio between biomass in the initial year relative to K is set using logbkfrac, the initial fishing mortality is set using logFO, process noise of F is set using logsdf, and finally observation noise on catches is specified using logsdc.

When printing the summary of the parameter estimates the true values are included as well as a check whether the true value was inside the 95% CIs. Similarly, the true biomass, fishing mortality, and reference points are included in the results plot using a yellow/orange colour.

Seasonal data

It is possible to simulate seasonal data (most often quarterly). Additional variables must be specified in the input list that define the type of seasonality to be used. Spline based seasonality is shown first (inp\$seasontype = 1). This is the default and therefore does not need to be explicitly specified. It is

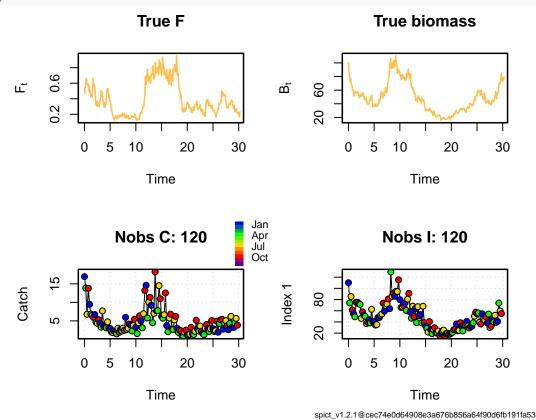
required that number of seasons is specified using nseasons (4 indicates quarterly), the order of the spline must be specified using splineorder (3 for quarterly data), time vectors for catch and index containing subannual time points must be specified, and finally the spline parameters (logphi) must be set. With four seasons logphi must be a vector of length 3, where each value in the vector gives the log fishing intensity relative to level in season four, which is log(1). An example of simulating seasonal data using a spline is



The data plot shows clear seasonality in the catches. To simulate seasonal data using the coupled SDE approach seasontype must be set to 2 and nseasons to 4.

spict_v1.2.1@cec74e0d64908e3a676b856a64f90d6fb191fa53





Estimation using quarterly data

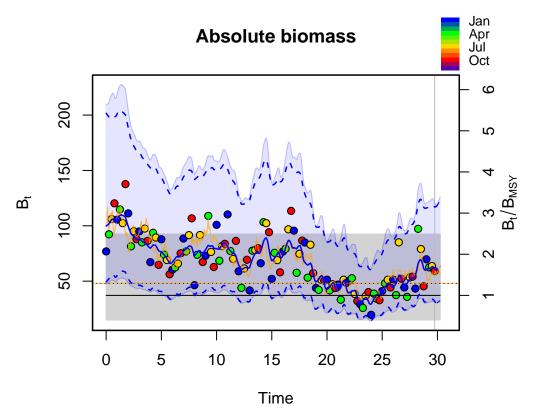
Catch information available in sub-annual aggregations, e.g. quarterly catch, can be used to estimate the seasonal pattern of the fishing mortality. The user can choose between two types of seasonality by setting seasontype to 1 or 2:

- 1. using cyclic B-splines.
- 2. using coupled stochastic differential equations (SDEs).

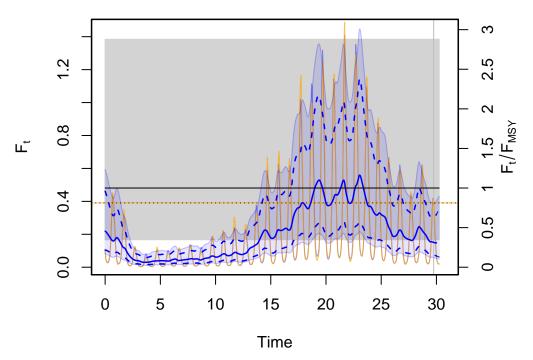
Technical description of the season types is found in Pedersen and Berg (2016).

Here, an example of a spline-based model fitted to quarterly data simulated in section is shown

```
seasonres <- fit.spict(seasonsim)
plotspict.biomass(seasonres)
plotspict.f(seasonres, qlegend=FALSE)
plotspict.season(seasonres)</pre>
```

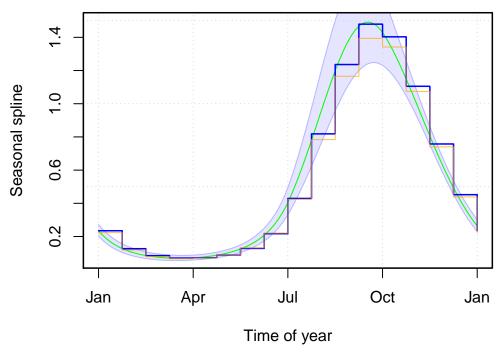


Absolute fishing mortality



spict_v1.2.1@cec74e0d64908e3a676b856a64f90d6fb191fa53

Spline order: 3

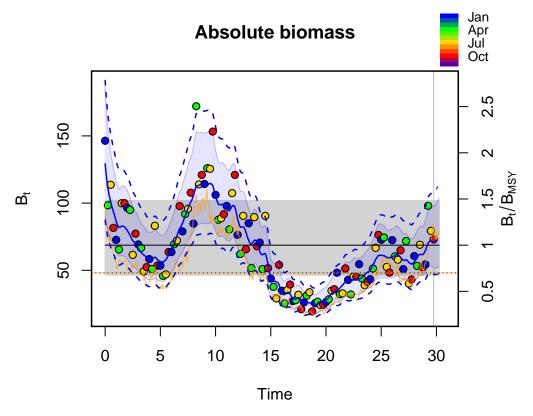


spict_v1.2.1@cec74e0d64908e3a676b856a64f90d6fb191fa53

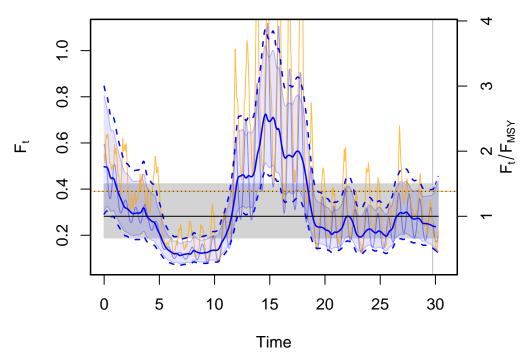
The model is able to estimate the seasonal variation in fishing mortality as seen both in the plot of F and in the plot of the estimated spline, where blue is the estimated spline, orange is the true spline, and green is the spline if time were truly continuous (it is discretised with the Euler steps shown by the blue line).

To fit the coupled SDE model run

```
seasonres2 <- fit.spict(seasonsim2)</pre>
sumspict.parest(seasonres2)
               estimate
                         true
                                     cilow
                                                  ciupp true.in.ci
                                                                        log.est
   alpha
            1.38654513
                         -9.0
                                0.74646650
                                              2.5754772
                                                                 -9
                                                                     0.3268151
   beta
                         -9.0
                                0.46862508
                                              1.0400093
                                                                 -9 -0.3593613
            0.69812209
                         -9.0
   r
            0.75461230
                                0.19653877
                                              2.8973404
                                                                 -9 -0.2815512
   rc
            0.57786149
                         -9.0
                                0.38165597
                                              0.8749343
                                                                 -9 -0.5484211
   rold
            0.46819698
                         -9.0
                                0.22851759
                                              0.9592627
                                                                  -9
                                                                    -0.7588662
            20.30400509
                         20.0 15.39627327
                                             26.7761305
                                                                     3.0108182
   K
          127.48850152 100.0 77.62144028
                                            209.3921211
                                                                      4.8480262
   q
            0.75175503
                           1.0
                                0.51602963
                                              1.0951612
                                                                  1 -0.2853448
            2.61174109
                          2.0
                                0.81672644
                                              8.3518681
                                                                      0.9600171
   n
                                                                  1
   sdb
            0.13137017
                           0.2
                                0.07696246
                                              0.2242408
                                                                    -2.0297362
            0.10517086
                           0.1
                                0.05695791
                                              0.1941944
                                                                    -2.2521690
   sdu
   sdf
            0.31639458
                           0.4
                                0.23247974
                                              0.4305989
                                                                    -1.1507652
                          0.2
   sdi
            0.18215067
                                0.15479277
                                              0.2143438
                                                                  1 -1.7029211
   sdc
            0.22088205
                                0.18154286
                                              0.2687458
                                                                    -1.5101265
            0.06185887
   lambda
                          0.1
                                0.00855678
                                              0.4471918
                                                                  1 -2.7828998
plotspict.biomass(seasonres2)
plotspict.f(seasonres2, qlegend=FALSE)
```



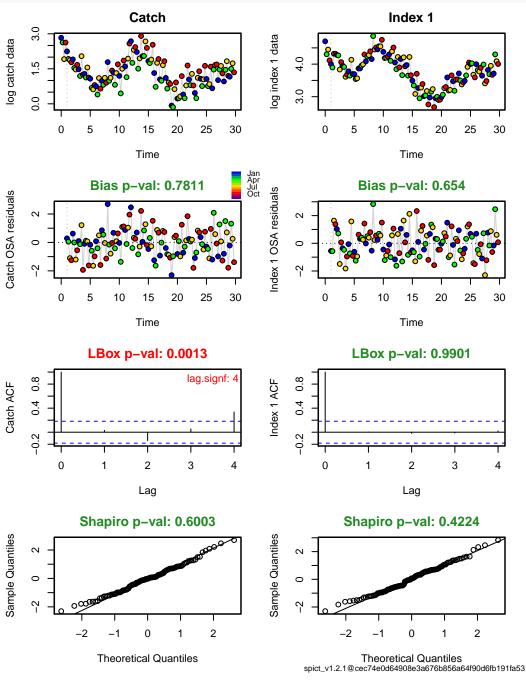
Absolute fishing mortality



spict_v1.2.1@cec74e0d64908e3a676b856a64f90d6fb191fa53

Two parameters related to the coupled SDEs are estimated (sdu and lambda) as evident from the summary of estimated parameters. In the plot of fishing mortality it is noted that the amplitude of the seasonal pattern

varies over time. This is a property of the coupled SDE model, which is not possible to obtain with the spline based seasonal model. The spline based model has a fixed amplitude and phases, which will lead to biased estimates and autocorrelation in residuals if in reality the seasonal pattern shifts a bit. This is illustrated by fitting a spline based model to data generated with a coupled SDE model



From the diagnostics it is clear that autocorrelation is present in the catch residuals.

Setting initial parameter values

Initial parameter values used as starting guess of the optimiser can be set using inp\$ini. For example, to specify the initial value of logK set

```
inp <- pol$albacore
inp$ini$logK <- log(100)</pre>
```

This procedure generalises to all other model parameters. If initial values are not specified they are set to default values. To see the default initial value of a parameter, here logK, run

```
inp <- check.inp(pol$albacore)
inp$ini$logK
[1] 5.010635</pre>
```

This can also be done posterior to fitting the model by printing res\$inp\$ini\$logK.

Checking robustness to initial parameter values

It is prudent to check that the same parameter estimates are obtained if using different initial values. If the optimum of the objective function is poorly defined, i.e. possibly containing multiple optima, it is possible that different parameter estimates will be returned depending on the initial values. To check whether this is the case run

```
set.seed(123)
check.ini(pol$albacore, ntrials=4)
   Checking sensitivity of fit to initial parameter values...
   Trial 1 ... model fitted!
   Trial 2 ... model fitted!
   Trial 3 ... model fitted!
   Trial 4 ... model fitted!
   $propchng
           logm logK logq logn logsdb logsdf logsdi logsdc
  Trial 1 -1.41 0.26 -0.12 -2.75
                                   -1.26
                                           1.30 -0.08
  Trial 2 0.34 -0.04 0.62 0.34 -0.51
                                         -0.21
  Trial 3 -1.69 -0.42 -0.23 -3.26
                                   -1.11
                                         -0.55 -0.40
                                                        -1.41
  Trial 4 1.03 0.19 0.06 -0.68
                                    0.60
                                           1.01 -1.32
   $inimat
          Distance logn logK logm logq logsdb logsdf logsdi logsdc
              0.00 0.69 5.01 3.41 -0.64 -1.61 -1.61
  Basevec
                                                        -1.61
  Trial 1
              4.22 -0.29 6.34 2.99 1.12
                                           0.42 - 3.70 - 1.48
                                                                0.20
  Trial 2
              3.48 0.93 4.81 5.51 -0.86 -0.79 -1.27
                                                        -3.44
                                                                0.23
  Trial 3
              4.52 -0.48 2.90 2.61 1.45
                                           0.18 - 0.72
                                                        -0.96
                                                                0.67
  Trial 4
              3.64 1.41 5.97 3.61 -0.21
                                         -2.58 -3.23
                                                         0.52
                                                                0.24
   $resmat
          Distance
                              K
                                        n sdb sdf
                                   q
                 0 22.58 201.48 0.35 0.69 0.01 0.37 0.11 0.04
  Basevec
  Trial 1
                 0 22.58 201.48 0.35 0.69 0.01 0.37 0.11 0.04
  Trial 2
                 0 22.58 201.48 0.35 0.69 0.01 0.37 0.11 0.04
  Trial 3
                 0 22.58 201.48 0.35 0.69 0.01 0.37 0.11 0.04
  Trial 4
                 0 22.58 201.48 0.35 0.69 0.01 0.37 0.11 0.04
   $obsC
   [1] 15.9 25.7 28.5 23.7 25.0 33.3 28.2 19.7 17.5 19.3 21.6 23.1 22.5 22.5
```

```
[15] 23.6 29.1 14.4 13.2 28.4 34.6 37.5 25.9 25.3
$timeC
 [1] 1967 1968 1969 1970 1971 1972 1973 1974 1975 1976 1977 1978 1979 1980
[15] 1981 1982 1983 1984 1985 1986 1987 1988 1989
$obsI
 [1] 61.89 78.98 55.59 44.61 56.89 38.27 33.84 36.13 41.95 36.63 36.33
[12] 38.82 34.32 37.64 34.01 32.16 26.88 36.61 30.07 30.75 23.36 22.36
[23] 21.91
$timeI
 [1] 1967 1968 1969 1970 1971 1972 1973 1974 1975 1976 1977 1978 1979 1980
[15] 1981 1982 1983 1984 1985 1986 1987 1988 1989
$check.ini
$check.ini$propchng
         logm logK
                    logq logn logsdb logsdf logsdi logsdc
Trial 1 -1.41 0.26 -0.12 -2.75
                                 -1.26
                                         1.30
                                               -0.08
Trial 2 0.34 -0.04 0.62 0.34
                                 -0.51
                                        -0.21
                                                1.14
                                                      -1.14
Trial 3 -1.69 -0.42 -0.23 -3.26
                                 -1.11
                                        -0.55
                                               -0.40
                                                      -1.41
Trial 4 1.03 0.19 0.06 -0.68
                                  0.60
                                         1.01 -1.32 -1.15
$check.ini$inimat
        Distance logn logK logm logq logsdb logsdf logsdi logsdc
            0.00 0.69 5.01 3.41 -0.64
                                        -1.61
                                              -1.61
                                                      -1.61
                                                             -1.61
Basevec
Trial 1
            4.22 -0.29 6.34 2.99 1.12
                                         0.42 - 3.70
                                                      -1.48
                                                               0.20
Trial 2
            3.48 0.93 4.81 5.51 -0.86
                                        -0.79
                                                      -3.44
                                                               0.23
                                               -1.27
Trial 3
            4.52 -0.48 2.90 2.61 1.45
                                         0.18
                                              -0.72
                                                      -0.96
                                                               0.67
Trial 4
                 1.41 5.97 3.61 -0.21
                                        -2.58
                                              -3.23
                                                        0.52
                                                               0.24
$check.ini$resmat
        Distance
                                      n sdb sdf
                            K
                                                   sdi
                     \mathbf{m}
                                 q
Basevec
               0 22.58 201.48 0.35 0.69 0.01 0.37 0.11 0.04
Trial 1
               0 22.58 201.48 0.35 0.69 0.01 0.37 0.11 0.04
Trial 2
               0 22.58 201.48 0.35 0.69 0.01 0.37 0.11 0.04
Trial 3
               0 22.58 201.48 0.35 0.69 0.01 0.37 0.11 0.04
Trial 4
               0 22.58 201.48 0.35 0.69 0.01 0.37 0.11 0.04
```

The argument ntrials set the number of different initial values to test for. To keep it simple only few trials are generated here, however for real data cases more should be used, say 30. The propching contains the proportional change of the new randomly generated initial value relative to the base initial value, inimat contains the new randomly generated initial values, and resmat contains the resulting parameter estimates and a distance from the estimated parameter vector to the base parameter vector. The distance should preferably be close to zero. If that is not the case further investigation is required, i.e. inspection of objective function values, differences in results and residual diagnostics etc. should be performed. The example shown here looks fine in that all converged runs return the same parameter estimates. One trial did not converge, however non-converging trials are to some extent expected as the initial parameters are generated independently from a wide uniform distribution and may thus by chance be very inappropriately chosen.

Phases and how to fix parameters

The package has the ability to estimate parameters in phases. Users familiar with AD model builder will know that this means that some parameters are held constant in phase 1, some are then released and estimated in phase 2, more are released in phase 3 etc. until all parameters are estimated. Per default all parameters are estimated in phase 1. As an example the standard deviation on the biomass process, logsdb, is estimated in phase 2:

```
inp <- pol$albacore
inp$phases$logsdb <- 2
res <- fit.spict(inp)
    Estimating - phase 1
    Estimating - phase 2</pre>
```

Phases can also be used to fix parameters to their initial value by setting the phase to -1. For example

```
inp <- pol$albacore</pre>
inp$phases$logsdb <- -1
inp$ini$logsdb <- log(0.1)</pre>
res <- fit.spict(inp)
summary(res)
  Convergence: 0 MSG: relative convergence (4)
   Objective function at optimum: 5.8647428
   Euler time step (years):
                             1/16 or 0.0625
  Nobs C: 23, Nobs I1: 23
   Priors
        logn ~
                 dnorm[log(2), 2^2]
   logalpha
                 dnorm[log(1), 2^2]
    logbeta
                 dnorm[log(1), 2^2]
   Fixed parameters
        fixed.value
   Model parameter estimates w 95% CI
              estimate
                            cilow
                                        ciupp
                                                 log.est
   alpha
             1.0503613 0.6791518
                                    1.6244657 0.0491342
   beta
             0.1713918 0.0256773
                                    1.1440113 -1.7638034
             0.3471988 0.1465244
                                    0.8227093 -1.0578579
   r
             1.7791121 0.2676089 11.8278559 0.5761144
   rc
             0.5694636 0.0689479
                                    4.7033865 -0.5630604
   rold
                                               3.3136273
            27.4846402 18.9163563 39.9339827
   K
           144.5708243 82.7912265 252.4509434 4.9737695
             0.4966500 0.2541097
                                    0.9706881 -0.6998696
    q
             0.3903056 0.0392947
                                    3.8768218 -0.9408251
   n
             0.3738951
                       0.2594015
                                    0.5389235 -0.9837801
    sdf
    sdi
             0.1050361 0.0679152
                                    0.1624466 - 2.2534509
    sdc
             0.0640825 0.0113802
                                    0.3608516 -2.7475835
   Deterministic reference points (Drp)
                          cilow
            estimate
                                     ciupp
                                              log.est
   Bmsyd 30.8970294 6.2838311 151.917901 3.4306600
   Fmsyd 0.8895561 0.1338045
                                  5.913928 -0.1170327
   MSYd 27.4846402 18.9163563 39.933983 3.3136273
```

```
Stochastic reference points (Srp)
                      cilow
        estimate
                                 ciupp
                                         log.est rel.diff.Drp
                                        3.428067 -0.0025962349
Bmsys 30.8170212
                  6.3481131 149.601746
Fmsvs 0.8901022 0.1349377
                               5.871466 -0.116419
                                                  0.0006135542
MSYs 27.4303408 18.8037385 40.014575 3.311650 -0.0019795378
States w 95% CI (inp$msytype: s)
                                          ciupp
                 estimate
                               cilow
                                                   log.est
B 1989.00
               43.5729051 21.6014377 87.892208
                                                3.7744355
F 1989.00
                0.5677372 0.2613795
                                      1.233170 -0.5660967
B 1989.00/Bmsy 1.4139233
                           0.3592721
                                      5.564527
                                                0.3463683
F_1989.00/Fmsy 0.6378337 0.1112640
                                      3.656454 -0.4496777
Predictions w 95% CI (inp$msytype: s)
               prediction
                                cilow
                                          ciupp
                                                   log.est
B_1990.00
               44.7705544 21.9026960 91.513965
                                                3.8015507
F_1990.00
                0.5737431
                           0.2522597
                                      1.304930 -0.5555735
B_1990.00/Bmsy 1.4527866 0.3371972
                                      6.259213
                                                0.3734835
F_1990.00/Fmsy 0.6445812 0.1037380 4.005138 -0.4391545
Catch_1990.00 25.8407642 15.9509270 41.862463
                                                3.2519533
E(B_inf)
               45.9909037
                                  NA
                                                3.8284436
```

Priors

SPiCT is a generalisation of previous surplus production models in the sense that stochastic noise is included in both observation and state processes of both fishing and biomass. Estimating all model parameters is only possible if data contain sufficient information, which may not be the case for short time series or time series with limited contrast. The basic data requirements of the model are limited to only catch and biomass index time series. More information may be available, which can be used to improve the model fit. This is particularly advantageous if the model is not able to converge with only catch and index time series. Additional information can then be included in the fit via prior distributions for model parameters.

Default priors and how to disable them

Quantities that are traditionally difficult to estimate are logn, and the noise ratios logalpha and logbeta where logalpha = logsdi - logsdb and logbeta = logsdc - logsdf, respectively. Therefore, to generally stabilise estimation default semi-informative priors are imposed on these quantities that inhibit them from taking extreme and unrealistic values. If informative data are available these priors should have limited effect on results, if informative data are not available estimates will reduce to the priors.

If informative data are available and the default priors therefore are unwanted they can be disabled using

```
inp <- pol$albacore
inp$priors$logn <- c(1, 1, 0)
inp$priors$logalpha <- c(1, 1, 0)
inp$priors$logbeta <- c(1, 1, 0)
fit.spict(inp)
   Convergence: 0 MSG: relative convergence (4)
   Objective function at optimum: 5.0598288
   Euler time step (years): 1/16 or 0.0625
   Nobs C: 23, Nobs II: 23</pre>
No priors are used
```

```
Model parameter estimates w 95% CI
           estimate
                          cilow
                                       ciupp
                                                log.est
alpha
         39.0512848
                     0.0402366 3.790092e+04 3.6648758
beta
         0.0245071
                      0.0000265 2.269298e+01 -3.7087912
r
         0.1955750
                     0.0313372 1.220581e+00 -1.6318113
          1.2604800
                     0.0097765 1.625128e+02 0.2314926
rc
         0.2835728
rold
                      0.0024028 3.346680e+01 -1.2602862
         24.3112479 12.0981969 4.885329e+01 3.1909391
        210.4516033 123.9786505 3.572379e+02 5.3492557
K
                     0.2070701 7.130113e-01 -0.9564779
 q
         0.3842438
         0.3103183
                     0.0004170 2.309134e+02 -1.1701567
 n
 sdb
         0.0028040
                      0.0000029 2.728495e+00 -5.8767196
 sdf
         0.3809116
                      0.2827808 5.130959e-01 -0.9651879
 sdi
         0.1094986
                      0.0812449 1.475777e-01 -2.2118438
         0.0093351
                      0.0000103 8.475654e+00 -4.6739791
 sdc
Deterministic reference points (Drp)
       estimate
                     cilow
                                ciupp
                                         log.est
Bmsyd 38.57459 0.5969777 2492.55343
                                      3.6525937
Fmsyd 0.63024 0.0048883
                             81.25639 -0.4616546
MSYd 24.31125 12.0981969
                             48.85329
                                      3.1909391
Stochastic reference points (Srp)
         estimate
                       cilow
                                  ciupp
                                           log.est rel.diff.Drp
Bmsys 38.5744682 0.5969873 2492.49789 3.6525906 -3.107517e-06
Fmsys 0.6302411 0.0048883
                               81.25590 -0.4616529 1.766958e-06
MSYs 24.3112135 12.0980452
                               48.85377 3.1909377 -1.413371e-06
States w 95% CI (inp$msytype: s)
                  estimate
                                cilow
                                            ciupp
                                                     log.est
B_1989.00
                54.0126818 28.3907719 102.7576780
                                                   3.9892189
F_1989.00
                 0.4528693 0.2235663
                                        0.9173593 -0.7921517
B_1989.00/Bmsy 1.4002184
                           0.0314790
                                       62.2830671
                                                   0.3366283
F_1989.00/Fmsy 0.7185652 0.0079264
                                       65.1416880 -0.3304988
Predictions w 95% CI (inp$msytype: s)
                prediction
                                cilow
                                           ciupp
                                                    log.est
B 1990.00
                52.5650582 29.3174862 94.2470077
                                                 3.9620516
F 1990.00
                 0.4858020 0.2370661 0.9955179 -0.7219542
B_1990.00/Bmsy 1.3626904 0.0266106 69.7815121 0.3094610
F_1990.00/Fmsy 0.7708193 0.0076917 77.2473688 -0.2603013
Catch_1990.00 25.2158689 15.5407632 40.9143385
                                                  3.2274735
                49.5039259
 E(B_inf)
                                   NA
                                              NA
                                                 3.9020520
```

The model is able to converge without priors, however the estimates of alpha, beta and n are very uncertain indicating that limited information is available about these parameters.

Setting a prior

The model parameters to which priors can be applied can be listed using

```
list.possible.priors()
  [1] "logn"    "logalpha"    "logbeta"    "logr"          "logK"
  [6] "logm"    "logq"    "iqgamma"    "logqf"    "logbkfrac"
```

```
[11] "logB" "logF" "logBBmsy" "logFFmsy" "logsdb"
[16] "isdb2gamma" "logsdf" "isdf2gamma" "logsdi" "isdi2gamma"
[21] "logsde" "isde2gamma" "logsdc" "isdc2gamma" "logsdm"
[26] "logpsi" "mu"
```

A prior is set using

```
inp <- pol$albacore</pre>
inppriors \log (300), 2, 1)
fit.spict(inp)
  Convergence: 0 MSG: relative convergence (4)
  Objective function at optimum: 3.697211
  Euler time step (years): 1/16 or 0.0625
  Nobs C: 23, Nobs I1: 23
  Priors
      logK ~ dnorm[log(300), 2^2]
       logn ~
              dnorm[log(2), 2^2]
   logalpha ~ dnorm[log(1), 2^2]
    logbeta ~ dnorm[log(1), 2^2]
  Model parameter estimates w 95% CI
            estimate
                         cilow
                                   ciupp
                                          log.est
                    1.2276015 59.6064748 2.1464133
   alpha
           8.5541219
   beta
           r
           0.2543931 0.0999822
                               0.6472737 -1.3688747
                     0.1423248
                                3.8567138 -0.2999139
   rc
           0.7408820
   rold
           22.5701177 17.0283130 29.9154832 3.1166268
         202.2160641 138.6995451 294.8195436 5.3093367
   K
           0.3499366 0.1930339
   q
                              0.6343737 -1.0500034
           n
   sdb
           sdf
           0.3672885 0.2672937
                               0.5046914 -1.0016078
   sdi
           0.1093772
                     0.0808912
                                0.1478947 - 2.2129524
   sdc
           0.0445545
                     0.0073418
                                0.2703825 -3.1110420
  Deterministic reference points (Drp)
         estimate
                     cilow
                               ciupp
                                       log.est
   Bmsyd 60.927699 15.2912404 242.765426 4.1096879
   Fmsvd 0.370441 0.0711624 1.928357 -0.9930611
   MSYd 22.570118 17.0283130 29.915483 3.1166268
  Stochastic reference points (Srp)
          estimate
                      cilow
                                ciupp
                                        log.est rel.diff.Drp
   Bmsys 60.9200355 15.2914370 242.701240 4.1095621 -1.257924e-04
   Fmsys 0.3704531 0.0711556 1.928668 -0.9930283 3.266221e-05
   MSYs 22.5680187 17.0227429 29.919706 3.1165338 -9.300660e-05
  States w 95% CI (inp$msytype: s)
                              cilow
                                         ciupp
                                                log.est
                  estimate
                59.4317253 31.0677433 113.6912307 4.0848282
   B_1989.00
   F 1989.00
                 0.4143985 0.2035123
                                     0.8438121 -0.8809271
   B_1989.00/Bmsy 0.9755694 0.3412397
                                     2.7890532 -0.0247339
   F_1989.00/Fmsy 1.1186260 0.2875234
                                     4.3520785 0.1121012
```

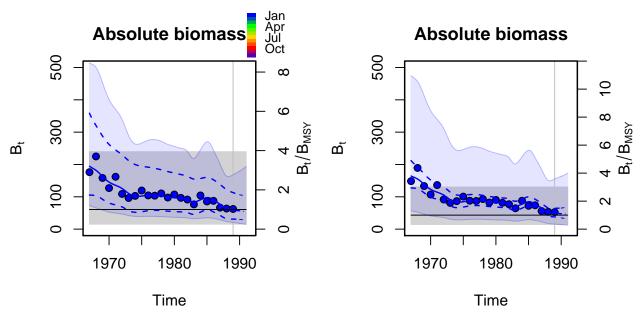
```
Predictions w 95% CI (inp$msytype: s)
                prediction
                                             ciupp
                                                       log.est
 B 1990.00
                56.7523819 30.1059283 106.9833428
                                                    4.0386976
 F 1990.00
                 0.4446518
                            0.2086071
                                         0.9477876 -0.8104637
 B_1990.00/Bmsy
                             0.2917620
                 0.9315881
                                         2.9745352 -0.0708645
 F 1990.00/Fmsy
                 1.2002917
                             0.2809798
                                         5.1274160
                                                    0.1825646
 Catch_1990.00
                                        39.9151741
                24.7355116 15.3286450
                                                    3.2082399
 E(B inf)
                50.1634075
                                                    3.9152858
```

This imposes a Gaussian prior on logK with mean log(300) and standard deviation 2. The third entry indicates that the prior is used (1 means use, 0 means do not use). From the summary it is evident that the default priors were also imposed.

Priors on random effects

Priors can be applied to random effects of the model, i.e. logB, logF, logBBmsy, (which is log(B/Bmsy)) logFFmsy (which is log(F/Fmsy)). An additional argument is required to specify these priors

```
inp <- pol$albacore
inp$priors$logB <- c(log(80), 0.1, 1, 1980)
par(mfrow=c(1, 2), mar=c(5, 4.1, 3, 4))
plotspict.biomass(fit.spict(pol$albacore), ylim=c(0, 500))
plotspict.biomass(fit.spict(inp), qlegend=FALSE, ylim=c(0, 500))</pre>
```



This imposes a Gaussian prior on logB with mean log(80), standard deviation 0.1 (very informative), the third entry in the vector indicates that the prior is used, the fourth entry indicates the year to which the prior should be applied, here 1980.

It is clear from the plots that the prior influences the results significantly. Furthermore, it is not only the biomass in the year 1980 that is affected, but the information propagates forward and backward because all estimates are correlated. In reality such an informative prior is rarely available, however it may be possible to derive information about the absolute biomass from acoustic survey and swept area estimates. It is, however, critical that the standard deviation used reflects the quality of the information.

Setting priors on the standard deviation of multiple indices

It is possible to set a prior for on some or all noise terms of multiple biomass indices

```
set.seed(123)
inp <- list(timeC=pol$albacore$timeC, obsC=pol$albacore$obsC)</pre>
inp$timeI <- list(pol$albacore$timeI, pol$albacore$timeI[10:23]+0.25)</pre>
inp$obsI <- list()</pre>
inp$obsI[[1]] <- pol$albacore$obsI * exp(rnorm(23, sd=0.1)) # Index 1
inp$obsI[[2]] <- 10*pol$albacore$obsI[10:23] # Index 2
inp$priors$logsdi <- list(c(1, 1, 0),</pre>
                                                 # No prior for index 1
                           c(log(0.1), 0.2, 1)) # Set a prior on index 2
res <- fit.spict(inp)</pre>
sumspict.priors(res)
   Priors
        logn ~ dnorm[log(2), 2^2]
    logalpha ~ dnorm[log(1), 2^2]
     logbeta ~ dnorm[log(1), 2^2]
     logsdi2 \sim dnorm[log(0.1), 0.2^2]
```

Fixing parameters using priors

Model parameters can be fixed using phases as described previously. This technique can, however, only be used to fix model parameters and therefore not derived quantities such as logalpha, logr (which is derived from logK, logm and logn). Fixing a parameter can be regarded as imposing an highly informative prior to the parameter

```
inp <- pol$albacore</pre>
inppriors \log <- c(\log(2), 1e-3)
inp$priors$logalpha <- c(log(1), 1e-3)
inp$priors$logbeta <- c(log(1), 1e-3)</pre>
fit.spict(inp)
   Convergence: 0 MSG: relative convergence (4)
   Objective function at optimum: -13.3777183
   Euler time step (years): 1/16 or 0.0625
   Nobs C: 23, Nobs I1: 23
   Priors
        logn ~
                dnorm[log(2), 0.001^2] (fixed)
   logalpha ~
                dnorm[log(1), 0.001^2] (fixed)
    logbeta ~
                dnorm[log(1), 0.001^2] (fixed)
   Model parameter estimates w 95% CI
                            cilow
             estimate
                                        ciupp
                                                 log.est
   alpha
            1.0000039 0.9980458 1.0019658 0.0000039
            0.9999976 0.9980395
   beta
                                   1.0019595 -0.0000024
            0.5046213 0.1875581
                                   1.3576733 -0.6839471
   r
                                    1.3576783 -0.6839453
            0.5046222 0.1875581
   rc
   rold
            0.5046231 0.1875573
                                   1.3576886 -0.6839435
            22.0086909 17.0613914 28.3905610 3.0914374
   \mathbf{m}
   K
           174.4569110 74.7554134 407.1305663 5.1616778
            0.3549421 0.1278982 0.9850325 -1.0358005
    q
            1.9999964 1.9960802
                                    2.0039202 0.6931454
```

```
sdb
         0.0966006 0.0704056
                                0.1325417 -2.3371705
sdf
         0.2102260 0.1562925
                                0.2827708 -1.5595721
         0.0966010 0.0704060
sdi
                                0.1325419 -2.3371666
                                0.2827699 -1.5595745
         0.2102255 0.1562923
sdc
Deterministic reference points (Drp)
                     cilow
        estimate
                                 ciupp
                                        log.est
Bmsyd 87.2283941 37.377636 203.5653831 4.468530
Fmsyd 0.2523111 0.093779
                            0.6788392 -1.377093
MSYd 22.0086909 17.061391 28.3905610 3.091437
Stochastic reference points (Srp)
        estimate
                      cilow
                                        log.est rel.diff.Drp
                                 ciupp
Bmsys 86.1721784 37.1707121 199.771377 4.456347 -0.012257038
Fmsys 0.2500268 0.0921861 0.678122 -1.386187 -0.009136167
MSYs 21.5429413 16.5473161 28.046743 3.070048 -0.021619591
States w 95% CI (inp$msytype: s)
                 estimate
                               cilow
                                          ciupp
                                                   log.est
B_1989.00
               59.8081015 20.7927035 172.031934
                                                4.0911411
F 1989.00
                0.4264686 0.1528595
                                      1.189821 -0.8522164
B 1989.00/Bmsy 0.6940535 0.4759258
                                       1.012154 -0.3652062
F 1989.00/Fmsy 1.7056917 1.0390604
                                       2.800015 0.5339707
Predictions w 95% CI (inp$msytype: s)
               prediction
                              cilow
                                          ciupp
                                                   log.est
B 1990.00
               54.5156897 17.2286845 172.500716 3.9984885
F 1990.00
                0.4313747 0.1427056
                                      1.303973 -0.8407781
B_1990.00/Bmsy 0.6326368 0.3741020
                                       1.069840 -0.4578588
F_1990.00/Fmsy 1.7253140 0.9361420
                                       3.179762 0.5454091
Catch_1990.00 22.6023846 14.8441308 34.415474 3.1180554
E(B_inf)
               20.7049018
                                  NA
                                             NA
                                                3.0303705
```

The summary indicates that the priors are so informative that the quantities are essentially fixed. It is also noted that the estimates of these quantities are very close to the mean of their respective priors.

Pitfalls when fixing parameters and specifying priors

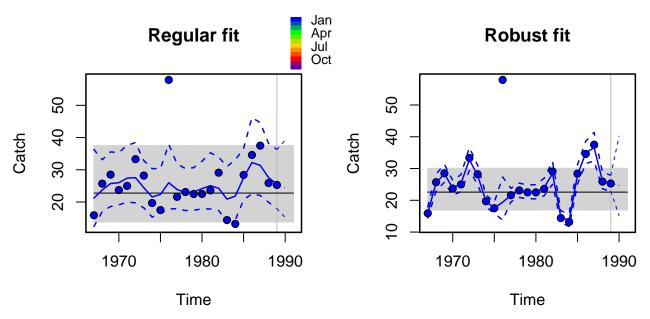
Particular caution is required when fixing a parameter that is highly correlated with other parameters because this will to some extent restrict the estimates of the correlated parameters. This could also be a problem when specifying priors depending on the amount of a priori information available.

Robust estimation (reducing influence of extreme observations)

The presence of extreme observations may inflate estimates of observation noise and increase the general uncertainty of the fit. To reduce this effect it is possible to apply a robust estimation scheme, which is less sensitive to extreme observations. An example with an extreme observation in the catch series is

```
inp <- pol$albacore
inp$obsC[10] <- 3*inp$obsC[10]
res1 <- fit.spict(inp)
inp$robflagc <- 1
res2 <- fit.spict(inp)
sumspict.parest(res2)</pre>
```

```
estimate
                               cilow
                                             ciupp
                                                      log.est
            8.01383375
                          1.14064161
                                       56.30298849
                                                    2.0811693
   alpha
   beta
            0.13903414
                          0.02002425
                                        0.96535421 -1.9730357
                                        0.65159133 -1.3592467
            0.25685420
                          0.10125070
   r
                                        3.84722637 -0.3101324
   rc
            0.73334989
                          0.13978955
   rold
            0.85759756
                          0.00140610 523.05883208
                                                   -0.1536203
           22.57344335
                         16.94359773
                                       30.07391659
                                                    3.1167741
   m
          202.06196157 137.06067492 297.89023247
                                                    5.3085744
   K
                                        0.64137140 -1.0565050
            0.34766878
                          0.18846113
   q
   n
            0.70049565
                          0.06408927
                                        7.65641659 -0.3559671
   sdb
            0.01371149
                          0.00196485
                                        0.09568409 -4.2895209
   sdf
            0.37086365
                          0.26568565
                                        0.51767886 -0.9919208
   sdi
            0.10988163
                          0.08106901
                                        0.14893450 -2.2083516
   sdc
            0.05156271
                          0.00843494
                                        0.31520244 -2.9649566
            0.95304961
                          0.72886830
                                        0.99351826
                                                    3.0105755
   pp
   robfac
           20.83563743
                          2.67330915 236.13438145
                                                    2.9874802
par(mfrow=c(1, 2))
plotspict.catch(res1, main='Regular fit')
plotspict.catch(res2, qlegend=FALSE, main='Robust fit')
```



It is evident from the plot that the presence of the extreme catch observation generally inflates the uncertainty of the estimated catches, while the robust fit is less sensitive. Robust estimation can be applied to index and effort data using robflagi and robflage respectively.

Robust estimation is implemented using a mixture of light-tailed and a heavy-tailed Gaussian distribution as described in Pedersen and Berg (2016). This entails two additional parameters (pp and robfac) that require estimation. This may not always be possible given the increased model complexity. In such cases these parameters should be fixed by setting their phases to -1.

Forecasting and management scenarios

To make a catch forecast a forecast interval needs to be specified. This is done by specifying the start of the interval (inp\$timepredc) and the length of the interval in years (inp\$dtpredc). For example, if a forecast

of the annual catch of 2018 is of interest, then inp\$timepredc = 2018 and inp\$dtpredc = 1. In addition to the forecast interval a fishing scenario needs to be specified. This is done by specifying a factor (inp\$ffac) to multiply the current fishing mortality by (i.e. the F at the last time point of the time period where data are available) and the time that management should start (inp\$manstart). The time point of the reported forecast of biomass and fishing mortality can be controlled by setting inp\$timepredi. Producing short-term forecasts entails minimal additional computing time.

Forecasts are produced as part of the usual model fitting. To illustrate the procedure, a short example using the South Atlantic albacore dataset of Polacheck, Hilborn, and Punt (1993) containing catch and commercial CPUE data in the interval 1967 to 1989 is presented. The code to obtain the forecasted annual catch in the interval starting 1991 under a management scenario where the fishing pressure is reduced by 25% starting in 1991, and a forecasted index in 1992 is:

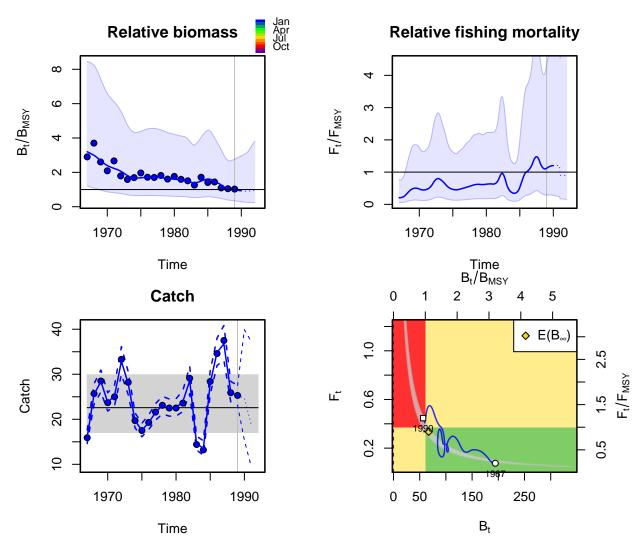
```
library(spict)
data(pol)
inp <- pol$albacore
inp$manstart <- 1991
inp$timepredc <- 1991
inp$dtpredc <- 1
inp$timepredi <- 1992
inp$ffac <- 0.75
res <- fit.spict(inp)</pre>
```

To specifically show forecast results use

```
sumspict.predictions(res)
                  prediction
                                   cilow
                                              ciupp
                                                         log.est
  B_1992.00
                  58.0404387 28.74512737 117.191776
                                                     4.06113999
  F 1992.00
                   0.3348379
                             0.09426505
                                           1.189374 -1.09410874
  B 1992.00/Bmsy 0.9556116
                             0.23937468
                                           3.814912 -0.04540377
  F 1992.00/Fmsy 0.9006312
                                           5.273748 -0.10465949
                              0.15380645
  Catch 1991.00
                  18.8028897
                              9.48829836
                                          37.261545
                                                     2.93401056
  E(B_inf)
                  67.1854881
                                      NA
                                                 NA
                                                     4.20745727
```

This output is also shown when using summary(res). The results can be plotted using plot(res), however to visualise the change in forecasted fishing mortality and associated change in forecasted catch more clearly we use

```
par(mfrow=c(2, 2), mar=c(4, 4.5, 3, 3.5))
plotspict.bbmsy(res)
plotspict.ffmsy(res, qlegend=FALSE)
plotspict.catch(res, qlegend=FALSE)
plotspict.fb(res, man.legend=FALSE)
```



Note in the plot that the decrease in fishing pressure results in a constant biomass as opposed to the expected decrease if fishing effort had remained constant.

Management scenarios

The package has a function that runs several predefined management scenarios, which can be presented in a forecast table. To perform the calculations required to produce the forecast table run:

```
res <- manage(res)
```

where res is the result of fit.spict() from the code above. Then, the results can be summarised (and extracted) by running:

```
df <- mansummary(res)
   Observed interval, index: 1967.00 - 1989.00
   Observed interval, catch: 1967.00 - 1990.00

Fishing mortality (F) prediction: 1992.00
Biomass (B) prediction: 1992.00
Catch (C) prediction interval: 1991.00 - 1992.00</pre>
```

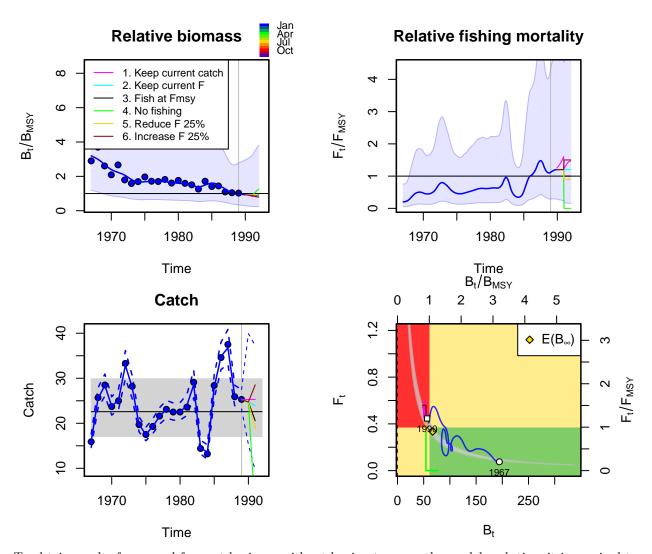
```
Predictions
                         C
                                    F B/Bmsy F/Fmsy perc.dB perc.dF
                              В
1. Keep current catch 25.3 47.7 0.545
                                       0.785
                                              1.465
                                                       -12.2
                                                                22.0
2. Keep current F
                                              1.201
                                                        -2.7
                      23.9 52.9 0.446
                                      0.870
                                                                 0.0
3. Fish at Fmsy
                      20.6 56.3 0.372 0.926
                                              1.000
                                                         3.6
                                                               -16.7
4. No fishing
                       0.0 77.0 0.000
                                       1.267
                                              0.001
                                                        41.8
                                                               -99.9
5. Reduce F 25%
                      18.8 58.0 0.335 0.955 0.901
                                                         6.9
                                                               -25.0
6. Increase F 25%
                      28.5 48.1 0.558 0.793 1.501
                                                       -11.3
                                                                25.0
95% CIs of absolute predictions
                      C.lo C.hi B.lo B.hi F.lo F.hi
1. Keep current catch 25.3 25.3 22.9 99.5 0.244 1.215
2. Keep current F
                      12.5 45.6 24.0 116.4 0.126 1.586
3. Fish at Fmsy
                      10.5 40.2 27.1 116.9 0.105 1.321
4. No fishing
                       0.0 0.1 48.5 122.3 0.000 0.002
5. Reduce F 25%
                       9.5 37.3 28.7 117.2 0.094 1.189
6. Increase F 25%
                     15.5 52.5 20.0 115.9 0.157 1.982
95% CIs of relative predictions
                      B/Bmsy.lo B/Bmsy.hi F/Fmsy.lo F/Fmsy.hi
1. Keep current catch
                                    2.640
                          0.234
                                               0.356
                                                         6.019
2. Keep current F
                          0.211
                                    3.595
                                              0.205
                                                         7.032
3. Fish at Fmsy
                          0.230
                                                         5.856
                                    3.737
                                               0.171
4. No fishing
                          0.334
                                    4.802
                                              0.000
                                                         0.007
5. Reduce F 25%
                          0.239
                                    3.815
                                               0.154
                                                         5.274
6. Increase F 25%
                          0.184
                                    3.413
                                              0.256
                                                         8.790
```

Then, df is a data frame with each line containing a line of the output

```
head(df)
                                 В
                                       F B/Bmsy F/Fmsy perc.dB perc.dF
   1. Keep current catch 25.3 47.7 0.545
                                         0.785
                                                1.465
                                                         -12.2
                                                                  22.0
                                                          -2.7
                                                                   0.0
   2. Keep current F
                         23.9 52.9 0.446 0.870
                                                 1.201
  3. Fish at Fmsy
                         20.6 56.3 0.372 0.926
                                                 1.000
                                                           3.6
                                                                 -16.7
  4. No fishing
                          0.0 77.0 0.000 1.267
                                                 0.001
                                                          41.8
                                                                  -99.9
   5. Reduce F 25%
                         18.8 58.0 0.335 0.955
                                                 0.901
                                                           6.9
                                                                  -25.0
  6. Increase F 25%
                         28.5 48.1 0.558 0.793 1.501
                                                         -11.3
                                                                  25.0
```

The resulting biomass, fishing mortality and catch of the management scenarios are included in the standard plots

```
par(mfrow=c(2, 2), mar=c(4, 4.5, 3, 3.5))
plotspict.bbmsy(res)
plotspict.ffmsy(res, qlegend=FALSE)
plotspict.catch(res, qlegend=FALSE)
plotspict.fb(res, man.legend=FALSE)
```



To obtain results for several forecast horizons without having to rerun the model each time it is required to set inp\$timepredc equal to the longest horizon of interest. For example

```
inp <- pol$albacore
inp$timepredc <- 1991
res <- fit.spict(inp)
res <- manage(res)</pre>
```

Then the management table for 1990 is:

```
mansummary(res, ypred=1, include.unc = FALSE)
   Observed interval, index: 1967.00 - 1989.00
   Observed interval, catch: 1967.00 - 1990.00
  Fishing mortality (F) prediction: 1991.00
   Biomass (B) prediction:
                                     1991.00
   Catch (C) prediction interval:
                                     1990.00 - 1991.00
   Predictions
                                       F B/Bmsy F/Fmsy perc.dB perc.dF
                            C
                                 В
   1. Keep current catch 25.3 53.7 0.472
                                          0.885
                                                 1.269
                                                           -4.9
                                                                    5.7
   2. Keep current F
                         24.7 54.3 0.446 0.894
                                                 1.201
                                                           -3.9
                                                                    0.0
```

```
3. Fish at Fmsy
                       21.3 57.8 0.372
                                        0.952
                                                1.000
                                                           2.3
                                                                 -16.7
4. No fishing
                        0.0 79.1 0.000
                                                0.001
                                                                 -99.9
                                         1.303
                                                          40.0
5. Reduce F 25%
                       19.4 59.6 0.335
                                        0.982
                                                0.901
                                                           5.5
                                                                 -25.0
6. Increase F 25%
                       29.5 49.5 0.558
                                       0.814
                                                1.501
                                                         -12.5
                                                                  25.0
```

and for 1991 is:

```
mansummary(res, vpred=2, include.unc = FALSE)
   Observed interval, index: 1967.00 - 1989.00
   Observed interval, catch:
                              1967.00 - 1990.00
  Fishing mortality (F) prediction: 1992.00
  Biomass (B) prediction:
                                      1992.00
   Catch (C) prediction interval:
                                      1991.00 - 1992.00
   Predictions
                            C
                                   В
                                         F B/Bmsy F/Fmsy perc.dB perc.dF
   1. Keep current catch 25.3
                               50.9 0.490
                                                   1.317
                                            0.837
                                                           -10.0
                                                                      9.7
                                                   1.201
                                                            -6.5
   2. Keep current F
                         23.9
                               52.9 0.446
                                            0.870
                                                                      0.0
   3. Fish at Fmsy
                         21.7
                               58.7 0.372
                                            0.967
                                                   1.000
                                                             3.9
                                                                    -16.7
   4. No fishing
                                                   0.001
                                                            77.6
                                                                    -99.9
                          0.0 100.4 0.000
                                            1.652
   5. Reduce F 25%
                         20.3 61.9 0.335
                                            1.019
                                                   0.901
                                                             9.5
                                                                    -25.0
   6. Increase F 25%
                         26.4 45.2 0.558
                                           0.745
                                                  1.501
                                                           -20.0
                                                                     25.0
```

Other model settings and options

catchunit - Define unit of catch observations

This will print the unit of the catches on relevant plots.

Example: inp\$catchunit <- "'000 t".

dteuler and eulertype - Temporal discretisation and time step

To solve the continuous-time system an Euler discretisation scheme is used. This requires a time step to be specified (dteuler). The smaller the time step the more accurate the approximation to the continuous-time solution, however with the cost of increased memory requirements and computing time. The default value of dteuler is 1/16, which seems sufficiently fine for most cases, and perhaps too fine for some cases. When fitting quarterly data and species with fast growth it is important to have a small dteuler. The influence of dteuler on the results can be checked by using different values and comparing resulting model estimates. If dteuler <- 1 the model essentially becomes a discrete-time model with one Euler step per year.

There are two possible temporal discretisation schemes which can be set to either eulertype = 'hard' (default) or eulertype = 'soft'. If eulertype = 'hard' then time is discretised into intervals of length dteuler. Observations are then assigned to these intervals. For annual and quarterly data dteuler = 1/16 is appropriate, however if fitting to monthly data dteuler should be changed to e.g. 1/24. If eulertype = 'soft' (careful, this feature has not been thoroughly tested), then time is discretised into intervals of length dteuler and additional time points corresponding to the times of observation are added to the discretisation. This feature is particularly useful if observations (most likely index series) are observed at odd times during the year. The model then estimates values of biomass and fishing mortality at the exact time of the observation instead of assigning the observation to an interval.

msytype - Stochastic and deterministic reference points

As default the stochastic reference points are reported and used for calculation of relative levels of biomass and fishing mortality. It is, however, possible to use the deterministic reference points by setting <code>inp\$msytype <- 'd'</code>.

do.sd.report - Perform SD report calculations

The sdreport step calculates the uncertainty of all quantities that are reported in addition to the model parameters. For long time series and with small dteuler this step may have high memory requirements and a substantial computing time. Thus, if one is only interested in the point estimates of the model parameters it is advisable to set do.sd.report <- 0 to increase speed.

reportall - Report all derived quantities

If uncertainties of some quantities (such as reference points) are required, but uncertainty on state variables (biomass and fishing mortality) are not needed, then reportall <- 0 can be used to increase speed.

optim.method - Report all derived quantities

Parameter estimation is per default performed using R's nlminb() optimiser. Alternatively it is possible to use optim by setting inp\$optim.method <- 'optim'.

References

Pedersen, Martin W, and Casper W Berg. 2016. "A Stochastic Surplus Production Model in Continuous Time." Fish and Fisheries. Wiley Online Library. doi:10.1111/faf.12174.

Polacheck, Tom, Ray Hilborn, and Andre E Punt. 1993. "Fitting Surplus Production Models: Comparing Methods and Measuring Uncertainty." *Canadian Journal of Fisheries and Aquatic Sciences* 50 (12). NRC Research Press: 2597–2607.