0.1 Explanation of Code

Here we have a bibd solver of design (6, 10, 3, 2, 5). We use the idea of backtracking and the program call stack to solve this problem. First, we initialize our blocks as lists within a list. We then define what constitutes as a complete block, a valid block, and how to find the first empty spot in a block. The main logic of the program guesses numbers in ascending order to speed up the result. Lastly, we test the run time of the definition.

```
1  import time
2
3  # BIBD conditions
4  nr_blocks = 10
5  pts_per_block = 3
6  nr_elements = 6
7  distinct = 2
8  blks_with_point = 5
9
10 blocks = [pts_per_block*[0] for _ in range(nr_blocks)]
11
12 # should work (not tested)
13 def is_complete(blocks):
14     for block in range(10):
```

```
        for i in range(3):
            if blocks[block][i] == 0:
                return False
    return True


# both conditions tested and working
def is_valid(blocks):
  # count data structures
  elCount = [0]*nr_elements
  pairs = {"12": 0, "13": 0, "14": 0, "15": 0, "16": 0, "23": 0, "24
   ": 0, "25": 0, "26": 0, "34": 0, "35": 0, "36": 0, "45": 0, "46":
    0, "56": 0}

  # check that an element appears exactly 5 times in different
   blocks
  for block in range(10):
    for i in range(3):
      # if the given position isn't a zero we want to investigate it
      if blocks[block][i] != 0:
        # record that we have seen the element
        elCount[(blocks[block][i]) - 1] += 1

```

```
34  # determine if the element count is valid
35  for num in elCount:
36    # if a element appears more than 5 times accross the blocks the
     solution is invalid
37    if num > 5:
38      return False
39
40  # check that any pair of elements is in two blocks
41  for block in range(10):
42    if blocks[block][1] != 0:
43      pair1 = str(blocks[block][0]) + str(blocks[block][1])
44      pairs[pair1] += 1
45    if blocks[block][2] != 0:
46      pair2 = str(blocks[block][1]) + str(blocks[block][2])
47      pairs[pair2] += 1
48      pair3 = str(blocks[block][0]) + str(blocks[block][2])
49      pairs[pair3] += 1
50    else:
51      # do nothing its a pair with a zero in it
52      pass
53
54  # determine if the pair count is valid
```

```
55    for num in pairs.values():
56      # if a given pair appears more then two times the solution is
       invlaid
57      if num > 2:
58        return False
59
60    # all validity tests passed
61    return True
62
63  # appears to be working (somewhat tested)
64  def find_first_empty(blocks):
65    for block in range(10):
66      for i in range(3):
67        if blocks[block][i] == 0:
68          return block, i
69
70  # prints blocks accordingly
71  def print_it(blocks):
72    for block in range(10):
73      print(blocks[block])
74
75  # main logic
```

```
76 def bibd(blocks):
77   if is_complete(blocks):
78     return blocks
79   # blk is a block , i an index, this is the first block with a 0
80   blk, i = find_first_empty(blocks)
81   for num in range(max(blocks[blk])+1, nr_elements+1):
82     blocks[blk][i] = num
83     if is_valid(blocks):
84       result = bibd(blocks)
85       if is_complete(result):
86         return result
87     blocks[blk][i] = 0
88   return blocks
89
90
91 # TESTING
92
93 # def(s) testing
94 # print(find_first_empty(blocks))
95 # print(is_complete(blocks))
96 # print_it(blocks)
97 # print(is_valid(blocks))
```

```
98 # print_it(blocks)
99 # [6, 0, 0]
100
101 # trial runner
102 start_time = time.perf_counter()
103 bibd(blocks)
104 print(time.perf_counter() - start_time)
```

Algorithm 1: **bibd solver Python 3.9**

0.2 Output

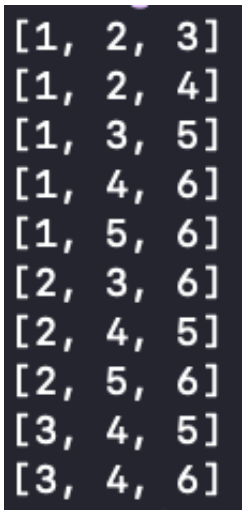

Figure 1: Output of Program

0.3 Run time

These run times were captured on a Quad-Core Intel Core i5 at 1.4 GHz.

bibd() Python 3.9

Trial #	bibd() (secs)
1	33.69
2	33.59
3	33.49
4	33.21
5	33.42
6	33.3
7	33.43
8	33.29
9	33.28
10	33.18
11	33.19
12	33.69
13	33.05
14	33.86
15	32.89
16	33.40
17	33.26
18	33.09
19	33.45
20	32.97

Figure 2: Table of run times