

March, 10th 2020 DU Bioinformatique intégrative Module 3: « R et statistiques »





Session 3

Statistiques pour les données omiques

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Helpers: Antoine Bridier-Nahmias, Anne Badel

Plan de la séance

Retour sur les séances 1 et 2:

- debrief sur les commandes R
- TP part I : données simulées
- debrief sur les stats de base

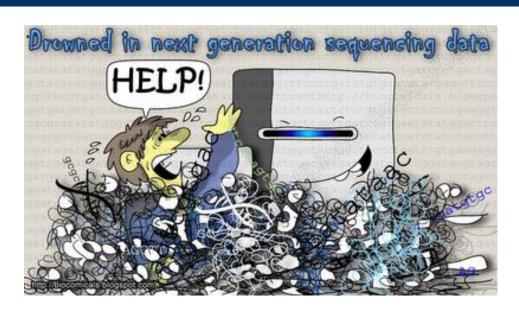
Coffee break

Statistiques pour les données omiques:

- TP part II : "industrialisation" des tests d'hypothèses
- cours part I :
 - donner du sens aux données omiques et problèmes de dimensionnalité
 - 1^{er} problème: tests multiples
- TP –part III: tests multiples
- cours part II :
 - 2^{ème} problème: estimation des paramètres des distributions
 - 3^{ème} problème: réduction de la dimensionnalité -> cf. sessions suivantes

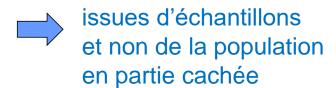
Liens

Deux difficultés dans la mise en evidence d'effet









1. Introduction: making sense of omic's data

Ome/Omics

COMMENTARY

'Ome Sweet 'Omics-A Genealogical Treasury of Words

By Joshua Lederberg and Alexa T. McCray

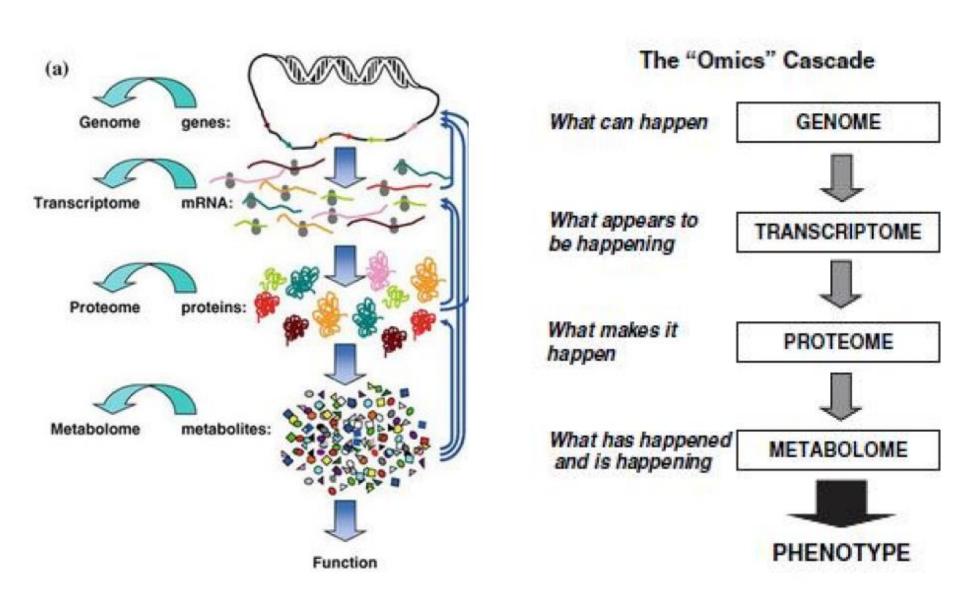
The Scientist 15[7]:8, Apr. 2, 2001

antigenome	immunogenome	plastidome
bacteriome	immunome	plerome
basidiome	haptenome	proteinome
biome	karyome	proteome
cardiome	leptome	psychome
caulome	microbiome	regulome
chondriome	mnemome	rhabdome
cladome	mycetome	rhizome
coelome	neurome	stereome
epigenome	odontome	thallome
erythrome	osteome	tracheome
genome	pharmacogenome	transcriptome
geome	phenome	trichome
hadrome	phyllome	vacuome
histome	physiome	

Genomics and Proteomics are the buzzwords of the dawning millennium. There is no counting of www.-ix.com and sites to be found on the Web. That most of these terms, old and new, have been contrived as slogans to attract attention, does not diminish their likely substance, and they are embedded in the advancing edge of science and technology.

https://lhncbc.nlm.nih.gov/system/files/pub2001047.pdf

Integration des données omiques



Heterogénéité des données omiques

Nature des données

- binaires (eg. présence ou absence d'un allèle ou d'un site de liaison)
- catégoriques (séquences de site consensus, isoforme exprimée)
- quantitative discrète (génotypes: 0, 1, 2)
- quantitative continue (niveau d'expression d'un gène ou d'une protéine)

Dimension des données (exemples chez l'homme)

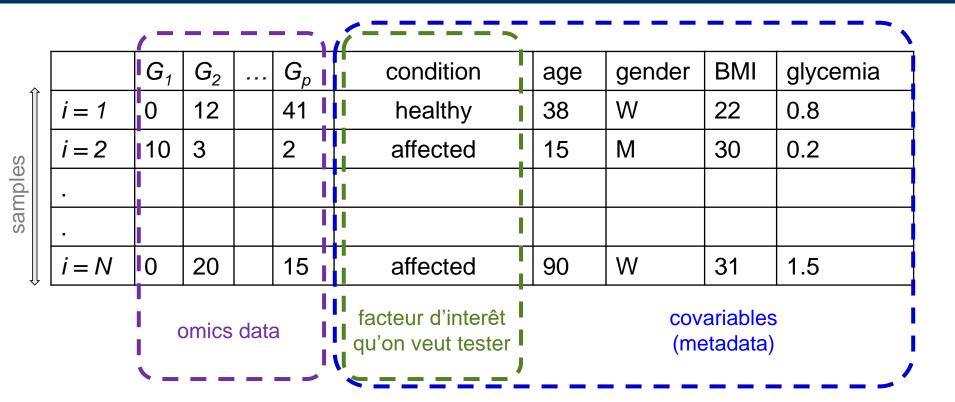
- génome (4x10⁶ de variants bi-alléliques de type SNP)
- transcriptome (20-60 000 gènes, 200 000 transcrits)
- protéome (18 000 protéines, 293 000 peptides)

Données manquantes (4000 protéines)

Structure des données

- corrélations entre les variables mesurées (déséquilibre de liaison, co-expression...)
- corrélations entre les types de données

En plus, des données non-omiques peuvent exister = co-variables



- Par exemple, on peut avoir le niveau d'expression par gène pour chaque échantillon
- On peut aussi avoir des données cliniques pour les échantillons incluant le facteur d'intérêt qu'on veut tester et d'autres covariables qui pourraient impacter les niveaux d'expression
- On souhaite expliquer les variations d'expression (variable expliquée) en fonction de covariables cliniques (variables explicatives)

Why using statistics?

Making sense of data

Aim: identify variables whose variation levels are associated with a phenotype or a covariate of interest (eg: response to stress, to a treatment, survival, mutation, tumor class, time...)

Variable to explain ~ explanatory variables + covariates + residual error

Problems addressed by statistics:

- 1. estimation: of the effects of interest and of how they vary
- 2. testing: = assessing the statistical significance of the observed effects

Quels facteurs peuvent expliquer la variation d'un trait?

Variation inter-groupes

- 1. Facteur/covariables d'intérêt => design experimental
 - conditions expérimentales testées: stimulus, traitement, temps, maladie...
 - √ variabilité génétique: mutation
 - ✓ tissus/type cellulaire...
- 2. Variation technique: réplicats techniques
 - ✓ experimental: lot, jour, expérimentateur, temperature ambiante...
 - ✓ multiplexage
 - √ variation de plate-forme

Variation intra-groupes

Variation biologique => réplicats biologiques

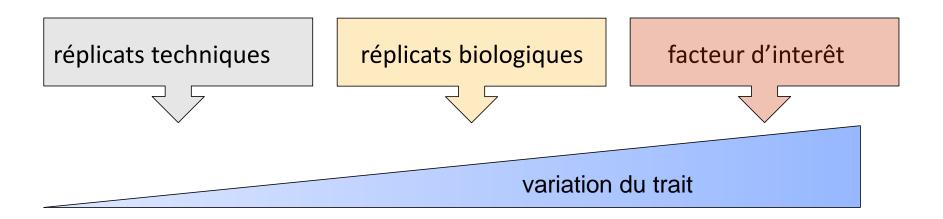
√ fluctuation d'échantillonnage

De l'importance d'un bon design experimental

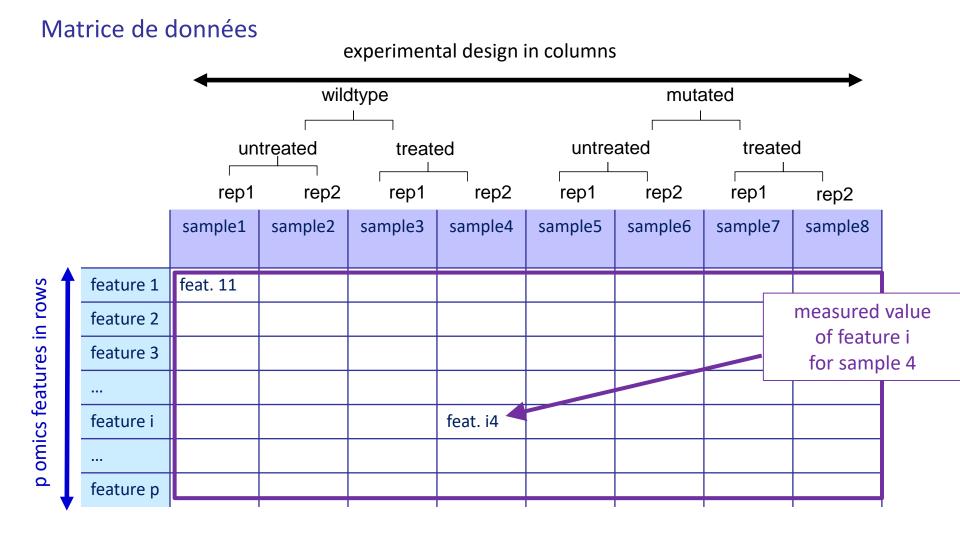
Les différences entre les conditions peuvent uniquement être testées si des **REPLICATS** sont inclus

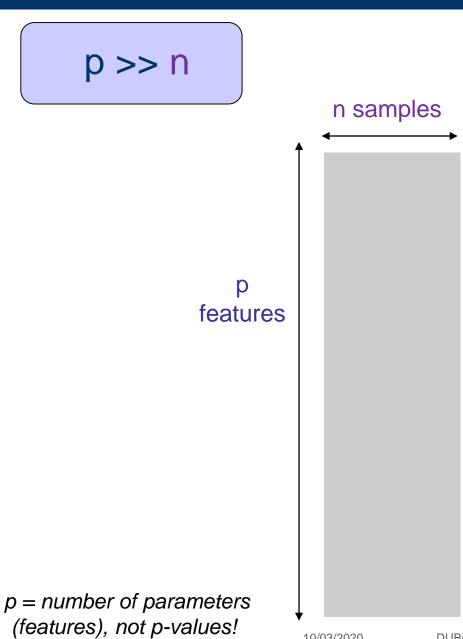
⇒ permettent de determiner quelles differences sont dues aux fluctuations aléatoires d'échantillonage

Ideal scenario :

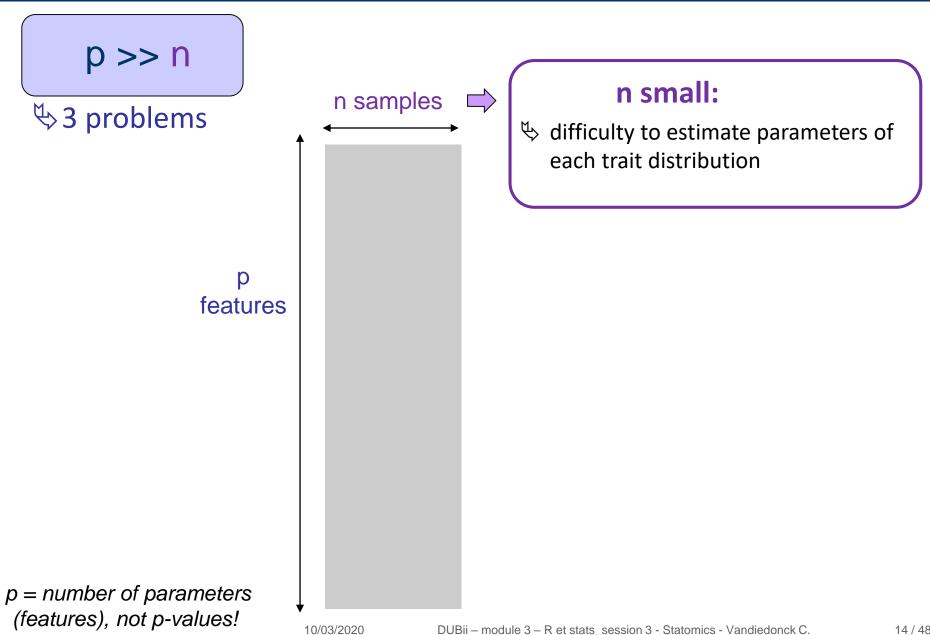


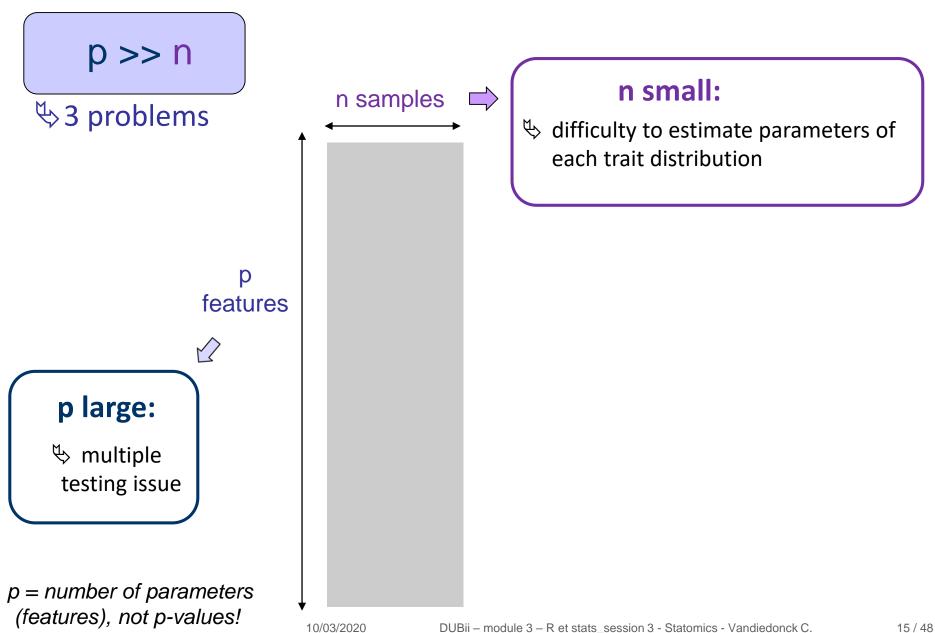
La structure des donées omiques

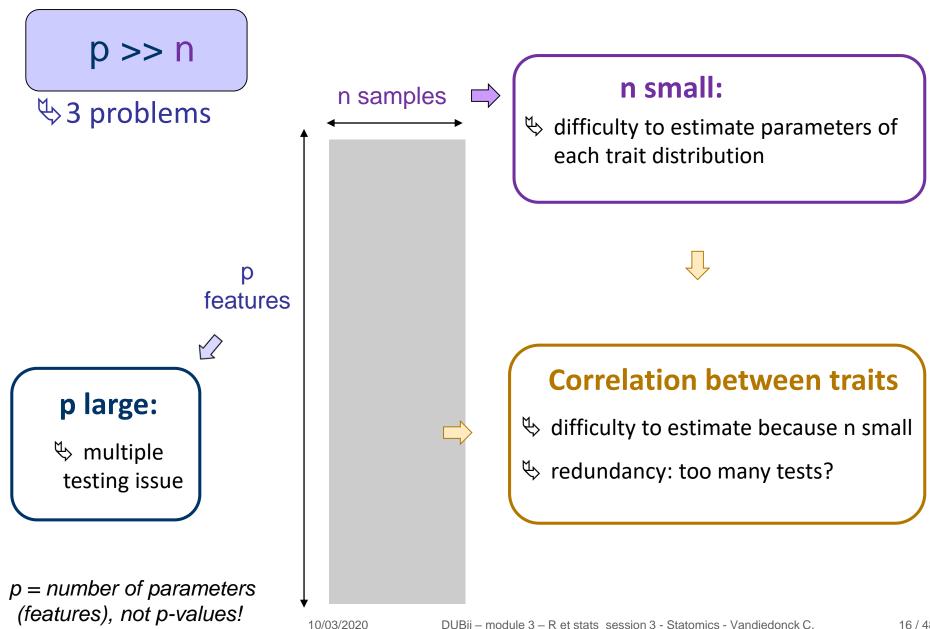












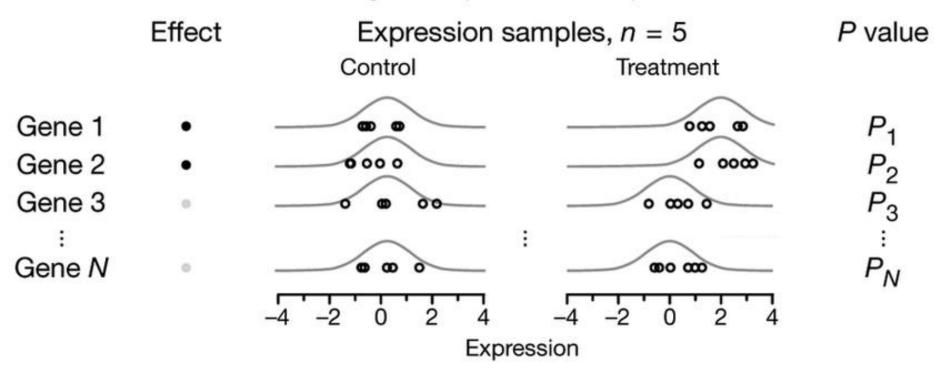
2. The 1st issue: multiple testing

The problem

We perform multiple tests = one per feature/trait

for each feature, we either reject or not H0 at a risk α = PCER = per-comparison error rate

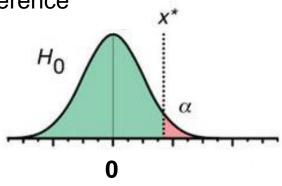
Simulation gene expression samples



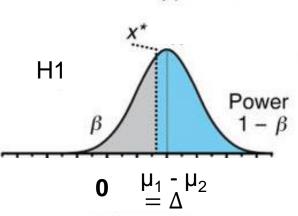
Test theory: alpha and beta risks

Null hypothesis
= no difference

 $\mu_1 = \mu_2$ $\Delta = 0$



Alternative hypothesis



= difference $\mu_1 \neq \mu_2$ $\Delta \neq 0$

Inference errors			
H ₀	Correct inference		
$1-\alpha$	1 - α		
	Power = 1- β		
H1 β 1 - β	Incorrect inference Type I error, α		
	Type II error, β		

Why is the problem so important?

Omics are big data:

A typical microarray or RNA-seq experiment: 10,000 genes

=> as many hypothesis tests

Just one hypothesis test:

For an α = 0.05, we tolerate to reject H₀ wrongly 5% of the times

but for 10,000 tests the number of false positives goes up to 500

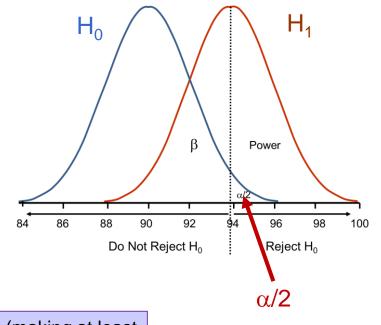
=> too many!!!

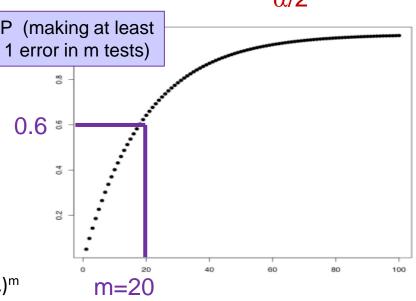
Expected value (e-value)

• Expected number of FP = E(FP)= $m\alpha$

Family-wise error rate (FWER)

- P(making an error) = α
- P(not making an error) = 1α
- P(not making an error in m tests)= $(1-\alpha)^m$
- **FWER** = P(making at least 1 error in m tests) = $1 (1-\alpha)^m$





Counting errors

Decision on H ₀	H _o True	H ₁ True	
reject	V (incorrect)	S	R
do not reject	٦	T (incorrect)	m-R
	m_0	m-m ₀	m

m = number of tests

 $R = number of rejected H_0$

 m_0 = number of true H_0

> only m and R are observed!

V = number of type I errors = false positives

By the way, where are:

the false negatives?

the true positives?

the true negatives?

Counting errors

Decision on H ₀	H _o True	H ₁ True	
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	m ₀	m-m ₀	m

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By the way, where are:

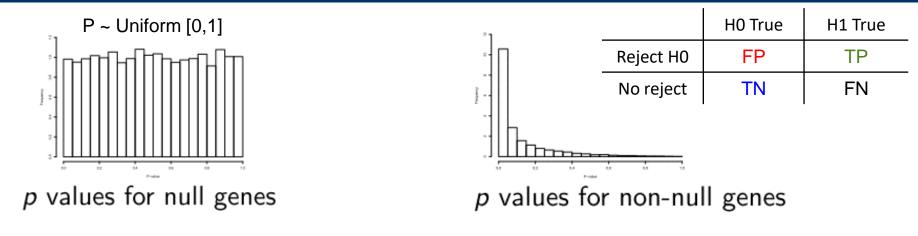
the false negatives?

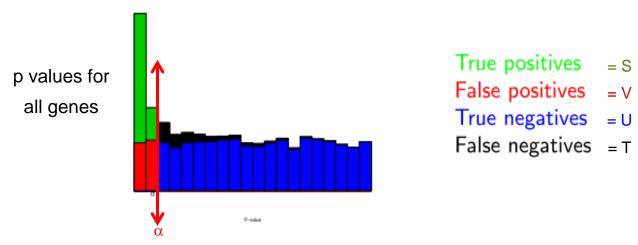
the true positives?

the true negatives?

	H0 True	H1 True
Reject H0	FP	TP
No reject	TN	FN

Controlling the type I error rate





Where to set the threshold of significance to control the type I error rate?

=> Trade-off between type I error and power!!

10/03/2020

Storey JD, Tibshirani R. Statistical significance for genomewide studies. PNAS. 2003 100:9440-5. PMID: 12883005; PubMed Central PMCID: PMC170937.

Bonferroni correction

Aim: to control the family-wise error rate (FWER):

- = the error rate across the whole collection/family of hypothesis tests
- = FWER = $P(V \ge 1)$ = probability of ≥ 1 false positive among all tests
- By "adjusting" the p value with the Bonferroni correction

$$set \alpha' = \alpha/m$$

reject hypotheses if $p < \alpha'$

✓ E.g. for a type I error rate of 0.05 per experiment (PCER) and m= 10 000 tests: $\alpha' = 0.05/10,000 = 5x10^{-6}$

very popular

the problem for "Omics" experiments: very conservative

=> alternative approaches investigated: very active area of current research in statistics!

False discovery rate (FDR)

We focus on positive tests (H₀ rejected):

FDR = proportion of false ^L positive among the set of rejected hypotheses (the "discoveries"):

✓
$$FDR = V/R$$

Decision on H ₀	H _o True	H ₁ True	
reject	V (incorrect)	S	R
do not reject	U	T (incorrect)	m-R
	m_0	m-m ₀	m

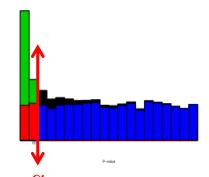
Decision on H ₀	H _o True	H ₁ True	
reject	V (incorrect)	S	R
do not reject	U	T (incorrect)	m-R
	m _o	m-m _o	m

A related parameter

= the False Positive Rate (FPR)

$$\checkmark$$
 FPR = V/m₀

	H0 True	H1 True
Reject H0	FP	TP
No reject	TN	FN



Benjamini-Hochberg procedure

To control FDR at level δ :

- ✓ order the unadjusted p-values: p1<p2<...<pm</p>
- ✓ find the test with the highest rank, j, for which the p value,

$$p_j \le \delta \frac{j}{m}$$

✓ Declare the tests of rank ≤ j as significant

1			

Example: m = 10 and $\delta = 0.05$

	Rank (j)	P-value	(j/m)× δ	Reject H ₀ ?	p _j x m /
	1	0.0008	0.005	1	0.008
	2	0.009	0.010	1	0.045
	3	0.018	0.015	0	0.06
l	4	0.030	0.020	0	0.075
	5	0.032	0.025	0	0.064
	6	0.048	0.030	0	0.08
	7	0.350	0.035	0	0.5
	8	0.781	0.040	0	0.976
	9	0.900	0.045	0	1
	10	0.993	0.050	0	0.993

Values expected for a uniform distribution of p_i between 0 and delta

Benjamini Y, Hochberg Y. Controlling the false discovery rate: a practical and powerful approach to multiple testing. JSTOR.1995, https://www.jstor.org/stable/2346101.

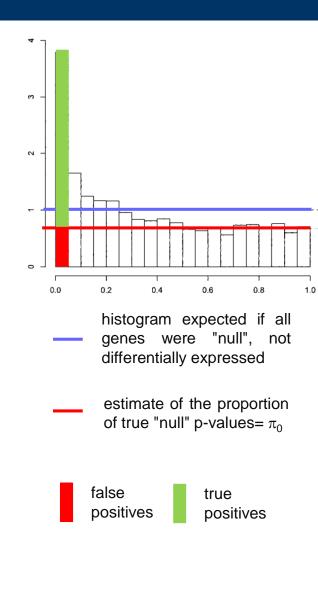
Adj. P val

Q values

Qvalue of a gene = expected proportion of false positives when calling that gene significant

- ✓ the q-value depends on the p-value for the test of the gene and on the distribution of the entire set of p-values from the family of tests being considered (Storey and Tibshiriani 2003)
- ✓ Thus, in a microarray study testing for differential expression, if gene X has a q-value of 0.013 it means that 1.3% of genes that show p-values at least as small as gene X are false positives
- ✓ The maths:
 - π_0 : the proportion of true null tests
 - $\alpha m \pi_0$: the number of false positives
 - $\alpha m \pi_0 / R$: an estimate of the FDR

	H0 True	H1 True	
Reject H0	FP	TP	R
No reject	TN	FN	m-R
	m ₀	m-m ₀	m ule 3 – R et stat



3. The 2nd issue: estimation of traits distribution (mean and variance)

To estimate or not to estimate?

1. No estimation when using non-parametric tests

- less power if data fit with parametric distribution
- not suitable for designs with several factors

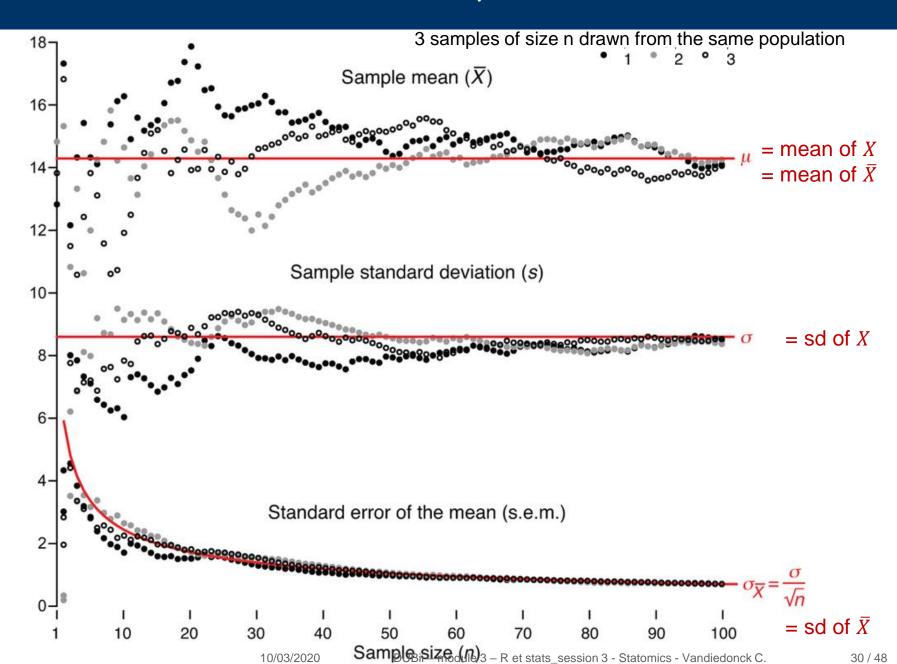
2. Random re-sampling

- approaching the distribution of p-values/statistics under null hypothesis by permutation (no replacement) of the levels of the factor of interest in the dataset => the empirical pvalue is the probability of observing the pvalue/statistic under the empirical distribution (cannot be lower than 1/1000 if 1000 permutations)
- estimating the CI of the distribution parameters by bootstrap (replacement) of the quantitated trait among all observed values within the dataset without changing the levels of the factor of interest
 - computationally intensive

3. Selecting a distribution law fitting the data

- estimation of mean and variance
- parametric tests

Better estimation when sample size is increased



Nature des données d'expression du transcriptome

Puces

L'abondance de chaque transcript dépend de l'intensité de fluorescence

=> variable quantitative continue

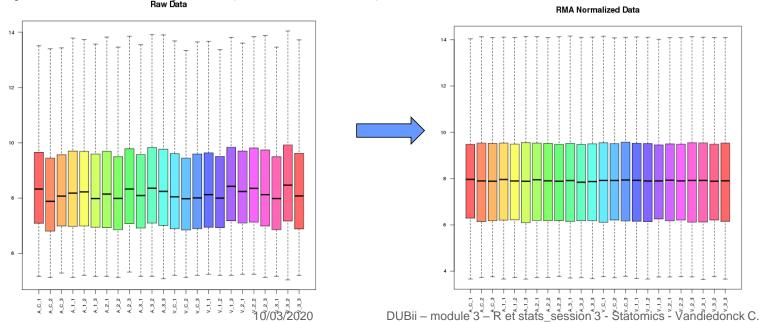
distribution asymétrique à droite

0 5 10 15 20 25 30 invensity

log2

-> le passage en log2 donne souvent une distribution 'normale' (1er sens de normalisation)

Il est aussi nécessaire de normaliser les échantillons entre eux (2ème sens de normalisation) pour pouvoir les comparer (même échelle)



Nature des données d'expression du transcriptome

RNASeq

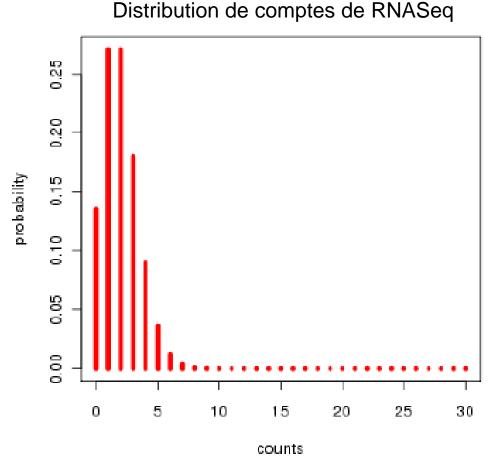
L'abondance des transcrits est mesurée par le nombre de lectures cartographies au niveau de la sequence génomique du transcrit

= comptes de lectures

🦫 Variable quantitative discrète

Iibrary I

Ygl = counts of reads mapping
to the feature/gene
gene g



=> Il faut utiliser la bonne loi de distribution (Poisson, Négative Binoimale...)

Estimating mean and variance in microarray experiments

Gene expression values are given by fluorescence intensities

- continuous variables
- assumed to fit a Student t distribution (after log2 transformation) of the difference mean

$$t_{\text{gene i}} = \frac{\bar{x_i}}{\tilde{s_i}/\sqrt{n}}$$

• but low number of replicates => difficult to estimate the variance

⇒ LIMMA (Linear Model for MicroArray experiments)

• uses a "moderated" t statistics using information from all genes (group of genes g like gene i) to estimate the variance

$$\tilde{t}_{\text{gene i}} = \frac{\bar{M}_i}{\tilde{s}_g/\sqrt{n}}$$

- allows for linear models
- design matrix => the factors to be accounted for in the model
- contrast matrix => which comparisons are of interest
- accounts for multiple testing: computes adjusted p-value (FDR B-H)

Estimating mean and variance in RNASeq experiments

In RNA-Seq, each feature (gene, exon, isoform) has an expression rate: each segment is sequenced with a low probability

Number of reads from gene g in library i can be captured by a Poisson model

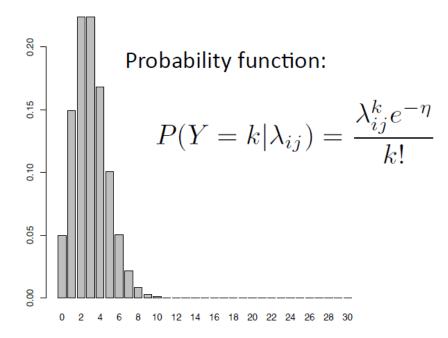
(Marioni et al. 2008)

$$r_{ij}$$
 ~Poisson $(\lambda_{ig} = \mu_{ig} k_{ig})$

where

 μ_{ig} is the concentration of the RNA k_{ig} is a normalisation constant

$$\hat{\mu}_{ig} = \frac{r_{ig}}{k_{ig}}$$



$$\lambda_{ig} = \mu_{ig} k_{ig} = E(r_{ij}) = Var(r_{ij})$$

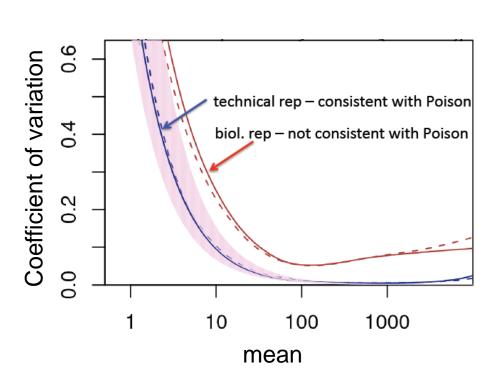
 $\$ If n Xiid ~Poisson (λ), Σ Xi ~Poisson (nλ)

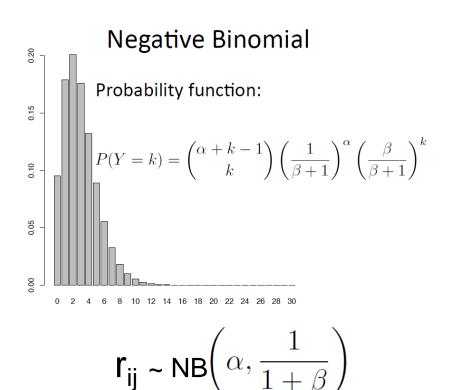
Need to account for extra variability

Poisson distribution accounts for technical variation

But biological noise induces an overdispersion

Convergence on a negative binomial model for count data

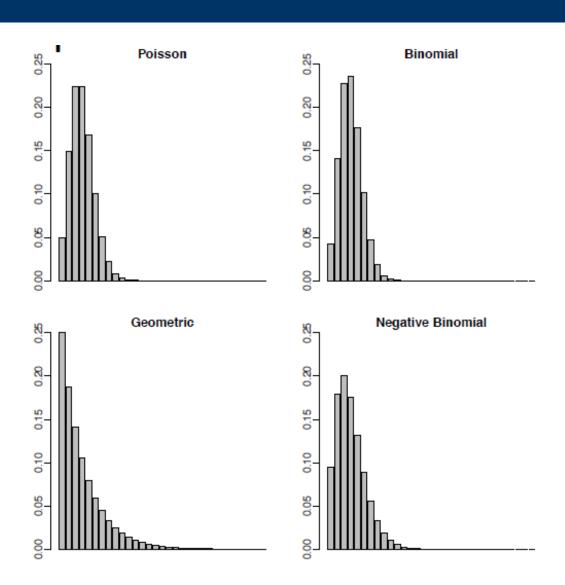




where α and β are the parameters of a gamma distribution followed by the rates of different samples

Examples of discrete distributions

- Binomial: probability of k successes of a Bernouilli variable
- Geometric: probability of k failures before 1st success
- Poisson: probability of k rare events
- Negative-binomial: probability of k failures before n successes



Modelling the variation

The example of DESeq and EdgeR

generalized linear model fitting the negative binomial distribution:

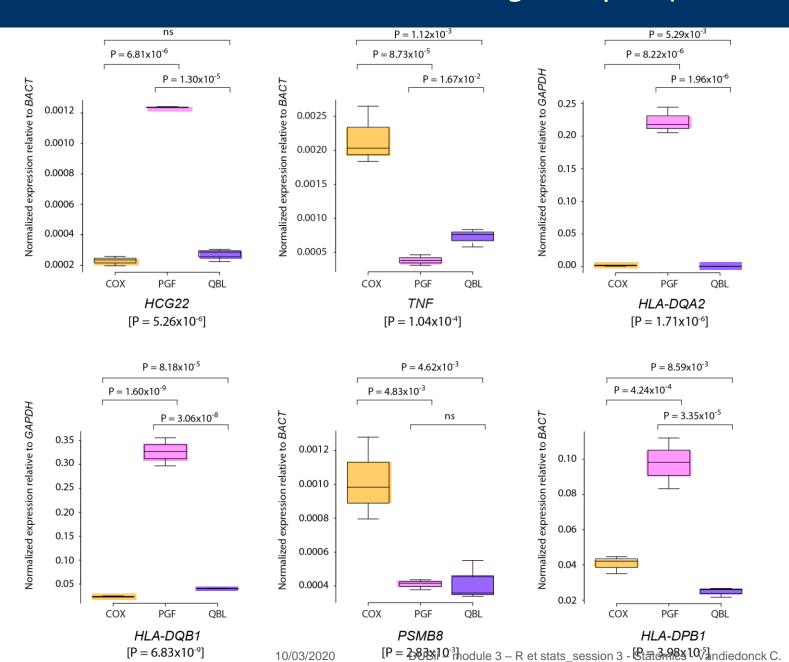
$$K_{ij} \sim NB(\mu_{ij}, \alpha_i)$$
 K_{ij} : counts of reads for gene i in sample j
 α_i : gene-specific dispersion parameter
 μ_{ii} : fitted mean

- $\mu_{ij} = s_j q_{ij}$ s_j : sample-specific size parameter q_{ij} : a parameter proportional to the expected true concentration of fragments for sample j
- $\log_2(q_{ij}) = x_{j.} \beta_i$ $\beta_i : \text{the log2 fold change for gene i for each column (j.) of the model matrix X}$

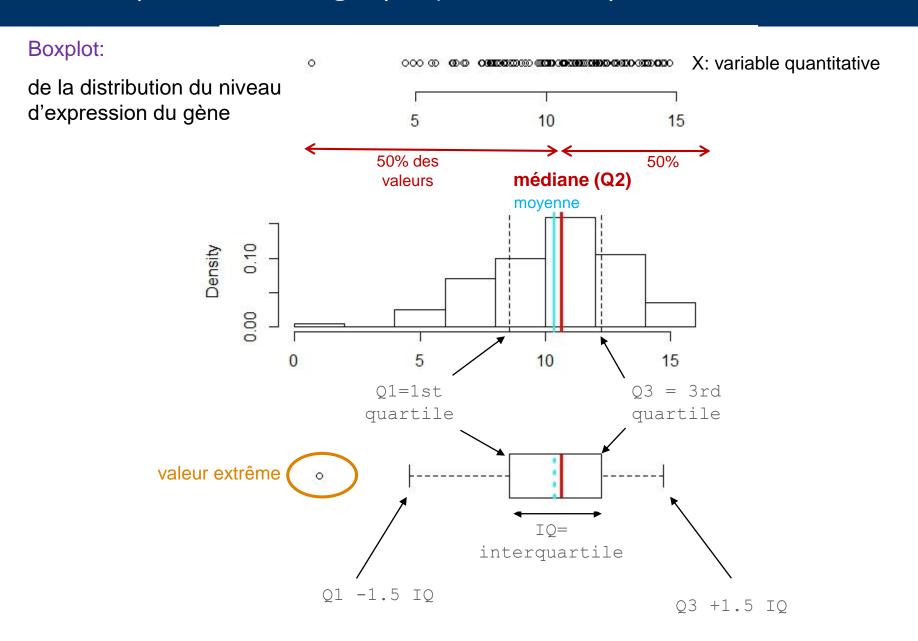
Exemple d'analyse de l'expression différentielle

Gene Name	Class	log2 (Fold Change)			Adj.P.Val
		COX vs PGF	QBL vs PGF	QBL vs COX	_
ZFP57	I	2.77	0.00	-2.76	1.22x10 ⁻¹⁴
HLA-DPB2 *	II	-3.19	-3.02	0.17	2.89×10^{-12}
HLA-DQA2	II	-2.45	-1.62	0.82	1.91x10 ⁻¹¹
HLA-DQB2	II	-2.74	-2.58	0.16	3.21x10 ⁻¹¹
HLA-21 *	I	-2.52	0.36	2.87	1.32×10^{-10}
TNF	III	1.90	1.03	-0.87	4.79×10^{-10}
HLA-DPB1	II	-2.08	-0.90	1.18	6.44x10 ⁻¹⁰
RPL32P1 *	II	-1.52	-1.19	0.33	2.07×10^{-09}
HLA-B	I	-0.06	-1.19	-1.13	6.59x10 ⁻⁰⁹
HLA-A	I	-1.51	-1.86	-0.35	2.30×10^{-08}
HLA-L *	I	-1.29	-1.47	-0.18	2.30×10^{-08}
XXbac-BPG254F23.6	II	-1.59	-1.59	0.00	2.50×10^{-08}
HCG22	I	-1.56	-1.26	0.30	2.96×10^{-08}
XXbac-BPG254F23.5	II	-1.42	-1.61	-0.19	1.33×10^{-07}
LTA	III	1.32	0.57	-0.75	2.04×10^{-07}
NCR3	III	0.87	0.95	0.08	4.95×10^{-07}
HLA-F	I	0.15	-0.90	-1.05	4.95×10^{-07}
HLA-DOA	II	-1.32	-0.89	0.43	5.07×10^{-07}
TAP1	II	0.97	0.08	-0.89	6.86×10^{-07}
LTB	III	-0.95	-0.06	0.89	7.02×10^{-07}
LST1	III	-0.18	0.48	0.66	9.42×10^{-07}
DAQB-335A13.8	I	0.61	-0.02	-0.63	1.12x10 ⁻⁰⁶
TCF19	I	1.11	0.62	-0.49	1.49×10^{-06}
CLIC1	III	1.22	0.57	-0.66	1.49x10 ⁻⁰⁶
HLA-DMA	II	-0.57	-0.89	-0.33	3.52×10^{-06}
BRD2	II	0.78	0.27	-0.51	3.60×10^{-06}
NRM	I	0.77	0.39	-0.38	4.48×10^{-06}
HLA-C	I	0.05	1.11	1.06	4.98x10 ⁻⁰⁶
PSMB9	II	0.42	-0.29	-0.71	6.05×10^{-06}
HCG27	I	0.56	0.06	-0.50	7.01x10 ⁻⁰⁶

Validation des meilleurs gènes par qPCR



Représentation graphique de l'analyse différentielle



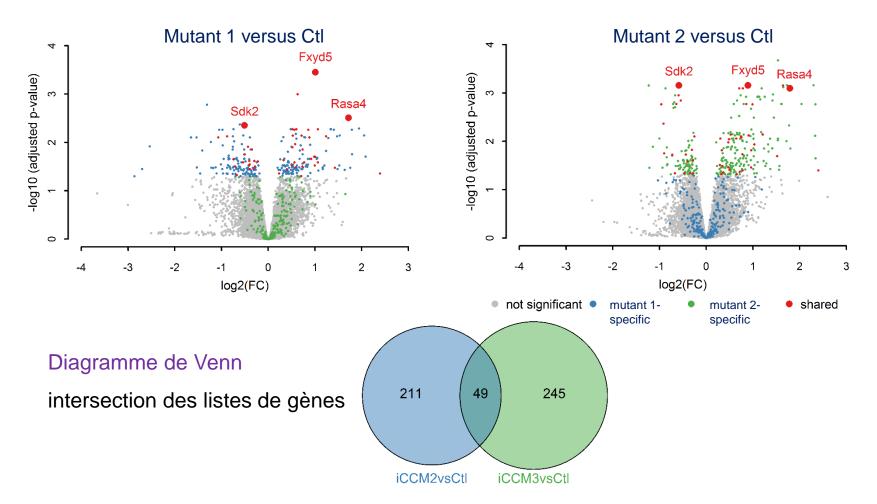
Représentation graphique de l'analyse différentielle

Volcano plots:

X = log2(Fold chnage)

Y = -log10 (pvalue)

Exemple ici chez la souris avec 2 gènes KO versus Wild Type



4. The 3rd issue: reducing dimensionality

-> cf. next sessions

5. Liens

Nature series: http://www.nature.com/collections/qghhqm

WEB COLLECTION

Statistics for biologists

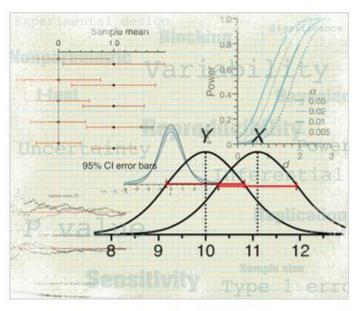
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Practical guides | Statistics in biology | Points of Significance | Other resources



There is no disputing the importance of statistical analysis in biological research, but too often it is considered only after an experiment is completed, when it may be too late.

This collection highlights important statistical issues that biologists should be aware of and provides practical advice to help them improve the rigor of their work.

Nature Methods' Points of Significance column on statistics explains many key statistical and experimental design concepts. Other resources include an online plotting tool and links to statistics guides from other publishers.

Image Credit: Erin DeWalt

Statistics in biology

Nature News | Editorial

Number crunch



Top picks

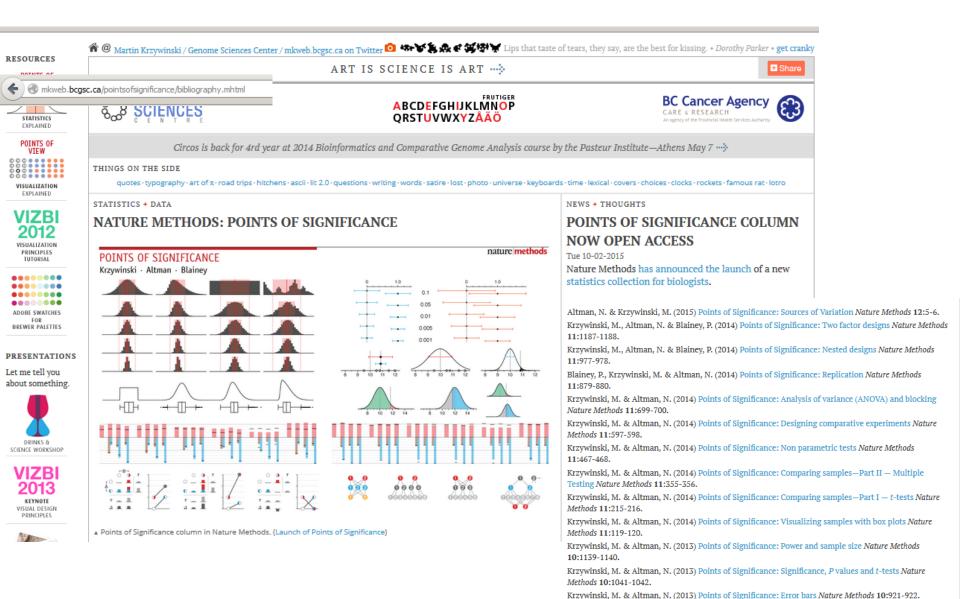
Nature News | News

Nature News | News

10/03/2020

DUBii - module 3 - R et stats_session 3 Schentific venethod CStatistical 44 / 48

Points of significance: http://mkweb.bcgsc.ca/pointsofsignificance/



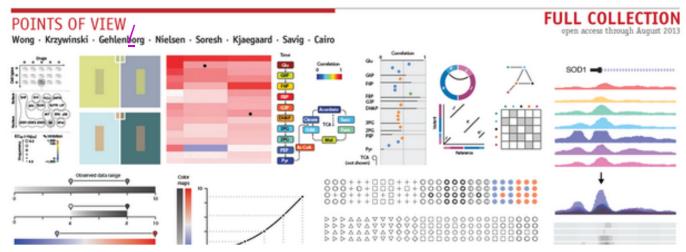
Krzywinski, M. & Altman, N. (2013) Points of Significance: Importance of being uncertain Nature Methods

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Points of view: http://mkweb.bcgsc.ca/pointsofview

COMMUNICATION + SCIENCE

NATURE METHODS: POINTS OF VIEW



▲ The full collection of a 35 Points of View column is now available. (3 years of Points of View)

PRACTICAL TIPS FOR EFFECTIVE FIGURES

POINTS OF VIEW — HISTORY

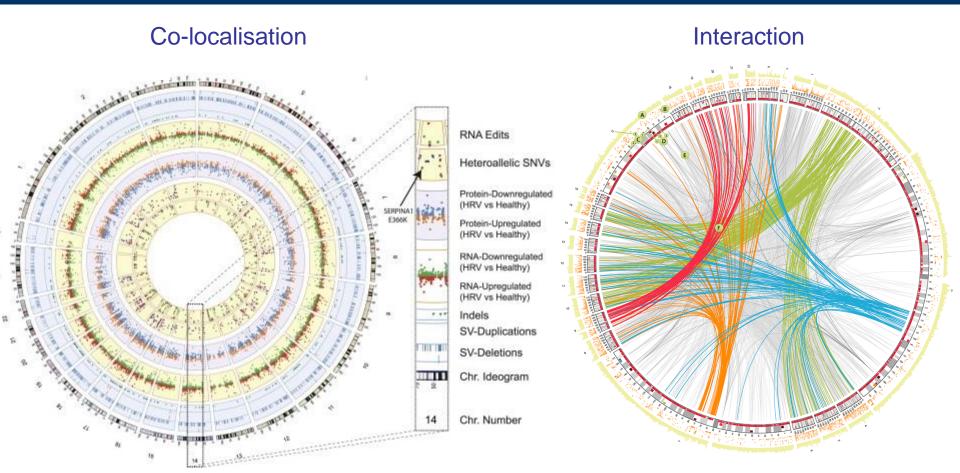
In its 2.5 year history, the PoV column has established a significant legacy— it is one of the most frequently accessed parts of Nature Methods. The reason I think is clear: the community sees the value in clear and effective visual communication and acknowledges the need for a forum in which best practices in the field are presented practically and accessibly.

Bang Wong, in collaboration with visiting authors (Noam Shoresh, Nils Gehlenborg, Cydney Nielsen and Rikke Schmidt Kjærgaard), has penned 29 columns in the period of August 2010 to December 2012, covering broad topics such as salience, Gestalt principles, color, typography, negative space, layout, and data integration.

When it was A.C. Greyling's turn to speak at a debate in which Christopher Hitchens and Richard Dawkins already made their points, Greyling said 103/2020 DUBii – module 3 – R et stats_session 3 - Statomics - Vandiedonck C.

Cirocs to represent genomic traits:

http://circos.ca/intro/genomic_data/



Personal Omics Profiling Reveals Dynamic Molecular and Medical Phenotypes

Rui Chen, ^{1,11} George I. Mias, ^{1,11} Jennifer Li-Pook-Than, ^{1,11} Lihua Jiang, ^{1,11} Hugo Y.K. Lam, ^{1,12} Rong Chen, ^{2,12} Elana Miriami, ¹ Konrad J. Karczewski, ¹ Manoj Hariharan, ¹ Frederick E. Dewey, ³ Yong Cheng, ¹ Michael J. Clark, ¹ Hogune Im, ¹ Lukas Habegger, ^{6,7} Suganthi Balasubramanian, ^{6,7} Maeve O'Huallachain, ¹ Joel T. Dudley, ² Sara Hillenmeyer, ¹ Rajini Haraksingh, ¹ Donald Sharon, ¹ Ghia Euskirchen, ¹ Phil Lacroute, ¹ Keith Bettinger, ¹ Alan P. Boyle, ¹ Maya Kasowski, ¹ Fabian Grubert, ¹ Scott Seki, ² Marco Garcia, ² Michelle Whirl-Carrillo, ¹ Mercedes Gallardo, ^{9,10} Maria A. Blasco, ⁹ Peter L. Greenberg, ⁴ Phyllis Snyder, ¹ Teri E. Klein, ¹ Russ B. Altman, ^{1,5} Atul J. Butte, ² Euan A. Ashley, ³ Mark Gerstein, ^{9,78} Kari C. Nadeau, ² Hua Tang, ¹ and Michael Snyder^{1,*} 10/03/2020

Towards an incerasing complexity of omics!

