

**HO CHI MINH CITY UNIVERSITY OF TECHNOLOGY  
OFFICE FOR INTERNATIONAL STUDY PROGRAM**

**SEMESTER: 251**



**LAB 1 REPORT**

**INSTRUCTOR:**

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**Class ID: CC04**

## 6.1 Exercise 1

Given the following circuit. Calculate the value of the voltage  $v_0$  and the current  $i$ . Then, simulate the circuit to check it out.

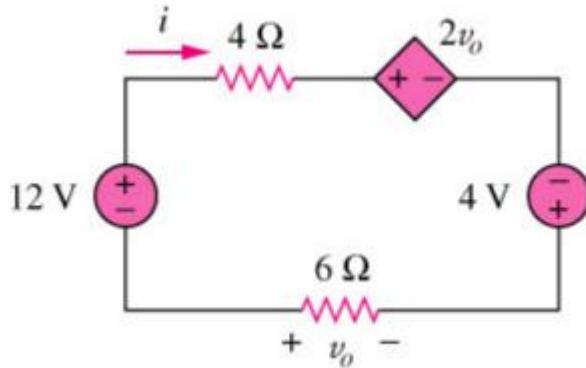


Figure 1.17: Find the voltage and the current in the given circuit using KVL

### 6.1.1 Calculation

Notes: Explanations, formulas, and equations are expected rather than only results.

According to KVL, we have we have the first equation:

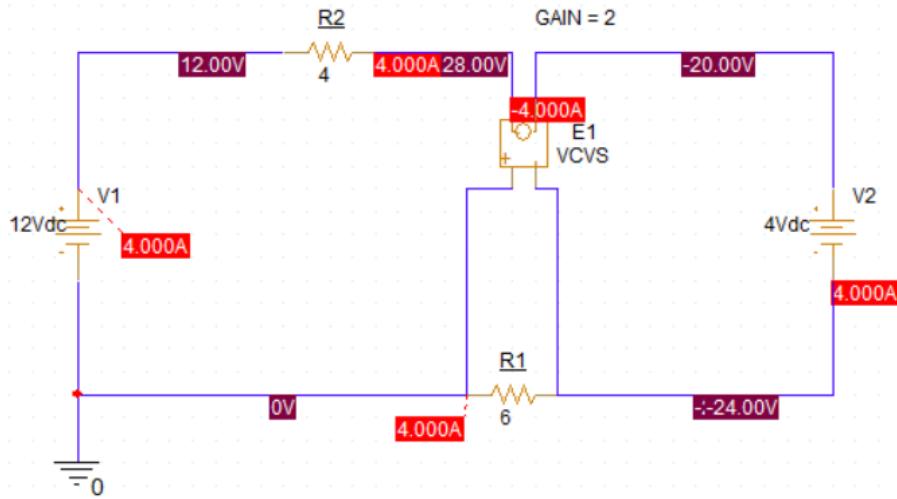
$$-12 - 4I - 2V_0 + V_0 + 4 = 0. \text{ Simplify: } 4I + V_0 = 16 \quad (1)$$

According to the Ohm's Law for the 6 Ω resistor we have:  $v_0 = -6I(V)$

From (1) and (2) we have:

$$4I - 6I = 16 \Leftrightarrow -2I = 16 \Leftrightarrow I = -8 \text{ then } V_0 = -6I = 6.8 = 48(V)$$

## 6.1.2 Stimulation



Result of exercise 1

## 6.2 Exercise 2

Given the following circuit, students rearrange the circuit to clarify its serial and/or parallel topology. Then, apply the knowledge you've learned to find the equivalent resistance value between two circuit terminals A and F. Finally, perform the simulation to check if the current through the whole circuit is correctly calculated.

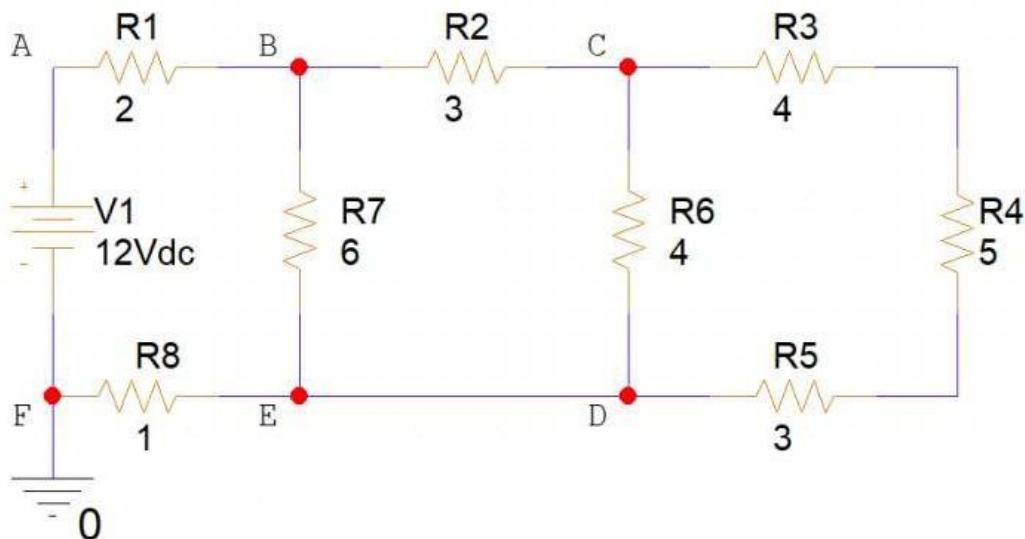
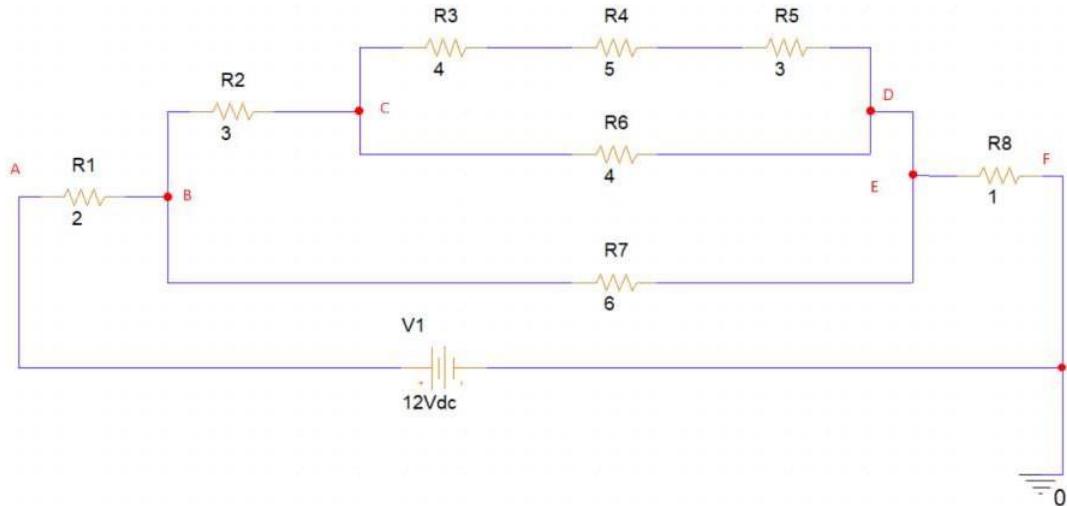


Figure 1.19: Find the equivalent resistance value between terminals A and F

## 6.2.1 Rearrange the circuit

Insert the rearranged circuit here. Don't forget the resistance values and the nodes' names



The rearranged circuit

## 6.2.2 Calculation

Because  $R_3, R_4, R_5$  are in series and they are parallel to  $R_6$ , we have:

$$R_{345} = R_3 + R_4 + R_5 = 4 + 5 + 3 = 12(\Omega)$$

$$R_{CD\_3456} = \frac{R_{345} \cdot R_6}{R_{345} + R_6} = \frac{12 \cdot 4}{12 + 4} = 3(\Omega)$$

Because  $R_2$  series with  $R_{CD\_3456}$  and they are parallel to  $R_7$

$$R_{13456} = R_2 + R_{CD} = 3 + 3 = 6(\Omega)$$

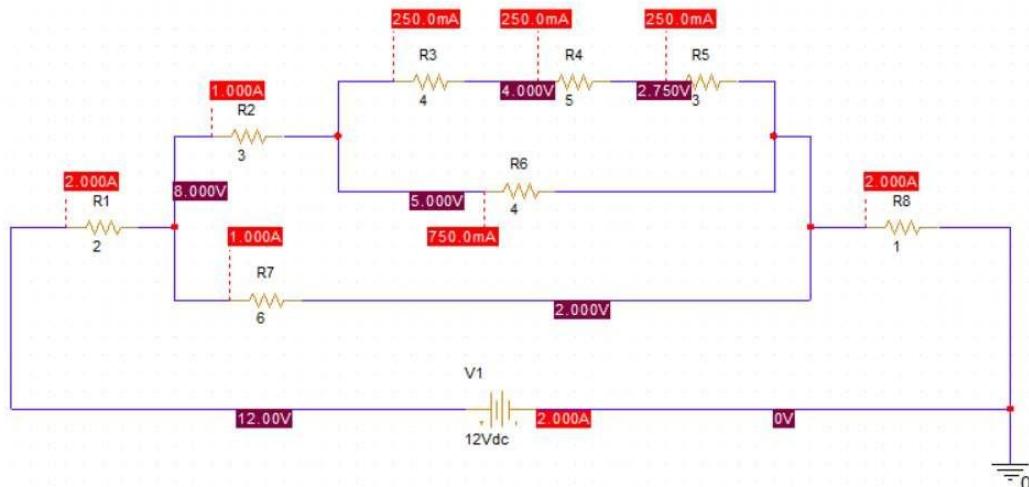
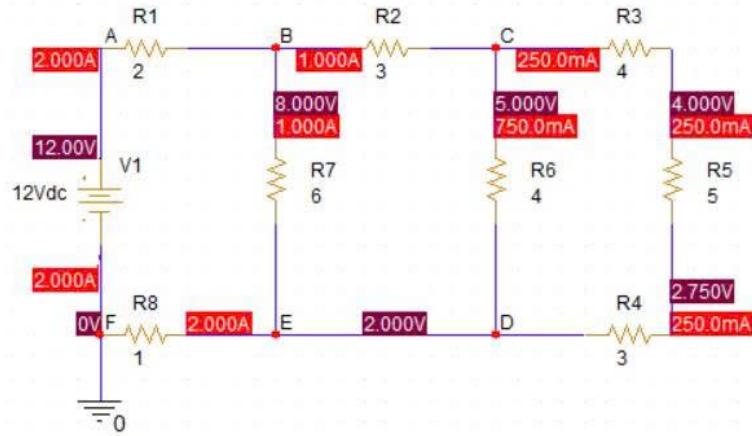
$$R_{BE} = \frac{R_{23456 \cdot R_7}}{R_{23456} + R_7} = 3(\Omega)$$

As  $R_{BE}, R_1, R_6$  are in series

$$R_{AF} = R_{BE} + R_1 + R_3 = 3 + 2 + 1 = 6(\Omega)$$

$$I_{AB} = \frac{V}{R_{AF}} = \frac{12}{6} = 2(A)$$

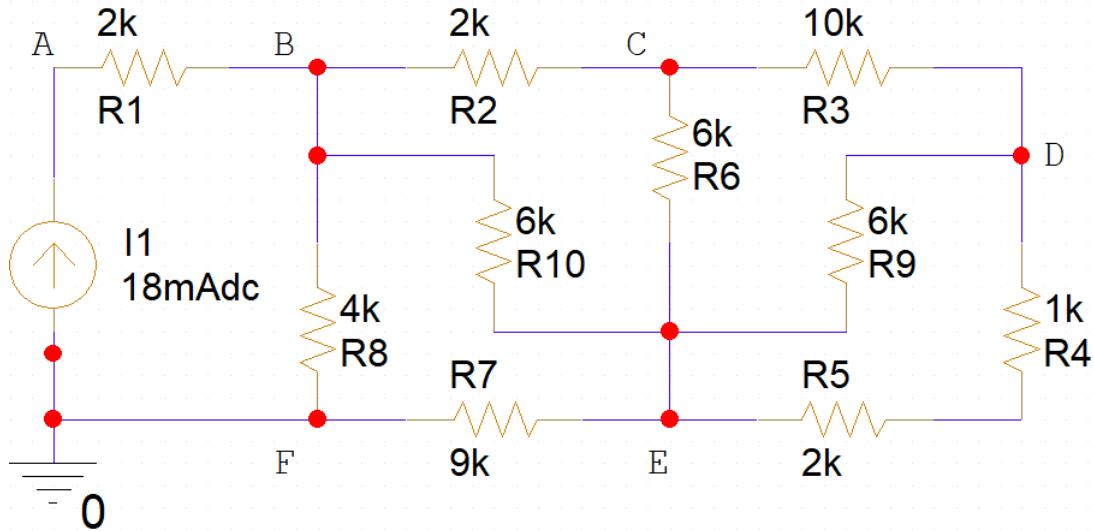
### 6.2.3 Stimulation



Results of both the rearranged circuit and the original circuit are the same

### 6.3 Exercise 3

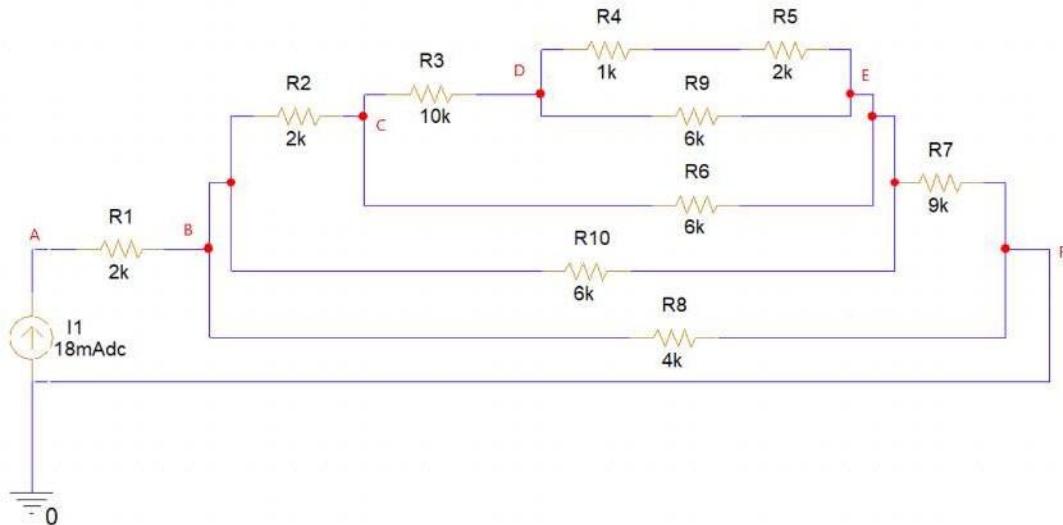
Given the following circuit, students rearrange the circuit to clarify its serial and/or parallel topology. Next, apply the knowledge you've learned to find the equivalent resistance value between two circuit terminals A and F, the voltage values at A, B, C, D, and E. Finally, perform the simulation to check your calculation.



*Figure 1.20:* Find the whole-circuit equivalent resistance  
and the voltages at A, B, C, D and E

### 6.3.1 Rearrange the circuit

Insert the rearranged circuit here. Don't forget the resistance values and the nodes' names



The rearranged circuit

### 6.3.2 Calculation

After rearranging the circuit, we can obtain:

$$R_{DE} = \frac{(R_4 + R_5) \cdot R_9}{(R_4 + R_5) + R_9} = \frac{(1+2) \cdot 6}{(1+2) + 6} = 2(k\Omega)$$

$$R_{3DE6} = \frac{(R_3 + R_{DE}) \cdot R_6}{(R_3 + R_{DE}) + R_6} = \frac{(10+2) \cdot 6}{(10+2) + 6} = 4(k\Omega)$$

$$R_{2C10} = \frac{(R_2 + R_{3D56}) \cdot R_{10}}{(R_2 + R_{3D56}) + R_{10}} = \frac{(2+4) \cdot 6}{(2+4) + 6} = 3(k\Omega)$$

$$R_{B78} = \frac{(R_{2C10} + R_7) \cdot R_8}{(R_{2C10} + R_7) + R_8} = \frac{(3+9) \cdot 4}{(3+9) + 4} = 3(k\Omega)$$

$$\Rightarrow R_{AF} = R_1 + R_{B78} = 2 + 3 = 5(k\Omega)$$

$$V_A = IR_{AF} = 18 \cdot 10^{-3} \cdot 5 \cdot 10^3 = 90(V)$$

$$V_B = IR_{B78} = 18 \cdot 10^{-3} \cdot 3 \cdot 10^3 = 54(V)$$

Apply KVL for 3 inner loops:

$$\begin{cases} 6 \cdot 10^3 I_2 + 9 \cdot 10^3 (18 \cdot 10^{-3} - I_1) = 4 \cdot 10^3 I_1 \\ 2 \cdot 10^3 (18 \cdot 10^{-3} - I_1 - I_2) + 6 \cdot 10^3 I_3 = 6 \cdot 10^3 I_2 \\ 12 \cdot 10^3 (18 \cdot 10^{-3} - I_1 - I_2 - I_3) = 6 \cdot 10^3 I_3 \end{cases}$$

$$\Rightarrow \begin{cases} I_1 = 0,027(A) \\ I_2 = 0,00225(A) \\ I_3 = 0,0015(A) \end{cases}$$

$$V_{BC} = R_2(I - I_1 - I_2) = 4,5(V)$$

$$\Rightarrow V_C = V_B - V_{BC} = 54 - 4,5 = 49,5(V)$$

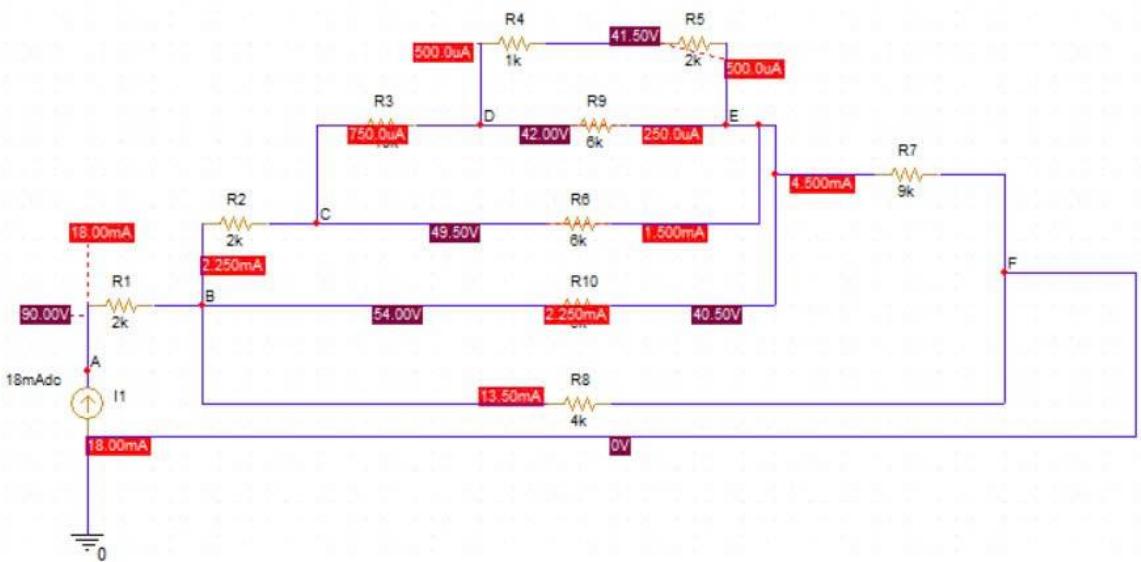
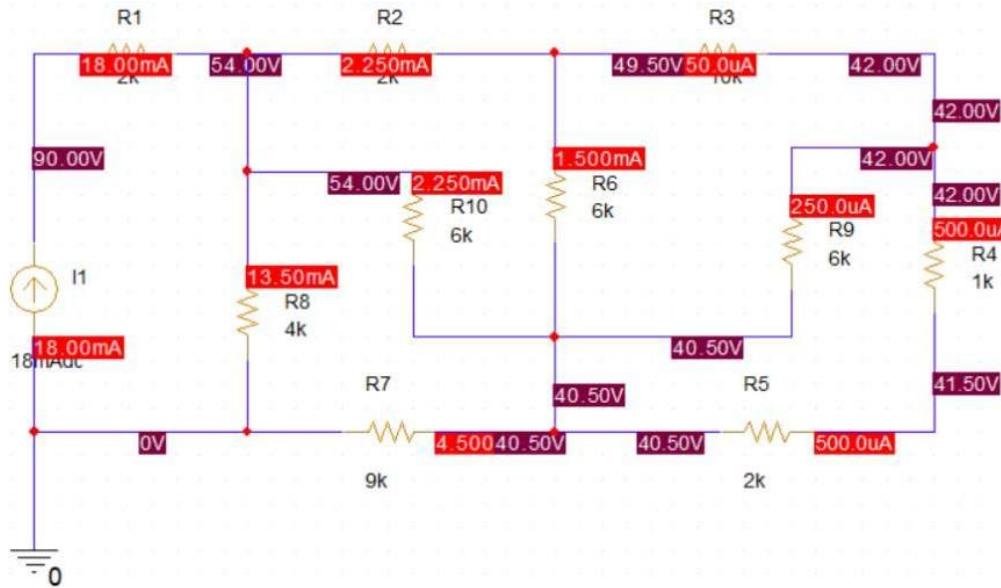
$$V_{CD} = R_3(I - I_1 - I_2 - I_3) = 7,5(V)$$

$$\Rightarrow V_D = V_C - V_{CD} = 49,5 - 7,5 = 42(V)$$

$$V_{CD} = R_{10} \cdot I_2 = 13,5(V)$$

$$\Rightarrow V_E = V_B - V_{BE} = 54 - 13,5 = 40,5(V)$$

### 6.3.3 Stimulation



Results of both the rearranged circuit and the original circuit are the same.

## 6.4 Exercise 4

Given the following circuit, find  $I_1$ ,  $I_2$ ,  $I_3$ ,  $V_a$ , and  $V_b$ . Present your calculation steps and check them out by performing the simulation.

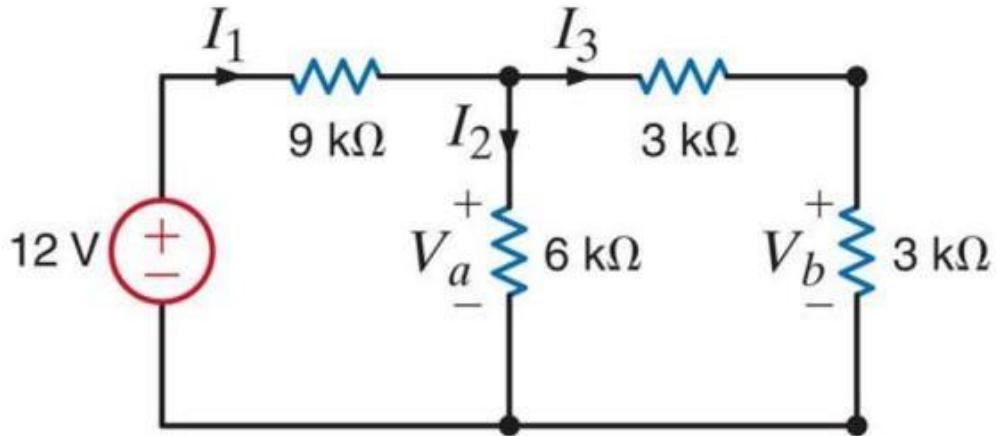


Figure 1.21: Find  $I_1$ ,  $I_2$ ,  $I_3$ ,  $V_a$ , and  $V_b$

### 6.4.1 Calculation

Notes: Explanations, formulas, and equations are expected rather than only results.

We first combine the two  $3\text{k}\Omega$  resistors in series, then that series branch is parallel with the  $6\text{k}\Omega$  branch, then add the series  $9\text{k}\Omega$ .

$$\text{So the circuit equivalent resistance: } R_{eq} = \frac{(3+3)\cdot 6}{(3+3)+6} + 9 = 12(\text{k}\Omega)$$

According to the Ohm's Law and KCL at the top node, we have the second equation:  $I_1 = \frac{V_s}{R_{eq}} = \frac{12}{12 \cdot 10^3} = 12\text{mA}$

Node voltage at the top node  $V_A = I_1 \cdot R_{parallel} = 1\text{mA} \cdot 3\text{k}\Omega = 3\text{V}$  with  $R_{parallel} = \frac{6 \cdot 6}{6+6} = 3\text{k}\Omega$ .

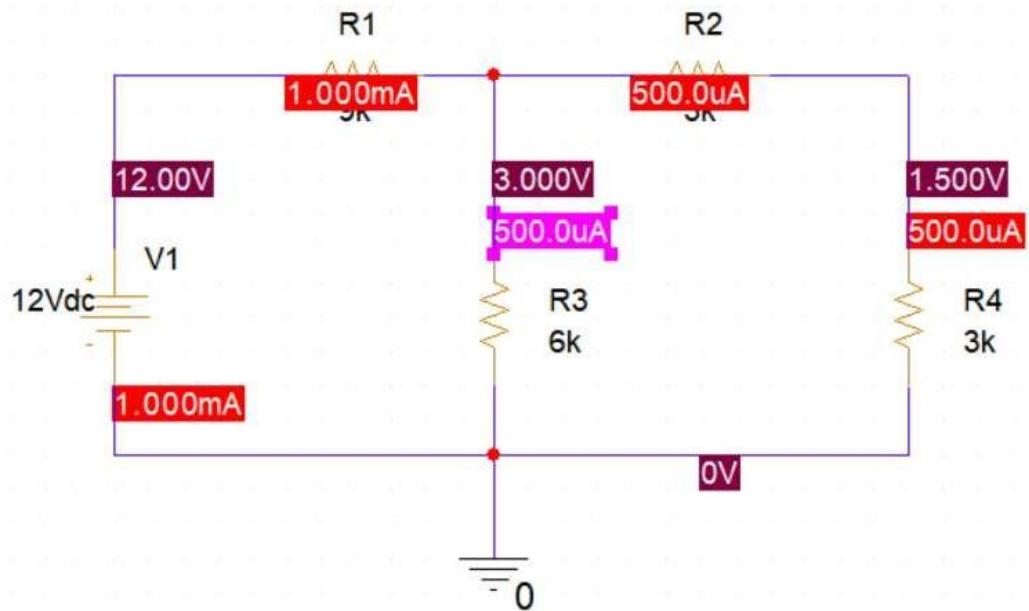
Each branch from that node has the same total resistance ( $\text{k}\Omega$ ), so the current split equally:

$$I_2 = \frac{V_a}{6\text{k}\Omega} = \frac{3\text{V}}{6\text{k}\Omega} = 0,5\text{mA}$$

$$I_3 = \frac{V_a}{3\text{k}\Omega} = 0,5\text{mA}$$

Therefore we have:  $R_{eq} = 12\text{k} = 12\text{k}\Omega$ ,  $I_1 = 1\text{mA}$ ,  $I_2 = 0,5\text{mA}$ ,  $I_3 = 0,5\text{mA}$ ,  $V_a = 3\text{V}$ ,  $V_b = I_3 \cdot 3\text{k}\Omega = 1,5\text{V}$

## 6.4.2 Simulation



The result using simulation tool.

## 6.5 Exercise 5

Given the network as shown below:

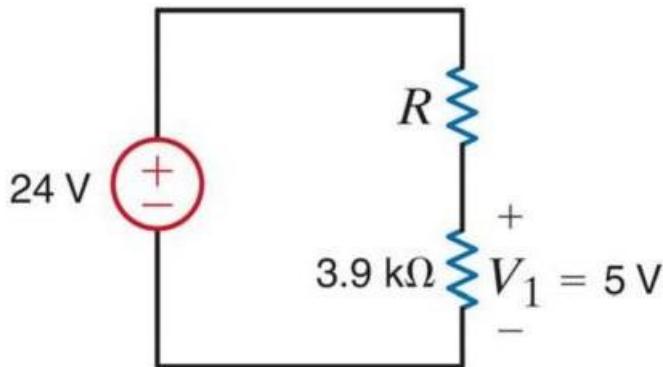


Figure 1.22: Select resistor R from the standard resistors list and do the following requirement.

Notes: Explanations, formulas, and equations are expected rather than only results.

- Find the required value for the resistor R.

$$I_1 = \frac{V_1}{R_1} = \frac{5}{3900} = \frac{1}{780} (A)$$

$$\Rightarrow R_1 = \frac{V}{I_1} = \frac{24-5}{\frac{1}{780}} = 14820 (\Omega)$$

- We have :

$$R_a = 14820.90\% = 13338 (\Omega)$$

$$R_b = 14820.110\% = 16302 (\Omega)$$

$$c. I_a = \frac{V}{R_a + R_{V_1}} = \frac{24}{13338 + 3900} = 1,39 (mA)$$

$$V_a = I_a \cdot R_{V_1} = 1,39 \cdot 10^{-3} \cdot 3900 = 5,429 (V)$$

$$I_b = \frac{V}{R_b + R_{V_1}} = \frac{24}{16302 + 3900} = 1,188 (mA)$$

$$V_b = I_b \cdot R_{V_1} = 1,188 \cdot 10^{-3} \cdot 3900 = 4,633 (V)$$

- The percent error in the voltage:

$$E_a = \left| \frac{5,459 - 5}{5} \right| \cdot 100\% = 8,58\%$$

$$E_b = \left| \frac{4,633 - 5}{5} \right| \cdot 100\% = 7,34\%$$

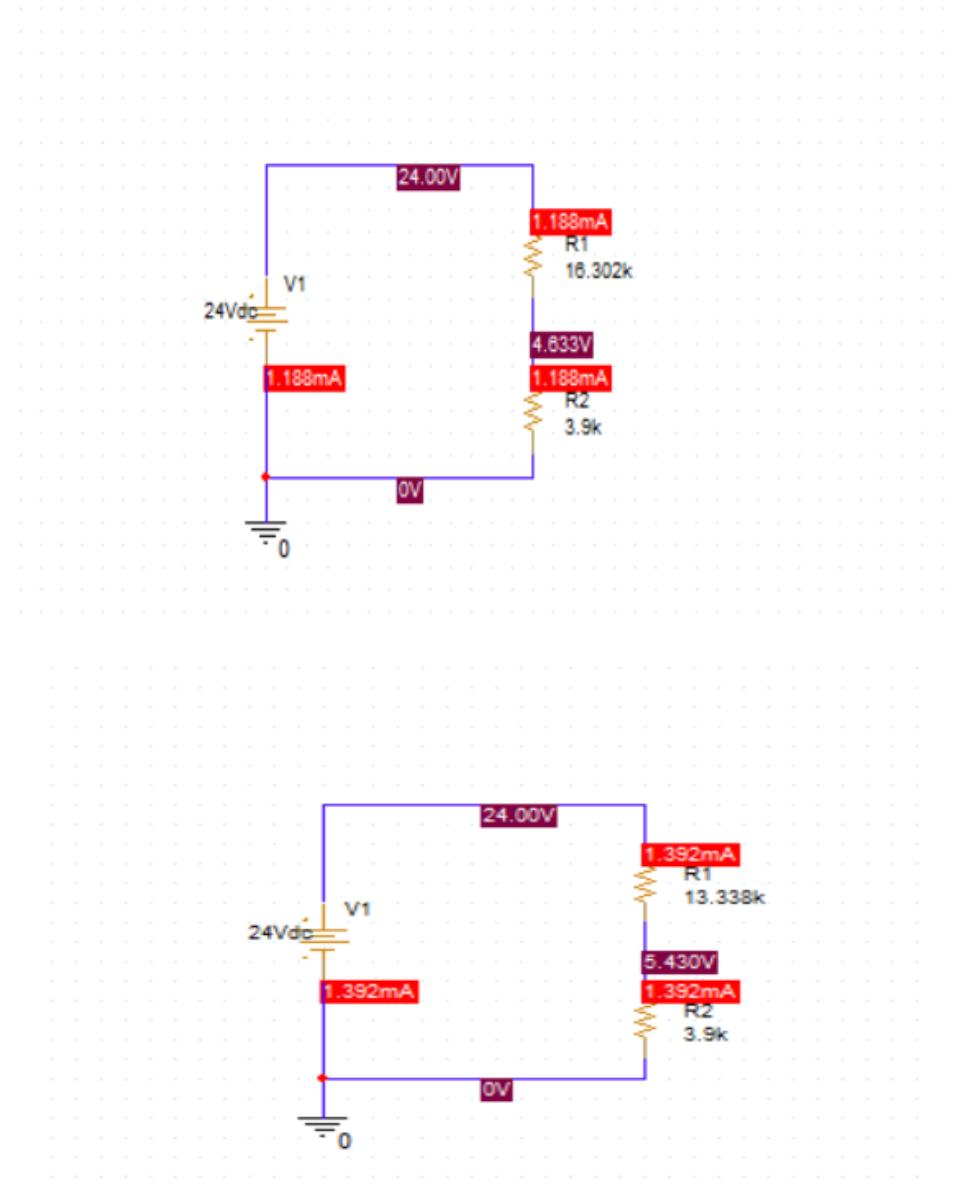
e. The power ratings:

$$P_a = I^2 a \cdot R = (1,39 \cdot 10^{-3})^2 (13338 + 3900) = 0,03(W)$$

$$P_b = I^2 b \cdot R = (1,188 \cdot 10^{-3})^2 (16302 + 3900) = 0,028(W)$$

## 6.5.1 Simulation

### Simulation result (image)



Results on simulation are the same with the calculation above.

## 6.6 Exercise 6

Given the following circuit. Apply the knowledge you've learned to transform it into another form in which you can find total equivalent resistance  $R_{ab}$  more easily. Next, find the value of the current  $i$  through the circuit and perform a simulation to check it out.

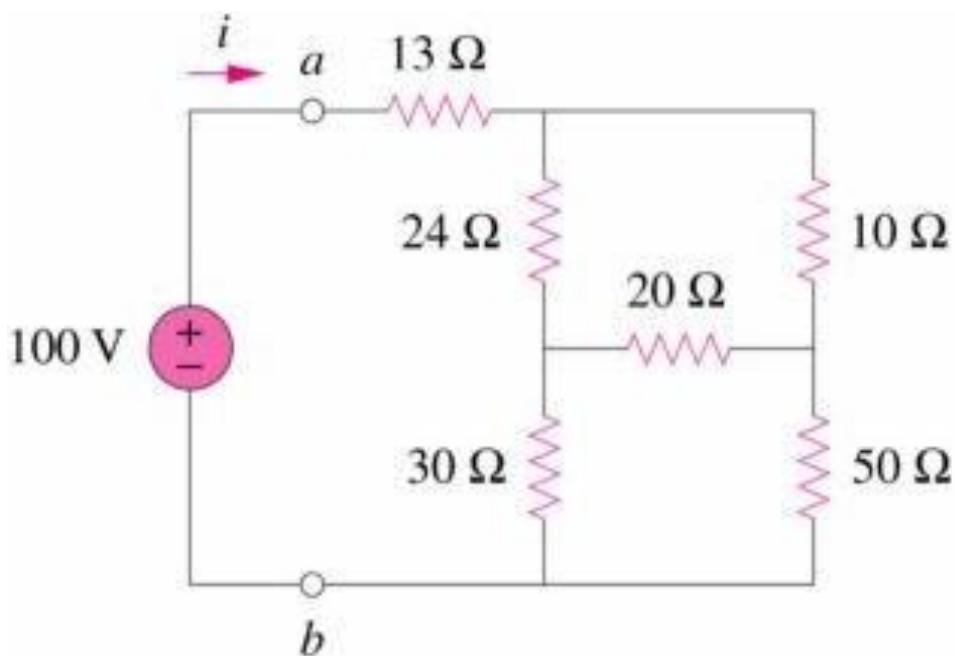
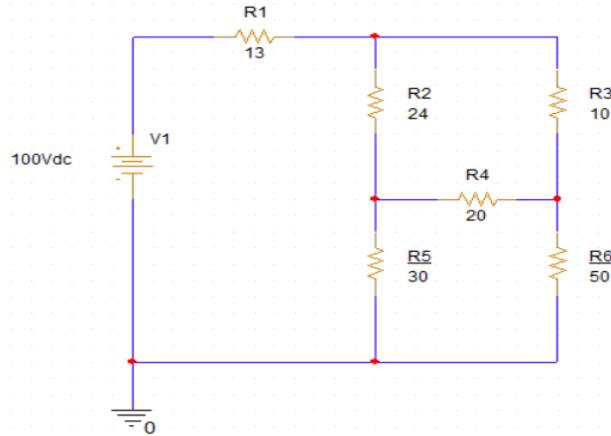


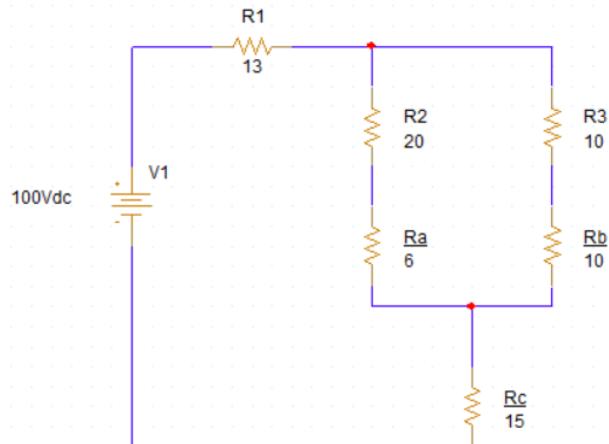
Figure 1.23: Transform the circuit, then find the equivalent resistance  $R_{ab}$  and the current  $i$  through the circuit.

## 6.6.1 Circuit transformation

Original Circuit:



Transformed circuit:



Since we have  $R_4, R_5, R_6$  are in delta shape we can turn it into wye shape:

$$R_a = \frac{R_4 \cdot R_5}{R_4 + R_5 + R_6} = \frac{20 \cdot 30}{20 + 30 + 50} = 6(\Omega)$$

$$R_b = \frac{R_4 \cdot R_6}{R_4 + R_5 + R_6} = \frac{20 \cdot 50}{20 + 30 + 50} = 10(\Omega)$$

$$R_c = \frac{R_5 \cdot R_6}{R_4 + R_5 + R_6} = \frac{30 \cdot 50}{20 + 30 + 50} = 15(\Omega)$$

## 6.6.2 Calculation

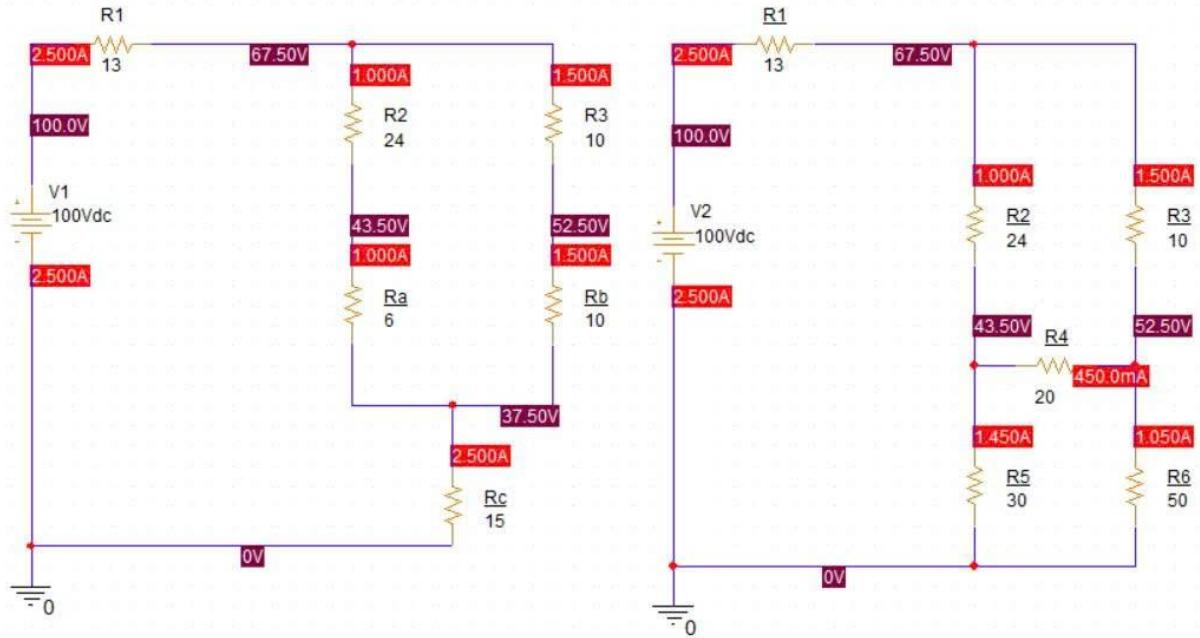
Notes: Explanations, formulas, and equations are expected rather than only results

$$R_{ab} = R_1 + \frac{R_{2a} \cdot R_{3b}}{R_{2a} + R_{3b}} + R_c = 13 + \frac{30 \cdot 20}{30 + 20} + 15 = 40(\Omega)$$

$$I = \frac{U}{R_{ab}} = \frac{100}{40} = 2,5(A)$$

### 6.6.3 Simulation

Simulation result (image):



### 6.7 Exercise 7

Given the following circuit. Apply the knowledge you've learned to transform it into another form in which you can find total equivalent resistance more easily. Next, find the value of the current  $I_S$  through the circuit and perform a simulation to check it out.

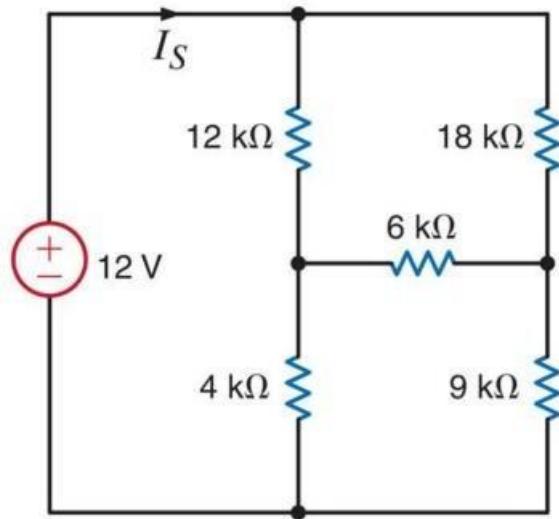
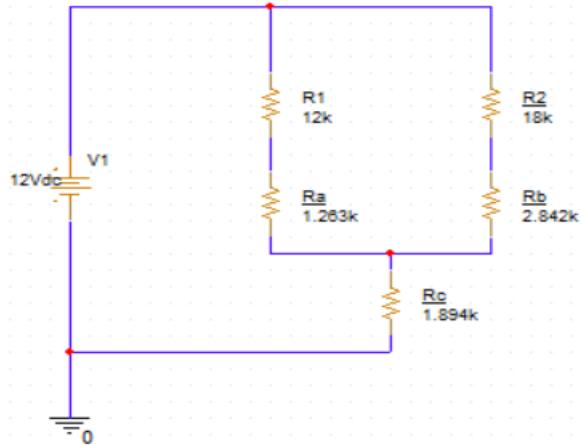


Figure 1.24: Transform the circuit, then find the equivalent resistance and the current  $I_S$  through the circuit.

### 6.7.1 Circuit transformation



*The transformed circuit*

Since we have  $R_3, R_4, R_5$  are in delta shape, we can turn it into wye shape:

$$R_a = \frac{R_3 \cdot R_4}{R_3 + R_4 + R_5} = \frac{6000 \cdot 4000}{6000 + 4000 + 9000} = 1263(\Omega)$$

$$R_b = \frac{R_3 \cdot R_5}{R_3 + R_4 + R_5} = \frac{6000 \cdot 9000}{6000 + 4000 + 9000} = 2842(\Omega)$$

$$R_c = \frac{R_4 \cdot R_5}{R_3 + R_4 + R_5} = \frac{4000 \cdot 9000}{6000 + 4000 + 9000} = 1894(\Omega)$$

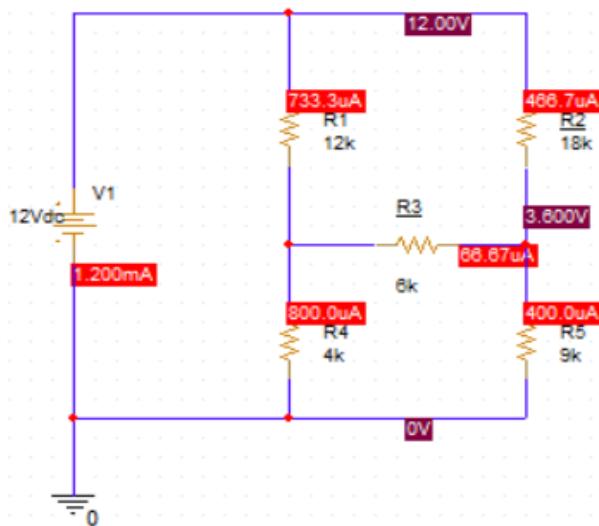
## 6.7.2 Calculations

$$R_{eq} = \frac{(R_1 + R_a)(R_2 + R_b)}{(R_1 + R_a) + (R_2 + R_b)} + R_C = 10(k\Omega)$$

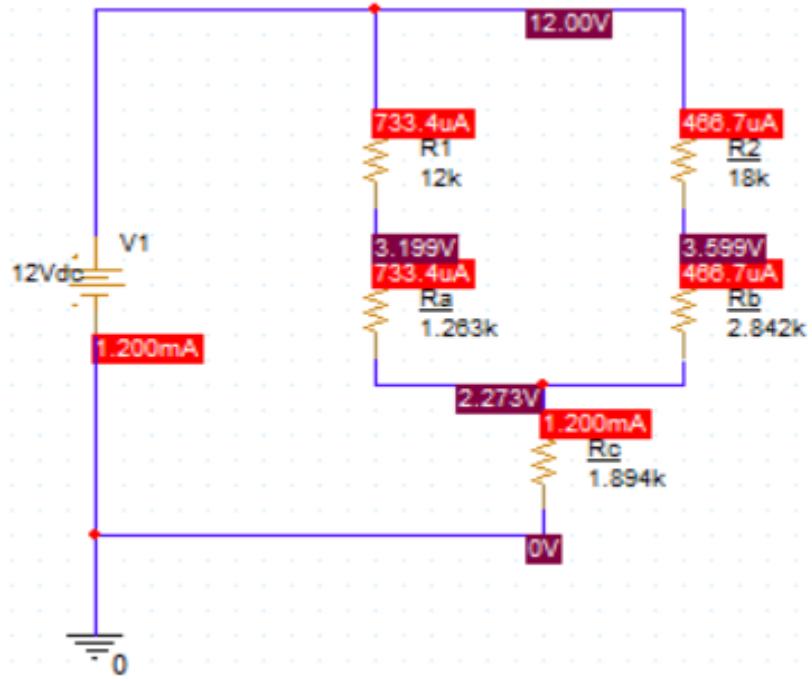
$$I = \frac{V}{R_{eq}} = \frac{12}{10000} = 1,2(mA)$$

## 6.7.3 Simulation

Simulation result (image):



The original circuit



The transformation circuit

## 6.8 Exercise 8

Given the following circuit with  $p_2$ ,  $p_3$ , and  $p_4$  are absorbing powers of unknown electrical elements. First, use the knowledge you've learned to identify whether they are active or passive elements (supplying or absorbing power). To an element absorbing power, use a pure resistor with a proper value as a representative. To a power element, use an ideal DC voltage source with the corresponding value as a representative. Next, redraw the circuit and calculate the power that each element absorbs. Note that here we use the passive sign convention. Then, perform a simulation with the elements determined by the previous step.

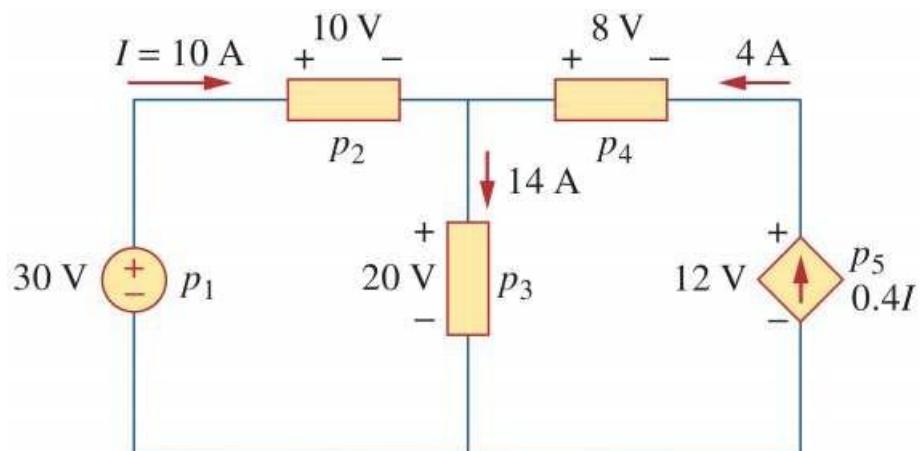


Figure 1.25: Determine the unknown elements and calculate the absorbing power of each

## 6.8.1 Identifying the unknown elements

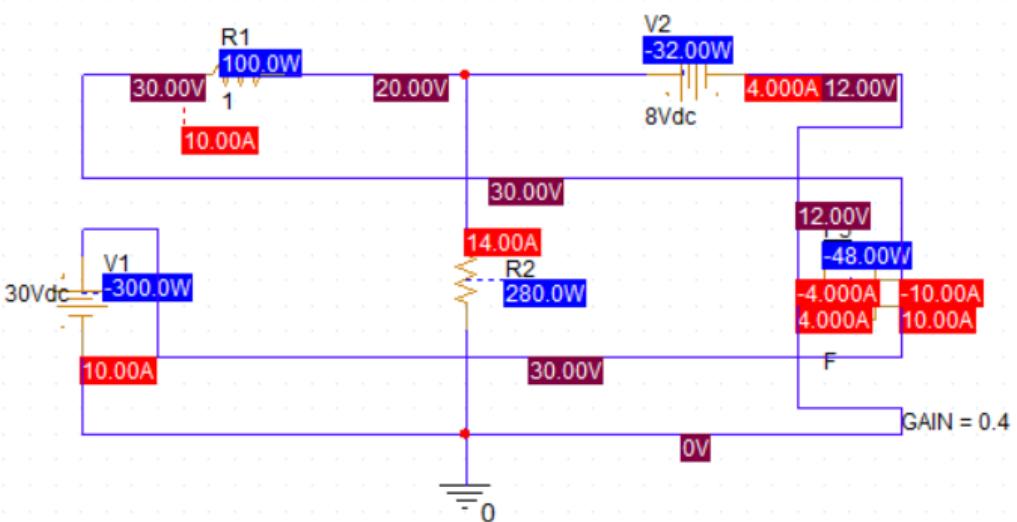
From the figure 1.2.5, we can see that the current 10A go into the positive pole at  $P_2$  so we have  $P_2 = U \cdot I = 10.10 = 100(W)$  (positive) so  $P_2$  is absorbing. The same with  $P_3$  so  $P_3 = U \cdot I = 14.20 = 280(W)$ . But we have the current 4A enter the negative pole of  $P_4$  so  $P_4 = 4.8 = 32(W)$  so  $P_4$  is a supply element.

## 6.8.2 Redraw the circuit for simulation

$$R_2 = \frac{U_2}{I} = \frac{10}{10} = 1(\Omega), R_3 = \frac{U_3}{I_3} = \frac{20}{14} = \frac{10}{7}(\Omega)$$

We replace the  $P_2, P_3$  with pure resistors with resistance  $1\Omega$  and  $\frac{10}{7}\Omega$  respectively

We replace the  $P_4$  with DC have 8V.



The simulation's result

## 6.9 Exercise 9

Given the following circuit. Find the voltage  $v$  and the current  $i_x$ . According to the result, determine the elements whose absorbing power respectively  $p_1$  and  $p_2$  are active or passive (calculations are required). Note that here we use the passive sign convention. If an element consumes power, use a pure resistor with an appropriate value as a representative. If it is a power supply element, use a corresponding ideal DC voltage source to represent it. Perform a simulation to check how the circuit works.

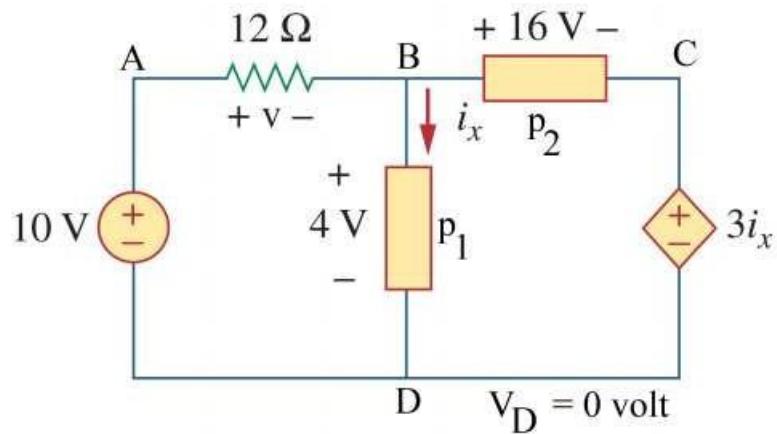


Figure 1.26: Find the unknown elements and variables, then check them out by simulation

## 6.9.1 Calculation

Notes: Explanations, formulas, and equations are expected rather than only results.

We have:

$V$ = voltage across the  $12 \Omega$  resistor (marked + at A, -at B)

$$\text{Formula } V = V_A - V_B$$

$$\text{So } V = V_A - V_B = 10 - 4 = 6(V)$$

$I_x$ = current defined in the problem as the current through the vertical 4-V element, positive downward ( $B \rightarrow D$ )

Relation from dependent source: the right-hand dependent voltage source gives  $V_C - V_D = 3I_x$

Also  $V_D = 0$  (and from the 16-V source  $V_B - V_C = 16$  so  $V_C = V_B - 16$ . With  $V_B = 4V$  we get

$$V_C = 4 - 16 = -12(V)$$

$$\text{So } I_x = \frac{V_C - V_D}{3} = \frac{-12 - 0}{3} = -4(A)$$

We have:  $P_1$  = power for the 4V element using passive sign convention  $P_1 = V_{BP} \cdot I$  where  $V_{BP} = +4V$  and I is the current entering the + terminal

$$\text{So } P_1 = 4 \cdot I_x = 4 \cdot (-4) = -16(W)$$

Interpretation  $P_1 < 0$  so the element is supplying 16W.

$I_{AB}$ =current through the  $12 \Omega$  resistor from  $A \rightarrow B$  (positive from A to B). Use Ohm's law

$$I_{AB} = \frac{V_A - V_B}{12} = \frac{6}{12} = 0,5(A)$$

$I_{BC}$  = current through the 16W source (top branch) from  $B \rightarrow C$ . Use KCL at node B. Current is leaving node B through resistor  $B \rightarrow A$  in  $\frac{V_B - V_A}{12}$ , through the top source  $I_{16}(B \rightarrow C)$ , and through the downward 4-V element ( $B \rightarrow D$ ) which is  $I_x$ . KCL given:

$$\frac{V_B - V_A}{12} + I_{16} + I_x = 0$$

$$\text{So } I_{16} = -\frac{V_B - V_A}{12} - I_x = -\frac{4 - 10}{12} - (-4) = 4,5(A)$$

$$\text{So } I_{BC} = I_{16} = 4,5(A) \text{ (B} \rightarrow \text{C)}$$

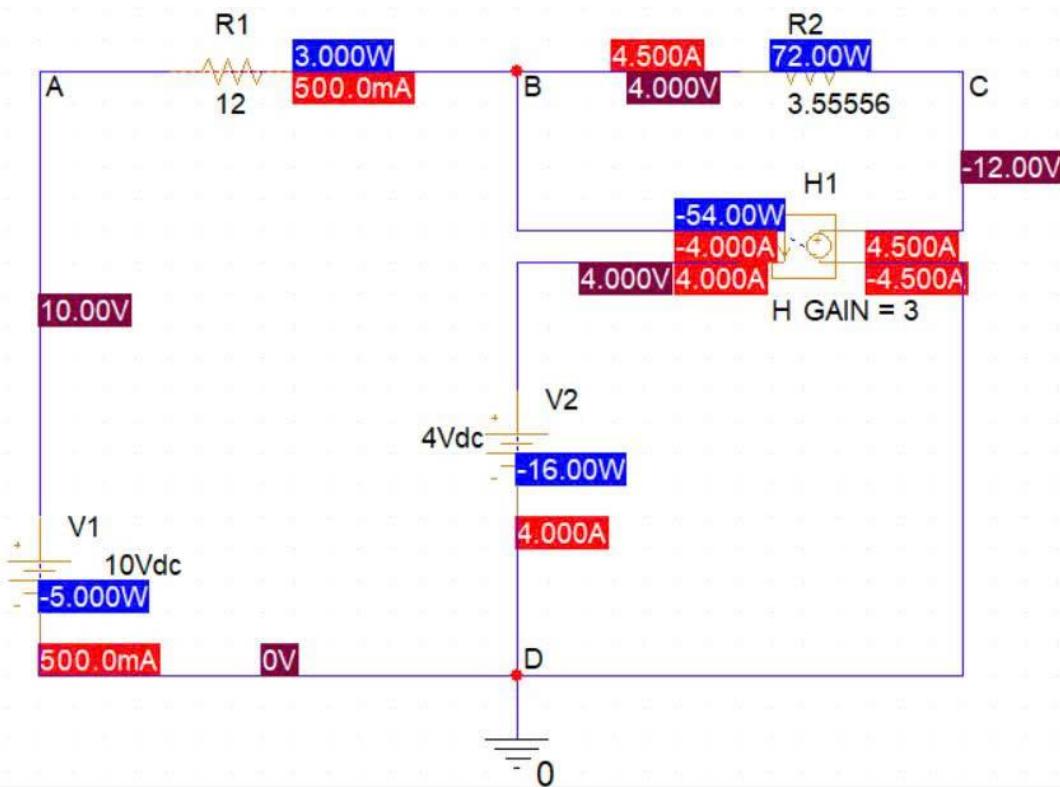
$P_2$ = power for the 16V element (+at A, - at C) using passive sign convention

$$P_2 = V_{BC} \cdot I_{16} = 16 \cdot 4,5 = 72(W)$$

$P_2 > 0$ , the 16 V source is absorbing 72W

$V_{CD}$  =voltage from C to D. We got  $V_C = -12V$ ,  $V_D = 0$ . So  $V_{CD} = V_C - V_D = -12(V)$

## 6.9.2 Simulation



The result in the simulation match with what we found

## 6.10 Exercise 10

Given the following circuit. Find the voltage V. You can do this in any way but remember to explain it in detail. Then simulate the circuit to check the result.

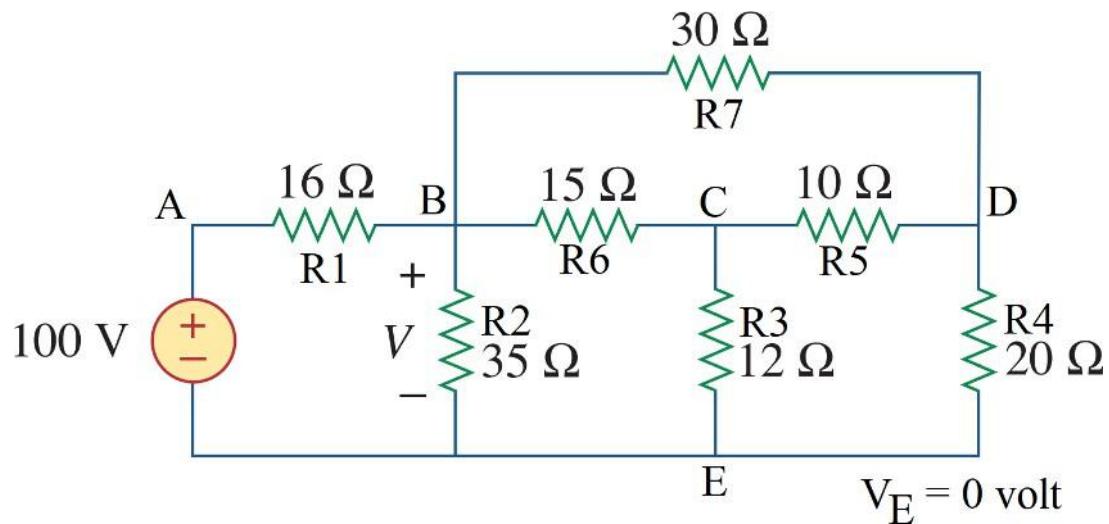
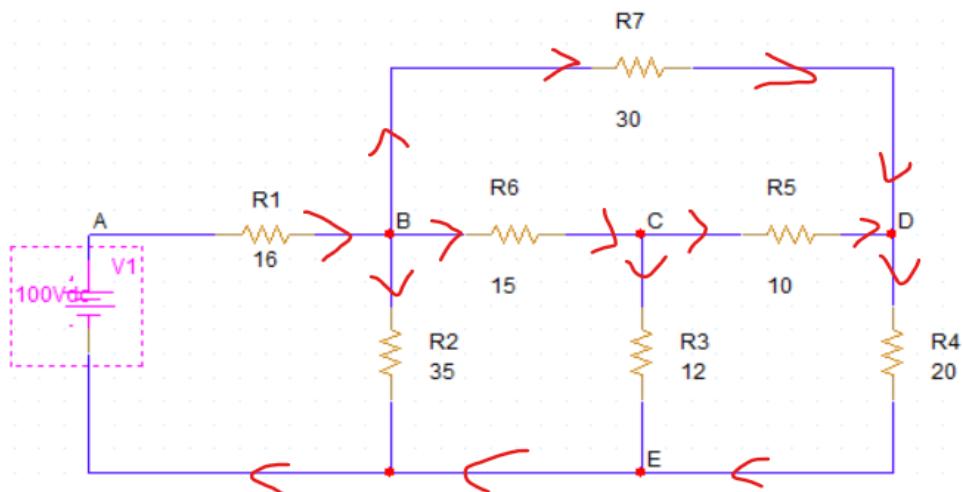


Figure 1.28: Find the voltage V

**Answer:**



Apply KVL for each loop, we have:

$$(1) 16I_1 + 35(I_1 - I_4) - 100 = 0$$

$$\Rightarrow 51I_1 - 35I_4 = 100$$

$$(2) 15I_2 + 10(I_2 - I_3) + 30(I_2 - I_4) = 0$$

$$\Rightarrow 55I_2 - 10I_3 - 30I_4 = 0$$

$$(3) 12I_3 + 10(I_3 - I_2) + 20(I_3 - I_4) = 0$$

$$\Rightarrow -10I_2 + 42I_3 - 20I_4 = 0$$

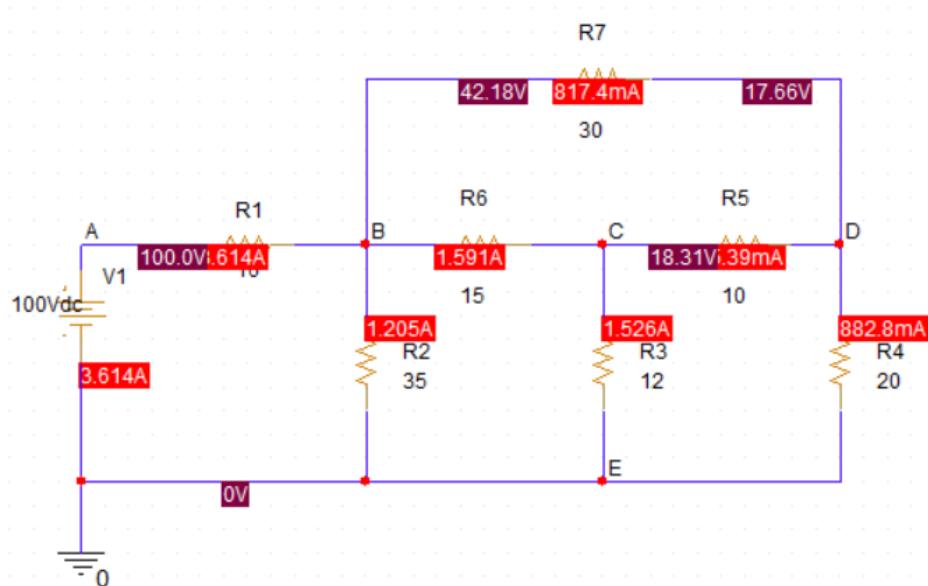
$$(4) 30(I_4 + I_2) + 10(I_4 - I_3) + 35(I_4 - I_1) = 0$$

$$\Rightarrow -35I_1 - 30I_2 - 20I_3 + 85I_4 = 0$$

From (1), (2), (3), (4)  $\Rightarrow I_1 = 3,61 A, I_2 = 1,59 A, I_3 = 1,52 A, I_4 = 2,4 A$

$$\Rightarrow V = R_2 \cdot I_{R_2} = 35 \cdot (3,613 - 2,408) = 42,175(V)$$

## Checking the results using simulation:



## List of References:

- [Ein05] Albert Einstein. “Zur Elektrodynamik bewegter Körper. (German) [On the electrodynamics of moving bodies]”. In: *Annalen der Physik* 322.10 (1905), pp. 891–921. DOI: <http://dx.doi.org/10.1002/andp.19053221004>.
- [Knu68] Donald E. Knuth. *The Art of Computer Programming*. Four volumes. Seven volumes planned. Addison-Wesley, 1968.
- [Knu73] Donald E. Knuth. “Fundamental Algorithms”. In: Addison-Wesley, 1973. Chap. 1.2.
- [Dir81] Paul Adrien Maurice Dirac. *The Principles of Quantum Mechanics*. International series of monographs on physics. Clarendon Press, 1981. ISBN: 9780198520115.
- [GMS93] Michel Goossens, Frank Mittelbach, and Alexander Samarin. *The LaTeX Companion*. Reading, Massachusetts: Addison-Wesley, 1993.
- [Gre93] George D. Greenwade. “The Comprehensive Tex Archive Network (CTAN)”. In: *TUGBoat* 14.3 (1993), pp. 342–351.
- [Hal] Gareth Halfacree. *The Official BBC micro:bit User Guide*. URL: <https://microbit.org/>. (accessed: 25.05.2018).
- [Knu] Donald Knuth. *Knuth: Computers and Typesetting*. URL: <http://www-cs-faculty.stanford.edu/~uno/abcde.html>. (accessed: 01.09.2016).