# Tree Predictors for Binary Classification

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## Abstract

This project implements a decision tree predictor for classifying mushrooms as poisonous or edible. The model is developed entirely from scratch in Python and is evaluated on two datasets: a primary dataset with 173 examples and 20 features (17 categorical, 3 metrical), and a secondary dataset with over 61,000 examples.

The decision tree uses single-feature binary tests: it performs threshold comparisons for numerical features and equality tests for categorical features. It supports three impurity measures: Gini index, entropy, and scaled entropy. Hyperparameter tuning was conducted using 5-fold cross-validation on the primary dataset, yielding an average accuracy of approximately 55%, and using an 80/20 train/test split on the secondary dataset, which achieved a test accuracy of about 95%.

Key components include pseudocode for tree prediction and hyperparameter evaluation, as well as a detailed feature importance analysis revealing that features such as stemheight, cap-surface, and stem-surface are particularly influential. These results demonstrate that, while decision trees may face challenges with small, noisy datasets, they perform robustly on large, clean datasets.

Overall, this work provides a comprehensive experimental framework and lays the ground-work for further extensions such as ensemble methods and pruning strategies.

## 1 Introduction

Decision trees are popular for classification due to their simplicity and interpretability. In this project, I implement a decision tree classifier from scratch in Python to determine whether mushrooms are poisonous or edible—a task with significant real-world implications.

The project uses two datasets:

• Primary Dataset: 173 examples with 20 features (17 categorical, 3 metrical). Using 5-fold cross-validation, the model achieves an average accuracy of approximately 55%.

• Secondary Dataset: Over 61,000 examples, where an 80/20 train/test split yields a test accuracy of roughly 95%.

## **Key Contributions**

- Implementation of a decision tree with single-feature binary tests.
- Support for multiple impurity measures: Gini, entropy, and scaled entropy.
- Adaptive hyperparameter tuning using grid search and cross-validation.
- Analysis of feature importance and detailed tree structure visualization.

## **Example Pseudocode for Prediction**

```
function predict(x, node):
    if node.is_leaf:
        return node.prediction
    if x[node.split_feature] <= node.split_value:
        return predict(x, node.left_child)
    else:
        return predict(x, node.right_child)</pre>
```

This report details the datasets, preprocessing steps, model design, hyperparameter tuning, and experimental results that demonstrate the strengths and limitations of decision trees under varying data conditions.

## 2. Dataset Description and Preprocessing

This section provides an overview of the datasets and details the preprocessing steps with concrete examples, numerical details, and pseudocode.

#### 2.1 Datasets

- **Primary Dataset:** Contains 173 examples and 20 features (17 categorical, 3 metrical).
  - Example Record:

```
* cap-diameter = [10, 20] \rightarrow converted to 15.0.
```

\* stem-height = [5, 15]  $\rightarrow$  converted to 10.0.

- Challenge: Small sample size may cause high variance.

- **Secondary Dataset:** Contains approximately 61,000 examples (about 353 per species).
  - Example Record:
    - \* cap-diameter = 15.26 (already numeric).
    - \* stem-height and stem-width are provided as single numerical values.
  - Advantage: Large and well-separated data allow for higher accuracy.

## 2.2 Preprocessing Steps

I performed the following preprocessing steps to ensure data quality and consistency:

- 1. **Drop Non-informative Columns:** Remove descriptive columns such as family and name since they do not aid in prediction.
- 2. Clean Metrical Features: For features like cap-diameter, stem-height, and stem-width:
  - Apply the clean metrical value function.
  - Example: The string "[10, 20]" is converted to (10 + 20)/2 = 15.0.
- 3. Clean Categorical Features: For features stored as list-like strings:
  - Use the clean nominal value function.
  - Example: The string "[x, f]" becomes x.
- 4. **Handle Missing Data:** Replace missing numerical values with None and missing categorical values with "unknown" to maintain consistency.
- 5. Convert Format: Transform the cleaned DataFrame into:
  - X: A list of dictionaries where each dictionary represents one record.
  - y: A list of corresponding class labels.

## 2.3 Preprocessing Pseudocode

```
Input: Raw CSV file with columns [family, name, ..., class]
Output: X (list of dicts), y (list of labels)

1. Read the CSV file with the appropriate delimiter (e.g., sep=";").
2. Remove the columns "family" and "name".
3. For each column (except "class"):
    if column is metrical:
        Apply clean_metrical_value(value)
    else:
```

```
Apply clean_nominal_value(value)

4. Convert the cleaned DataFrame into:
    X = list of records (each record is a dictionary of features)
    y = list of class labels

5. Return X and y
```

By following these preprocessing steps, I ensured that both the primary and secondary datasets are standardized and free from ambiguous values. This guarantees that the data are ready for training and evaluation of the decision tree model.

## 3. Methodology

This section details the approach used to build the decision tree classifier, with concrete examples, numerical thresholds, and pseudocode. The key aspects are the design of the tree predictor, the impurity measures, stopping criteria, and hyperparameter tuning.

## 3.1 Tree Predictor Design

The decision tree is implemented via two classes: Node and DecisionTree. A Node object holds:

- is leaf: A Boolean flag that is True if the node is terminal.
- **prediction**: The class label for leaf nodes.
- **split\_feature** and **split\_value**: The feature and its corresponding threshold (for numeric features) or category (for categorical features) used to split the data.
- left child and right child: References to the child nodes.
- samples\_count: The number of training samples that reach this node.
- **impurity**: The impurity value computed at the node.

The DecisionTree class builds the tree recursively. For example, if a node contains 173 samples and the best split is found on stem-width with a threshold of 7.5, the node is divided into:

- Left child: Samples with stem-width  $\leq 7.5$ .
- Right child: Samples with stem-width > 7.5.

#### Pseudocode for Recursive Tree Construction:

```
function build_tree(X, y, indices, depth):
   node.samples_count = len(indices)
   if (all labels are equal) or (len(indices) < min_samples_in_leaf)
      or (max_depth is set and depth >= max_depth):
        node.is_leaf = True
        node.prediction = majority_class(y[indices])
        return node
   best_feature, best_threshold, gain, left_idx, right_idx = find_best_split(X, y, i
   node.split_feature = best_feature
   node.split_value = best_threshold
   node.left_child = build_tree(X, y, left_idx, depth + 1)
   node.right_child = build_tree(X, y, right_idx, depth + 1)
   return node
```

For prediction, the process traverses the tree until reaching a leaf:

```
function predict(x, node):
    if node.is_leaf:
        return node.prediction
    if x[node.split_feature] <= node.split_value:
        return predict(x, node.left_child)
    else:
        return predict(x, node.right_child)</pre>
```

## 3.2 Impurity Measures

Splits are evaluated by the decrease in impurity. Three measures are implemented:

• Gini Index:

$$G = 1 - \sum p_i^2.$$

Example: For labels [e, e, p, p, p],

$$G = 1 - \left( \left(\frac{2}{5}\right)^2 + \left(\frac{3}{5}\right)^2 \right) \approx 0.48.$$

• Entropy:

$$H = -\sum p_i \log_2 p_i.$$

**Example:** For the same labels,

$$H \approx -(0.4\log_2 0.4 + 0.6\log_2 0.6) \approx 0.971.$$

• Scaled Entropy:

$$H_{\text{scaled}} = \frac{H}{\log_2(K)},$$

where K is the number of classes. For binary classification (K = 2), this equals standard entropy.

## 3.3 Stopping Criteria

To prevent overfitting, the tree stops splitting when:

- Node Purity: All samples at a node have the same label.
- Minimum Samples per Leaf: If the number of samples is less than min\_samples\_in\_leaf (e.g., 5).
- Maximum Depth: If the current depth reaches or exceeds max depth.

Example: A node with 3 samples stops splitting if min\_samples\_in\_leaf is 5.

## 3.4 Hyperparameter Tuning and Evaluation

An adaptive strategy was used for tuning:

• Primary Dataset: 5-fold cross-validation was performed over:

```
\label{eq:continuous_problem} \begin{split} &- \max\_\mathtt{depth} \in \{3, 5, 7, \mathtt{None}\}, \\ &- \min\_\mathtt{samples\_in\_leaf} \in \{1, 5, 10\}. \end{split}
```

The optimal settings were max\_depth = 5 and min\_samples\_in\_leaf = 5, yielding  $\sim 55\%$  accuracy.

• Secondary Dataset: An 80/20 train/test split was used. Although grid search initially suggested an unbounded tree, I fixed max\_depth at 15 to ensure efficient training. This configuration yielded a test accuracy of ~ 95.2%.

#### Pseudocode for Hyperparameter Tuning:

```
for max_depth in {3, 5, 7, None}:
    for min_samples in {1, 5, 10}:
        perform 5-fold CV:
            for each fold:
                train tree with (max_depth, min_samples)
               compute fold accuracy
                average_accuracy = mean(accuracy_scores)
select parameters with highest average_accuracy
if max_depth == None and dataset is large:
    set max depth = 15
```

## 3.5 Implementation Summary

In summary, my decision tree predictor:

- Uses single-feature binary tests (threshold for numeric features and equality for categorical ones).
- Supports three impurity measures: Gini, entropy, and scaled entropy.
- Stops growing based on node purity, minimum samples per leaf, and maximum depth.
- Is optimized via grid search with cross-validation (or train/test split) based on dataset size.

This methodology provides a modular and numerically grounded approach that balances model complexity with generalization, as will be demonstrated in the subsequent experimental results.

## 4. Experimental Results

This section presents the quantitative performance of the decision tree classifier on both datasets, along with examples, numerical details, and pseudocode to clarify the evaluation process.

## 4.1 Primary Dataset Results

• Dataset Size: 173 examples.

• Evaluation Method: 5-fold cross-validation.

• Average Accuracy: Approximately 54.9%.

• Observations: Due to the limited number of examples, the model exhibits high variance. In several folds, the accuracy ranged between 50% and 60%, which indicates that the decision boundaries learned on such a small dataset are unstable.

#### Example Split and Tree Structure:

```
Node: if stem-width <= 7.5? (samples: 173)
Node: if gill-spacing <= d? (samples: 73)
Node: if stem-height <= 3.25? (samples: 12)
Leaf: prediction = p (samples: 2)</pre>
```

```
Node: if Cap-surface <= d? (samples: 10)
  Leaf: prediction = p (samples: 1)
  Node: if Cap-surface <= l? (samples: 9)
    Leaf: prediction = p (samples: 1)
  Leaf: prediction = e (samples: 8)
Node: if gill-color <= n? (samples: 61)
  Leaf: prediction = p (samples: 9)
  Node: if stem-height <= 6.75? (samples: 52)
    Node: if stem-height <= 6.25? (samples: 43)
    Leaf: prediction = p (samples: 40)
    Leaf: prediction = e (samples: 3)
  Leaf: prediction = p (samples: 9)</pre>
```

### Feature Importances (Excerpt):

• stem-width: 0.0448

• gill-spacing: 0.0584

• stem-height: 0.0784

#### Pseudocode for Cross-Validation Evaluation:

```
for each fold in 5-fold CV:
    split data into training and validation sets
    train decision tree on training set
    for each instance in validation set:
        predict label using tree.predict(instance)
    compute fold accuracy = (# correct predictions) / (total validation samples)
average_accuracy = mean(accuracy_scores)
```

Hyperparameter Tuning Impact: The grid search over max\_depth and min\_samples\_in\_leaf on the primary dataset showed that using max\_depth = 5 and min\_samples\_in\_leaf = 5 yielded the highest average accuracy (around 55%). These settings helped reduce over-fitting on the limited data by preventing the tree from growing too deep or splitting on very few examples.

## 4.2 Secondary Dataset Results

- Dataset Size: Approximately 61,000 examples.
- Evaluation Method: 80% train / 20% test split.
- Test Accuracy: Approximately 95.2%.
- Hyperparameter Override: Although the grid search initially suggested max\_depth = None, I set max\_depth to 15 to reduce training time and control model complexity.

### Example Split and Tree Structure (Excerpt):

```
Node: if stem-width <= 8.31? (samples: 48855)

Node: if gill-spacing <= d? (samples: 20946)

Node: if stem-height <= 3.73? (samples: 3430)

Node: if cap-surface <= s? (samples: 981)

Leaf: prediction = e (samples: 190)

Node: if cap-shape <= b? (samples: 791)

Leaf: prediction = e (samples: 18)

Node: if cap-shape <= f? (samples: 773)

Leaf: prediction = e (samples: 7)

...
```

#### Confusion Matrix:

5223 151 430 6410

#### **Analysis:**

- True Positives (Class e): 5223 instances.
- False Negatives (Class e predicted as p): 151 instances.
- False Positives (Class p predicted as e): 430 instances.
- True Negatives (Class p): 6410 instances.

These numbers indicate that the model has high sensitivity (recall) for class e (0.97) and high precision for class p (0.98), which is critical in applications where misclassification can have severe consequences.

#### Classification Report (Excerpt):

- Class e: Precision 0.92, Recall 0.97, F1-score 0.95.
- Class p: Precision 0.98, Recall 0.94, F1-score 0.96.

#### Feature Importances (Excerpt):

• cap-surface: 0.1411

• stem-surface: 0.0923

• stem-width: 0.0657

**Hyperparameter Tuning Impact:** For the secondary dataset, the grid search suggested an unbounded tree. However, to manage training time and complexity, I fixed max\_depth at 15. This decision maintained a high test accuracy (95.2%) while reducing overfitting and computational cost.

#### Pseudocode for Secondary Dataset Evaluation:

```
Split data into training (80%) and test (20%) sets
if max_depth is None:
    max_depth = 15
Train decision tree on training set with specified hyperparameters
for each instance in test set:
    predict label using tree.predict(instance)
Compute test accuracy = (# correct predictions) / (total test samples)
Output confusion matrix and classification report
```

In summary, the experimental results demonstrate that the decision tree predictor performs robustly on large datasets, achieving high accuracy and low misclassification rates. The detailed analysis of confusion matrices, feature importances, and the effect of hyperparameter tuning provides strong evidence of the model's effectiveness.

### 5. Discussion

The experimental results provide valuable insights into the behavior of the decision tree classifier across different data regimes.

## 5.1 Data Size Impact

- Primary Dataset: With only 173 examples, the 5-fold cross-validation yielded an average accuracy of approximately 54.9%. Accuracy across folds ranged from 50% to 60%, indicating high variance due to limited data.
- Secondary Dataset: The larger dataset (about 61,000 examples) achieved a test accuracy of approximately 95.2%. This substantial improvement underscores the importance of ample, high-quality data for robust model training.

## 5.2 Model Complexity and Overfitting

- On the primary dataset, the model often built deeper trees (depths up to 7) despite the small sample size, suggesting potential overfitting.
- For the secondary dataset, I capped the maximum depth at 15. This restriction reduced training time by roughly 40% and prevented the model from capturing noise, ensuring better generalization.

## 5.3 Impurity Measures and Stopping Criteria

• Impurity Measures: Both Gini and entropy produced similar splits for binary classification. Scaled entropy, however, normalizes the entropy by  $\log_2(K)$  (with K=2 in this case), which is useful for extending the approach to multi-class

scenarios. For instance, for a node with labels [e, e, p, p, p], standard entropy is  $\approx 0.971$ ; scaled entropy remains 0.971 for binary problems.

- Stopping Criteria: Three criteria were used to prevent uncontrolled growth:
  - Node purity: Splitting stops if all examples in a node share the same label.
  - Minimum samples per leaf: A node with fewer than 5 samples is not split, reducing overfitting by approximately 10% in validation accuracy.
  - Maximum depth: The tree halts splitting once the depth limit is reached.

## 5.4 Feature Importance Insights

- Primary Dataset: stem-height (0.0784) and Cap-surface (0.0638) were the most influential features.
- Secondary Dataset: cap-surface (0.1411) and stem-surface (0.0923) emerged as key predictors, with their contributions exceeding those of features such as stem-width (0.0657) by more than 50%.

## 5.5 Pseudocode for Evaluating a Stopping Condition

```
if (all samples have the same label) or
  (number of samples < min_samples_in_leaf) or
  (current_depth >= max_depth):
    mark node as leaf and assign majority class prediction
```

Overall, these findings indicate that while decision trees can achieve excellent performance on large, clean datasets, their reliability diminishes with limited data. Careful hyperparameter tuning, along with well-designed stopping criteria and impurity measures, is crucial to balance model complexity and generalization.

## 6. Conclusion

- The decision tree predictor was implemented from scratch using single-feature binary tests.
- It supports three impurity measures: Gini, entropy, and scaled entropy, along with multiple stopping criteria (node purity, minimum samples per leaf, and maximum depth).
- Experiments on the primary dataset (173 examples) showed limited performance (CV accuracy  $\sim 55\%$ ) due to the small sample size, while the secondary dataset (over 61,000 examples) achieved high accuracy (test accuracy  $\sim 95.2\%$ ).

- Hyperparameter tuning (using grid search and cross-validation) and the use of scaled entropy provided valuable insights into model behavior and feature importance.
- The results emphasize the importance of dataset size and quality, as well as the need for controlling model complexity to prevent overfitting.

In summary, the project demonstrates that even a basic decision tree can perform well on large, clean datasets, while its performance is limited on small, noisy datasets. Future work may include extending the model to ensemble methods, such as random forests, and exploring pruning techniques to further enhance generalization.

## **Declaration**

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