# Topic 8 Graph and Circuit

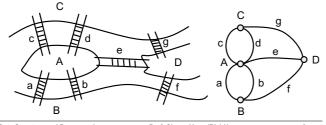
資料結構與程式設計 Data Structure and Programming

11/13/2019

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# The First Use of Graph

- ◆ Köigsberg Bridge Problem
  - Leonhard Euler, 1736
  - Starting at one land, is it possible to walk across all bridges exactly once and returning to the starting land area?



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#### From CS to EE? What does that mean?

- Most people think that "Data Structure" is a CS class
  - A "must" subject for CS entrance exam
- ◆ In EE area, many problems can be either mapped as graphic problems, or resolved by graphic algorithms
  - e.g. Circuit netlist, network, communication, etc.
  - Understanding graphic data structure and algorithms will be very helpful

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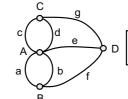
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# **Eulerian Theorem**

- ◆ There is a walk starting at any vertex, going through each edge exactly once and terminating at the starting vertex, iff the degree of each vertex is even.
  - → Eulerian walk



No Eulerian walk, since all 4 vertices are of odd degree.

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# **Definition of a Graph**

- ◆ A graph, G(V, E)
  - V: a finite, nonempty set of vertices → V(G)
  - E: a set of pairs of vertices these pairs are called edges → E(G)
- 1. Undirected Graph
  - Every pair of vertices representing any edge is unordered
  - i.e. (u, v) and (v, u) represent the same edge
- 2. Directed Graph (Digraph)
  - Order of the pair of vertices matters
  - <u, v>: 'u' is the tail and 'v' is the head
  - e.g. A circuit is a directed graph



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# **Terminologies**

- ◆ Path
  - A sequence of vertices in which each vertex is adjacent to the next one
    - e.g. {  $n_1$ ,  $e_1$ ,  $n_2$ ,  $e_2$ ,  $n_3$ ,  $e_3$ , ...,  $e_{k-1}$ ,  $n_k$  }
- Simple path
  - All vertices in a path are distinct
- ◆ Length of a path
  - The number of edges in a path
- ◆ Loop (self-edge)
  - An edge with 2 identical end-points
- ◆ Cycle
  - A path with identical start and end points

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# **Terminologies**

- ◆ Given 2 nodes u, v, and an undirected edge (u, v)
  - u and v are called adjacent
  - The edge (u, v) is incident on vertices u and v
- → If <u, v> is a directed edge
  - u is adjacent to v, and v is adjacent from u



- ◆ Degree of a vertex
  - The number of edges incident to it
- → If the graph is directed
  - In-degree
    - The number of edges for which the vertex is the head
  - Out-degree
    - The number of edges for which the vertex is the tail

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# **Graph Properties**

- ◆ Subgraph G(V', E') of G(V, E)
  - V' ⊆ V: E' ⊆ E
- ◆ Simple graph
  - No loops and no two edges link the same vertex pair
- Multigraph
  - Not simple graph
- Weighted graph
  - Each edge is associated with some weight
- Hypergraph
  - An extension of a graph where edges may be incident to any number of vertices



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# **Complete Graph**

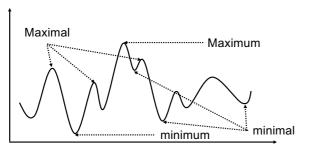
- ◆ Complete graph
  - Each vertex is adjacent to all the other vertices in the graph
  - For complete graph with n vertices
     #edges = n (n 1) / 2
- Clique of a graph
  - Complete subgraph
- ◆ Complement G(V', E') of a graph G(V, E)
  - V' = V;  $E \cap E' = \emptyset$
  - G(V, E ∪ E') is a complete graph

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# (FYI) Maximal vs. Maximum



- In many problems, finding maximum/minimum is very hard
   Finding maximal/minimal is the only possibility
- How to find a better maximal/minimal?

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## **Undirected Graph Properties**

- Two vertices u and v are said to be connected
  - iff there a path from u to v
- ◆ A graph is said to be connected
  - iff every vertex pair is connected
  - → A tree is a connected acyclic graph
- ◆ A connected component (or simply component) of a graph
  - A <u>maximal</u> connected subgraph

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# **Undirected Graph Properties**

- Cutset
  - A minimal set of edges whose removal from the graph makes the graph disconnected



◆ Bipartite graph

 Vertex set can be partitioned into 2 subsets such that each edge has end-points in different subsets



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# **Undirected Graph Properties**

- ◆ Plannar graph
  - A diagram on a plane surface such that no two edges cross





- ◆ Two graphs are isomorphic
  - There is a one-to-one correspondence between their vertex sets and preserves adjacency





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# **Undirected Graph Properties**

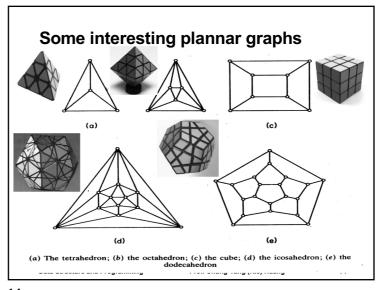
- Each undirected graph can be characterized by four numbers
- 1. Clique number ω(G)
  - The cardinality of its largest clique, called clique number
- Chromatic number χ(G)
  - The minimum number of colors needed to color the vertices, such that no edge has endpoints with the same color
  - e.g. A bipartite graph is a 2-colorable graph

Property:  $\omega(G) \leq \chi(G)$ 

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# **Undirected Graph Properties**

- Clique cover number κ(G)
  - A graph is said to be partitioned into cliques if its vertex set is partitioned into (disjoint) subsets, each one including a clique
  - The cardinality of a minimum clique partition is called Clique cover number
- 4. Stability number α(G)
  - A stable set, or independent set, is a subset of vertices with the property that no two vertices in the stable set are adjacent
  - The stability number is the cardinality of its largest stable set
  - A coloring of a graph is a partition of the vertices into subsets, such that each is a stable set

Property:  $\alpha(G) \leq \kappa(G)$ 

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# **Perfect Graph**

- ◆ A graph is said to be perfect iff
  - $\omega(G) = \chi(G)$  (clique = chromatic)
  - $\alpha(G) = \kappa(G)$  (stability = clique covering)



$$\omega(G) = \chi(G) = 3$$

$$\alpha(G) = \kappa(G) = 2$$

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# **Directed Graph Properties**

- ◆ A digraph is said to be strongly connected
  - Iff for every pair of distinct vertices u and v, there is a path from u to v, also from v to u





- ◆ Strongly connected component (SCC)
  - Maximal subgraph that is strongly connected
  - If a graph is strongly connected, it has only one SCC
  - Linear time algorithm for finding SCCs: Robert E. Tarjan, Depth-first search and linear graph algorithms, SIAM Journal on Computing, 1(2):146-160, 1972.

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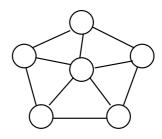
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# Any graph that is NOT perfect?

◆ That is:

Clique number  $\omega(G)$  < Chromatic number  $\chi(G)$ Stability number  $\alpha(G)$  < Clique cover number  $\kappa(G)$ 



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# **Directed Acyclic graph (DAG)**

- ◆ A directed graph that has no cycle
- ◆ Can represent partially ordered set
  - A vertex v is a successor (descendant) of a vertex u
    - If there is a path from u to v
    - Called direct successor if the path is an edge
  - Predecessor (ancestor)
- ◆ Polar DAG
  - A DAG with 2 distinguished vertices
    - A source and a sink
  - All vertices are reachable from the source
  - Sink is reachable from all the vertices
  - A generic polar DAG may have multiple sources and sinks

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# Partially vs. Totally Ordered Set

- ◆ A relation "≤" is a partial order on a set S if it has:
  - 1. Reflexivity:  $a \le a$  for all  $a \in S$
  - 2. Antisymmetry:  $a \le b$  and  $b \le a$  implies a = b.
  - 3. Transitivity:  $a \le b$  and  $b \le c$  implies  $a \le c$
- ◆ A relation "≤" is a total order on a set S if it has the above 3 properties and the following:
  - 4. Comparability (trichotomy law): For any  $a, b \in S$ , either  $a \le b$  or  $b \le a$

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# **Graphic Algorithms**

- The importance of learning "graphs" is that many practical problems can be modeled and then solved by standard/well-known graphic algorithms
  - 1. Breadth-First Search and Depth-First Search
  - 2. Topological Sort
  - 3. Strongly Connected Component
  - 4. Shortest and Longest Path Algorithms
  - 5. Minimum Spanning Tree
  - 6. Maximum Flow and Minimum Cut
- Please refer to "Algorithm" book or class for more information
  - We may cover some of them if we have time...

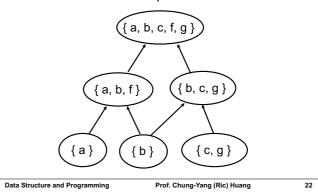
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# **A Partial Order Example**

◆ The "containment" relation among the subsets of a set is a partial order



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# **Graph Traversal**

- In many graph (DAG) applications, it is important to go through every vertex in certain order
  - e.g. checkSum(), simulate(), etc
- ◆ Topological order
  - An order sorted by certain relationship of adjacent vertices
  - e.g
    - For each vertex, it has higher order than all of its predecessors, and lower order than all of its successors

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# Depth-First Traversal (Take 1)

```
void
Graph::dfsTraversal(const List<Node*>& sinkList)
{
    for_each_sink(node, sinkList)
        node->dfsTraversal(_dfsList);
}
// post order traversal
void Node::dfsTraversal(List<Node *>& dfsList)
{
    for_each_predecessor(next, _predecessors)
        next->dfsTraversal(dfsList);
    dfsList.push_back(this);
}
Any Problem??
```

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# **Depth-First Traversal (Take 3)**

**Depth-First Traversal (Take 2)** 

```
void
Graph::dfsTraversal(const List<Node*>& sinkList)
{
    for_each_sink(node, sinkList)
        node->dfsTraversal(_dfsList);
}
// post order traversal
void Node::dfsTraversal(List<Node *>& dfsList)
{
    for_each_predecessor(next, _predecessors)
        if (!next->isMarked()) {
            next->setMarked();
            next->dfsTraversal(dfsList);
    }
    dfsList.push_back(this);
}
Any Problem??
```

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# **Depth-First Traversal (Take 4)**

◆ Remember: use "static data member in a class" class <sup>™</sup>

```
{
    static unsigned __globalRef;
    unsigned __ref;

public:
    T() : __ref(0) {}
    bool isGlobalRef(){    return (_ref == _GlobalRef); }
    void setToGlobalRef(){    _ref = _globalRef; }
    static void setGlobalRef() { __globalRef++; }
}.
```

 Use this method to replace "setMarked()" functions in graph traversal problems

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## **Depth-First Traversal (Take 4)** void Graph::dfsTraversal(const List<Node\*>& sinkList) Node::setGlobalRef(); for each sink(node, sinkList) node->dfsTraversal( dfsList); // post order traversal void Node::dfsTraversal(List<Node \*>& dfsList) for each predecessor(next, predecessors) if (!next->isGlobalRef()) { next->setToGlobalRef(); next->dfsTraversal(dfsList); dfsList.push back(this); Anv Problem? Data Structure and Programming Prof. Chung-Yang (Ric) Huang

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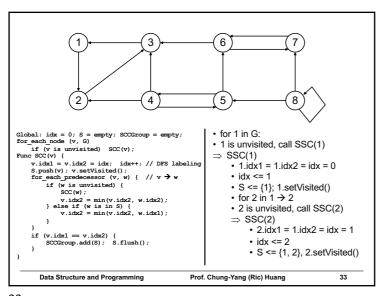
```
Breath-First Traveral
 algorithm levelOrder (TreeNode t)
    Input: a tree node (can be considered to be a
       tree)
    Output: None.
    Let Q be a Queue
    Q.enqueue(t)
    while the Q is not empty
       tree = Q.dequeue()
       Visit node tree
       if tree has a left child
             Q.enqueue(left child of tree)
       if tree has a right child
             Q.enqueue (right child of tree)
How about the "marked" and "loop" Issues ??
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```

```
Depth-First Traversal (Take 5)
Graph::dfsTraversal(const List<Node*>& sinkList)
   Node::setGlobalRef();
   for each sink(node, sinkList)
     node->dfsTraversal( dfsList, fbList);
// post order traversal
void Node::dfsTraversal
(List<Node *>& dfsList, list<NodePair>& fbList)
  for each predecessor(next, predecessors)
     if (!next->isGlobalRef()) {
        next->setToGlobalRef();
         next->setActive();
        next->dfsTraversal(dfsList, fbList);
        next->unsetActive();
     else if (next->isActive())
        fbList.push back(NodePair(this, next));
   dfsList.push back(this);
                               // not push back(next); why?
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```

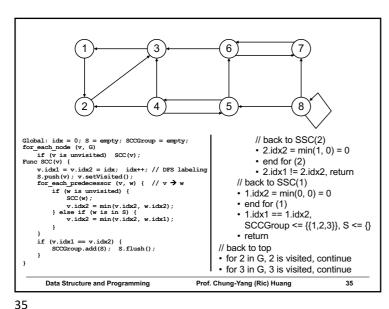
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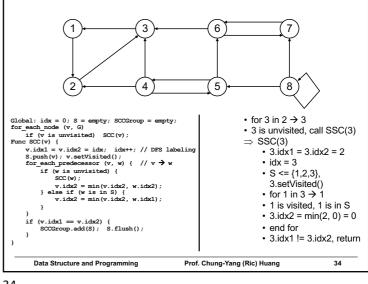
```
Tarjan's Strongly Connected Components (SCC) algorithm
```

```
Global: idx = 0; S = empty; SCCGroup = empty;
 for each node (v, G)
     if (v is unvisited) SCC(v);
 Func SCC(v) {
     v.idx1 = v.idx2 = idx; idx++; // DFS labeling
     S.push(v); v.setVisited();
     for each predecessor (v, w) \{ // v \rightarrow w \}
         if (w is unvisited) {
             SCC(w);
             v.idx2 = min(v.idx2, w.idx2);
         } else if (w is in S) {
             v.idx2 = min(v.idx2, w.idx1);
     if (v.idx1 == v.idx2) {
         SCCGroup.add(S); S.flush();
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```



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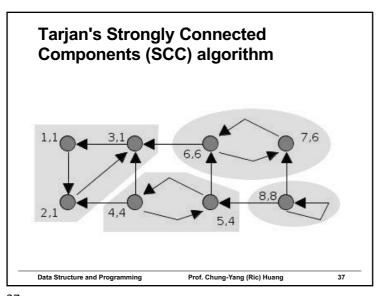
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                                                          5
                                                                                8

    for 4 in G:

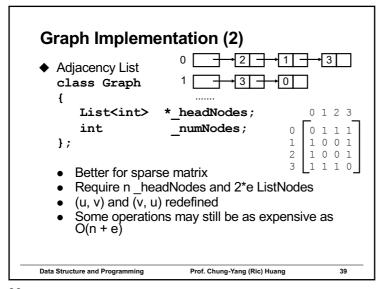
Global: idx = 0; S = empty; SCCGroup = empty;
for_each_node (v, G)

    4 is unvisited, call SSC(4)

   if (v is unvisited) SCC(v);
                                                         \Rightarrow SSC(4)
    v.idx1 = v.idx2 = idx; idx++; // DFS labeling
                                                              • 4.idx1 = 4.idx2 = idx = 3
    S.push(v); v.setVisited();
for each predecessor (v, w) { // v → w
                                                              idx <= 4</li>
        if (w is unvisited) {
                                                              • S <= {4}; 4.setVisited()
            SCC (w);
                                                              • for 2 in 4 \rightarrow 2
        v.idx2 = min(v.idx2, w.idx2);
} else if (w is in S) {
                                                              • 2 is visited but 2 is NOT in S
            v.idx2 = min(v.idx2, w.idx1);
                                                              • for 3 in 4 \rightarrow 3
                                                              · 3 is visited but 3 is NOT in S
    if (v.idx1 == v.idx2) {
                                                              • for 5 in 4 → 5
        SCCGroup.add(S); S.flush();
                                                              • 5 is unvisited, call SSC(5)
                                                              ⇒ SSC(5)...
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```



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**Graph Implementation (1)**  Adjacency Matrix class Graph bool \_adjacency[n][n]; }; For undirected graph → upper triangle 0 1 1 1 How to perform traversal? 1 0 0 1 1 Difficult to implement 1 0 0 1 various graphic algorithms 3 1 1 1 1 0\_ • Could be a sparse matrix Complexity can be as high as O(n<sup>2</sup>) Prof. Chung-Yang (Ric) Huang **Data Structure and Programming** 

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```
Graph Implementation (3)

    Adjacency Multilist

                                                 0 1 N1 N3
   class Edge
                                                  0 2 N2 N3
                  visited;
      bool
                                                  0 3 0 N4
                  vertex1, vertex2;
      int
       Edge
                * path1, * path2;
                                                  1 2 N4 N5
   };
                                                  1 3 0 N5
   class Graph
                                                  2 3 0 0
       Edge**
                  headNodes;
       int
                  numNodes;
   };
      Same memory requirement as "adjacent list"
       (except for _visited field))
      Not very intuitive to understand
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```

# **Graph Implementation (4)**

```
class Node
  Array<Node *> successors;
  Array<Node *> predecessors;
};
class Graph
  Array<Node *>
                     nodes;
   // Array<Node *>
                     sinks;
   // Array<Node *> sources;
```

- Memory usage is about the same (n + 2 \* e)
- A more intuitive implementation

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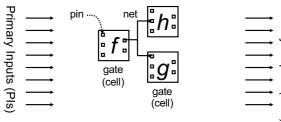
Two dynamic arrays

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#### Circuit

◆ A directed diagram for representing the current flow of an electronic design



- ♦ h and g are f's fanouts
- ♦ f is h's and g's fanin

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# **Graph Implementation (5)**

◆ To contain data in nodes template <class T> class Node data; Array<Node<T> \*> successors; Array<Node<T> \*> predecessors; template <class T> class Graph Array<Node<T> \*> }; Data Structure and Programming Prof. Chung-Yang (Ric) Huang

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# **Circuit Implementation (1)**

```
◆ Cell-based implementation (1)
   class Gate
      GateType
      GateFlag
                      flag; // visited, etc
      Array<Gate *>
                      faninList;
      Array<Gate *>
                      fanoutList;
   class Circuit
     Array<Gate *>
                      piList;
                      poList;
      Array<Gate *>
      Array<Gate *>
                      _totalList;
```

Gate::\_type is to distinguish different functionalities Drawback: usually need a BIG switch in codes

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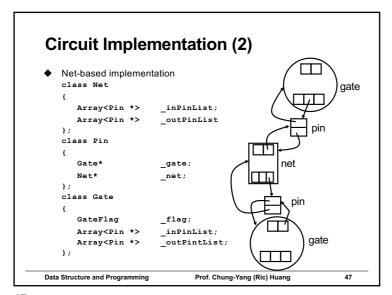
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# **Circuit Implementation (2)**

```
◆ Cell-based implementation (2)
   class Gate
      GateFlag
                      flag;
     Array<Gate *>
                      faninList;
     Array<Gate *>
                     fanoutList;
  class And : public Gate
  };
  class Circuit
     Array<Gate *>
                     piList;
     Array<Gate *>
                      poList;
     Array<Gate *>
                     totalList;
```

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# **Virtual Functions for Different Types of Gates**

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# **Circuit Implementation (3)**

- ◆ AND-Inverter Graph (AIG)
- ◆ All the Boolean functions can be represented by "And: ∧" and "Inverter: ¬"
  - e.g.  $OR(a, b) = \neg(\neg a \land \neg b)$
- ◆ As for circuit implementation, it is better to have simpler data structure
  - · AIG is enough
  - Two classes: AndGate and InvGate?
    - InvGate is kind of unnecessary...
  - One class: NandGate?
    - Still need an object to represent an Inverter
  - → Solution: AndGate with (optional) inverted inputs

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# **AIG Implementation**

```
class AigGate {
   Array<AigGateV> faninList;
                     _ref;
   size t
   static size t globalRef s
};
class AigGateV {
   #define NEG 0x1
   AigGateV(AigGate* g, size_t phase):
       gateV(size t(g) + phase) { }
   AigGate* gate() const {
      return (AigGate*) (_gateV & ~size_t(NEG)); }
   bool isInv() const { return ( gateV & NEG); }
   size t
                     gateV;
};
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```

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#### **AIGER ASCII Format**

- ASCII format contains several sections
  - Header
  - Inputs
  - Latches // ignored in HW#6
  - Outputs
  - ANDs
  - Symbols
  - Comments
- Except for header, any of the above sections can be omitted if it is not necessary
  - However, their relative order cannot be altered

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#### **AIGER Format**

- ◆ An simplified, well-accepted AIG format
  - Documents and source codes available at: http://fmv.jku.at/aiger/
- ◆ Two versions
  - ASCII format: text format ← HW #6
  - Binary format: more compact representation
  - → In HW#6 and final project, we will handle ASCII format only

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#### **AIGER ASCII Format**

- ◆ Header
  - [Syntax] aag MILOA
    - aag: specify ASCII AIG format
      - · [cf] aig: specify binary format
    - M: maximal variable index
    - I, L, O, A: number of inputs, latches, outputs, AND gates
  - [Example] aag 7 2 0 2 3
  - [Note]
    - Exact ONE space before M, I, L, O, A
    - "A" must be immediately followed by a "new line" char.
    - If all variables are used and there are no unused AND gates, then M = I + L + A.

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#### **AIGER ASCII Format**

- Variables and Literals
  - Each input, latch, and AND gate is assigned with a distinct variable ID (i.e. an unsigned number)
    - Between [1, M]
    - Variable 0 means constant FALSE.
    - The input, latch, and AND variable IDs can be arbitrary. No one is necessarily bigger/smaller than the other.
  - A "literal" is a positive or negative form of a variable
    - Let v be the ID of a variable, than the literal (2v) and (2v+1) stands for the positive and negative forms of the variable, respectively
    - e.g. Literal 12 is the positive form of variable 6
       Literal 1 stands for constant TRUE

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# **AIGER ASCII Format**

- Latches
  - [Syntax] <currStateLiteralID> <nextStateLiteralID>
  - [Example] 8 15
  - [Note]
    - Each line defines exactly one latch, which contains the current state literal ID followed by the next state ID
    - Currnet states are non-negative (as inputs), so their literal IDs must be even numbers
    - Next states can be inverted (as outputs), so their literal IDs can be positive or negative

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#### **AIGER ASCII Format**

- ◆ Inputs
  - [Syntax] <inputLiteralID>
  - [Example] 2
  - [Note]
    - Each line defines exactly one input, which is represented as a literal ID
    - Inputs are non-negative, so the literal IDs must be even numbers
- ◆ Example

```
aag 3 2 0 1 1 // header
2 // input 0
4 // input 1
```

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# **AIGER ASCII Format**

- Outputs
  - [Syntax] <outputLiteralD>
  - [Example] 9
  - [Note]
    - Each line defines exactly one output, which is represented as a literal ID
    - Outputs can be inverted, so their literal IDs can be even or odd
- ◆ Example

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#### **AIGER ASCII Format**

- ◆ AND gates
  - [Syntax] <LHS> <RHS1> <RHS2>
  - [Example] 12 7 15
  - [Note]
    - Each line defines exactly one AND gate, which containts the LHS literal followed by exactly two RHS literals
    - LHS literals must be even, and the RHS literals can be even or odd (i.e. non-inverted or inverted)
- ◆ Example

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# **AIGER ASCII Format**

- ◆ Comments
  - [Syntax] c

[anything]...

• [Example] c

Game over!!

- [Note]
  - The comment section starts with a *c* character followed by a new line. The following lines are comments.

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#### **AIGER ASCII Format**

- ◆ Symbols
  - [Syntax] [ilo]<position> <symbolicName>
  - [Example] i0 reset

ol done

- [Note]
  - Each line defines exactly one symbolic name for inputs, latches, or outputs
  - There is at most ONE symbolic name for each input, latch, or output
  - osition> denotes the position of the corresponding input/latch/output is defined in it section. It counts from 0.
  - Symbolic name can contain any printable character, except for "new line"
    - [Note] White space and numbers are allowed in names

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# **Notes on AIGER Format**

- ◆ No leading or trailing spaces in each line
- ♦ No empty line
- "New line" character must present at the end of each line
- All parsed tokens in the same line, except for comments, must be separated by exactly ONE space character
- Need to identify undefined literals and floating signals in parser

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#### **AIGER Examples** 1. Empty circuit aag 0 0 0 0 0 // header 2. And gate aag 3 2 0 1 1 // header // input #0 (var id = 1) // input #1 (var id = 2) 4 // output #0 (var id = 3) // AND gate 3 = 1 & 2 624 Or gate aag 3 2 0 1 1 // input #0 (var id = 1) // input #1 (var id = 2) // output #0 (var id = 3) 635 // AND gate 3 = !1 & !2

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#### Some notes about HW#6

◆ Topic: An AIGER parser

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- Parse an AIGER netlist file into a circuit data structure (a DAG)
  - Note: Error handling can be VERY complicated... Try to work on "good" circuits first!!
- Check for floating/undefined variables
- Check for cyclic conditions
- Report circuit statistics
- Report gate connections
- Perform logic simulations
- Output AIG file

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```
AIGER Examples
4. Half Adder
   aag 7 2 0 2 3
                      // header line
                      // input #0
   2
                                     1st addend bit 'x'
   4
                      // input #1
                                     2nd addend bit 'y'
   6
                      // output #0
                                      sum bit
                      // output #1
                                                'c'
   12
                      // AND gate #0 x ^ y
   6 13 15
   1224
                      // AND gate #1
                                       x & y
   14 3 5
                      // AND gate #2
                                       !x & !y
   i0 x
                      // symbol
                      // symbol
   i1 y
   o0 s
                      // symbol
   o1 c
                      // symbol
                      // comment header
   half adder
                      // comment
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```