Topic 12 Cache vs. hash

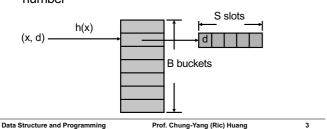
資料結構與程式設計 Data Structure and Programming

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Hash Table

- 1. Buckets: the table is composed of B buckets (usually a large number)
- 2. Each bucket can hold up to S slots of data (usually a smaller number)
- Given a data d with key x, a hash function h(x) is used to compute the corresponding bucket number



From O(log n) to O(1)?

- For set and map, they have good complexity for "insert", "delete" and "find" operations
 → O(log n)
- ♦ However, in set and map, all the data are sorted --
 - Can output the data in ascending/descending order
 - Can get the list of elements with values in certain range
- What if we don't care about the order, and just want to have fast "insert", "delete" and "find" operations?
 - Can we gain something (complexity) back for not sorting the data?

Think: How do you retrieve memory?

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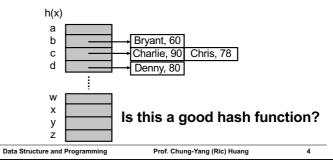
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Hash Table Example

◆ Record: (student name, score)

◆ Hash table: 26 buckets

◆ Hash function = the first character of name



Complexity Analysis

- ◆ Depending on how the s slots are designed
- ◆ However, the worse case...
 - Insert: O(1)
 - Assuming it takes O(1) to compute h(x)
 - Delete: $O(s) \rightarrow can they be O(log s)$?
 - Find: O(s) → what's the price to pay?
- ◆ Because s is usually a smaller number (e.g.
 2) → Very efficient

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Hash Functions

- ♦ Convert key x to an integer b as the bucket index $(0 \le b \le B 1)$
 - Generally O(1) complexity
- Discuss: how's the hash function used in slide #4 (student name, score) example?
 - No good, the first characters of names are usually not evenly distributed among 26 letters
 - Some buckets may become full easily (e.g. 'c'), while some may be empty (e.g. 'x')
- Ideal: for all possible key values, approximately the same number of keys get mapped into each bucket
 - → Uniform Hash Function

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Hash Table Design Issues

- 1. Choice of hash function
- 2. Overflow handling methods
- 3. Size (number of buckets) of hash table

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Hash Function Methods

- Summation
 - e.g. Adding the ASCII values of some/all the characters together
- Shif
 - e.g. Keys are pointers; because pointer values are multiplier of 4 (or 8)
 - \rightarrow h(x) = (x >> 2) ...
 - e.g. x.p, x.q are two pointers;
 - \rightarrow h(x) = (x.p >> 3) + (x.q >> 6);
- Division
 - · e.g. Divide a prime number
- ◆ Others: folding, mid-square, digit analysis, etc
- ◆ Usually: mixed of the above

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Collision and Overflow

- ◆ Collision
 - Two non-identical keys are hashed into the same bucket
 - At most (s − 1) collisions for a buckets
 - Reduced by better hash function
- Overflow
 - When a new key is hashed into a full bucket
- → For better hash performance, we should try to produce less collisions and prevent overflow

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Hash Table Size

- Hash table size (number of buckets) also affects the occurrence of overflow
 - Too small → Overflow happens
 - Too large → Waste of memory
- 1. Static hashing
 - Fixed-size hash table
 - Easier to implement; better if the number of possible elements is known in advance
- 2. Dynamic hashing
 - Hash table size can grow when necessary
 - When it grows, rehashing is needed

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Overflow Handling

- Overflow may still happen when more and more data are stored into the hash
- 1. Open addressing
 - Find a non-full bucket to insert the new key
 - Linear probing, quadratic probling, rehashing, (pseudo)random probing, etc
- 2. Chaining
 - Use linked list, dynamic array, or other kinds of ADT to make the s extendible

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HW#7 -- Hash Implementation (myHashSet.h)

```
    operator () → as the hash function

class HashSet
                                (i.e. d() % numBuckets to return
                                bucket index)

 operator == → to compare if the

public:
                                data are equivalent (or have the
   class iterator
                                same key)
       friend class HashSet<Data>;
private:
                                numBuckets;
   // Each buckets[i] is a vector<Data>
   vector<Data>*
                                buckets;
};
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```

Supported functions in class HashSet

```
iterator begin() const; // Point to the first valid data
iterator end() const; // Past the end
bool empty() const; // return true if no valid data
size_t size() const; // number of valid data
vector<Data>& operator [] (size_t i) { return _buckets[i]; }
const vector<Data>& operator [](size_t i) const;
void init(size_t b); // initialize Hash with _numBuckets = b
void reset();
```

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Another Hash Implementation Example (myHashMap.h)

```
template <class HashKey, class HashData>
class HashMap
{
    typedef pair<HashKey, HashData> HashNode;
public:
    class iterator
    {
        friend class HashMap<HashKey, HashData>;
        };
private:
        size_t __numBuckets;
        vector<HashNode>* __buckets;
};

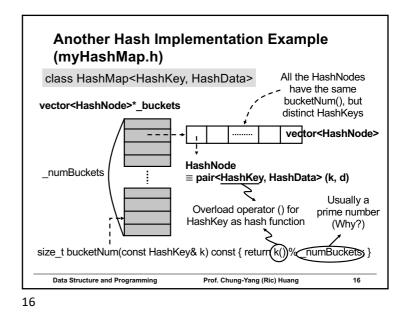
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```

Supported functions in class HashSet // check if d is in the hash... // if yes, return true; else return false; bool check(const Data& d) const; // query if d is in the hash... // if yes, replace d with the data in the hash and return true; // else return false; bool query(Data& d) const; // update the entry in hash that is equal to d (i.e. == return true) // if found, update that entry with d and return true; // else insert d into hash as a new entry and return false; bool update(const Data& d); // return true if inserted successfully (i.e. d is not in the hash) // return false is d is already in the hash ==> will not insert bool insert(const Data& d);

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Class HashKey

- ◆ To use Hash ADT, you should define your own HashKey class.

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class Hash::iterator

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Example of using class Hash

- ◆ Locating an address
- typedef string Address;
 typedef pair<float, float> Location;
 class AddressKey {
 public:
 size_t operator() () const { ...; }
 bool operator == (const Address& a) {
 return (_addr == a._addr); }
 private:
 Address _addr;
 };

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Supported functions in class HashMap

```
iterator begin() const; // Point to the first valid data iterator end() const; // Pass the end bool empty() const; // return true if no valid data size_t size() const; // number of valid data vector<HashNode>& operator [] (size_t i) { return _buckets[i]; } const vector<HashNode>& operator [](size_t i) const; void init(size_t b); // initialize Hash with _numBuckets = b void reset(); bool check(const HashKey& k, HashData& n); bool insert(const HashKey& k, const HashData& d); bool replaceInsert(const HashKey& k, HashData d); void forceInsert(const HashKey& k, HashData d);
```

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Hash Classes in STL

- Since C++-11, STL supports and standardizes the following associative containers that implement Hash
- 1. unordered set
- 2. unordered multiset
- 3. unordered map
- 4. unordered multimap

[Ref] Deprecated, non-standard STL implementations:

- hash set
- 2. hash_multiset
- 3. hash_map
- hash_multimap

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Member Functions of class unordered_set

- iterator begin(); const_iterator cbegin() const; iterator begin(n); // get the first element in bucket[n] // see also cbegin(n), end(), end(n), cend(), cend(n)
- 2. size_type bucket_count() const; size_type bucket(k) const;
- pair<iterator, bool> insert(const value_type& k); void insert(InputIterator f, InputIterator I);
- 4. iterator erase(const_iterator pos); // to the next iterator size_type erase(const key_type& k); // #elms erased iterator erase(const_iterator first, const_iterator last);
- 5. iterator find(k) const; size type count(k) const;
- float load_factor() const; // = size() / bucket_count() float max_load_factor() const; void max_load_factor(l); void rehash(size_type n);

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class unordered_set in STL

- unordered_set<Key[, Hash, Pred, Alloc]>
 - class Key: element type
 - class Hash: hash function (optional; default = hash<Key>)
 - class Pred: equality checking for class Key (optional; default = equal_to<Key>)
 - class Alloc: used for internal memory management (optional; default = alloc)

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Other Hash Classes in STL

- ◆ class unordered_multiset
 - Similar to unordered_set, but allow elements with identical keys
- class unordered_map
 - unordered_map<Key, Data[, Hash, Pred, Alloc]>
- ◆ class unordered_multimap
 - Similar to unordered_map, but allow elements with identical keys

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Cache in Programming

- ◆ Structurally similar to hash, however
 - Usually smaller number of buckets
 - Each bucket contains exactly 1 element
 - When collision happens, the old data is overwritten by the new one
 - Easier to implement than hash
- ◆ Usually used as computational cache
 - (input parameters) → computational results
- ◆ There is no STL implement yet

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Example of using class Cache (BDD project)

◆ Computed table

$$ITE(F, G, H) = F * G + \overline{F} * H$$

F, G, H: BddNode (contains a size t data)

- → Requires expensive recursive calls to compute ITE() functions (O(|H|*|G|*|H|))
- → The computed table (cache) is to record the result (as CacheData) with respect to the ITE parameters (as CacheKey)
- → So next time when the same ITE(F, G, H) computation is required, we can immediately look up the cached result

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Cache Implementation in util/myHashMap.h

```
template <class CacheKey, class CacheData>
class Cache
   typedef pair<CacheKey, CacheData> CacheNode;
public:
   // No need to implement class iterator (why?)
   void init(size_t s);
   void reset();
   size t size() const;
   CacheNode& operator [] (size t i);
   const CacheNode& operator [](size t i) const;
   bool read(const CacheKey& k, CacheData& d) const;
   void write(const CacheKey& k, const CacheData& d);
private:
                    _size;
   size t
   CacheNode*
                    cache; // new CacheNode[ size]
};
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```