Assignment 1 - Decision Tree Classifiers

Overview

This decision tree classifier is implemented as an extension of the <u>anytree</u> (https://anytree.readthedocs.io/en/latest/index.html) module. By inheriting from the any tree node class, the tree structure is easily maintained and all custom code is simply added to the class.

Data manipulation is performed using <u>pandas (https://pandas.pydata.org/)</u>, which has many low-level functions built in to perform functions not directly related to the Decision Tree Classifier algorithms that are the focus of the assignment.

Part 1: Splitting Algorithm

The splitting algorithm is implemented as follows

```
if stop criterion have not been met:
    compute the optimal split among all features and all split values of eac
h feature
    split the samples into two subsamples based on this optimal split
    for each sample subset, apply the splitting algorithm
```

The stopping criterion, as specified, are that either the sample set is pure or all features of the set are identical. Pandas was used to quickly perform both of these checks. Purity was checked by looking at the number of unique labels within the set. Feature similarity was checked by ensuring that more than one sample still existed when duplicate features were removed

Part 2: Pruning Algorithm

The pruning algorithm is implemented as follows:

```
Set the best observed accuracy to 0

At the root node:

Make a list of all descendants of the node

For each descendant:

temporarily remove the node and its descendants

calculate the accuracy of the new tree

Add the node back into the tree

if the new accuracy is greater than the current best accuracy:

update best accuracy

track the node that whose removal gave this accuracy

Remove the best node (and its descendants) that gives the best resultant accuracy
```

Anytree makes this process very simple, since many of these steps simply involve changing a node's parent temporarily and then iterating over the new tree

Part 3: Data Analysis

```
In [1]:
        #import pandas for dataset manipulation, anytree for tree visualizati
        on, and supporting modules
        import pandas as pd
        import numpy as np
        import matplotlib.pyplot as plt
        import os as os
        import anytree as at
        import anytree.exporter as texporter
        import copy as copy
```

```
class DTCNode(at.Node):
    def __init__(self, name, samples, features,impurityType, resultVa
l, parent=None):
        self.name = name
        self.totalNodes = np.nan #hasn't been calculated yet
        self.totalLeafNodes = np.nan #hasn't been calculated yet
        self.parent = parent
        self.splitFeature = None
        self.splitValue = np.nan
        self.samples = samples
        self.trueSamples = None
        self.falseSamples = None
        self.features = features
        self.resultVal = resultVal
        self.label = self.computeLabel()
        self.impurityType = impurityType
        self.impurity = self.computeImpurity(self.samples)
        if not self.stopCriterionIsMet():
            [self.splitFeature,
             self.splitValue,
             self.trueSamples,
             self.falseSamples,
             isLeaf] = self.computeOptimalSplit()
            if isLeaf: #this conditional is needed to due to what see
ms to be a numerical rounding error when a set
                       #is largely biased towards a single label, suc
h as 180 0's and a single 1
                self.name = self.label
            else:
                self.name = self.name + "\n" + self.splitFeature + "
 <= " + str(self.splitValue)
                DTCNode("True", self.trueSamples, self.features, self
.impurityType, True, parent=self)
                DTCNode("False", self.falseSamples, self.features, se
lf.impurityType, False, parent=self)
        else:
            self.name = self.label
        if parent == None:
            self.countNodes()
            self.saveAsPNG(self.name)
    def stopCriterionIsMet(self):
        return self.samplesArePure(self.samples) or self.sampleFeatur
esAreIdentical(self.samples)
    # samples are pure if all the labels are the same
    # use pandas built-ins to do a bit of the heavy lifting
    # by counting the number of unique values within the label colum
n,
    # if it is pure, there will only be a single unique value
    def samplesArePure(self, samples):
         return samples[samples.columns[0]].nunique() == 1
```

```
# again use pandas built-ins for heavy lifting
    # by removing all rows with duplicate feature values.
    # If all features are identical for all samples,
    # only one row will be remaining
    def sampleFeaturesAreIdentical(self, samples):
        return len(samples.drop duplicates(self.features).index) == 1
    # iterate through all features(and possible splits within those f
eatures)
    # in the node's samples and find the feature/split combo that min
imizes the resultant
    # child node's weighted impurity.
    def computeOptimalSplit(self):
        bestImpurity = 1
        bestFeature = None
        bestValue = None
        bestTrueSubSample = None
        bestFalseSubSample = None
        #iterate through each feature
        for feature in self.features:
            #create an ordered list of values
            orderedValueList = self.samples[feature].sort values(asce
nding=True).drop duplicates()
            #create array of potential split values by averaging adja
cent values in the list
            splitVals = []
            orderedValueList=orderedValueList.values
            for i in range(1,orderedValueList.size-1):
                #print(i)
                #print(orderedValueList[i-1])
                #print(orderedValueList[i])
                splitVals.append((orderedValueList[i]+orderedValueLis
t[i-1])/2)
            for value in splitVals:
                [tempTrueSamples, tempFalseSamples] = self.split(feat
ure, value)
                tempImpurity = self.computeWeightedImpurity(self.samp
les,
                                                            tempTrueSa
mples,
                                                            tempFalseS
amples)
                if tempImpurity < bestImpurity:</pre>
                    #print("Found a better split criterion!")
                    #print(bestFeature, bestValue)
                    bestImpurity = tempImpurity
                    bestFeature = feature;
                    bestValue = value
                    bestTrueSubSample = tempTrueSamples
                    bestFalseSubSample = tempFalseSamples
                    #print(bestTrueSubSample)
                    #print(bestFalseSubSample)
        return [bestFeature, bestValue, bestTrueSubSample, bestFalseS
ubSample, bestFeature==None]
    # returns two subsamples by splitting a node's samples based on a
```

```
specified
   # feature and value
   # Uses pandas for heavy lifting
   def split(self, feature, value):
       # pandas supports boolean indexing, which makes this pretty t
rivial
        trueSubSamples = self.samples[self.samples[feature] <= value]</pre>
        falseSubSamples = self.samples[self.samples[feature] > value]
        return [trueSubSamples, falseSubSamples]
   def computeImpurity(self, samples):
        if self.impurityType == "Gini":
            return self.giniImpurity(samples)
       elif self.impurityType == "Entropy":
            return self.entropyImpurity(samples)
       else:
            raise ValueError("A valid impurity measure type was not s
pecified!")
   # calculates the weighted impurity of a node's children
   # this function takes many shortcuts due to the assumptions
    # that it will only be computing the weighted impurity for
   # a group of two nodes (the two children of a parent node)
   def computeWeightedImpurity(self, parentSamples, subSamples1, sub
Samples2):
        totalSamples = len(parentSamples.index)
        totalSubSamples1 = len(subSamples1.index)
        totalSubSamples2 = len(subSamples2.index)
        return ((totalSubSamples1/totalSamples)*self.computeImpurity(
subSamples1) +
                (totalSubSamples2/totalSamples)*self.computeImpurity(
subSamples2))
   # calculate the gini index of a set of samples
   # this function takes many shortcuts due to the assumption
   # that it will only be computing the gini index of binary data
   def giniImpurity(self, samples):
        #check if the sample set is pure
        if self.samplesArePure(samples):
            return 0
        #print(samples)
        value counts = samples[samples.columns[0]].value counts()
        labelOneCounts = value counts[0]
        labelTwoCounts = value counts[1]
        totalCounts = labelOneCounts + labelTwoCounts
        return 1 - np.square(labelOneCounts/totalCounts) - np.square(
labelTwoCounts/totalCounts)
   # calculate the entropy of a set of samples
    # this function takes many shortcuts due to the assumption
   # that it will only be computing the gini index of binary data
   def entropyImpurity(self, samples):
       #check if the sample set is pure
        if self.samplesArePure(samples):
            return 0
        value counts = samples[samples.columns[0]].value counts()
```

```
labelOneCounts = value counts[0]
        labelTwoCounts = value counts[1]
        totalCounts = labelOneCounts + labelTwoCounts
        return (-(labelOneCounts/totalCounts)*np.log2(labelOneCounts/
totalCounts) -
                (labelTwoCounts/totalCounts)*np.log2(labelTwoCounts/t
otalCounts))
    def computeLabel(self):
        # assign a label to the node that is the label
        # with the largest frequency within the nodes samples
        # value_counts returns frequency counts in descending order
        # by default, so grab the index of the first one
        return self.samples[self.samples.columns[0]].value counts().i
ndex[0]
    def classify(self, sample):
        if self.is leaf:
            return self.label
        elif len(self.children) == 1:
            return self.children[0].classify(sample)
        else:
            if (sample[self.splitFeature].values[0] <= self.splitValu</pre>
e) == self.children[0].resultVal:
                return self.children[0].classify(sample)
            else:
                return self.children[1].classify(sample)
    # Classifies a dataset and generates stats using the provide actu
al labels
    # Returns classification accuracy and a dataframe with relevant c
lassification stats
    def performClassification(self, samples, labels):
        results = []
        for i in range(0, len(samples.index)):
            results.append(self.classify(samples.iloc[[i]]))
        results = np.asarray(results)
        labels = np.asarray(labels)
        accurateResults = np.equal(results, labels)
        # true positives are when both the actual label and the resul
t are of class 1
        truePositives = np.logical and(results, labels)
        # true negative are when both the actual label and the result
are of class 0
        # This is the NOR operator, which is broken into not(or) for
numpy
        trueNegatives = np.logical not(np.logical or(results, labels
))
        # false positives are when the actual label is class 0 and th
e result is class 1
        # this is XOR of results and labels ANDed with the results ar
ray
        falsePositives = np.logical and(np.logical xor(results, label
```

```
s), results)
        # false negatives are when the actual label is class 1 and th
e result is class 0
        # this is XOR of results and labels ANDed with the labels arr
ay
        falseNegatives = np.logical and(np.logical xor(results, label
s), labels)
        classificationDF = pd.DataFrame({'True Label': labels,
                                           'Classified Label': results
                                           'Correct Classification': a
ccurateResults.astype(int),
                                           'True Positive': truePositi
ves.astype(int),
                                           'False Positive': falsePosi
tives.astype(int),
                                           'True Negative': trueNegati
ves.astype(int),
                                           'False Negative': falseNega
tives.astype(int)})
        return [np.sum(accurateResults)/len(samples.index), classific
ationDF1
    # removes the single best node from the tree that gives the best
 return possible
    # Along with modifying the tree, it returns the new accuracies ba
sed on training,
    # validation, and test data and a boolean stating whether a node
was able to be removed
    # (if there is only a root node, no pruning will be performed.)
    def pruneSingleGreedyNode(self,training,trainingLabels, validatio
n, validationLabels, test, testLabels):
        if len(self.children) == 0:
            [trainingAccuracy, trainingDF] = self.performClassificati
on(training, trainingLabels)
            [validationAccuracy, validationDF] = self.performClassifi
cation(validation, validationLabels)
            [testAccuracy, testDF] = self.performClassification(test,
 testLabels)
            return [self.totalLeafNodes, self.totalNodes,
                    trainingAccuracy, trainingDF,
                    validationAccuracy, validationDF,
                    testAccuracy, testDF,
                    True]
        bestValidationAccuracy = 0
        bestValidationDF = None
        bestNode = None
        for node in self.descendants:
            parent = node.parent
            node.parent = None
            [validationAccuracy, bestValidationDF] = self.performClas
sification(validation, validationLabels)
            node.parent = parent;
            if validationAccuracy > bestValidationAccuracy:
```

```
bestValidationAccuracy = validationAccuracy
                validationDF = df
                bestNode = node
        bestNode.parent = None
        [trainingAccuracy, trainingDF] = self.performClassification(t
raining, trainingLabels)
        [testAccuracy, testDF] = self.performClassification(test, tes
tLabels)
        #update node count
        self.countNodes()
        singleton = self.totalNodes == 1
        return [self.totalLeafNodes, self.totalNodes,
                trainingAccuracy, trainingDF,
                bestValidationAccuracy, bestValidationDF,
                testAccuracy, testDF,
                singleton]
    #counts the number of leaf nodes and total number of nodes at thi
s node's point and below in a tree
    def countNodes(self):
        self.totalLeafNodes = 0
        self.totalNodes = 1
        if self.is leaf:
            self.totalLeafNodes = 1
        else:
            for node in self.children:
                [numLeafs, numNodes] = node.countNodes()
                self.totalLeafNodes += numLeafs
                self.totalNodes += numNodes
        return [self.totalLeafNodes, self.totalNodes]
    # renders currrent tree using graphviz and saves it as a png
    def saveAsPNG(self, name):
        texporter.DotExporter(self).to picture(name.strip() + '.png')
```

Data Analysis Cont'd

The next step is to read in the datasets. The first run will use dataset 2, which contains the 80%/10%/10% split between Training/Validation/Testing data.

```
In [75]: # Read in training dataset to be used
         training = pd.read_csv('cancer_datasets_v2/training_2.csv')
         #training.head()
         trainingLabels = training[training.columns[0]]
In [76]:
         # create a list of attributes for use later
         # only need to do this once since all data has the same features
         features = training.columns[1:]
```

```
In [77]: # Read in validation dataset to be used
  validation = pd.read_csv('cancer_datasets_v2/validation_2.csv')
  #validation.head()
  validationLabels = validation[validation.columns[0]]

In [78]: # Read in test datasets to be used
  test = pd.read_csv('cancer_datasets_v2/testing_2.csv')
  #test.head()
  testLabels = test[test.columns[0]]
```

Data Analysis: Training

The following block trains the tree on this data, using the **Entropy** impurity measure.

```
In [79]: # Train the tree
t2 = DTCNode("Dataset2", training, features, "Entropy", True, parent=N
one)
```

Data Analysis: Training Results

The following code blocks provide the total number of nodes and leaf nodes as well as the classification accuracy on the training and testing data.

```
In [80]: [totalLeafNodes, totalNodes] = t2.countNodes()
    print("Total Nodes", totalNodes)
    print("Total Leaf Nodes", totalLeafNodes)

Total Nodes 29
    Total Leaf Nodes 15

In [81]: [trainingAccuracy, trainingResultsDF] = t2.performClassification(training, trainingLabels)
    [testAccuracy, testResultsDF] = t2.performClassification(test, testLabels)
    print("Training Accuracy: ", trainingAccuracy)
    print("Training Accuracy: ", testAccuracy)

Training Accuracy: 0.9978021978021978
    Test Accuracy: 0.8771929824561403
In [82]: t2.saveAsPNG('UnprunedDataset2')
```

Data Analysis: Training with other dataset

The same analysis is performed with dataset 1, which contains the 70%/10%/20% split between Training/Validation/Testing data

```
In [83]: | # Read in training dataset to be used
         training = pd.read_csv('cancer_datasets_v2/training_1.csv')
         #training.head()
         trainingLabels = training[training.columns[0]]
         # create a list of attributes for use later
In [84]:
         # only need to do this once since all data has the same features
         features = training.columns[1:]
         # Read in validation dataset to be used
In [85]:
         validation = pd.read_csv('cancer_datasets_v2/validation_1.csv')
         #validation.head()
         validationLabels = validation[validation.columns[0]]
         # Read in test datasets to be used
In [86]:
         test = pd.read_csv('cancer_datasets_v2/testing_1.csv')
         #test.head()
         testLabels = test[test.columns[0]]
In [87]: # Train the tree
         t1 = DTCNode("Dataset1", training, features, "Entropy", True, parent=N
         print("Total Nodes", t1.totalNodes)
In [88]:
         print("Total Leaf Nodes", t1.totalLeafNodes)
         Total Nodes 33
         Total Leaf Nodes 17
In [89]:
         [trainingAccuracy, trainingResultsDF] = t1.performClassification(trai
         ning, trainingLabels)
         [testAccuracy, testResultsDF] = t1.performClassification(test, testLa
         print("Training Accuracy: ", trainingAccuracy)
         print("Test Accuracy: ", testAccuracy)
         Training Accuracy: 1.0
         Test Accuracy: 0.9298245614035088
```

In [92]: trainingResultsDF.describe()

Out[92]:

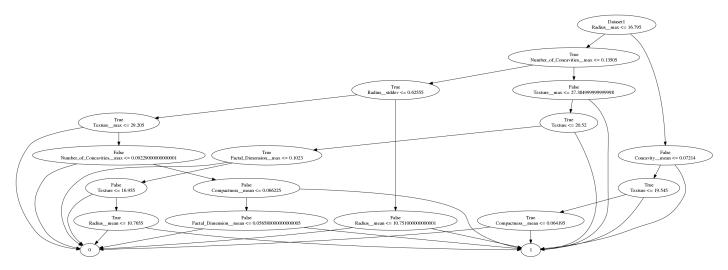
	True Label	Classified Label	Correct Classification	True Positive	False Positive	True Negative	False Negative
count	398.000000	398.000000	398.0	398.000000	398.0	398.000000	398.0
mean	0.429648	0.429648	1.0	0.429648	0.0	0.570352	0.0
std	0.495649	0.495649	0.0	0.495649	0.0	0.495649	0.0
min	0.000000	0.000000	1.0	0.000000	0.0	0.000000	0.0
25%	0.000000	0.000000	1.0	0.000000	0.0	0.000000	0.0
50%	0.000000	0.000000	1.0	0.000000	0.0	1.000000	0.0
75%	1.000000	1.000000	1.0	1.000000	0.0	1.000000	0.0
max	1.000000	1.000000	1.0	1.000000	0.0	1.000000	0.0

In [90]: t1.saveAsPNG('UnprunedDataset1')

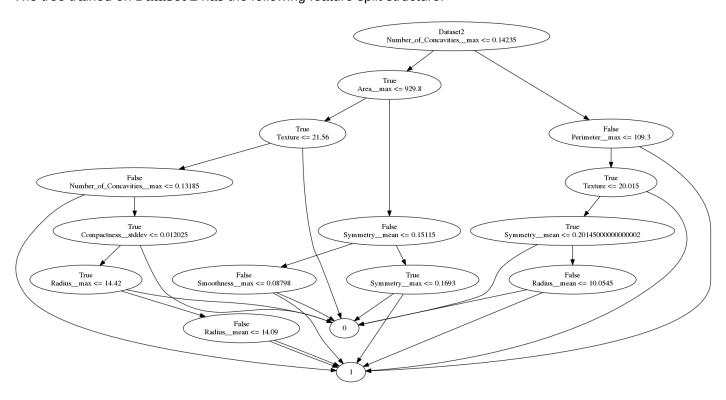
Data Analysis: Dataset Comparison

As can be seen, dataset 1 has a higher initial accuracy, for both testing and training data. On the other hand, dataset 2, which consists of a larger percentage of training data, has slightly few nodes in this unpruned state. It is also interesting to note the completely different set of features and split values that appear between both trees.

The tree trained on **Dataset 1** has the following feature split strucuture:



The tree trained on **Dataset 2** has the following feature split structure:



These pictures will also be submitted separately to easier viewing

Data Analysis: Pruning

```
In [96]:
         t1Copy = copy.deepcopy(t1)
         initialLeafNodes = t1Copy.totalLeafNodes
         initialNodes = t1Copy.totalNodes
         [initialTrainingAcc, initialTrainingDF] = t1Copy.performClassificatio
         n(training, trainingLabels)
         [initialValidationAcc, initialValidationDF] = t1Copy.performClassific
         ation(validation, validationLabels)
         [initialTestAcc, df] = t1Copy.performClassification(test, testLabels)
         initialFPRate = df['False Positive'].sum() / (df['False Positive'].su
         m() + df['True Negative'].sum())
         initialTPRate = df['True Positive'].sum() / (df['True Positive'].sum
         () + df['False Negative'].sum())
         initialPrecision = df['True Positive'].sum() / (df['True Positive'].s
         um() + df['False Positive'].sum())
         initialRecall = initialTPRate
         pruningData = [[initialLeafNodes,
                         initialNodes,
                         initialTrainingAcc,
                         initialValidationAcc,
                         initialTestAcc,
                         initialFPRate,
                         initialTPRate,
                         initialPrecision,
                         initialRecall
         pr = t1Copy.pruneSingleGreedyNode(training, trainingLabels,
                                                        validation, validationL
         abels,
                                                        test, testLabels)
         while(not pr[8]):
             prunedLeafNodes = pr[0]
             prunedNodes = pr[1]
             prunedTrainingAcc = pr[2]
             prunedValidationAcc = pr[4]
             prunedTestAcc = pr[6]
             df = pr[7]
             prunedFPRate = df['False Positive'].sum() / (df['False Positive']
          .sum() + df['True Negative'].sum())
             prunedTPRate = df['True Positive'].sum() / (df['True Positive'].s
         um() + df['False Negative'].sum())
             prunedPrecision = df['True Positive'].sum() / (df['True Positive']
         1.sum() + df['False Positive'].sum())
             prunedRecall = prunedTPRate
             pruningData.append([prunedLeafNodes,
                                  prunedNodes,
                                  prunedTrainingAcc,
                                  prunedValidationAcc,
                                  prunedTestAcc,
                                  prunedFPRate,
                                  prunedTPRate,
                                  prunedPrecision,
                                  prunedRecall])
             pr = t1Copy.pruneSingleGreedyNode(training, trainingLabels,
                                                        validation, validationL
```

```
abels,
                                               test, testLabels)
# convert array to pandas dataframe for easier visualization
pruningDF = pd.DataFrame(pruningData, columns=['Number of Leaf Nodes'
                                                 'Number of Nodes',
                                                 'Training Accuracy',
                                                 'Validation Accuracy',
                                                 'Test Accuracy',
                                                 'FP Rate',
                                                 'TP Rate',
                                                 'Precision',
                                                 'Recall'])
pruningDF.describe()
```

/home/jeb/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.p y:33: RuntimeWarning: invalid value encountered in long_scalars

Out[96]:

	Number of Leaf Nodes	Number of Nodes	Training Accuracy	Validation Accuracy	Test Accuracy	FP Rate	TP Rate	Precision
count	13.000000	13.000000	13.000000	13.000000	13.000000	13.000000	13.000000	12.000000
mean	7.846154	16.000000	0.855624	0.993252	0.853576	0.043077	0.654832	0.895296
std	5.273300	10.336021	0.096375	0.011411	0.064200	0.031342	0.217978	0.063817
min	1.000000	2.000000	0.570352	0.964912	0.657895	0.000000	0.000000	0.818182
25%	4.000000	8.000000	0.846734	0.982456	0.842105	0.026667	0.692308	0.849894
50%	5.000000	11.000000	0.849246	1.000000	0.868421	0.040000	0.692308	0.889394
75%	12.000000	24.000000	0.896985	1.000000	0.877193	0.080000	0.743590	0.935484
max	17.000000	33.000000	1.000000	1.000000	0.929825	0.080000	0.948718	1.000000

In [97]: pruningDF.head(14)

Out[97]:

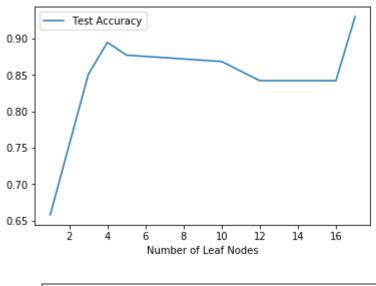
	Number of Leaf Nodes	Number of Nodes	Training Accuracy	Validation Accuracy	Test Accuracy	FP Rate	TP Rate	Precision	Recall
0	17	33	1.000000	0.982456	0.929825	0.080000	0.948718	0.860465	0.948718
1	16	32	0.904523	1.000000	0.842105	0.080000	0.692308	0.818182	0.692308
2	12	25	0.896985	1.000000	0.842105	0.080000	0.692308	0.818182	0.692308
3	12	24	0.896985	1.000000	0.842105	0.080000	0.692308	0.818182	0.692308
4	10	21	0.891960	1.000000	0.868421	0.040000	0.692308	0.900000	0.692308
5	10	20	0.891960	1.000000	0.868421	0.040000	0.692308	0.900000	0.692308
6	5	11	0.849246	1.000000	0.877193	0.053333	0.743590	0.878788	0.743590
7	5	10	0.849246	1.000000	0.877193	0.053333	0.743590	0.878788	0.743590
8	4	9	0.846734	1.000000	0.894737	0.026667	0.743590	0.935484	0.743590
9	4	8	0.846734	1.000000	0.894737	0.026667	0.743590	0.935484	0.743590
10	3	7	0.839196	0.982456	0.850877	0.000000	0.564103	1.000000	0.564103
11	3	6	0.839196	0.982456	0.850877	0.000000	0.564103	1.000000	0.564103
12	1	2	0.570352	0.964912	0.657895	0.000000	0.000000	NaN	0.000000
4									•

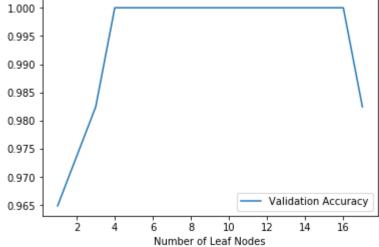
Accuracy Plots

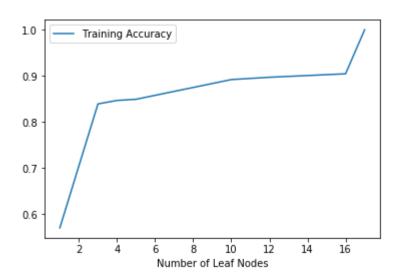
Based on this data, the most accurate tree is the initial unpruned tree. Ignoring that outlier though, the test plot shows that accuracy does increase when pruning initial nodes from the tree, indicating that overfitting is occuring. There is a marked dropoff in accuracy when the tree is pruned too far

```
pruningDF.plot(x='Number of Leaf Nodes', y='Test Accuracy')
pruningDF.plot(x='Number of Leaf Nodes', y='Validation Accuracy')
pruningDF.plot(x='Number of Leaf Nodes', y='Training Accuracy')
```

Out[102]: <matplotlib.axes._subplots.AxesSubplot at 0x7f7e18b99748>





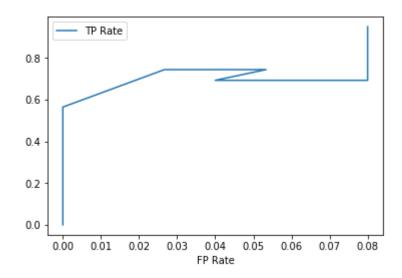


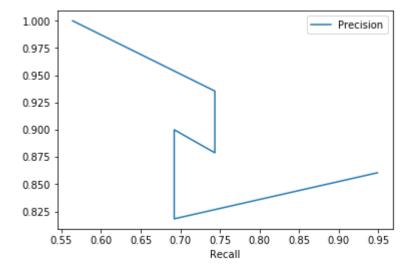
ROC and Precision-Recall Plots for Test Data

As can be see, there are some erors in these plots, so not very much information could be gleaned from them.

```
In [103]:
          # ROC plot
          pruningDF.plot(x='FP Rate', y = 'TP Rate')
          # Precision-Recall Plot
          pruningDF.plot(x='Recall', y='Precision')
```

Out[103]: <matplotlib.axes._subplots.AxesSubplot at 0x7f7e190a2860>

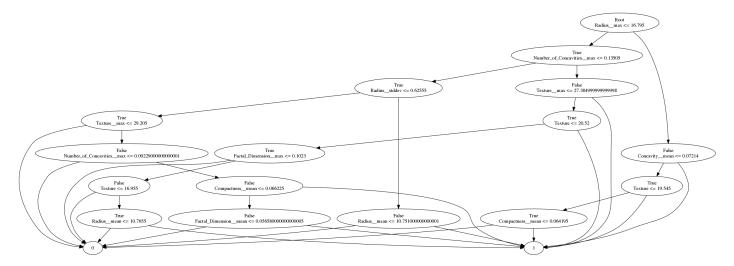




Tree Visualization

The following figure is a graphical representation of a tree trained on dataset 1 and using Entropy as the impurity measure. When viewing the tree, the True/False values at the top of each node represent the result of evaluating its parents feature split. The feature split of each node is then listed.

Note that due to the limitations of anytree's utilization of graphviz, all nodes with the same name are treated as a single node. Hence, the visualization only shows two leaf nodes named with the two possible labels, when in fact each arrow pointing to the leaf node is actually a distinct node. This is verified by the count metrics implemented in the code to determine the total number of nodes and leaf nodes (see above)



This picture will also be submitted separately.

In []:
